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1 EECS 442 PS2: Frequency and Signal Processing

Please provide the following information (e.g. Aparajito Saha, rajsaha):

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```
Important: after you download the .ipynb file, please name it ____<your_uniqname>__<your_umid>.ipynb___ before you submit it to Canvas.
```

Example: rajsaha_00000000.ipynb.

2 Setup

Run the following code to import the modules you'll need. After your finish the assignment, remember to run all the cells and save the notebook to your local machine as a .ipynb file for Canvas submission.

```
[2]: import numpy as np, matplotlib as mpl, matplotlib.pyplot as plt, os
  import urllib.request
  import math
  from PIL import Image
  import scipy.ndimage # For image filtering
  from scipy import signal
  from scipy import fft
  import imageio # For loading images
  import ssl
  ssl._create_default_https_context = ssl._create_unverified_context
```

3 Problem 2.1: Image blending

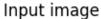
3.1 (a) Reconstructing an image

In this problem, we construct a Laplacian pyramid with 4 levels. We use the Laplacian pyramid to reconstruct the original image.

```
img = Image.open('bbb.jpg')
img = img.resize((400,200))
img=np.array(img)

plt.figure()
plt.title('Input image')
plt.axis('off')
plt.imshow(img)
```

[3]: <matplotlib.image.AxesImage at 0x7b36d3f30650>





[4]: (1440, 808)

```
[5]: def pyramid_upsample(img, kernel_size=(5,5)):

"""

Upsamples the given pyramid image.

Input:

- img: an image of shape M x N x C
```

```
- kernel_size: a tuple representing the shape of the 2D kernel
 Returns:
  - upsampled: an image represented as an array of shape 2M x 2N x C
 # TODO: Implement pyramid upsampling.
 # Insert zeros between pixels
 upsampled = np.zeros((img.shape[0] * 2, img.shape[1] * 2, img.shape[2]))
 upsampled[::2, ::2, :] = img
 # Apply Gaussian filter (sigma=1)
 radius = (kernel_size[0]//2, kernel_size[1]//2, 0)
 upsampled = scipy.ndimage.gaussian_filter(upsampled, sigma=1, radius=radius)__
→* 4
 END OF YOUR CODE
 return upsampled
def pyramid downsample(img, kernel size=(5,5)):
 Downsamples the given pyramid image.
 Input:
  - imq: an image of shape M x N x C
  - kernel_size: a tuple representing the shape of the 2D kernel
 Returns:
  - downsampled: an image of shape M/2 \times N/2 \times C
 # TODO: Implement pyramid downsampling.
 # Apply Gaussian filter (sigma=1)
 radius = (kernel_size[0]//2, kernel_size[1]//2, 0)
 blurred img = scipy.ndimage.gaussian filter(img, sigma=1, radius=radius)
 # discard every other pixel
 downsampled = np.zeros((img.shape[0] // 2, img.shape[1] // 2, 3))
 downsampled = blurred_img[::2, ::2, :]
 END OF YOUR CODE
 return downsampled
def gen gaussian pyramid(img, num levels):
```

```
n n n
 Generates an entire Gaussian pyramid.
 Input:
  - imq: an image of shape M x N x C
  - num_levels: number of levels in the Gaussian pyramid
 Return:
  - gp: list, the generated levels (imgs) of the Gaussian pyramid
 # TODO: Construct a Gaussian pyramid given a base image `img`.
 gp = []
 for i in range(num levels):
  if i == 0:
   gp = [img]
  else:
   gp.append(pyramid_downsample(gp[i-1]))
 END OF YOUR CODE
 return gp
def gen_laplacian_pyramid(gp, num_levels):
 Generates an entire Laplacian pyramid.
  gp: list, levels of a Gaussian pyramid
 Return:
  lp: list, the generated levels (imgs) of the Laplacian pyramid
 # TODO: Construct a Laplacian pyramid qiven a base Gaussian pyramid `qp`.
 lp = [gp[-1]]
 for i in range(num_levels-1, 0, -1):
  level = (gp[i - 1] - pyramid_upsample(gp[i]))
  lp.append(level)
 END OF YOUR CODE
 return lp
def reconstruct_img(lp):
 Reconstructs an image using a laplacian pyramid.
 Input:
```

```
[6]: # Run above functions and visualize results on bbb.jpg
     img = np.array(img).astype('float')
     num_levels = 4 # including the original img
     gp = gen_gaussian_pyramid(img, num_levels)
     lp = gen_laplacian_pyramid(gp, num_levels)
     recon_img = reconstruct_img(lp)
     print("Gaussian pyramid:")
     for i, level in enumerate(gp):
       print("Level {}:".format(i), level.shape)
       plt.figure(figsize=[plt.rcParams.get('figure.figsize')[0]/(2**i),plt.rcParams.

→get('figure.figsize')[1]/(2**i)])
       plt.title("Level {}:".format(i))
       plt.axis('off')
       level=(level-np.amin(level))/(np.amax(level)-np.amin(level))
       plt.imshow(level)
     print("Laplacian pyramid:")
     for i, level in enumerate(lp):
       print("Level {}:".format(i), level.shape)
       level_plot=level.clip(0, 255).astype('uint8')
       plt.figure(figsize=[plt.rcParams.get('figure.figsize')[0]/
      ⇔(2**(num_levels-i-1)),plt.rcParams.get('figure.figsize')[1]/
      \hookrightarrow (2**(num levels-i-1))])
       plt.title("Level {}:".format(i))
      plt.axis('off')
       plt.imshow(level_plot)
```

```
img=img.astype(np.uint8)
plt.figure()
plt.title("Original Image")
plt.axis('off')
plt.imshow(img)

recon_img=recon_img.astype(np.uint8)
plt.figure()
plt.title("Reconstructed Image")
plt.axis('off')
plt.imshow(recon_img)
```

Gaussian pyramid:

Level 0: (808, 1440, 3)
Level 1: (404, 720, 3)
Level 2: (202, 360, 3)
Level 3: (101, 180, 3)
Laplacian pyramid:
Level 0: (101, 180, 3)
Level 1: (202, 360, 3)
Level 2: (404, 720, 3)
Level 3: (808, 1440, 3)

[6]: <matplotlib.image.AxesImage at 0x7b36c549b110>

Level 0:



Level 1:



Level 2:



Level 3:



Level 0:



Level 1:



Level 2:



Level 3:



Original Image



Reconstructed Image



3.2 (b) Blending two images

In this problem, we blend an image of an orange and an apple.

```
[9]: # Download the `orange.jpg` and `apple.jpg` images.
base_url = 'https://www.eecs.umich.edu/courses/eecs442/fa24/ims'
for name in ['orange.jpg', 'apple-ps2.jpg']:
```

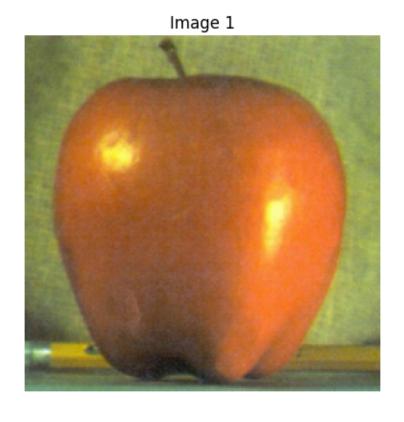
```
[10]: def pyramid_blend(img1, img2, mask, num_levels=6):
      This function produces the Laplacian pyramid blend of two images.
       - img1: N x M x C uint8 array image
       - imq2: N x M x C uint8 array image
       - mask: N x M array, all elements are either Os or 1s
       - num_levels: int, height of the pyramid
      Return:
       - img_blend: the blended image, an N x M x C uint8 array
      # Build Gaussian pyramids for img1, img2, and mask
      gp1, gp2, gpm = gen_gaussian_pyramid(img1, num_levels),__
      →num levels)
      # Build Laplacian pyramids for imq1 and imq2
      lp1, lp2, lpm = gen_laplacian_pyramid(gp1, num_levels),__
     ogen_laplacian_pyramid(gp2, num_levels), gen_laplacian_pyramid(gpm, u
     →num_levels)
      # TODO: Construct the Laplacian pyramid and use it to blend the images.
      blended_pyramid = []
      for i, (11, 12) in enumerate(zip(lp1, lp2)):
```

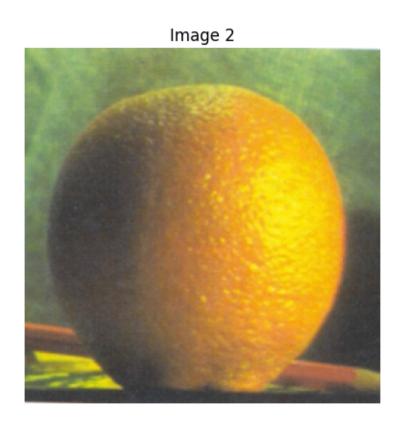
Please describe the difference between the blended images as the number of levels in the Laplacian pyramid varies: how does the result change as we increase the number of levels?

Answer: As the number of levels in the Laplacian pyramid increases, the blending becomes smoother, with a more gradual transition at the boundaries, which reduces the visibility of sharp edges in the blended regions.

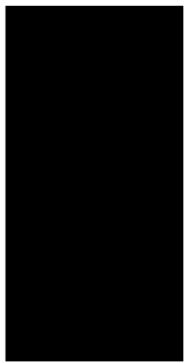
```
[11]: # Display images and mask
      # Plotting image 1 - Apple
      plt.figure()
      plt.title('Image 1')
      plt.axis('off')
      plt.imshow(img1)
      # Plotting image 2 - Orange
      plt.figure()
      plt.title('Image 2')
      plt.axis('off')
      plt.imshow(img2)
      # Plotting the mask
      plt.figure()
      plt.title('Mask')
      plt.axis('off')
      plt.imshow(mask * 255)
```

[11]: <matplotlib.image.AxesImage at 0x7b36ba4f0b90>

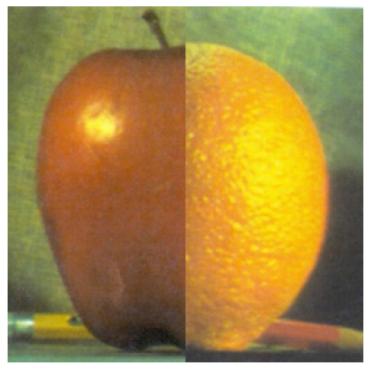




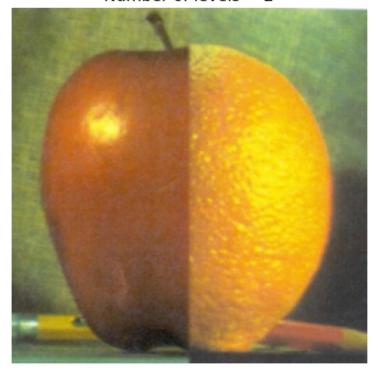
Mask

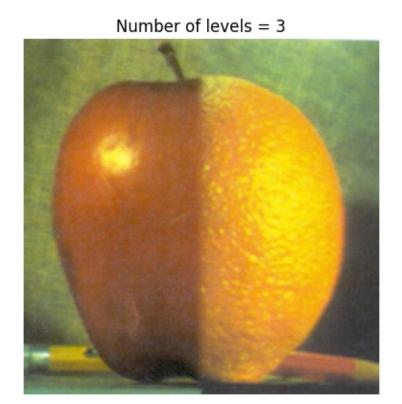


Number of levels = 1

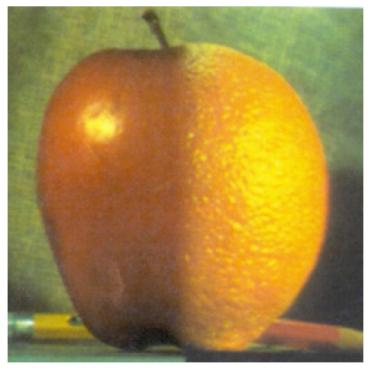


Number of levels = 2

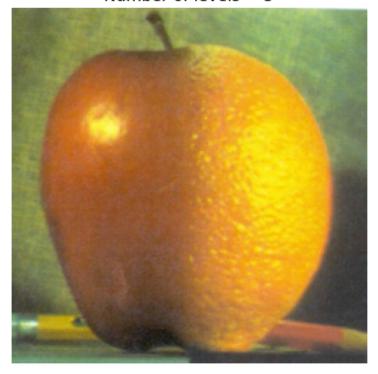




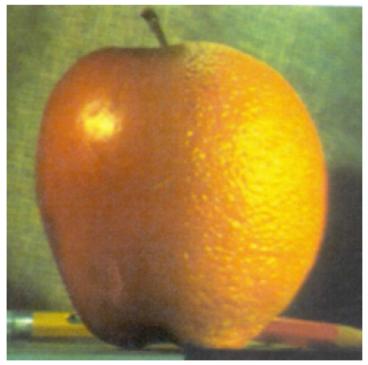
Number of levels = 4



Number of levels = 5







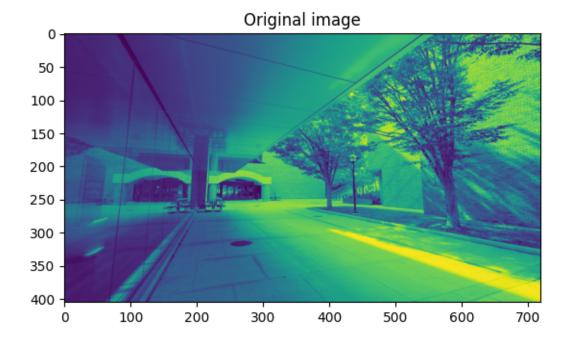
4 Problem 2.2: 2D DFT and the Convolution Theorem

(a) Please match the images in the left column of Figure 2 to their corresponding spectrum visualization in the right column.

Answer: 1:E, 2:C, 3:D, 4:A, 5:B

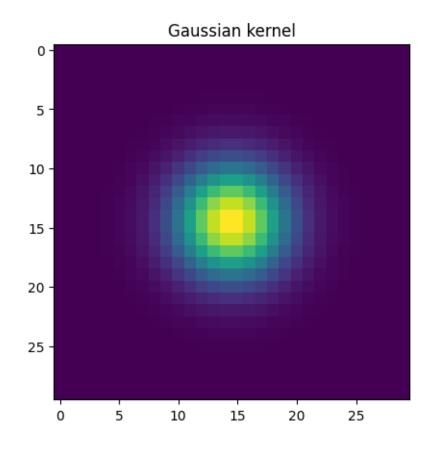
(b) In this problem, we compare the output of a Gaussian filter through i) direct convolution in the spatial domain and ii) multiplication in the frequency domain.

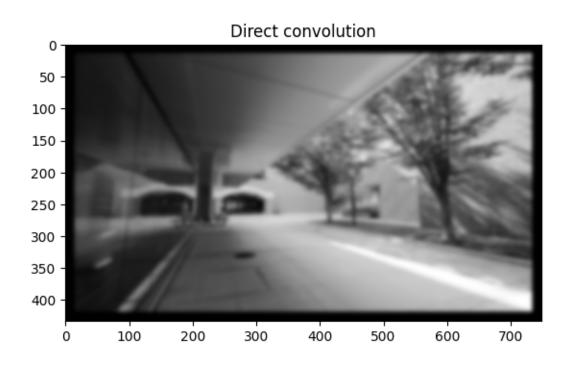
```
img = img.resize((new_width, new_height))
img = np.array(img)
plt.figure()
plt.imshow(img)
plt.title('Original image')
plt.show()
# Make a 2-D kernel Gaussian kernel
t = np.linspace(-10, 10, 30)
bump = np.exp(-0.1*t**2)
bump /= np.trapz(bump) # normalize the integral to 1
kernel = bump[:, np.newaxis] * bump[np.newaxis, :]
plt.imshow(kernel)
plt.title('Gaussian kernel')
plt.show()
# Convolution in spatial domain
# TODO: Convolve the gaussian filter with the image in the spatial domain. #
img1 = signal.convolve2d(img, kernel)
END OF YOUR CODE
plt.figure()
plt.title('Direct convolution')
plt.imshow(img1, cmap='gray')
plt.show()
# Multiplication in frequency domain
# This shape needs to be passed into the fft2 function
shape = (img.shape[0]+kernel.shape[0]-1, img.shape[1]+kernel.shape[1]-1)
# TODO: Use the convolution theorem to convolve the provided image with
                                                   #
     a Gaussian filter.
# Perform FFT on the image and kernel
img_fft = fft.fft2(img, shape)
kernel_fft = fft.fft2(kernel, shape)
# Multiply in the frequency domain and perform inverse FFT
img2 = fft.ifft2(img_fft * kernel_fft).real
```

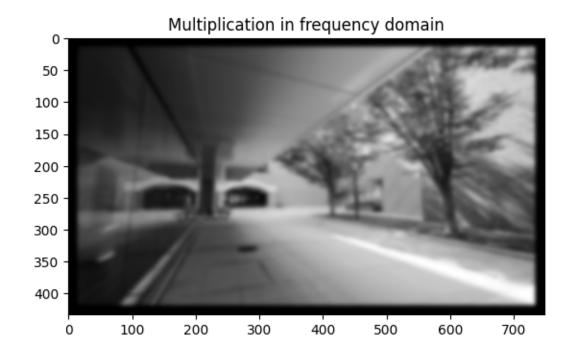


/tmp/ipython-input-1727537708.py:22: DeprecationWarning: `trapz` is deprecated. Use `trapezoid` instead, or one of the numerical integration functions in `scipy.integrate`.

bump /= np.trapz(bump) # normalize the integral to 1



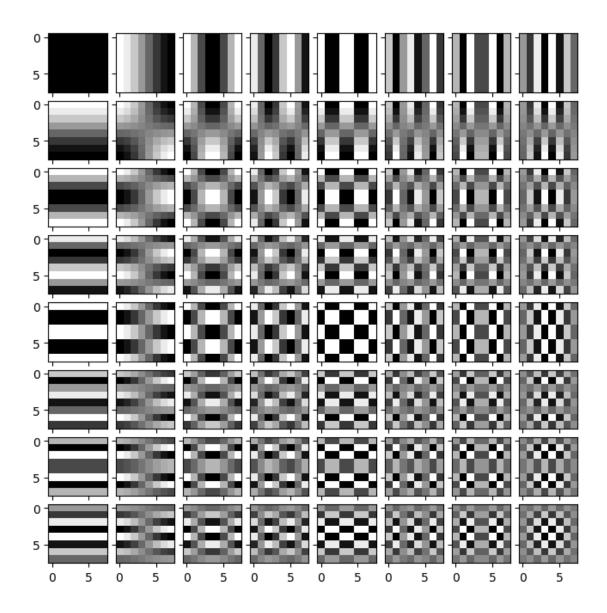




5 Problem 2.3 JPEG: Image Compression

5.1 (a) Basis for 2D Discrete Cosine Transform

```
#
                            END OF YOUR CODE
 → #
return DCT_basis
# Build the DCT basis and visualize it.
import matplotlib.pyplot as plt
from mpl_toolkits.axes_grid1 import ImageGrid
Nx, Ny = 8, 8
DCT_basis = build_2D_DCT_basis(Nx, Ny)
fig = plt.figure(figsize=(8., 8.))
grid = ImageGrid(fig, 111, # similar to subplot(111)
             nrows_ncols=(Ny, Nx), # creates a grid of axes
             axes_pad=0.1, # pad between axes in inch.
for ax, im in zip(grid, DCT_basis.reshape(-1,Ny,Nx)):
   # Iterating over the grid returns the Axes.
   ax.imshow(im, cmap = 'gray')
plt.show()
```



5.2 (b) 2D Discrete Cosine Transform

```
[15]: def DCT_2D(image_patch):
    """

    2D DCT transform of image patch of shape (H,W)
    """

    H,W = image_patch.shape
    DCT_basis = build_2D_DCT_basis(W,H)
    DCT_coeffcients = np.zeros([H,W])

    for h in range(H):
        for w in range(W):
```

```
norm_const_h = 1/np.sqrt(H) if h == 0 else np.sqrt(2/H)
      norm_const_w = 1/np.sqrt(W) if w == 0 else np.sqrt(2/W)
      DCT_coeffcients[h,w] = norm_const h * norm_const w * (DCT_basis[h, w] *__
 →image_patch).sum()
 return DCT_coeffcients
def IDCT 2D(image spectrum):
  2D inverse DCT trasform.
 H,W = image_spectrum.shape
 DCT_basis = build_2D_DCT_basis(W,H)
 image = np.zeros([H,W])
 norm_matrix = 1/np.sqrt(H*W) * np.ones([H,W])
 norm_matrix[1:,0] *= np.sqrt(2)
 norm_matrix[0,1:] *= np.sqrt(2)
 norm matrix[1:,1:] *= 2
 for h in range(H):
   for w in range(W):
     norm const h = 1/np.sqrt(H) if h == 0 else np.sqrt(2/H)
     norm_const_w = 1/np.sqrt(W) if w == 0 else np.sqrt(2/W)
      image += norm_const_h * norm_const_w * (DCT_basis[h, w] *_
 →image_spectrum[h,w])
 return image
image patch = np.random.rand(8,8)
# Verify above gives same result as using scipy fftpack
from scipy import fftpack
def dct_2d(image):
   return fftpack.dct(fftpack.dct(image.T, norm='ortho').T, norm='ortho')
def idct 2d(image):
   return fftpack.idct(fftpack.idct(image.T, norm='ortho').T, norm='ortho')
print(np.abs(DCT 2D(image patch) - dct 2d(image patch)).sum())
print(np.abs(IDCT_2D(image_patch) - idct_2d(image_patch)).sum())
```

- 3.1787072973799013e-14
- 2.256875242245826e-14

5.3 (c) JPEG Image Compression

```
[17]: #Download the image to be compressed
!wget -O original-ps2.png "https://www.eecs.umich.edu/courses/eecs442/fa24/ims/
original-ps2.png"
```

```
--2025-09-17 01:43:53--
https://www.eecs.umich.edu/courses/eecs442/fa24/ims/original-ps2.png
```

```
Resolving www.eecs.umich.edu (www.eecs.umich.edu)... 141.212.113.116
Connecting to www.eecs.umich.edu (www.eecs.umich.edu)|141.212.113.116|:443... connected.
```

ERROR: cannot verify www.eecs.umich.edu's certificate, issued by 'CN=InCommon RSA Server CA 2,0=Internet2,C=US':

Unable to locally verify the issuer's authority.

To connect to www.eecs.umich.edu insecurely, use `--no-check-certificate'.

5.3.1 Utility functions

We will first define some utility functions. You don't need to implement anything in this block or read all of its details. The only important functions in this part you may want to look at to understand better are quantize and load quantization table.

```
[18]: # We will first define some utility functions. You don't need to implement
      →anything in this block or read all of its details.
      # The only important functions in this part you may want to look at to,
       →understand better are 'quantize' and 'load_quantization_table'.
      # Code in this part is based on https://qithub.com/qhallak/jpeq-python
      from queue import PriorityQueue
      class HuffmanTree:
        Class for creating Huffman Table, given an input array. The huffman encodes
        input data based on their appearance frequency,
        i.e., assign a shorter code for more frequently appearing values.
        def __init__(self, arr):
            q = PriorityQueue()
            # calculate frequencies and insert them into a priority queue
            for val, freq in self.__calc_freq(arr).items():
                q.put(self.__Node.init_leaf(val, freq))
            while q.qsize() >= 2:
                u = q.get()
                v = q.get()
                q.put(self.__Node.init_node(u, v))
            self. root = q.get()
            # dictionaries to store huffman table
            self.__value_to_bitstring = dict()
        def value_to_bitstring_table(self):
            if len(self._value_to_bitstring.keys()) == 0:
                self.__create_huffman_table()
            return self.__value_to_bitstring
        def __create_huffman_table(self):
            def tree_traverse(current_node, bitstring=''):
                if current_node is None:
                    return
```

```
if current_node.is_leaf():
            self.__value_to_bitstring[current_node.value] = bitstring
        tree_traverse(current_node.left_child, bitstring + '0')
        tree_traverse(current_node.right_child, bitstring + '1')
    tree_traverse(self.__root)
def __calc_freq(self, arr):
   freq_dict = dict()
    for elem in arr:
        if elem in freq_dict:
            freq_dict[elem] += 1
        else:
            freq_dict[elem] = 1
    return freq_dict
class __Node:
    def __init__(self, value, freq, left_child, right_child):
        self.value = value
        self.freq = freq
        self.left_child = left_child
        self.right_child = right_child
    @classmethod
    def init_leaf(cls, value, freq):
        return cls(value, freq, None, None)
    @classmethod
    def init_node(cls, left_child, right_child):
        freq = left_child.freq + right_child.freq
        return cls(None, freq, left_child, right_child)
    def is_leaf(self):
        return self.value is not None
    def __eq__(self, other):
        stup = self.value, self.freq, self.left_child, self.right_child
        otup = other.value, other.freq, other.left_child, other.right_child
        return stup == otup
    def __nq__(self, other):
        return not (self == other)
    def __lt__(self, other):
        return self.freq < other.freq</pre>
```

```
def __le__(self, other):
      return self.freq < other.freq or self.freq == other.freq</pre>
   def __gt__(self, other):
      return not (self <= other)</pre>
   def __ge__(self, other):
      return not (self < other)</pre>
def load_quantization_table(component):
  # Quantization tables determine how much DCT coefficents are divided during
  # quantization. Larger value means it is more likely to be a O after
\hookrightarrow division.
  # Setting large values like 100000 means that frequency component is set to \Box
\hookrightarrow 0 for sure.
  if component == 'dc_only':
     q = np.array([[1, 100000, 100000, 100000, 100000, 100000, 100000]
→100000],
              →100000],
              →100000],
              →100000],
              →1000001.
              [100000, 100000, 100000, 100000, 100000, 100000, 100000, 100000, 100000]
→100000].
              →100000],
              →100000]])
  elif component == 'first_3':
     q = np.array([[1, 1, 100000, 100000, 100000, 100000, 100000],
              →1000001.
              →100000],
              →100000],
              [100000, 100000, 100000, 100000, 100000, 100000, 100000, 100000]
→100000].
              →100000],
              →100000].
```

```
[100000, 100000, 100000, 100000, 100000, 100000, 100000, 100000]
→100000]])
  elif component == 'first_6':
     q = np.array([[1, 1, 1, 100000, 100000, 100000, 100000, 100000],
               [1, 1, 100000, 100000, 100000, 100000, 100000, 100000],
               →100000],
               →100000],
               →100000],
               →100000],
               →100000],
               [100000, 100000, 100000, 100000, 100000, 100000, 100000, __
→100000]])
  elif component == 'first_10':
     q = np.array([[1, 1, 1, 1, 100000, 100000, 100000, 100000],
               [1, 1, 1, 100000, 100000, 100000, 100000, 100000],
               [1, 1, 100000, 100000, 100000, 100000, 100000, 100000],
               [1, 100000, 100000, 100000, 100000, 100000, 100000, __
→100000],
               [100000, 100000, 100000, 100000, 100000, 100000, 100000, __
→100000].
               →100000],
               →100000].
               →100000]])
  #q1 and q2 are some more realistic quantization values. You can try these, \Box
→but no need to report any result from using 'q1' or 'q2'.
  elif component == 'q1':
     q = np.array([[2, 2, 2, 2, 3, 4, 5, 6],
               [2, 2, 2, 2, 3, 4, 5, 6],
               [2, 2, 2, 2, 4, 5, 7, 9],
               [2, 2, 2, 4, 5, 7, 9, 12],
               [3, 3, 4, 5, 8, 10, 12, 12],
               [4, 4, 5, 7, 10, 12, 12, 12],
               [5, 5, 7, 9, 12, 12, 12, 12],
               [6, 6, 9, 12, 12, 12, 12, 12]])
  elif component == 'q2':
     q = np.array([[16, 11, 10, 16, 24, 40, 51, 61],
               [12, 12, 14, 19, 26, 58, 60, 55],
```

```
[14, 13, 16, 24, 40, 57, 69, 56],
                      [14, 17, 22, 29, 51, 87, 80, 62],
                      [18, 22, 37, 56, 68, 109, 103, 77],
                      [24, 35, 55, 64, 81, 104, 1113, 92],
                      [49, 64, 78, 87, 103, 121, 120, 101],
                      [72, 92, 95, 98, 112, 100, 103, 99]])
    else:
        raise ValueError((
            "Unrecognized compoents, '{comp}' was found").format(comp=component))
    return q
def zigzag_points(rows, cols):
    # constants for directions
    UP, DOWN, RIGHT, LEFT, UP_RIGHT, DOWN_LEFT = range(6)
    # move the point in different directions
    def move(direction, point):
        return {
            UP: lambda point: (point[0] - 1, point[1]),
            DOWN: lambda point: (point[0] + 1, point[1]),
            LEFT: lambda point: (point[0], point[1] - 1),
            RIGHT: lambda point: (point[0], point[1] + 1),
            UP_RIGHT: lambda point: move(UP, move(RIGHT, point)),
            DOWN_LEFT: lambda point: move(DOWN, move(LEFT, point))
        }[direction](point)
    # return true if point is inside the block bounds
    def inbounds(point):
        return 0 <= point[0] < rows and 0 <= point[1] < cols</pre>
    # start in the top-left cell
    point = (0, 0)
    # True when moving up-right, False when moving down-left
    move_up = True
    for i in range(rows * cols):
        yield point
        if move_up:
            if inbounds(move(UP_RIGHT, point)):
                point = move(UP_RIGHT, point)
            else:
                move_up = False
                if inbounds(move(RIGHT, point)):
                    point = move(RIGHT, point)
                else:
                    point = move(DOWN, point)
        else:
            if inbounds(move(DOWN_LEFT, point)):
                point = move(DOWN_LEFT, point)
```

```
else:
                move_up = True
                if inbounds(move(DOWN, point)):
                    point = move(DOWN, point)
                else:
                    point = move(RIGHT, point)
def bits_required(n):
   n = abs(n)
    result = 0
    while n > 0:
        n >>= 1
        result += 1
    return result
def binstr_flip(binstr):
    # check if binstr is a binary string
    if not set(binstr).issubset('01'):
        raise ValueError("binstr should have only '0's and '1's")
    return ''.join(map(lambda c: '0' if c == '1' else '1', binstr))
def uint_to_binstr(number, size):
    return bin(number)[2:][-size:].zfill(size)
def int_to_binstr(n):
    if n == 0:
        return ''
    binstr = bin(abs(n))[2:]
    # change every 0 to 1 and vice verse when n is negative
    return binstr if n > 0 else binstr_flip(binstr)
def flatten(lst):
    return [item for sublist in 1st for item in sublist]
#Utility functions for encoding and writing to files below
def quantize(block, component):
    q = load_quantization_table(component)
    return (block / q).round().astype(np.int32)
def block to zigzag(block):
    return np.array([block[point] for point in zigzag_points(*block.shape)])
def run_length_encode(arr):
    # determine where the sequence is ending prematurely
    last_nonzero = -1
    for i, elem in enumerate(arr):
```

```
if elem != 0:
            last_nonzero = i
    # each symbol is a (RUNLENGTH, SIZE) tuple
    symbols = []
    # values are binary representations of array elements using SIZE bits
    values = []
    run_length = 0
    for i, elem in enumerate(arr):
        if i > last_nonzero:
            symbols.append((0, 0))
            values.append(int_to_binstr(0))
            break
        elif elem == 0 and run_length < 15:</pre>
            run_length += 1
        else:
            size = bits_required(elem)
            symbols.append((run_length, size))
            values.append(int_to_binstr(elem))
            run_length = 0
    return symbols, values
def write_to_file(filepath, dc, ac, blocks_count, tables):
    try:
        f = open(filepath, 'w')
    except FileNotFoundError as e:
        raise FileNotFoundError(
                "No such directory: {}".format(
                    os.path.dirname(filepath))) from e
    #f.write('1')
    for table_name in ['dc_y', 'ac_y']:
        # 16 bits for 'table_size'
        f.write(uint_to_binstr(len(tables[table_name]), 16))
        for key, value in tables[table_name].items():
            if table_name == 'dc_y':
                # 4 bits for the 'category'
                # 4 bits for 'code_length'
                # 'code_length' bits for 'huffman_code'
                f.write(uint_to_binstr(key, 4))
                f.write(uint_to_binstr(len(value), 4))
                f.write(value)
            else:
```

```
# 4 bits for 'run_length'
                # 4 bits for 'size'
                # 8 bits for 'code_length'
                # 'code_length' bits for 'huffman_code'
                f.write(uint_to_binstr(key[0], 4))
                f.write(uint_to_binstr(key[1], 4))
                f.write(uint_to_binstr(len(value), 8))
                f.write(value)
    # 32 bits for 'blocks_count'
    f.write(uint_to_binstr(blocks_count, 32))
    for b in range(blocks_count):
        for c in range(1):
            category = bits_required(dc[b, c])
            symbols, values = run_length_encode(ac[b, :, c])
            dc_table = tables['dc_y']
            ac_table = tables['ac_y']
            f.write(dc_table[category])
            f.write(int_to_binstr(dc[b, c]))
            #bit count ac = 0
            for i in range(len(symbols)):
                f.write(ac_table[tuple(symbols[i])])
                f.write(values[i])
                \#bits\_written = len(ac\_table[tuple(symbols[i])]) +_{\sqcup}
 \rightarrow len(values[i])
                #bit_count_ac += bits_written
            #print('Block {}:{} bits'.format(b,bit_count_ac))
    f.close()
def HuffmanEncode im(filepath, im):
    """Huffman encoding the gray scale image directly.
        filepath: [Location to save the encoded file]
        im ([numpy array]): Shape (H, W)
    im = im.flatten()
    pixel_count = len(im)
    f = open(filepath,'w')
    H_Tree = HuffmanTree(im.flatten())
    H_table = H_Tree.value_to_bitstring_table()
    # 16 bits for 'table_size'
    f.write(uint_to_binstr(len(H_table), 16))
```

```
for key, value in H_table.items():
            # 4 bits for the 'category'
            # 4 bits for 'code_length'
            # 'code_length' bits for 'huffman_code'
            f.write(uint_to_binstr(key, 4))
            f.write(uint_to_binstr(len(value), 4))
            f.write(value)
    # 32 bits for 'pixel_count'
    f.write(uint_to_binstr(pixel_count, 32))
    for item in im:
        f.write(H_table[item])
    f.close()
def write_as_binary(string_file_path, output_file_path):
    f = open(string_file_path,'r')
    binary_string = f.read()
    f_binary = open(output_file_path,mode='wb')
    #Remainder bits are not written for simplicity.
    for i in range(len(binary_string) // 8):
        byte = bytes([int(binary_string[8*i:8*i+8],2)])
        f_binary.write(byte)
    f.close()
    f_binary.close()
# Utility functions for decode
class JPEGFileReader:
    TABLE\_SIZE\_BITS = 16
    BLOCKS_COUNT_BITS = 32
    DC\_CODE\_LENGTH\_BITS = 4
    CATEGORY_BITS = 4
    AC_CODE_LENGTH_BITS = 8
    RUN_LENGTH_BITS = 4
    SIZE BITS = 4
    def __init__(self, filepath):
        self.__file = open(filepath, 'r')
    def read_int(self, size):
        if size == 0:
            return 0
        # the most significant bit indicates the sign of the number
```

```
bin_num = self.__read_str(size)
    if bin_num[0] == '1':
        return self.__int2(bin_num)
    else:
        return self.__int2(binstr_flip(bin_num)) * -1
def read_dc_table(self):
    table = dict()
    table_size = self.__read_uint(self.TABLE_SIZE_BITS)
    for _ in range(table_size):
        category = self.__read_uint(self.CATEGORY_BITS)
        code_length = self.__read_uint(self.DC_CODE_LENGTH_BITS)
        code = self.__read_str(code_length)
        table[code] = category
    return table
def read_ac_table(self):
    table = dict()
    table_size = self.__read_uint(self.TABLE_SIZE_BITS)
    for _ in range(table_size):
        run_length = self.__read_uint(self.RUN_LENGTH_BITS)
        size = self. read uint(self.SIZE BITS)
        code_length = self.__read_uint(self.AC_CODE_LENGTH_BITS)
        code = self.__read_str(code_length)
        table[code] = (run_length, size)
    return table
def read_blocks_count(self):
    return self.__read_uint(self.BLOCKS_COUNT_BITS)
def read_huffman_code(self, table):
    prefix = ''
    while prefix not in table:
        prefix += self.__read_char()
    return table[prefix]
def __read_uint(self, size):
    if size <= 0:
        raise ValueError("size of unsigned int should be greater than 0")
    return self.__int2(self.__read_str(size))
def __read_str(self, length):
    return self.__file.read(length)
def __read_char(self):
```

```
return self.__read_str(1)
    def __int2(self, bin_num):
        return int(bin_num, 2)
def read_image_file(filepath):
    reader = JPEGFileReader(filepath)
    tables = dict()
    for table_name in ['dc_y', 'ac_y']:
        if 'dc' in table_name:
            tables[table_name] = reader.read_dc_table()
        else:
            tables[table_name] = reader.read_ac_table()
    blocks_count = reader.read_blocks_count()
    dc = np.empty((blocks_count, 1), dtype=np.int32)
    ac = np.empty((blocks_count, 63, 1), dtype=np.int32)
    for block_index in range(blocks_count):
        for component in range(1):
            dc_table = tables['dc_y']
            ac_table = tables['ac_y']
            category = reader.read_huffman_code(dc_table)
            dc[block_index, component] = reader.read_int(category)
            cells_count = 0
            while cells_count < 63:</pre>
                run_length, size = reader.read_huffman_code(ac_table)
                if (run_length, size) == (0, 0):
                    while cells_count < 63:</pre>
                        ac[block_index, cells_count, component] = 0
                        cells_count += 1
                else:
                    for i in range(run_length):
                        ac[block_index, cells_count, component] = 0
                        cells count += 1
                    if size == 0:
                        ac[block_index, cells_count, component] = 0
                    else:
                        value = reader.read_int(size)
                        ac[block_index, cells_count, component] = value
                    cells_count += 1
```

```
return dc, ac, tables, blocks_count

def zigzag_to_block(zigzag):
    # assuming that the width and the height of the block are equal
    rows = cols = int(math.sqrt(len(zigzag)))

if rows * cols != len(zigzag):
    raise ValueError("length of zigzag should be a perfect square")

block = np.empty((rows, cols), np.int32)

for i, point in enumerate(zigzag_points(rows, cols)):
    block[point] = zigzag[i]

return block

def dequantize(block, component):
    q = load_quantization_table(component)
    return block * q
```

5.3.2 Encoding and Decoding

```
[]: # Encoding
   # Path to the input image file to be compressed.
   input_file = './original-ps2.png'
   # Path for the encoded code file.
   output_file = './encoded_as_string'
   # TODO: Specify the quantization table to use here.
   # Your options: 'dc_only', 'first_3', 'first_6', 'first_10'
                                                   #
   quantization_table = load_quantization_table('first_10')
   END OF YOUR CODE
   image = Image.open(input_file)
   npmat = np.array(image, dtype=np.int16)[:,:,None]
   rows, cols = npmat.shape[0], npmat.shape[1]
   # block size: 8x8
   if rows % 8 == cols % 8 == 0:
```

```
blocks_count = rows // 8 * cols // 8
else:
   raise ValueError(("the width and height of the image should both be_
 →mutiples of 8"))
# dc is the top-left cell of the block, ac are all the other cells
dc = np.empty((blocks_count, 1), dtype=np.int32)
ac = np.empty((blocks count, 63, 1), dtype=np.int32)
block_index = 0
for i in range(0, rows, 8):
   for j in range(0, cols, 8):
       for k in range(1):
            # split 8x8 block and center the data range on zero
            # [0, 255] --> [-128, 127]
            block = npmat[i:i+8, j:j+8, k] - 128
            dct matrix = DCT 2D(block)
            quant_matrix = quantize(dct_matrix,quantization_table)
            zz = block_to_zigzag(quant_matrix)
            dc[block index, k] = zz[0]
            ac[block_index, :, k] = zz[1:]
       block_index += 1
H_DC_Y = HuffmanTree(np.vectorize(bits_required)(dc[:, 0]))
H_AC_Y = HuffmanTree(flatten(run_length_encode(ac[i, :, 0])[0] for i in_
 →range(blocks_count)))
tables = {'dc_y': H_DC_Y.value_to_bitstring_table(), 'ac_y': H_AC_Y.
 →value_to_bitstring_table()}
write_to_file(output_file, dc, ac, blocks_count, tables)
write_as_binary(output_file, 'encoded_as_binary')
print('Finished encoding and writing data to file.')
# Printing the original image size and compressed file size
file_name = "original-ps2.png"
file_stats = os.stat(file_name)
size_ori = file_stats.st_size / (1024)
print('Orignal image size is {:.0f} kB'.format(size_ori))
file name = "encoded as binary"
file_stats = os.stat(file_name)
size_compressed = file_stats.st_size / (1024)
print('Compressed file size is {:.0f} kB'.format(size_compressed))
```

```
print('Compression ratio is {:.2f}'.format(size_compressed/size_ori))
# Decoding
# Path to the encoded as string file.
encoded_string_file = 'encoded_as_string'
dc, ac, tables, blocks_count = read_image_file(encoded_string_file)
# Assuming that the block is a 8x8 square
block_side = 8
# Assuming that the image height and width are equal
image_side = int(math.sqrt(blocks_count)) * block_side
blocks_per_line = image_side // block_side
npmat = np.empty((image_side, image_side, 1), dtype=np.uint8)
for block_index in range(blocks_count):
   i = block_index // blocks_per_line * block_side
   j = block_index % blocks_per_line * block_side
   for c in range(1):
       zigzag = [dc[block_index, c]] + list(ac[block_index, :, c])
        quant_matrix = zigzag_to_block(zigzag)
        dct_matrix = dequantize(quant_matrix, quantization_table)
       block = IDCT 2D(dct matrix)
        npmat[i:i+8, j:j+8, c] = (block + 128).clip(0,255)
print('Finished decoding file.')
plt.figure(figsize=(8,8))
plt.imshow(npmat[:,:,0],cmap='gray')
plt.title('Decoded_image')
image = Image.fromarray(npmat[:,:,0], 'L')
image.save('Decoded.png', compress_level=0)
```

Direct Huffman encoding the image, without DCT.

6 Convert Notebook to PDF

```
[]: # generate pdf
     # Please provide the full path of the notebook file below
     # Important: make sure that your file name does not contain spaces!
     notebookpath = '/content/drive/My Drive/EECS 442 - Computer Vision/Hw/hw2/
      opohsun_40183452.ipynb' # Ex: notebookpath = '/content/drive/My Drive/Colab∟
      →Notebooks/EECS 442 Fall 2024 - PS2.ipynb'
     drive mount point = '/content/drive/'
     from google.colab import drive
     drive.mount(drive mount point)
     file_name = notebookpath.split('/')[-1]
     get_ipython().system("apt update && apt install texlive-xetex_
      →texlive-fonts-recommended texlive-generic-recommended")
     get_ipython().system("pip install pypandoc")
     get_ipython().system("apt-get install texlive texlive-xetex texlive-latex-extrau
      ⇔pandoc")
     get_ipython().system("jupyter nbconvert --to PDF {}".format(notebookpath.
      →replace(' ', '\\ ')))
     from google.colab import files
     files.download(notebookpath.split('.')[0]+'.pdf')
    Mounted at /content/drive/
    Hit:1 https://cli.github.com/packages stable InRelease
    Get:2 https://cloud.r-project.org/bin/linux/ubuntu jammy-cran40/ InRelease
    [3,632 B]
    Hit:3 https://developer.download.nvidia.com/compute/cuda/repos/ubuntu2204/x86 64
    InRelease
    Get:4 http://security.ubuntu.com/ubuntu jammy-security InRelease [129 kB]
    Hit:5 http://archive.ubuntu.com/ubuntu jammy InRelease
    Get:6 https://r2u.stat.illinois.edu/ubuntu jammy InRelease [6,555 B]
    Get:7 http://archive.ubuntu.com/ubuntu jammy-updates InRelease [128 kB]
    Get:8 http://archive.ubuntu.com/ubuntu jammy-backports InRelease [127 kB]
    Get:9 https://r2u.stat.illinois.edu/ubuntu jammy/main all Packages [9,278 kB]
    Get:10 http://security.ubuntu.com/ubuntu jammy-security/main amd64 Packages
    [3,311 \text{ kB}]
    Get:11 http://archive.ubuntu.com/ubuntu jammy-updates/universe amd64 Packages
    [1,581 \text{ kB}]
    Get:12 http://archive.ubuntu.com/ubuntu jammy-updates/main amd64 Packages [3,638
    Get:13 https://r2u.stat.illinois.edu/ubuntu jammy/main amd64 Packages [2,799 kB]
    Get:14 http://archive.ubuntu.com/ubuntu jammy-updates/restricted amd64 Packages
    [5,665 kB]
    Hit:15 https://ppa.launchpadcontent.net/deadsnakes/ppa/ubuntu jammy InRelease
    Hit:16 https://ppa.launchpadcontent.net/graphics-drivers/ppa/ubuntu jammy
    InRelease
```

Hit:17 https://ppa.launchpadcontent.net/ubuntugis/ppa/ubuntu jammy InRelease Fetched 26.7 MB in 3s (8,583 kB/s) Reading package lists... Done Building dependency tree... Done Reading state information... Done 38 packages can be upgraded. Run 'apt list --upgradable' to see them. W: Skipping acquire of configured file 'main/source/Sources' as repository 'https://r2u.stat.illinois.edu/ubuntu jammy InRelease' does not seem to provide it (sources.list entry misspelt?) Reading package lists... Done Building dependency tree... Done Reading state information... Done E: Unable to locate package texlive-generic-recommended Collecting pypandoc Downloading pypandoc-1.15-py3-none-any.whl.metadata (16 kB) Downloading pypandoc-1.15-py3-none-any.whl (21 kB) Installing collected packages: pypandoc Successfully installed pypandoc-1.15 Reading package lists... Done Building dependency tree... Done Reading state information... Done The following additional packages will be installed: dvisvgm fonts-droid-fallback fonts-lato fonts-lmodern fonts-noto-mono fonts-texgyre fonts-urw-base35 libapache-pom-java libcmark-gfm-extensions0.29.0.gfm.3 libcmark-gfm0.29.0.gfm.3 libcommons-logging-java libcommons-parent-java libfontbox-java libgs9 libgs9-common libidn12 libijs-0.35 libjbig2dec0 libkpathsea6 libpdfbox-java libptexenc1 libruby3.0 libsynctex2 libteckit0 libtexlua53 libtexluajit2 libwoff1 libzzip-0-13 lmodern pandoc-data poppler-data preview-latex-style rake ruby ruby-net-telnet ruby-rubygems ruby-webrick ruby-xmlrpc ruby3.0 rubygems-integration t1utils teckit tex-common tex-gyre texlive-base texlive-binaries texlive-fonts-recommended texlive-latex-base texlive-latex-recommended texlive-pictures texlive-plain-generic tipa xfonts-encodings xfonts-utils Suggested packages: fonts-noto fonts-freefont-otf | fonts-freefont-ttf libavalon-framework-java libcommons-logging-java-doc libexcalibur-logkit-java liblog4j1.2-java texlive-luatex pandoc-citeproc context wkhtmltopdf librsvg2-bin groff ghc nodejs php python libjs-mathjax libjs-katex citation-style-language-styles poppler-utils ghostscript fonts-japanese-mincho | fonts-ipafont-mincho fonts-japanese-gothic | fonts-ipafont-gothic fonts-arphic-ukai fonts-arphic-uming fonts-nanum ri ruby-dev bundler debhelper gv | postscript-viewer perl-tk xpdf | pdf-viewer xzdec texlive-fonts-recommended-doc texlive-latex-base-doc python3-pygments icc-profiles libfile-which-perl libspreadsheet-parseexcel-perl texlive-latex-extra-doc texlive-latex-recommended-doc texlive-pstricks dot2tex prerex texlive-pictures-doc vprerex default-jre-headless tipa-doc

The following NEW packages will be installed:

```
dvisvgm fonts-droid-fallback fonts-lato fonts-lmodern fonts-noto-mono
  fonts-texgyre fonts-urw-base35 libapache-pom-java
  libcmark-gfm-extensions0.29.0.gfm.3 libcmark-gfm0.29.0.gfm.3
  libcommons-logging-java libcommons-parent-java libfontbox-java libgs9
  libgs9-common libidn12 libijs-0.35 libjbig2dec0 libkpathsea6 libpdfbox-java
  libptexenc1 libruby3.0 libsynctex2 libteckit0 libtexlua53 libtexluajit2
  libwoff1 libzzip-0-13 lmodern pandoc pandoc-data poppler-data
  preview-latex-style rake ruby ruby-net-telnet ruby-rubygems ruby-webrick
 ruby-xmlrpc ruby3.0 rubygems-integration t1utils teckit tex-common tex-gyre
  texlive texlive-base texlive-binaries texlive-fonts-recommended
  texlive-latex-base texlive-latex-extra texlive-latex-recommended
  texlive-pictures texlive-plain-generic texlive-xetex tipa xfonts-encodings
 xfonts-utils
0 upgraded, 58 newly installed, 0 to remove and 38 not upgraded.
Need to get 202 MB of archives.
After this operation, 728 MB of additional disk space will be used.
Get:1 http://archive.ubuntu.com/ubuntu jammy/main amd64 fonts-droid-fallback all
1:6.0.1r16-1.1build1 [1,805 kB]
Get:2 http://archive.ubuntu.com/ubuntu jammy/main amd64 fonts-lato all 2.0-2.1
[2.696 kB]
Get:3 http://archive.ubuntu.com/ubuntu jammy/main amd64 poppler-data all
0.4.11-1 [2,171 kB]
Get:4 http://archive.ubuntu.com/ubuntu jammy/universe amd64 tex-common all 6.17
[33.7 kB]
Get:5 http://archive.ubuntu.com/ubuntu jammy/main amd64 fonts-urw-base35 all
20200910-1 [6,367 kB]
Get:6 http://archive.ubuntu.com/ubuntu jammy-updates/main amd64 libgs9-common
all 9.55.0~dfsg1-Oubuntu5.12 [753 kB]
Get:7 http://archive.ubuntu.com/ubuntu jammy-updates/main amd64 libidn12 amd64
1.38-4ubuntu1 [60.0 kB]
Get:8 http://archive.ubuntu.com/ubuntu jammy/main amd64 libijs-0.35 amd64
0.35-15build2 [16.5 kB]
Get:9 http://archive.ubuntu.com/ubuntu jammy/main amd64 libjbig2dec0 amd64
0.19-3build2 [64.7 kB]
Get:10 http://archive.ubuntu.com/ubuntu jammy-updates/main amd64 libgs9 amd64
9.55.0~dfsg1-Oubuntu5.12 [5,031 kB]
Get:11 http://archive.ubuntu.com/ubuntu jammy-updates/main amd64 libkpathsea6
amd64 2021.20210626.59705-1ubuntu0.2 [60.4 kB]
Get:12 http://archive.ubuntu.com/ubuntu jammy/main amd64 libwoff1 amd64
1.0.2-1build4 [45.2 kB]
Get:13 http://archive.ubuntu.com/ubuntu jammy/universe amd64 dvisvgm amd64
2.13.1-1 [1,221 kB]
Get:14 http://archive.ubuntu.com/ubuntu jammy/universe amd64 fonts-lmodern all
2.004.5-6.1 [4,532 kB]
Get:15 http://archive.ubuntu.com/ubuntu jammy/main amd64 fonts-noto-mono all
20201225-1build1 [397 kB]
Get:16 http://archive.ubuntu.com/ubuntu jammy/universe amd64 fonts-texgyre all
```

20180621-3.1 [10.2 MB]

```
Get:17 http://archive.ubuntu.com/ubuntu jammy/universe amd64 libapache-pom-java all 18-1 [4,720 B]
```

Get:18 http://archive.ubuntu.com/ubuntu jammy/universe amd64 libcmark-gfm0.29.0.gfm.3 amd64 0.29.0.gfm.3-3 [115 kB]

Get:19 http://archive.ubuntu.com/ubuntu jammy/universe amd64 libcmark-gfm-extensions0.29.0.gfm.3 amd64 0.29.0.gfm.3-3 [25.1 kB]

Get:20 http://archive.ubuntu.com/ubuntu jammy/universe amd64 libcommons-parent-java all 43-1 [10.8 kB]

Get:21 http://archive.ubuntu.com/ubuntu jammy/universe amd64 libcommons-logging-java all 1.2-2 [60.3 kB]

Get:22 http://archive.ubuntu.com/ubuntu jammy-updates/main amd64 libptexenc1 amd64 2021.20210626.59705-1ubuntu0.2 [39.1 kB]

Get:23 http://archive.ubuntu.com/ubuntu jammy/main amd64 rubygems-integration all 1.18 [5,336 B]

Get:24 http://archive.ubuntu.com/ubuntu jammy-updates/main amd64 ruby3.0 amd64 3.0.2-7ubuntu2.11 [50.1 kB]

Get:25 http://archive.ubuntu.com/ubuntu jammy-updates/main amd64 ruby-rubygems
all 3.3.5-2ubuntu1.2 [228 kB]

Get:26 http://archive.ubuntu.com/ubuntu jammy/main amd64 ruby amd64 1:3.0~exp1
[5,100 B]

Get:27 http://archive.ubuntu.com/ubuntu jammy/main amd64 rake all 13.0.6-2 [61.7 kB]

Get:28 http://archive.ubuntu.com/ubuntu jammy/main amd64 ruby-net-telnet all
0.1.1-2 [12.6 kB]

Get:29 http://archive.ubuntu.com/ubuntu jammy-updates/main amd64 ruby-webrick all 1.7.0-3ubuntu0.2 [52.5 kB]

Get:30 http://archive.ubuntu.com/ubuntu jammy-updates/main amd64 ruby-xmlrpc all 0.3.2-1ubuntu0.1 [24.9 kB]

Get:31 http://archive.ubuntu.com/ubuntu jammy-updates/main amd64 libruby3.0 amd64 3.0.2-7ubuntu2.11 [5,114 kB]

Get:32 http://archive.ubuntu.com/ubuntu jammy-updates/main amd64 libsynctex2 amd64 2021.20210626.59705-1ubuntu0.2 [55.6 kB]

Get:33 http://archive.ubuntu.com/ubuntu jammy/universe amd64 libteckit0 amd64 2.5.11+ds1-1 [421 kB]

Get:34 http://archive.ubuntu.com/ubuntu jammy-updates/main amd64 libtexlua53 amd64 2021.20210626.59705-1ubuntu0.2 [120 kB]

Get:35 http://archive.ubuntu.com/ubuntu jammy-updates/main amd64 libtexluajit2 amd64 2021.20210626.59705-1ubuntu0.2 [267 kB]

Get:36 http://archive.ubuntu.com/ubuntu jammy/universe amd64 libzzip-0-13 amd64 0.13.72+dfsg.1-1.1 [27.0 kB]

Get:37 http://archive.ubuntu.com/ubuntu jammy/main amd64 xfonts-encodings all 1:1.0.5-Oubuntu2 [578 kB]

Get:38 http://archive.ubuntu.com/ubuntu jammy/main amd64 xfonts-utils amd64 1:7.7+6build2 [94.6 kB]

Get:39 http://archive.ubuntu.com/ubuntu jammy/universe amd64 lmodern all 2.004.5-6.1 [9,471 kB]

Get:40 http://archive.ubuntu.com/ubuntu jammy/universe amd64 pandoc-data all
2.9.2.1-3ubuntu2 [81.8 kB]

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Get:41 http://archive.ubuntu.com/ubuntu jammy/universe amd64 pandoc amd64
2.9.2.1-3ubuntu2 [20.3 MB]
Get:42 http://archive.ubuntu.com/ubuntu jammy/universe amd64 preview-latex-style
all 12.2-1ubuntu1 [185 kB]
Get:43 http://archive.ubuntu.com/ubuntu jammy/main amd64 t1utils amd64
1.41-4build2 [61.3 kB]
Get:44 http://archive.ubuntu.com/ubuntu jammy/universe amd64 teckit amd64
2.5.11+ds1-1 [699 kB]
Get:45 http://archive.ubuntu.com/ubuntu jammy/universe amd64 tex-gyre all
20180621-3.1 [6,209 kB]
Get:46 http://archive.ubuntu.com/ubuntu jammy-updates/universe amd64 texlive-
binaries amd64 2021.20210626.59705-1ubuntu0.2 [9,860 kB]
Get:47 http://archive.ubuntu.com/ubuntu jammy/universe amd64 texlive-base all
2021.20220204-1 [21.0 MB]
Get:48 http://archive.ubuntu.com/ubuntu jammy/universe amd64 texlive-fonts-
recommended all 2021.20220204-1 [4,972 kB]
Get:49 http://archive.ubuntu.com/ubuntu jammy/universe amd64 texlive-latex-base
all 2021.20220204-1 [1,128 kB]
Get:50 http://archive.ubuntu.com/ubuntu jammy/universe amd64 texlive-latex-
recommended all 2021.20220204-1 [14.4 MB]
Get:51 http://archive.ubuntu.com/ubuntu jammy/universe amd64 texlive all
2021.20220204-1 [14.3 kB]
Get:52 http://archive.ubuntu.com/ubuntu jammy/universe amd64 libfontbox-java all
1:1.8.16-2 [207 kB]
Get:53 http://archive.ubuntu.com/ubuntu jammy/universe amd64 libpdfbox-java all
1:1.8.16-2 [5,199 kB]
Get:54 http://archive.ubuntu.com/ubuntu jammy/universe amd64 texlive-pictures
all 2021.20220204-1 [8,720 kB]
Get:55 http://archive.ubuntu.com/ubuntu jammy/universe amd64 texlive-latex-extra
all 2021.20220204-1 [13.9 MB]
Get:56 http://archive.ubuntu.com/ubuntu jammy/universe amd64 texlive-plain-
generic all 2021.20220204-1 [27.5 MB]
Get:57 http://archive.ubuntu.com/ubuntu jammy/universe amd64 tipa all 2:1.3-21
[2,967 \text{ kB}]
Get:58 http://archive.ubuntu.com/ubuntu jammy/universe amd64 texlive-xetex all
2021.20220204-1 [12.4 MB]
Fetched 202 MB in 4s (45.0 MB/s)
Extracting templates from packages: 100%
Preconfiguring packages ...
Selecting previously unselected package fonts-droid-fallback.
(Reading database ... 126435 files and directories currently installed.)
Preparing to unpack .../00-fonts-droid-fallback 1%3a6.0.1r16-1.1build1_all.deb
Unpacking fonts-droid-fallback (1:6.0.1r16-1.1build1) ...
Selecting previously unselected package fonts-lato.
Preparing to unpack .../01-fonts-lato_2.0-2.1_all.deb ...
Unpacking fonts-lato (2.0-2.1) ...
Selecting previously unselected package poppler-data.
```

```
Preparing to unpack .../02-poppler-data_0.4.11-1_all.deb ...
Unpacking poppler-data (0.4.11-1) ...
Selecting previously unselected package tex-common.
Preparing to unpack .../03-tex-common_6.17_all.deb ...
Unpacking tex-common (6.17) ...
Selecting previously unselected package fonts-urw-base35.
Preparing to unpack .../04-fonts-urw-base35 20200910-1 all.deb ...
Unpacking fonts-urw-base35 (20200910-1) ...
Selecting previously unselected package libgs9-common.
Preparing to unpack .../05-libgs9-common_9.55.0~dfsg1-Oubuntu5.12_all.deb ...
Unpacking libgs9-common (9.55.0~dfsg1-Oubuntu5.12) ...
Selecting previously unselected package libidn12:amd64.
Preparing to unpack .../06-libidn12_1.38-4ubuntu1_amd64.deb ...
Unpacking libidn12:amd64 (1.38-4ubuntu1) ...
Selecting previously unselected package libijs-0.35:amd64.
Preparing to unpack .../07-libijs-0.35_0.35-15build2_amd64.deb ...
Unpacking libijs-0.35:amd64 (0.35-15build2) ...
Selecting previously unselected package libjbig2dec0:amd64.
Preparing to unpack .../08-libjbig2dec0_0.19-3build2_amd64.deb ...
Unpacking libjbig2dec0:amd64 (0.19-3build2) ...
Selecting previously unselected package libgs9:amd64.
Preparing to unpack .../09-libgs9 9.55.0~dfsg1-0ubuntu5.12 amd64.deb ...
Unpacking libgs9:amd64 (9.55.0~dfsg1-Oubuntu5.12) ...
Selecting previously unselected package libkpathsea6:amd64.
Preparing to unpack .../10-libkpathsea6_2021.20210626.59705-1ubuntu0.2_amd64.deb
Unpacking libkpathsea6:amd64 (2021.20210626.59705-1ubuntu0.2) ...
Selecting previously unselected package libwoff1:amd64.
Preparing to unpack .../11-libwoff1_1.0.2-1build4_amd64.deb ...
Unpacking libwoff1:amd64 (1.0.2-1build4) ...
Selecting previously unselected package dvisvgm.
Preparing to unpack .../12-dvisvgm_2.13.1-1_amd64.deb ...
Unpacking dvisvgm (2.13.1-1) ...
Selecting previously unselected package fonts-lmodern.
Preparing to unpack .../13-fonts-lmodern 2.004.5-6.1 all.deb ...
Unpacking fonts-Imodern (2.004.5-6.1) ...
Selecting previously unselected package fonts-noto-mono.
Preparing to unpack .../14-fonts-noto-mono_20201225-1build1_all.deb ...
Unpacking fonts-noto-mono (20201225-1build1) ...
Selecting previously unselected package fonts-texgyre.
Preparing to unpack .../15-fonts-texgyre_20180621-3.1_all.deb ...
Unpacking fonts-texgyre (20180621-3.1) ...
Selecting previously unselected package libapache-pom-java.
Preparing to unpack .../16-libapache-pom-java_18-1_all.deb ...
Unpacking libapache-pom-java (18-1) ...
Selecting previously unselected package libcmark-gfm0.29.0.gfm.3:amd64.
Preparing to unpack .../17-libcmark-gfm0.29.0.gfm.3_0.29.0.gfm.3-3_amd64.deb ...
Unpacking libcmark-gfm0.29.0.gfm.3:amd64 (0.29.0.gfm.3-3) ...
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Selecting previously unselected package libcmark-gfm-
extensions0.29.0.gfm.3:amd64.
Preparing to unpack .../18-libcmark-gfm-
extensions0.29.0.gfm.3_0.29.0.gfm.3-3_amd64.deb ...
Unpacking libcmark-gfm-extensions0.29.0.gfm.3:amd64 (0.29.0.gfm.3-3) ...
Selecting previously unselected package libcommons-parent-java.
Preparing to unpack .../19-libcommons-parent-java 43-1 all.deb ...
Unpacking libcommons-parent-java (43-1) ...
Selecting previously unselected package libcommons-logging-java.
Preparing to unpack .../20-libcommons-logging-java_1.2-2_all.deb ...
Unpacking libcommons-logging-java (1.2-2) ...
Selecting previously unselected package libptexenc1:amd64.
Preparing to unpack .../21-libptexenc1_2021.20210626.59705-1ubuntu0.2_amd64.deb
Unpacking libptexenc1:amd64 (2021.20210626.59705-1ubuntu0.2) ...
Selecting previously unselected package rubygems-integration.
Preparing to unpack .../22-rubygems-integration_1.18_all.deb ...
Unpacking rubygems-integration (1.18) ...
Selecting previously unselected package ruby3.0.
Preparing to unpack .../23-ruby3.0 3.0.2-7ubuntu2.11 amd64.deb ...
Unpacking ruby3.0 (3.0.2-7ubuntu2.11) ...
Selecting previously unselected package ruby-rubygems.
Preparing to unpack .../24-ruby-rubygems_3.3.5-2ubuntu1.2_all.deb ...
Unpacking ruby-rubygems (3.3.5-2ubuntu1.2) ...
Selecting previously unselected package ruby.
Preparing to unpack .../25-ruby_1%3a3.0~exp1_amd64.deb ...
Unpacking ruby (1:3.0~exp1) ...
Selecting previously unselected package rake.
Preparing to unpack .../26-rake_13.0.6-2_all.deb ...
Unpacking rake (13.0.6-2) ...
Selecting previously unselected package ruby-net-telnet.
Preparing to unpack .../27-ruby-net-telnet_0.1.1-2_all.deb ...
Unpacking ruby-net-telnet (0.1.1-2) ...
Selecting previously unselected package ruby-webrick.
Preparing to unpack .../28-ruby-webrick 1.7.0-3ubuntu0.2 all.deb ...
Unpacking ruby-webrick (1.7.0-3ubuntu0.2) ...
Selecting previously unselected package ruby-xmlrpc.
Preparing to unpack .../29-ruby-xmlrpc_0.3.2-1ubuntu0.1_all.deb ...
Unpacking ruby-xmlrpc (0.3.2-1ubuntu0.1) ...
Selecting previously unselected package libruby3.0:amd64.
Preparing to unpack .../30-libruby3.0_3.0.2-7ubuntu2.11_amd64.deb ...
Unpacking libruby3.0:amd64 (3.0.2-7ubuntu2.11) ...
Selecting previously unselected package libsynctex2:amd64.
Preparing to unpack .../31-libsynctex2 2021.20210626.59705-1ubuntu0.2 amd64.deb
Unpacking libsynctex2:amd64 (2021.20210626.59705-1ubuntu0.2) ...
Selecting previously unselected package libteckit0:amd64.
Preparing to unpack .../32-libteckit0_2.5.11+ds1-1_amd64.deb ...
```

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Unpacking libteckit0:amd64 (2.5.11+ds1-1) ...
Selecting previously unselected package libtexlua53:amd64.
Preparing to unpack .../33-libtexlua53 2021.20210626.59705-1ubuntu0.2 amd64.deb
Unpacking libtexlua53:amd64 (2021.20210626.59705-1ubuntu0.2) ...
Selecting previously unselected package libtexluajit2:amd64.
Preparing to unpack
.../34-libtexluajit2_2021.20210626.59705-1ubuntu0.2_amd64.deb ...
Unpacking libtexluajit2:amd64 (2021.20210626.59705-1ubuntu0.2) ...
Selecting previously unselected package libzzip-0-13:amd64.
Preparing to unpack .../35-libzzip-0-13_0.13.72+dfsg.1-1.1_amd64.deb ...
Unpacking libzzip-0-13:amd64 (0.13.72+dfsg.1-1.1) ...
Selecting previously unselected package xfonts-encodings.
Preparing to unpack .../36-xfonts-encodings 1%3a1.0.5-Oubuntu2_all.deb ...
Unpacking xfonts-encodings (1:1.0.5-Oubuntu2) ...
Selecting previously unselected package xfonts-utils.
Preparing to unpack .../37-xfonts-utils_1%3a7.7+6build2_amd64.deb ...
Unpacking xfonts-utils (1:7.7+6build2) ...
Selecting previously unselected package lmodern.
Preparing to unpack .../38-lmodern 2.004.5-6.1 all.deb ...
Unpacking lmodern (2.004.5-6.1) ...
Selecting previously unselected package pandoc-data.
Preparing to unpack .../39-pandoc-data_2.9.2.1-3ubuntu2_all.deb ...
Unpacking pandoc-data (2.9.2.1-3ubuntu2) ...
Selecting previously unselected package pandoc.
Preparing to unpack .../40-pandoc_2.9.2.1-3ubuntu2_amd64.deb ...
Unpacking pandoc (2.9.2.1-3ubuntu2) ...
Selecting previously unselected package preview-latex-style.
Preparing to unpack .../41-preview-latex-style 12.2-1ubuntu1 all.deb ...
Unpacking preview-latex-style (12.2-1ubuntu1) ...
Selecting previously unselected package tlutils.
Preparing to unpack .../42-t1utils_1.41-4build2_amd64.deb ...
Unpacking t1utils (1.41-4build2) ...
Selecting previously unselected package teckit.
Preparing to unpack .../43-teckit 2.5.11+ds1-1 amd64.deb ...
Unpacking teckit (2.5.11+ds1-1) ...
Selecting previously unselected package tex-gyre.
Preparing to unpack .../44-tex-gyre_20180621-3.1_all.deb ...
Unpacking tex-gyre (20180621-3.1) ...
Selecting previously unselected package texlive-binaries.
Preparing to unpack .../45-texlive-
binaries_2021.20210626.59705-1ubuntu0.2_amd64.deb ...
Unpacking texlive-binaries (2021.20210626.59705-1ubuntu0.2) ...
Selecting previously unselected package texlive-base.
Preparing to unpack .../46-texlive-base_2021.20220204-1_all.deb ...
Unpacking texlive-base (2021.20220204-1) ...
Selecting previously unselected package texlive-fonts-recommended.
Preparing to unpack .../47-texlive-fonts-recommended 2021.20220204-1_all.deb ...
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Unpacking texlive-fonts-recommended (2021.20220204-1) ...
Selecting previously unselected package texlive-latex-base.
Preparing to unpack .../48-texlive-latex-base 2021.20220204-1 all.deb ...
Unpacking texlive-latex-base (2021.20220204-1) ...
Selecting previously unselected package texlive-latex-recommended.
Preparing to unpack .../49-texlive-latex-recommended 2021.20220204-1 all.deb ...
Unpacking texlive-latex-recommended (2021.20220204-1) ...
Selecting previously unselected package texlive.
Preparing to unpack .../50-texlive 2021.20220204-1 all.deb ...
Unpacking texlive (2021.20220204-1) ...
Selecting previously unselected package libfontbox-java.
Preparing to unpack .../51-libfontbox-java_1%3a1.8.16-2_all.deb ...
Unpacking libfontbox-java (1:1.8.16-2) ...
Selecting previously unselected package libpdfbox-java.
Preparing to unpack .../52-libpdfbox-java_1%3a1.8.16-2_all.deb ...
Unpacking libpdfbox-java (1:1.8.16-2) ...
Selecting previously unselected package texlive-pictures.
Preparing to unpack .../53-texlive-pictures 2021.20220204-1 all.deb ...
Unpacking texlive-pictures (2021.20220204-1) ...
Selecting previously unselected package texlive-latex-extra.
Preparing to unpack .../54-texlive-latex-extra 2021.20220204-1 all.deb ...
Unpacking texlive-latex-extra (2021.20220204-1) ...
Selecting previously unselected package texlive-plain-generic.
Preparing to unpack .../55-texlive-plain-generic_2021.20220204-1_all.deb ...
Unpacking texlive-plain-generic (2021.20220204-1) ...
Selecting previously unselected package tipa.
Preparing to unpack .../56-tipa_2%3a1.3-21_all.deb ...
Unpacking tipa (2:1.3-21) ...
Selecting previously unselected package texlive-xetex.
Preparing to unpack .../57-texlive-xetex_2021.20220204-1_all.deb ...
Unpacking texlive-xetex (2021.20220204-1) ...
Setting up fonts-lato (2.0-2.1) ...
Setting up fonts-noto-mono (20201225-1build1) ...
Setting up libwoff1:amd64 (1.0.2-1build4) ...
Setting up libtexlua53:amd64 (2021.20210626.59705-1ubuntu0.2) ...
Setting up libijs-0.35:amd64 (0.35-15build2) ...
Setting up libtexluajit2:amd64 (2021.20210626.59705-1ubuntu0.2) ...
Setting up libfontbox-java (1:1.8.16-2) ...
Setting up rubygems-integration (1.18) ...
Setting up libzzip-0-13:amd64 (0.13.72+dfsg.1-1.1) ...
Setting up fonts-urw-base35 (20200910-1) ...
Setting up poppler-data (0.4.11-1) ...
Setting up tex-common (6.17) ...
update-language: texlive-base not installed and configured, doing nothing!
Setting up libjbig2dec0:amd64 (0.19-3build2) ...
Setting up libteckit0:amd64 (2.5.11+ds1-1) ...
Setting up libapache-pom-java (18-1) ...
Setting up ruby-net-telnet (0.1.1-2) ...
```

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Setting up xfonts-encodings (1:1.0.5-Oubuntu2) ...
Setting up tlutils (1.41-4build2) ...
Setting up libidn12:amd64 (1.38-4ubuntu1) ...
Setting up fonts-texgyre (20180621-3.1) ...
Setting up libkpathsea6:amd64 (2021.20210626.59705-1ubuntu0.2) ...
Setting up ruby-webrick (1.7.0-3ubuntu0.2) ...
Setting up libcmark-gfm0.29.0.gfm.3:amd64 (0.29.0.gfm.3-3) ...
Setting up fonts-lmodern (2.004.5-6.1) ...
Setting up libcmark-gfm-extensions0.29.0.gfm.3:amd64 (0.29.0.gfm.3-3) ...
Setting up fonts-droid-fallback (1:6.0.1r16-1.1build1) ...
Setting up pandoc-data (2.9.2.1-3ubuntu2) ...
Setting up ruby-xmlrpc (0.3.2-1ubuntu0.1) ...
Setting up libsynctex2:amd64 (2021.20210626.59705-1ubuntu0.2) ...
Setting up libgs9-common (9.55.0~dfsg1-Oubuntu5.12) ...
Setting up teckit (2.5.11+ds1-1) ...
Setting up libpdfbox-java (1:1.8.16-2) ...
Setting up libgs9:amd64 (9.55.0~dfsg1-Oubuntu5.12) ...
Setting up preview-latex-style (12.2-1ubuntu1) ...
Setting up libcommons-parent-java (43-1) ...
Setting up dvisvgm (2.13.1-1) ...
Setting up libcommons-logging-java (1.2-2) ...
Setting up xfonts-utils (1:7.7+6build2) ...
Setting up libptexenc1:amd64 (2021.20210626.59705-1ubuntu0.2) ...
Setting up pandoc (2.9.2.1-3ubuntu2) ...
Setting up texlive-binaries (2021.20210626.59705-1ubuntu0.2) ...
update-alternatives: using /usr/bin/xdvi-xaw to provide /usr/bin/xdvi.bin
(xdvi.bin) in auto mode
update-alternatives: using /usr/bin/bibtex.original to provide /usr/bin/bibtex
(bibtex) in auto mode
Setting up lmodern (2.004.5-6.1) ...
Setting up texlive-base (2021.20220204-1) ...
/usr/bin/ucfr
/usr/bin/ucfr
/usr/bin/ucfr
/usr/bin/ucfr
mktexlsr: Updating /var/lib/texmf/ls-R-TEXLIVEDIST...
mktexlsr: Updating /var/lib/texmf/ls-R-TEXMFMAIN...
mktexlsr: Updating /var/lib/texmf/ls-R...
mktexlsr: Done.
tl-paper: setting paper size for dvips to a4:
/var/lib/texmf/dvips/config/config-paper.ps
tl-paper: setting paper size for dvipdfmx to a4:
/var/lib/texmf/dvipdfmx/dvipdfmx-paper.cfg
tl-paper: setting paper size for xdvi to a4: /var/lib/texmf/xdvi/XDvi-paper
tl-paper: setting paper size for pdftex to a4: /var/lib/texmf/tex/generic/tex-
ini-files/pdftexconfig.tex
Setting up tex-gyre (20180621-3.1) ...
Setting up texlive-plain-generic (2021.20220204-1) ...
```

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Setting up texlive-latex-base (2021.20220204-1) ...
Setting up texlive-latex-recommended (2021.20220204-1) ...
Setting up texlive-pictures (2021.20220204-1) ...
Setting up texlive-fonts-recommended (2021.20220204-1) ...
Setting up tipa (2:1.3-21) ...
Setting up texlive (2021.20220204-1) ...
Setting up texlive-latex-extra (2021.20220204-1) ...
Setting up texlive-xetex (2021.20220204-1) ...
Setting up rake (13.0.6-2) ...
Setting up libruby3.0:amd64 (3.0.2-7ubuntu2.11) ...
Setting up ruby3.0 (3.0.2-7ubuntu2.11) ...
Setting up ruby (1:3.0~exp1) ...
Setting up ruby-rubygems (3.3.5-2ubuntu1.2) ...
Processing triggers for man-db (2.10.2-1) ...
Processing triggers for mailcap (3.70+nmu1ubuntu1) ...
Processing triggers for fontconfig (2.13.1-4.2ubuntu5) ...
Processing triggers for libc-bin (2.35-Oubuntu3.8) ...
/sbin/ldconfig.real: /usr/local/lib/libtbbmalloc.so.2 is not a symbolic link
/sbin/ldconfig.real: /usr/local/lib/libtcm.so.1 is not a symbolic link
/sbin/ldconfig.real: /usr/local/lib/libtbbmalloc proxy.so.2 is not a symbolic
link
/sbin/ldconfig.real: /usr/local/lib/libtbbbind.so.3 is not a symbolic link
/sbin/ldconfig.real: /usr/local/lib/libtcm_debug.so.1 is not a symbolic link
/sbin/ldconfig.real: /usr/local/lib/libur_adapter_level_zero_v2.so.0 is not a
symbolic link
/sbin/ldconfig.real: /usr/local/lib/libur_adapter_opencl.so.0 is not a symbolic
link
/sbin/ldconfig.real: /usr/local/lib/libur loader.so.0 is not a symbolic link
/sbin/ldconfig.real: /usr/local/lib/libtbb.so.12 is not a symbolic link
/sbin/ldconfig.real: /usr/local/lib/libtbbbind_2_5.so.3 is not a symbolic link
/sbin/ldconfig.real: /usr/local/lib/libhwloc.so.15 is not a symbolic link
/sbin/ldconfig.real: /usr/local/lib/libur_adapter_level_zero.so.0 is not a
symbolic link
/sbin/ldconfig.real: /usr/local/lib/libumf.so.0 is not a symbolic link
/sbin/ldconfig.real: /usr/local/lib/libtbbbind 2 0.so.3 is not a symbolic link
```