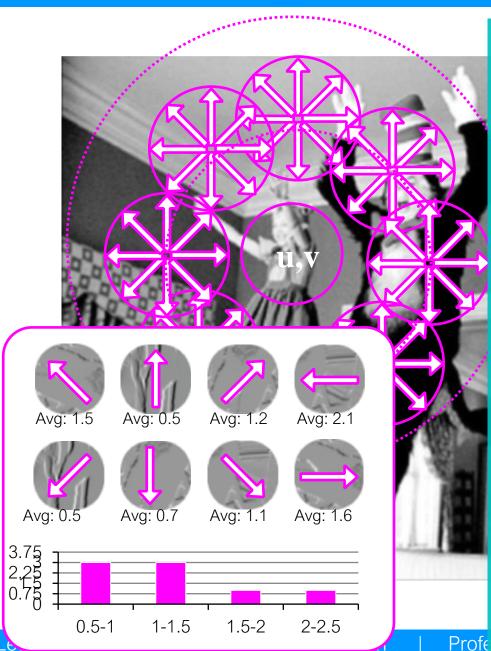
Lecture Notes for **Machine Learning in Python**

Professor Eric Larson

Logistic Regression

Last Time: DAISY



- 1. Select *u*,*v* pixel location in image
- 2. Take histogram of average gradient magnitudes in circle

for each orientation $h_{\Sigma}(u,v)$

- 3. Select circles in a ring, R
- For each circle on the ring, take another

histogram $h_{\Sigma}(\mathbf{l}_{O}(u, v, R_{1}))$

- 5. Repeat for more rings
- Save all histograms as "descriptors"

$$[h_{\Sigma}(\cdot),h_{\Sigma}(\cdot),h_{\Sigma}(\cdot)...]$$

7. Can concatenate descriptors

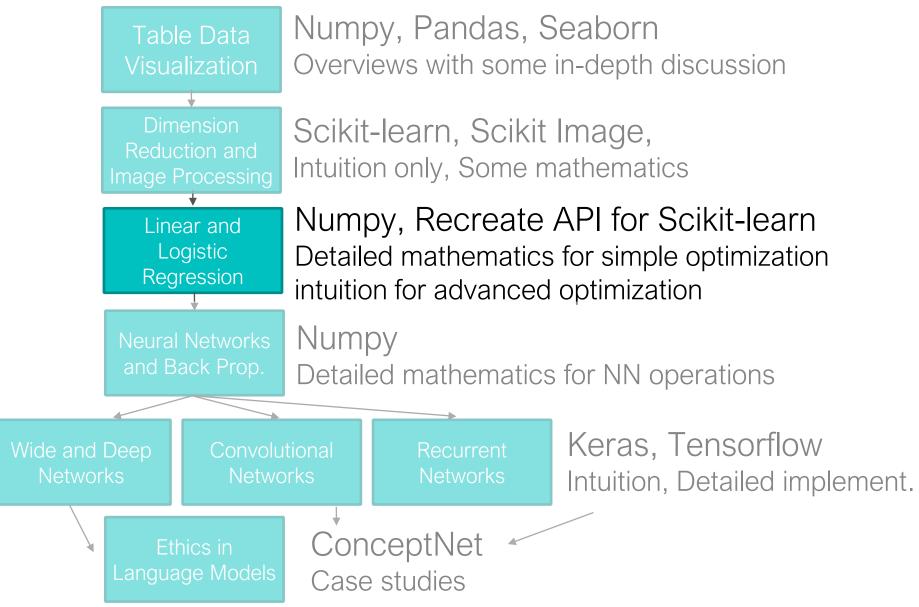
so as "feature" vector at that nivel

Class Announcements

Lab 2 Due Saturday, Feb 20

- TIPS
 - Read the questions carefully
 - Seek TA support office hours and through e-mail
 - Instructor (virtual + in-person) office hour: Monday 3 4 pm (zoom link will be posted on Canvas)

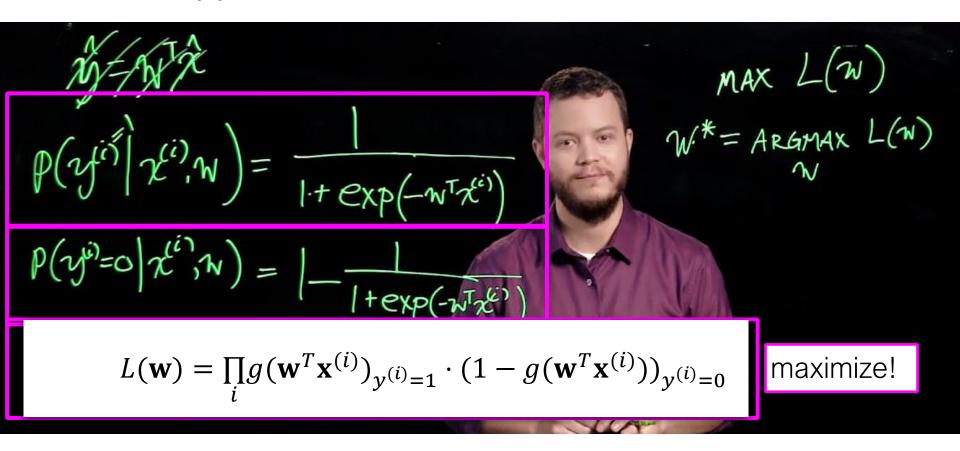
Class Overview, by topic



Logistic Regression

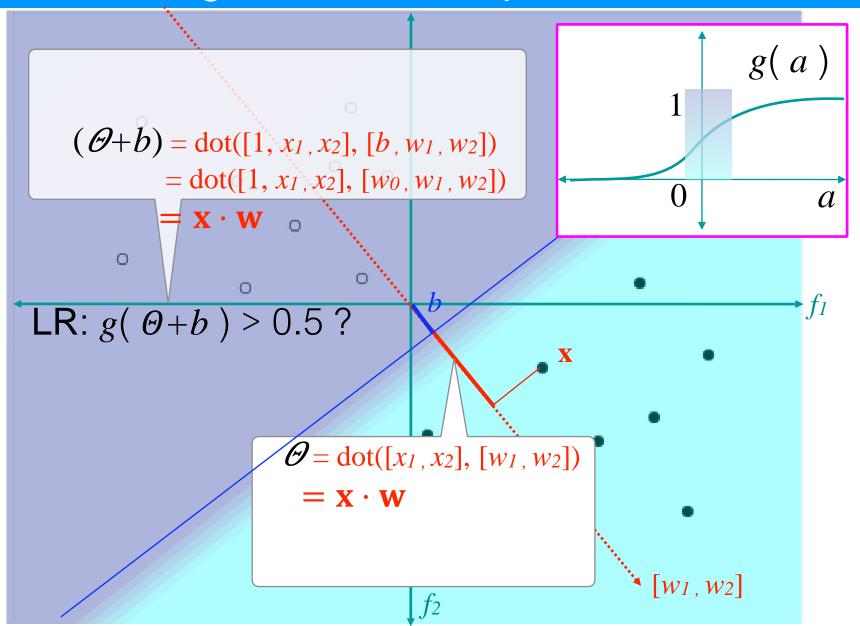
Setting Up Binary Logistic Regression

From flipped lecture:

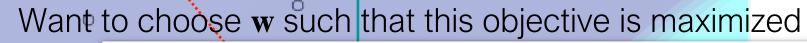


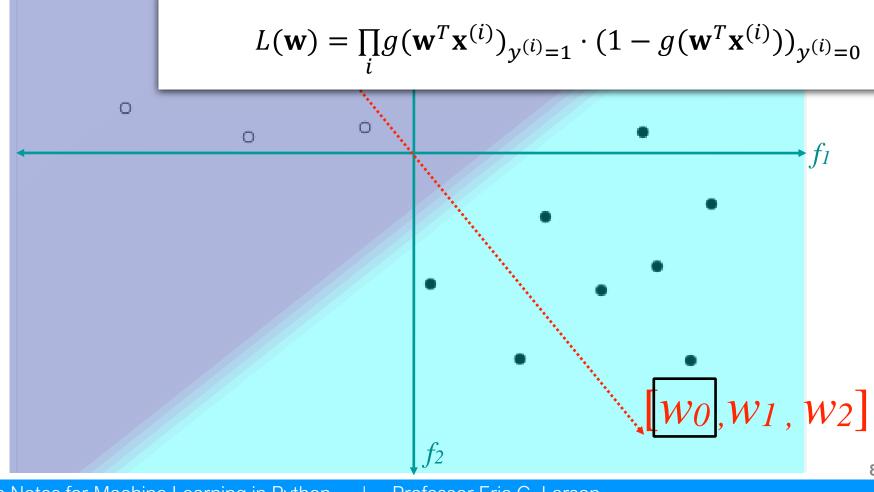
where g(.) is a sigmoid

What do weights and intercept define?



Changing w alters probability





How do you optimize iteratively?

- Objective Function: the function we want to minimize or maximize
- Parameters: what are the parameters of the model that we can change?
- Update Formula: what update "step"can we take for these parameters to optimize the objective function?

$$L(\mathbf{w}) = \prod_{i} g(\mathbf{w}^T \mathbf{x}^{(i)})_{y^{(i)}=1} \cdot (1 - g(\mathbf{w}^T \mathbf{x}^{(i)}))_{y^{(i)}=0}$$

Logistic Regression Optimization Procedure

$$L(\mathbf{w}) = \prod_i g(\mathbf{w}^T \mathbf{x}^{(i)})_{y^{(i)}=1} \cdot (1 - g(\mathbf{w}^T \mathbf{x}^{(i)}))_{y^{(i)}=0}$$

Simplify $L(\mathbf{w})$ with **logarithm**, $l(\mathbf{w})$

$$l(\mathbf{w}) = \sum_{i} y^{(i)} \ln(g(\mathbf{w}^T \mathbf{x}^{(i)})) + (1 - y^{(i)}) \ln(1 - g(\mathbf{w}^T \mathbf{x}^{(i)}))$$

Take Gradient

$$\frac{\partial}{\partial w_j} l(\mathbf{w}) = -\sum_i (y^{(i)} - g(\mathbf{w}^T \mathbf{x}^{(i)})) x_j^{(i)}$$

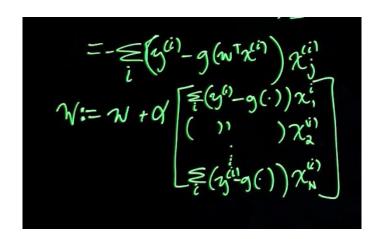
- **Use** gradient to **update** equation for w
 - Video Supplement (also on canvas):
 - https://www.youtube.com/watch?v=FGnoHdjFrJ8

Binary Solution for Update Equation

Use gradient inside update equation for w

$$\frac{\partial}{\partial w_j} l(\mathbf{w}) = -\sum_{i} (y^{(i)} - g(\mathbf{w}^T \mathbf{x}^{(i)})) x_j^{(i)}$$

$$w_j \leftarrow w_j + \eta \sum_{i=1}^{M} (y^{(i)} - g(\mathbf{w}^T \mathbf{x}^{(i)})) x_j^{(i)}$$
 $new \ value \quad old \ value \quad gradient$



Visualizing weight updates with gradient

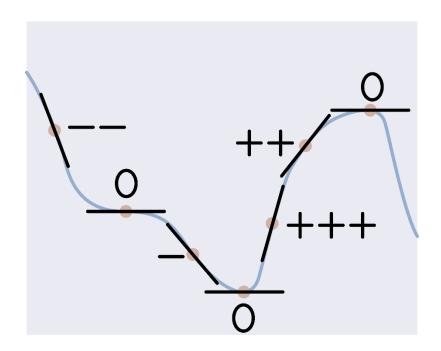
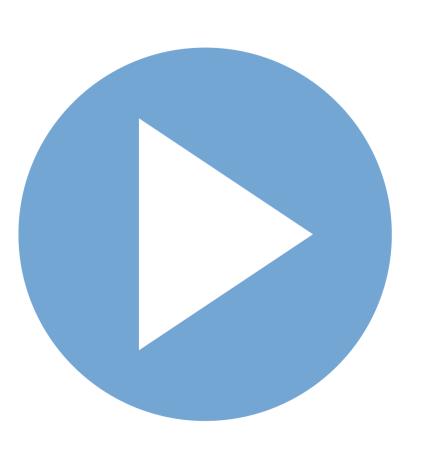


Figure credits: Andrew Glassner

Demo

05. Logistic Regression.ipynb

Programming
Vectorization
Regularization
Multi-class extension



Other Tutorials:

http://blog.yhat.com/posts/logistic-regression-python-rodeo.html

http://scikit-learn.org/stable/auto_examples/linear_model/plot_iris_