

## 1.2 Graphical representation of the operating characteristics.

$$d^* = \lfloor 30.0063 \rfloor = 30$$

Embedded curve:  $(FPR_0, TPR, d)$

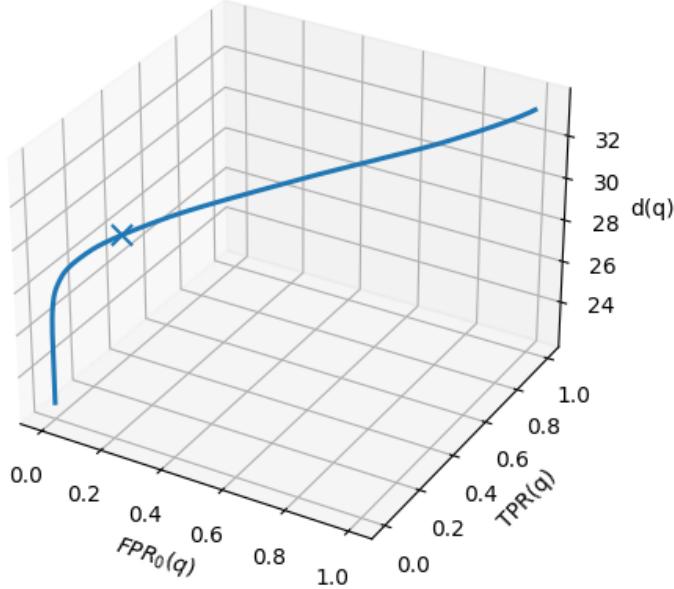


Figure 1: Three-dimensional representation of the decision curve  $q \mapsto (FPR_0(q), TPR(q), d(q))$ . The highlighted point corresponds to the selected operating probability  $q^*$  and its associated threshold  $d^*$ .

## 1.2 Graphical representation of the operating characteristics.

While the calibration procedure is entirely defined through the rates  $TPR(q)$ ,  $FPR_0(q)$  and  $FPR_1(q)$ , we favor a three-dimensional graphical representation of the decision rule. Indeed, plotting the curve

$$q \mapsto (FPR_0(q), TPR(q), d(q))$$

allows the evolution of the decision threshold to be visualized jointly with the corresponding operating characteristics. In contrast, two-dimensional ROC projections such as  $TPR$  versus  $FPR_0$  or  $FPR_1$  necessarily suppress the information carried by the threshold  $d(q)$  and may visually collapse distinct operating regimes onto the same curve. The three-dimensional embedding therefore provides a more informative graphical summary of the procedure, while relying on the same underlying probabilistic quantities and leaving the detection rule itself unchanged.