

AI1110 : Probability and Random Variables

Assignment 4

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Abstract—This document provides the solution of Assignment 4 (NCERT CLASS 11 Exercise 16.3 21)

Question Exercise 16.3.21: In a class of 60 students, 30 opted for NCC, 32 opted for NSS and 24 opted for both NCC and NSS. If one of these students is selected at random, find the probability that

- (i) The student opted for NCC or NSS.
- (ii) The student has opted neither NCC nor NSS.
- (iii) The student has opted NSS but not NCC.

Solution : Let us define random variables X, Y , where $X, Y \in \{0, 1\}$, such that

| Random variable | Value | Description |
|-----------------|-------|-------------------|
| X | 0 | not opted for NCC |
| X | 1 | opted for NCC |
| Y | 0 | not opted for NSS |
| Y | 1 | opted for NSS |

TABLE I

From the given data, we can write

$$\Pr(X = 1) = \frac{30}{60}$$

$$= \frac{1}{2}$$

$$\Pr(Y = 1) = \frac{32}{60}$$

$$= \frac{8}{15}$$

$$\Pr(X + Y = 2) = \frac{24}{60}$$

$$= \frac{2}{5}$$

- (i) The probability of the event "the student opted for NCC or NSS" can be described as $\Pr(X + Y > 0)$. In other words, either of random variables X, Y should be equal to 1.

$$\begin{aligned} \Pr(X + Y > 0) &= \Pr(X = 1) + \Pr(Y = 1) \\ &\quad - \Pr(X + Y = 2) \end{aligned} \quad (7)$$

$$\implies = \frac{1}{2} + \frac{8}{15} - \frac{2}{5} \quad (8)$$

$$\implies = \frac{19}{30} \quad (9)$$

$$\therefore \Pr(X + Y > 0) = \frac{19}{30} \quad (10)$$

- (ii) The probability of the event "the student has opted neither NCC nor NSS" can be described as " $\Pr(X + Y = 0)$ ". In other words, both the random variables X, Y should be 0. Now we can write,

$$\Pr(X + Y = 0) = 1 - \Pr(X + Y > 0) \quad (11)$$

Using (10)

$$\Pr(X + Y = 0) = 1 - \frac{19}{30} \quad (12)$$

$$= \frac{11}{30} \quad (13)$$

- (iii) The probability of the event "the student has opted NSS but not NCC" can be described as " $\Pr(Y = 1 \text{ and } X = 0)$ ".

We can write

$$\begin{aligned} \Pr(Y = 1 \text{ and } X = 0) &= \Pr(Y = 1) \\ &\quad - \Pr(Y = 1 \text{ and } X = 1) \end{aligned} \quad (14)$$

$$= \Pr(Y = 1) - \Pr(X + Y = 2) \quad (15)$$

Using (4) and (6),

$$\Pr(Y = 1 \text{ and } X = 0) = \frac{8}{15} - \frac{2}{5} \quad (16)$$

$$= \frac{2}{15} \quad (17)$$

$$\therefore \Pr(Y = 1 \text{ and } X = 0) = \frac{2}{15} \quad (18)$$