

# CS 6501 Natural Language Processing

## Probabilistic Context-Free Grammars

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ENGINEERING

# Overview

1. About Group Project Proposal
2. Introduction
3. Context-Free Grammars
4. Ambiguity
5. Probabilistic CFGs
6. Penn Treebank

# About Group Project Proposal

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# Goal of the Group Project

An opportunity to work on a larger NLP system on a topic of your choice

# Proposal Outline

## 1. Problem definition

- ▶ What is the problem? Input and Output?
- ▶ Why it is interesting/challenging?
- ▶ Is this relevant to your own research project? What is the connection?

## 2. Related work

- ▶ Any existing work on this topic?
- ▶ What is the difference?

## 3. Data

- ▶ What data you will use?
- ▶ What is the data size, in terms of the number of words/sentences/documents?

# Proposal Outline (Cont.)

## 4. Proposed method(s)

- ▶ What method/model/algorithm are you planning to use?
- ▶ Does this involve some existing implementations/packages? How?

## 5. Evaluation plan

- ▶ How will you evaluate your results? What evaluation metrics that you will use?
- ▶ What are your criteria of success?

# Requirements

- ▶ No more than **two** pages, including references
- ▶ Proposal due on Oct. 5th, 11:59PM
- ▶ Proposal template: the last NIPS submission template
  - ▶ include all the group members in the author list
  - ▶ please do not modify the template

# Proposal Presentation

- ▶ Each group: 5-minute presentation and 3-minute QA
- ▶ About 5-page slides
  - ▶ one section per slide

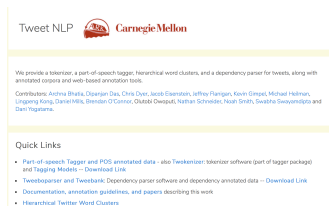


# Example Projects

In addition to the projects I suggested before

1. NLP techniques on social media
2. Conversational modeling
3. Question answering

# NLP techniques on Social Media

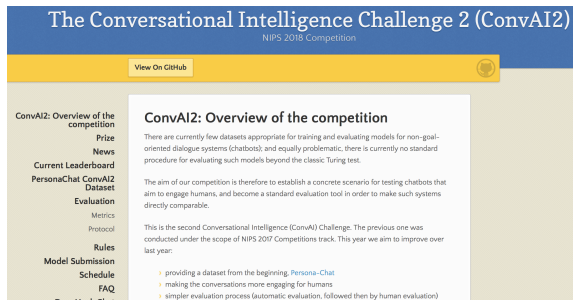


<http://www.cs.cmu.edu/~ark/TweetNLP/>

## Example projects


1. POS tagger/syntactic parser on tweets
2. Word embeddings on tweets and its application on sentiment classification

# Conversational Modeling



1. Build non-goal-oriented dialogue systems
2. Build a conversational model that can generate diverse responses

# Question Answering

Dataset	Multi turn	Text- based	Dialog Acts	Simple Evaluation	Unanswerable Questions	Asker Can't See Evidence
 QuAC	✓	✓	✓	✓	✓	✓
CoQA (Reddy et al., 2018)	✓	✓	✗	✓	✓	✗
CSQA (Saha et al., 2018)	✓	✗	✗	✗	✓	✗
CQA (Talmor and Berant, 2018)	✓	✓	✗	✓	✗	✓
SQA (Iyyer et al., 2017)	✓	✗	✗	✓	✗	✗
NarrativeQA (Kociský et al., 2017)	✗	✓	✗	✗	✗	✓
TriviaQA (Joshi et al., 2017)	✗	✓	✗	✓	✗	✓
SQuAD 2.0 (Rajpurkar et al., 2018)	✗	✓	✗	✓	✓	✗
MS Marco (Nguyen et al., 2016)	✗	✓	✗	✗	✓	✓
NewsQA (Trischler et al., 2016)	✗	✓	✗	✓	✓	✓

[Choi et al., 2018]

# Further Comments

Two ways to evaluate your project by yourself

- ▶ Practical values

- ▶ How it helps me get some experience of using NLP tools?
- ▶ How it helps me get some experience of training DL models?
- ▶ Is it worth to put it on my resume when I am looking for a job/internship?

# Further Comments

Two ways to evaluate your project by yourself

- ▶ Practical values

- ▶ How it helps me get some experience of using NLP tools?
- ▶ How it helps me get some experience of training DL models?
- ▶ Is it worth to put it on my resume when I am looking for a job/internship?

- ▶ Research values

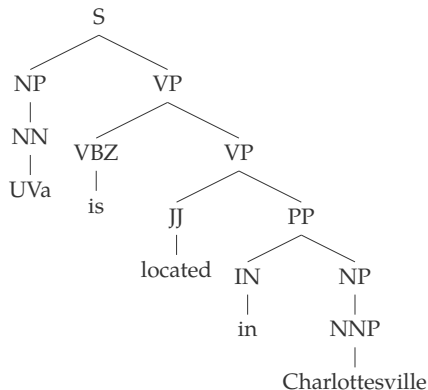
- ▶ How this project is relevant to my research?
- ▶ How this project help me understand resolving some real problems using NLP techniques?
- ▶ Will this eventually lead to an academic paper?

# Introduction

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# Parsing

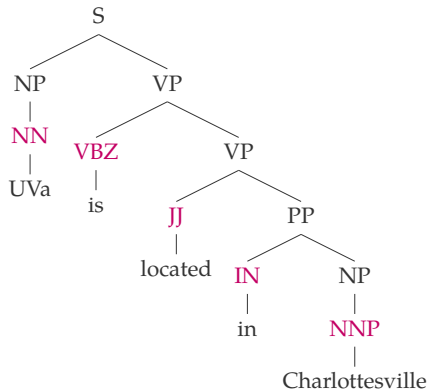
- ▶ Input: UVa is located in Charlottesville
- ▶ Output:





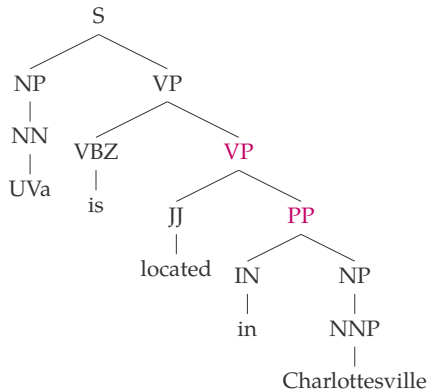
# Information Conveyed by Parse Trees

Part of speech for each word



# Information Conveyed by Parse Trees (II)

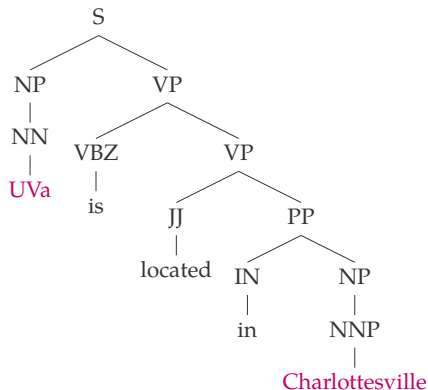
## Phrase



- ▶ PP: *in Charlottesville*
- ▶ VP: *located in Charlottesville*

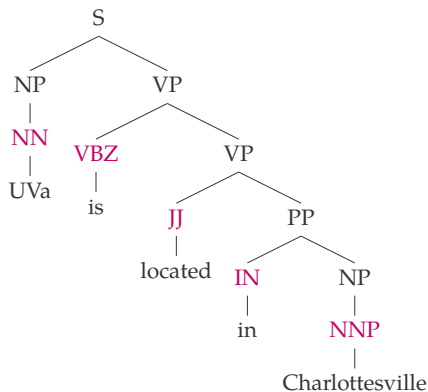
# Information Conveyed by Parse Trees (III)

## Useful relationships



Relationship between **UVa** and **Charlottesville**

# An Example Application



- Question answering: *what is the location of UVa?*

# Context-Free Grammars

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# Formal Definition

A context free grammar  $G = (N, \Sigma, R, S)$  where

- ▶  $N$ : a set of non-terminal symbols
- ▶  $S \in N$ : a distinguished start symbol
- ▶  $\Sigma$ : a set of terminal symbols
- ▶  $R$ : a set of rules of the form  $X \rightarrow Y_1 Y_2 \cdots Y_n$  for  $n \geq 0, X \in N, Y_i \in N \cup \Sigma$

# A Context-Free Grammar for English

- ▶  $N = \{S, NP, VP, PP, DT, Vi, Vt, NN, IN\}$
- ▶  $S = S$
- ▶  $\Sigma =$   
 $\{\text{sleeps, saw, man, woman, telescope, the, with, in}\}$
- ▶  $R$

S	→	NP	VP
VP	→	Vi	
VP	→	Vt	NP
VP	→	VP	PP
NP	→	DT	NN
NP	→	NP	PP
PP	→	IN	NP

Vi	→	sleeps
Vt	→	saw
NN	→	man
NN	→	woman
NN	→	telescope
DT	→	the
IN	→	with
IN	→	in

# (Left-Most) Derivations

S	→	NP	VP
VP	→	Vi	
VP	→	Vt	NP
VP	→	VP	PP
NP	→	DT	NN
NP	→	NP	PP
PP	→	IN	NP

Vi	→	sleeps
Vt	→	saw
NN	→	man
NN	→	woman
NN	→	telescope
DT	→	the
IN	→	with
IN	→	in

- ▶ Left-most derivation: always pick the left-most non-terminal symbol for replacement



# An Example

S	→	NP	VP
VP	→	Vi	
VP	→	Vt	NP
VP	→	VP	PP
NP	→	DT	NN
NP	→	NP	PP
PP	→	IN	NP

Vi	→	sleeps
Vt	→	saw
NN	→	man
NN	→	woman
NN	→	telescope
DT	→	the
IN	→	with
IN	→	in

Derivation	Rules used
S	$S \rightarrow NP VP$
NP VP	

# An Example

S	→	NP	VP
VP	→	Vi	
VP	→	Vt	NP
VP	→	VP	PP
NP	→	DT	NN
NP	→	NP	PP
PP	→	IN	NP

Vi	→	sleeps
Vt	→	saw
NN	→	man
NN	→	woman
NN	→	telescope
DT	→	the
IN	→	with
IN	→	in

Derivation	Rules used
S	$S \rightarrow NP VP$
NP VP	$NP \rightarrow DT NN$
DT NN VP	

# An Example

S	→	NP	VP
VP	→	Vi	
VP	→	Vt	NP
VP	→	VP	PP
NP	→	DT	NN
NP	→	NP	PP
PP	→	IN	NP

Vi	→	sleeps
Vt	→	saw
NN	→	man
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NN	→	telescope
DT	→	the
IN	→	with
IN	→	in

Derivation	Rules used
S	$S \rightarrow NP VP$
NP VP	$NP \rightarrow DT NN$
DT NN VP	$DT \rightarrow the$
the NN VP	

# An Example

S	→	NP	VP
VP	→	Vi	
VP	→	Vt	NP
VP	→	VP	PP
NP	→	DT	NN
NP	→	NP	PP
PP	→	IN	NP

Vi	→	sleeps
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NN	→	man
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NN	→	telescope
DT	→	the
IN	→	with
IN	→	in

Derivation	Rules used
S	$S \rightarrow NP VP$
NP VP	$NP \rightarrow DT NN$
DT NN VP	$DT \rightarrow the$
the NN VP	$NN \rightarrow man$
the man VP	

# An Example

S	→	NP	VP
VP	→	Vi	
VP	→	Vt	NP
VP	→	VP	PP
NP	→	DT	NN
NP	→	NP	PP
PP	→	IN	NP

Vi	→	sleeps
Vt	→	saw
NN	→	man
NN	→	woman
NN	→	telescope
DT	→	the
IN	→	with
IN	→	in

Derivation	Rules used
S	$S \rightarrow NP VP$
NP VP	$NP \rightarrow DT NN$
DT NN VP	$DT \rightarrow the$
the NN VP	$NN \rightarrow man$
the man VP	$VP \rightarrow Vi$
the man Vi	

# An Example

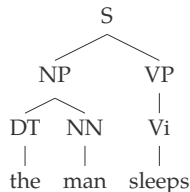
S	→	NP	VP
VP	→	Vi	
VP	→	Vt	NP
VP	→	VP	PP
NP	→	DT	NN
NP	→	NP	PP
PP	→	IN	NP

Vi	→	sleeps
Vt	→	saw
NN	→	man
NN	→	woman
NN	→	telescope
DT	→	the
IN	→	with
IN	→	in

Derivation	Rules used
S	$S \rightarrow NP VP$
NP VP	$NP \rightarrow DT NN$
DT NN VP	$DT \rightarrow the$
the NN VP	$NN \rightarrow man$
the man VP	$VP \rightarrow Vi$
the man Vi	$Vi \rightarrow sleeps$
the man sleeps	

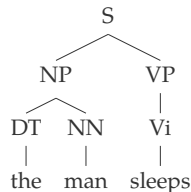
# From Derivations to Parse Tree

Derivation	Rules used
S	$S \rightarrow NP VP$
NP VP	
DT NN VP	$DT \rightarrow \text{the}$
the NN VP	$NN \rightarrow \text{man}$
the man VP	$VP \rightarrow Vi$
the man Vi	$Vi \rightarrow \text{sleeps}$
the man sleeps	



# From Derivations to Parse Tree

Derivation	Rules used
S	$S \rightarrow NP VP$
NP VP	$NP \rightarrow DT NN$
DT NN VP	$DT \rightarrow \text{the}$
the NN VP	$NN \rightarrow \text{man}$
the man VP	$VP \rightarrow Vi$
the man Vi	$Vi \rightarrow \text{sleeps}$
the man sleeps	





# Properties of CFGs

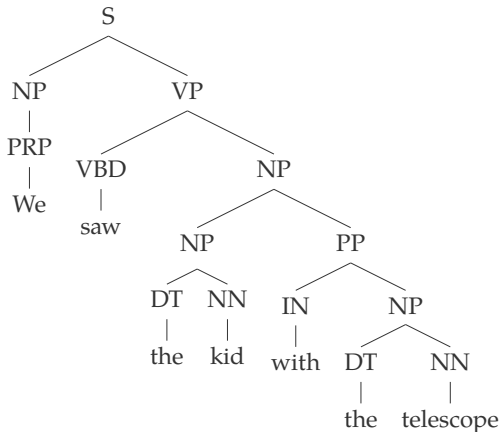
- ▶ A CFG defines a set of possible derivations
- ▶ A string  $s \in \Sigma^*$  is in the language defined by the CFG if there is at least one derivation that yield  $s$
- ▶ Each string in the language generated by the CFG may have more than one derivation (“ambiguity”)

# Ambiguity



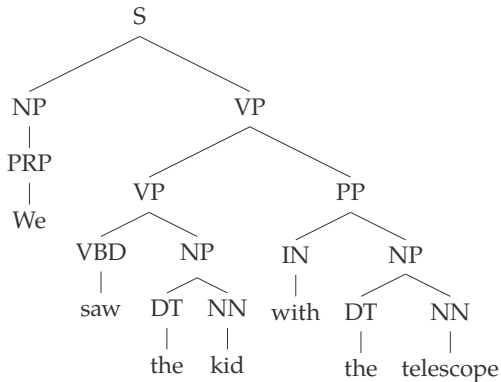
# An Example of Ambiguity

Sentence: *We saw the kid with the telescope*



# An Example of Ambiguity (II)

Sentence: *We saw the kid with the telescope*



# Problem with Parsing: Ambiguity

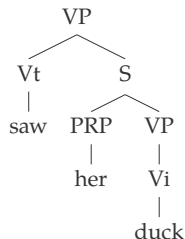
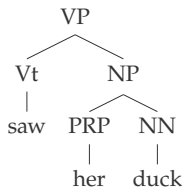
Sentence: *She announced a program to promote safety in trucks and vans*



# Sources of Ambiguity (I)

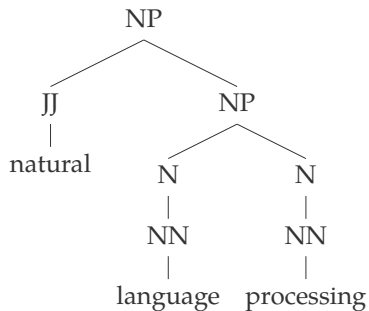
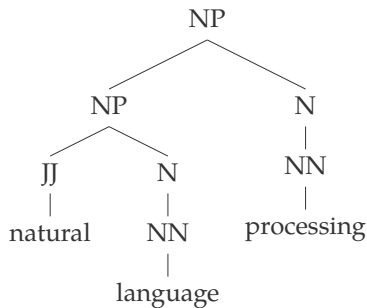
## Part-of-Speech ambiguity

- ▶ NN → duck
- ▶ Vi → duck



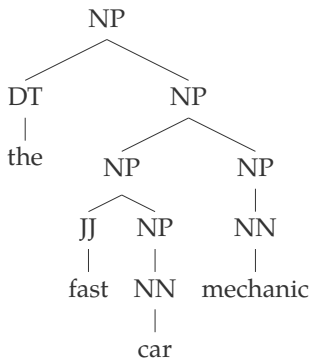
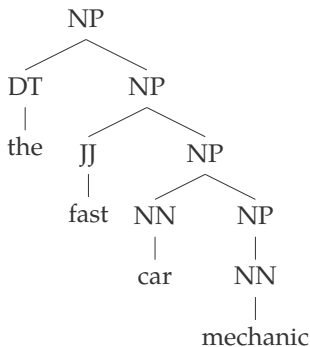
# Sources of Ambiguity (II)

## Noun premodifiers



# Sources of Ambiguity (III)

## Noun premodifiers





# Probabilistic CFGs

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# A Probabilistic Context-Free Grammar (PCFG)

- ▶  $N$ : a set of non-terminal symbols
- ▶  $S \in N$ : a distinguished start symbol
- ▶  $\Sigma$ : a set of terminal symbols

S	$\Rightarrow$	NP	VP	1.0
VP	$\Rightarrow$	Vi		0.4
VP	$\Rightarrow$	Vt	NP	0.4
VP	$\Rightarrow$	VP	PP	0.2
NP	$\Rightarrow$	DT	NN	0.3
NP	$\Rightarrow$	NP	PP	0.7
PP	$\Rightarrow$	P	NP	1.0

Vi	$\Rightarrow$	sleeps	1.0
Vt	$\Rightarrow$	saw	1.0
NN	$\Rightarrow$	man	0.7
NN	$\Rightarrow$	woman	0.2
NN	$\Rightarrow$	telescope	0.1
DT	$\Rightarrow$	the	1.0
IN	$\Rightarrow$	with	0.5
IN	$\Rightarrow$	in	0.5

# Probability of a Tree

The probability of a tree  $t$  with rules

$$\alpha_1 \rightarrow \beta_1, \alpha_2 \rightarrow \beta_2, \dots, \alpha_n \rightarrow \beta_n$$

is

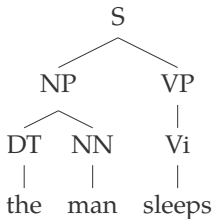
$$P(t) = \prod_{i=1}^n P(\alpha_i \rightarrow \beta_i) \quad (1)$$

where  $P(\alpha \rightarrow \beta)$  is the rule of  $\alpha \rightarrow \beta$

# An Example

S	⇒	NP	VP	1.0
VP	⇒	Vi		0.4
VP	⇒	Vt	NP	0.4
VP	⇒	VP	PP	0.2
NP	⇒	DT	NN	0.3
NP	⇒	NP	PP	0.7
PP	⇒	P	NP	1.0

Vi	⇒	sleeps	1.0
Vt	⇒	saw	1.0
NN	⇒	man	0.7
NN	⇒	woman	0.2
NN	⇒	telescope	0.1
DT	⇒	the	1.0
IN	⇒	with	0.5
IN	⇒	in	0.5



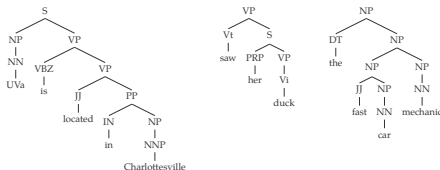
# Properties of PCFGs

- ▶ Assigns a probability to each derivation, or parse-tree, allowed by the underlying CFG
- ▶ If one sentence has more than one derivations, we can rank them based on their probabilities
- ▶ The most likely parse tree for a sentence is

$$\arg \max_{t \in \mathcal{T}(s)} P(t) \quad (2)$$

# Deriving a PCFG from a Corpus

- Given a set of example trees (a treebank), the underlying CFG can simply be **all rules seen in the corpus**



- Maximum likelihood estimates:

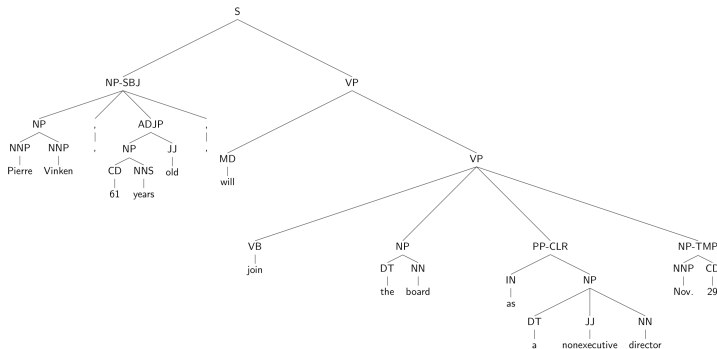
$$P(\alpha \rightarrow \beta) \approx \frac{c(\alpha \rightarrow \beta)}{c(\alpha)} \quad (3)$$

Penn Treebank



# Penn Treebank

- ▶ 50,000 sentences with associated trees
- ▶ Usual setup: 40,000 training sentences, 2,400 test sentences





# Some Penn Treebank Rules with Counts

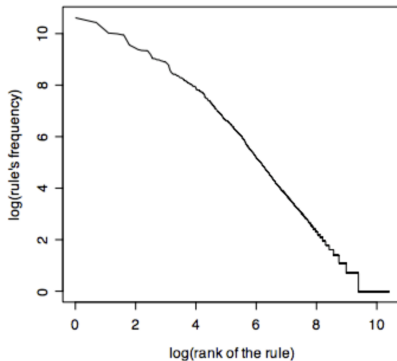
40717 PP → IN NP  
33803 S → NP-SBJ VP  
22513 NP-SBJ → -NONE-  
21877 NP → NP PP  
20740 NP → DT NN  
14153 S → NP-SBJ VP .  
12922 VP → TO VP  
11881 PP-LOC → IN NP  
11467 NP-SBJ → PRP  
11378 NP → -NONE-  
11291 NP → NN

...

989 VP → VBG S  
985 NP-SBJ → NN  
983 PP-MNR → IN NP

100 VP → VBD PP-PRD  
100 PRN → : NP :  
100 NP → DT JJS  
100 NP-CLR → NN  
99 NP-SBJ-1 → DT NNP  
98 VP → VBN NP PP-DIR  
98 VP → VBD PP-TMP  
98 PP-TMP → VBG NP  
97 VP → VBD ADVP-TMP VP  
...  
10 WHNP-1 → WRB JJ  
10 VP → VP CC VP PP-TMP  
10 VP → VP CC VP ADVP-MNR  
10 VP → VBZ S , SBAR-ADV  
10 VP → VBZ S ADVP-TMP

# Penn Treebank Rules: Statistics



# Summary

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# Reference



Choi, E., He, H., Iyyer, M., Yatskar, M., Yih, W.-t., Choi, Y., Liang, P., and Zettlemoyer, L. (2018).  
Quac: Question answering in context.  
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