

Sizing of Motor

Moment of Inertia of Roller1

Assuming the Roller as a cylinder with radius r and length l .

Density of mild steel = 7860 kg/m³

Radius of Roller1 = 20 mm

Length of Roller1 = 109 mm

$$\begin{aligned} J_{roller1} &= \rho \pi r^4 l \\ &= 1.37 \times 10^{-4} \text{ kg m}^2 \end{aligned}$$

Moment of Inertia of Roller2

Assuming the Roller as a cylinder with radius r and length l .

Density of mild steel = 7860 kg/m³

Radius of Roller2 = 22.5 mm

Length of Roller2 = 80 mm

$$\begin{aligned} J_{roller2} &= \rho \pi r^4 l \\ &= 1.61 \times 10^{-4} \text{ kg m}^2 \end{aligned}$$

Moment of Inertia of Shaft 1

Assuming the Shaft as a cylinder with radius r and length l .

Density of mild steel = 7860 kg/m³

Radius of Shaft1 = 6.5 mm

Length of Shaft1 = 61 cm

$$\begin{aligned} J_{shaft1} &= \rho \pi r^4 l \\ &= 2.69 \times 10^{-5} \text{ kg m}^2 \end{aligned}$$

Moment of Inertia of Shaft 2

Assuming the Shaft as a cylinder with radius r and length l .

Density of mild steel = 7860 kg/m³

Radius of Shaft2 = 6.5 mm

Length of Shaft2 = 20.7 cm

$$\begin{aligned} J_{shaft2} &= \rho \pi r^4 l \\ &= 9.12 \times 10^{-6} \text{ kg m}^2 \end{aligned}$$

Moment of Inertia of Shaft 3

Assuming the Shaft as a cylinder with radius r and length l .

Density of mild steel = 7860 kg/m³

Radius of Shaft3 = 6.5 mm

Length of Shaft3 = 20.4 cm

$$J_{shaft\ 3} = \rho \pi r^4 l$$

$$= 8.99 \times 10^{-6} \text{ kg m}^2$$

Moment of Inertia of Shaft 4

Assuming the Shaft as a cylinder with radius r and length l .

Density of mild steel = 7860 kg/m³

Radius of Shaft4 = 6.5 mm

Length of Shaft4 = 15.1 cm

$$J_{shaft\ 4} = \rho \pi r^4 l$$

$$= 6.65 \times 10^{-6} \text{ kg m}^2$$

Moment of Inertia of Sprocket 1

Assuming the Sprocket as a cylinder with radius r and length l .

Density of mild steel = 7860 kg/m³

Radius of Sprocket1 = 12.9 mm

Length of Sprocket1 = 20.3 mm

$$J_{sprocket\ 1} = \rho \pi r^4 l$$

$$= 1.57 \times 10^{-5} \text{ kg m}^2$$

Moment of Inertia of Sprocket 2

Assuming the Sprocket as a cylinder with radius r and length l .

Density of mild steel = 7860 kg/m³

Radius of Sprocket2 = 17.6 mm

Length of Sprocket2 = 39 mm

$$J_{sprocket\ 2} = \rho \pi r^4 l$$

$$= 9.24 \times 10^{-5} \text{ kg m}^2$$

Moment of Inertia of Spring

Assuming the spring is uniformly distributed along axis

Radius of thickness of spring = 3 mm

Radius of spring = 45 mm

Length of spring = 150 mm

$$J_{spring} = \frac{\rho \pi r^2 R^2 l}{8}$$

$$= 8.44 \times 10^{-6} \text{ kg m}^2$$

Torque Calculation

$$\begin{aligned} J_{load} &= J_{shaft1} + J_{shaft2} + J_{shaft3} + J_{shaft4} + J_{roller2} + J_{roller1} + 2 \times J_{sprocket1} + 2 \times J_{sprocket1} + 2 \times J_{spring} \\ &= 5.82 \times 10^{-4} \text{ kg m}^2 \end{aligned}$$

$$\begin{aligned} T_a &= \frac{J_{Load} \times V}{9.55 \times t} \\ &= 0.12 \text{ Nm} \end{aligned}$$

$$\begin{aligned} \text{Min Torque Needed} &= T_a \times \text{FOS} \\ &= 0.12 \times 2 \\ &= 0.24 \text{ Nm} \end{aligned}$$