

# Artificial Neural Networks - Assignment 3

## Group 21

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# Convergence and Attractors

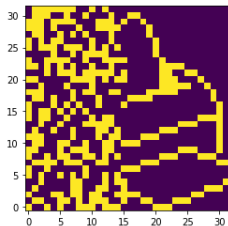
Given the following initial patterns:

$$\begin{array}{lcl} x1d = & \left| \begin{array}{cccccccc} -1 & -1 & 1 & -1 & 1 & -1 & -1 & 1 \end{array} \right. \\ x2d = & \left| \begin{array}{cccccccc} -1 & -1 & -1 & -1 & -1 & 1 & -1 & -1 \end{array} \right. \\ x3d = & \left| \begin{array}{cccccccc} -1 & 1 & 1 & -1 & -1 & 1 & -1 & 1 \end{array} \right. \end{array}$$

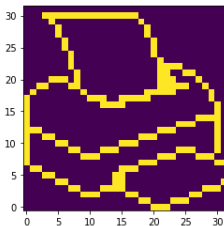
- The network converged after two iterations
- All 3 patterns are attractors - total of 14
- 1 bit or 2 bit distortion: patterns converge to the attractors
- More than half distorted: network can't recall

# Sequential Update

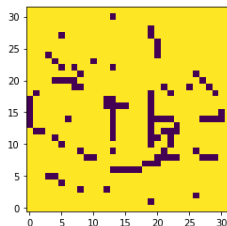
The first three patterns are stable



**Figure:** Degraded pattern **p10** of the original pattern **p1** — noise/degradation in half the image.

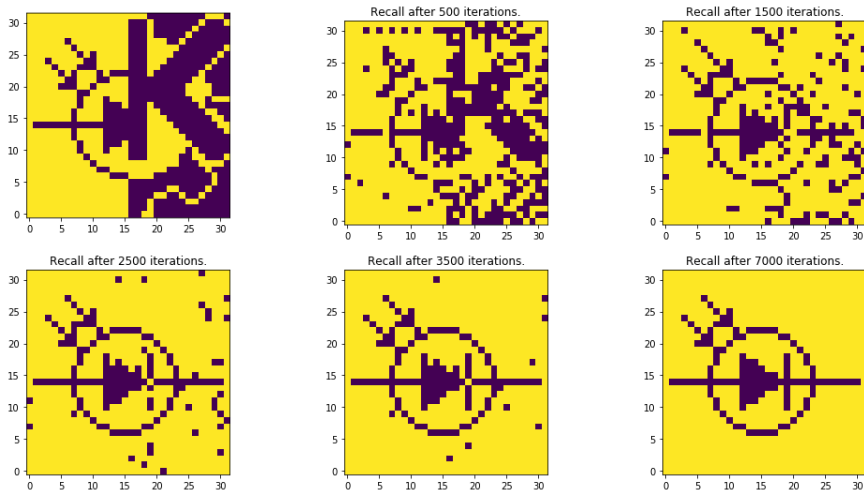


**Figure:** Degraded pattern **p10** after sequential update, converged to stable pattern **p1**.



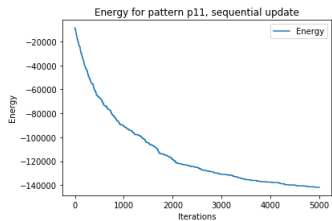
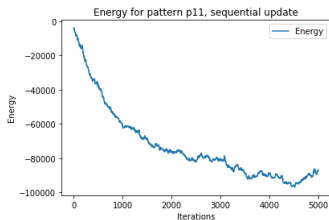
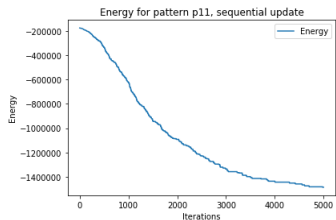
**Figure:** Recalled pattern **p11** — didn't converge to any stable pattern, and is instead spurious.

# Random Sequential Update



**Figure:** Pattern **p11** converging to learned pattern **p3** with sequential update

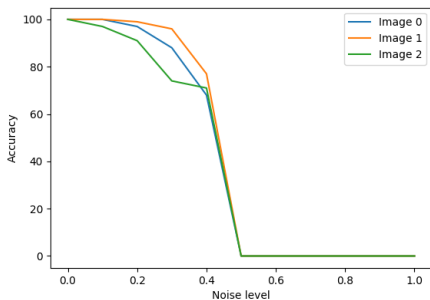
# Energy



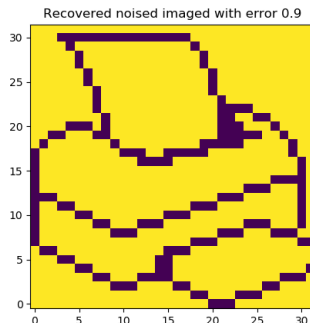
Pattern	Energy
<b>p1</b>	-1470864.0
<b>p2</b>	-1395344.0
<b>p3</b>	-1494272.0
<b>p10</b>	-1631244.0
<b>p11</b>	-1395344.0

# Distortion Resistance

## Images data



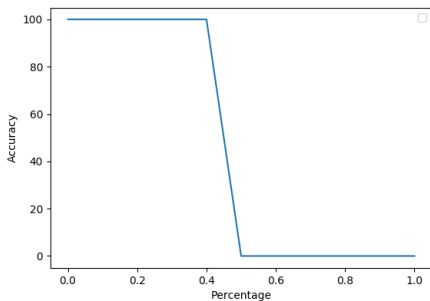
**Figure:** Plot of image 0 recovered for different noise percentage



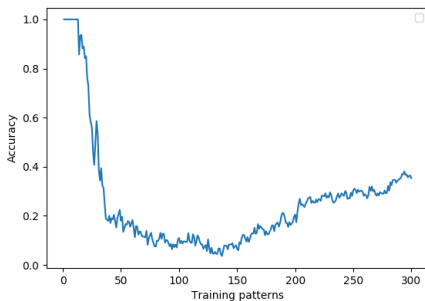
**Figure:** Image 0 recovered with 90% noise

# Capacity

## Random Patterns



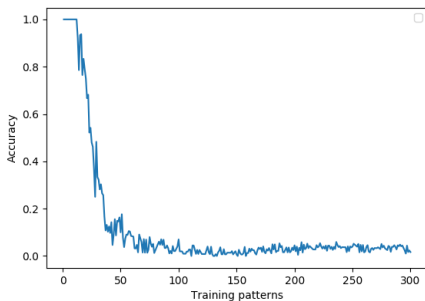
**Figure:** Plot of random patterns recovered for different noise percentage with 4 patterns train



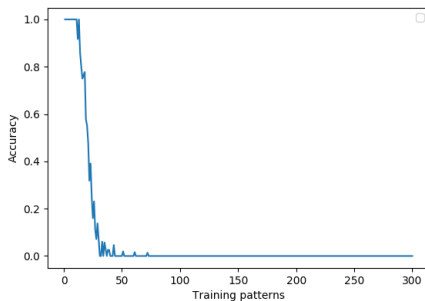
**Figure:** Plot of random patterns recovered for different number of patterns

# Capacity

## Random Patterns with noise



**Figure:** Plot of random patterns recovered for different number of patterns with 1% noise

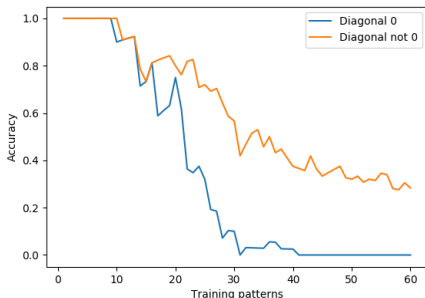


**Figure:** Plot of random patterns recovered for different number of patterns with 10% noise

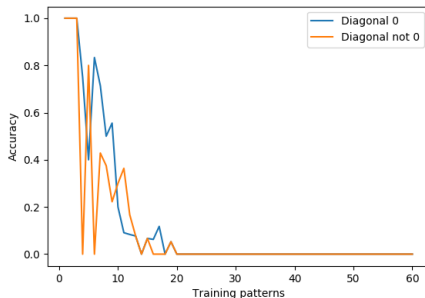


# Capacity

## Random Patterns Diagonal 0

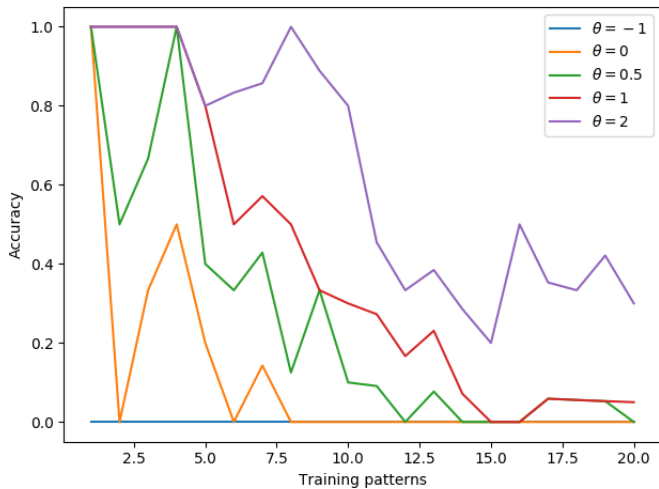


**Figure:** Plot of random patterns recovered for different number of patterns with main diagonal equal and different from 0.



**Figure:** Plot of random patterns recovered for different number of patterns with main diagonal equal and different from 0 and 40% noise.

# Sparse Patterns



# Sparse Patterns

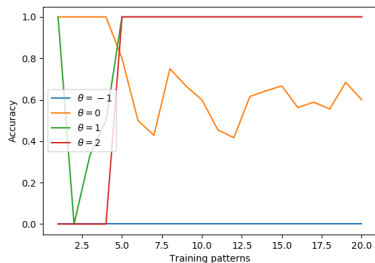


Figure: Plot of random patterns recovered for  $\theta = 1$  and  $\rho = 0.01$

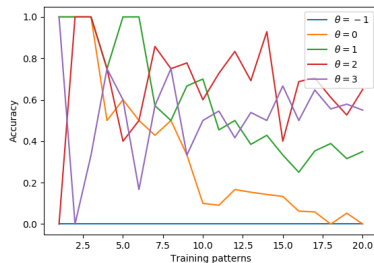


Figure: Plot of random patterns recovered for  $\theta = 1$  and  $\rho = 0.05$