

Problem Description: Carol Prime Number Check

Objective: Write a function `isCarolPrime(n)` that takes a positive integer `n` and returns `True` if `n` is a Carol prime number, and `False` otherwise.

Definition:

A Carol prime is a prime number that is of the form $(2^m - 1)^2 - 2$ where m is a positive integer. Not all numbers of this form are prime, but those that are, are called Carol primes.

For example, for $m = 2$, the Carol number is $(2^2 - 1)^2 - 2 = 3^2 - 2 = 7$, which is a prime number.

Parameters:

- `n (int)`: A positive integer which needs to be checked if it is a Carol prime number.

Returns:

- `bool`: `True` if `n` is a Carol prime number, `False` otherwise.

Examples:

1. Example 1:

- **Input:** `n = 7`
- **Output:** `True`
- **Explanation:** For $m=2$, the Carol number is $(2^2 - 1)^2 - 2 = 3^2 - 2 = 7$, which is a prime number.

2. Example 2:

- **Input:** `n = 47`
- **Output:** `True`
- **Explanation:** For $m=3$, the Carol number is $(2^3 - 1)^2 - 2 = 7^2 - 2 = 47$, which is a prime number.

3. Example 3:

- **Input:** `n = 15`
- **Output:** `False`
- **Explanation:** 15 is not of the form $(2^m - 1)^2 - 2$ where m is a positive integer, nor is it prime.

4. Example 4:

- **Input:** `n = 23`
- **Output:** `False`

- **Explanation:** 23 is a prime number but not a Carol number.

Explanation of Sample Input and Output:

- For the input $n = 7$, the function returns **True** because 7 is a Carol prime number for $m=2$ as $2^m = 2^2 = 4$ and $4 + 3 = 7$.
- For the input $n = 47$, the function returns **True** because 47 is a Carol prime number for $m=5$ as $2^m = 2^5 = 32$ and $32 + 15 = 47$.
- For the input $n = 15$, the function returns **False** because 15 is neither a prime number nor of the form $(2^m - 1)^2 - 2$.
- For the input $n = 23$, the function returns **False** because although 23 is a prime number, it is not a Carol number.

Hints:

- A number of the form $(2^m - 1)^2 - 2$ can be calculated for various values of m and checked for primality.
- Check if the given number matches any Carol numbers up to a reasonable value of m and if it is prime.