

AI1110 : Probability and Random Variables

Assignment 3

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Abstract—This document provides the solution of Assignment 3 (NCERT CLASS 9 Statistics Exercise 14.4 Q.2)

Question Exercise 14.4.2 : In a mathematics test given to 15 students, the following marks (out of 100) are recorded: Find the mean, median and mode

41 39 48 52 46 62 54 40 96 52
98 40 42 52 62

TABLE I

of these scores.

Solution :

- 1) Mean of the scores : The number of students scoring a certain score is called as frequency of that score. For instance, 2 students got 52 marks then frequency of 52 marks will be 2. With this knowledge we can construct a frequency distribution table as shown below,

Marks	Frequency
39	1
40	2
41	1
42	1
46	1
48	1
52	3
54	1
60	1
62	1
96	1
98	1
Total	15

TABLE II

Using this frequency distribution we will find mean(m) of the data by vector approach. We know that,

$$m = \frac{\mathbf{f}^T \mathbf{x}}{\mathbf{1}^T \mathbf{f}} \quad (1)$$

where, \mathbf{f} is the frequency vector and \mathbf{x} is the class marks vector. We can get these vectors from Table II. On solving,

$$m = 54.8 \quad (2)$$

Hence, the mean of the scores is 54.8.

- 2) Median of the scores: To find the median we will arrange the scores of students in ascending order, 39,40,40,41,42,46,48,52,52,52,54,60,62,96,98.

Key Concept:

- a) For a sorted data if number of observations(N) is odd, then median of the data will be $\left(\frac{N+1}{2}\right)^{th}$ observation.
b) If the number of observations(N) is even, then median will be the mean of $\left(\frac{N}{2}\right)^{th}$ and $\left(\frac{N+2}{2}\right)^{th}$ observations.

In this case, the number of observations is odd (15), so the median will be $\frac{15+1}{2}^{th} = 8^{th}$ observation.

$$\Rightarrow \text{median} = 52 \quad (3)$$

Hence, median of scores will be 52.

- 3) Mode of scores: To find mode of the scores, from Table II we see that 52 occur maximum number of times in the data (frequency = 3),

$$\Rightarrow \text{mode} = 52 \quad (4)$$

Hence, mode of scores will be 52.