```
In [1]: import pandas as pd
        import os
        import urllib
        from sklearn.decomposition import PCA
        from sklearn.decomposition import KernelPCA
        import numpy as np
        from scipy.signal import periodogram
        import statsmodels.api as sm
        import dask.dataframe as dd
        from statsmodels.tsa.stattools import adfuller
        from statsmodels.graphics.tsaplots import plot acf
        from statsmodels.graphics.tsaplots import plot pacf
        from statsmodels.tsa.arima model import ARIMA
        from matplotlib import pyplot as plt
        from sklearn.preprocessing import StandardScaler
        from sklearn.metrics import r2_score
        from sklearn.metrics import mean squared error
        from sklearn.ensemble import RandomForestRegressor
        from sklearn.model selection import GridSearchCV
        from sklearn.model selection import PredefinedSplit
        import warnings
        warnings.filterwarnings('ignore')
```

Theoretic part

Multiple choice questions: please select all that applies and explain your answer.

Question 1 (Autocorrelation).

The autocorrelation plot of the daily time-series has local peaks at t=7,14,21,28 etc.. How would you interpret that?

- A. The time-series reaches its maximum on the days 7,14,21,28...
- B. The time-series reaches its minimum on the days 7,14,21,28...
- C. The time-series is likely to have a periodic pattern with a period of 7 days
- D. The time-series is likely to have 7 periods per day
- E. The appropriate AR model for the time-series should have at least 7 terms.

Your answer:

C

Since the period has 7 cycles, strongly suggest that the periodic pattern with 1 week.

Question 2 (Stationarity).

Which of the following time-series models are always stationary:

- A. Linear trend
- B. MA(1) model
- C. White noise
- D. Random walk
- E. ARMA(1,2) model
- F. ARIMA(1,1,1) model

Your answer:

B

the q parameter in the MA(q) used for the lagged errors, the more errors the model has, the more complex the prediction has. So when q is as small as 1, the noise of the model is lower, and causing it station.

C

White noise has constant mean and variance, so it is station.

Question 3 (PCA).

Which of the following statements regarding the model dimensionality reduction through Principal Component Analysis (PCA) are true:

- A. Leading principal components of the features are the most efficient for modeling the output variable.
- B. Principal components of the standardized features are uncorrelated and this way less exposed to multicollinearity.
- C. The model using principal components of the features can't overfit.
- D. Feature selection based on the principal components of the features is often more efficient in preventing overfitting comparered the feature selection over the original features.

E. Principal components are harder to interpret compared to the original features making the PCA regression model less interpretable compared to the regression model using original features.

Your answer:

B

One of the key benefits of PCA is that it transforms the original features into a new set of variables (the principal components) that are orthogonal (uncorrelated) to each other. This characteristic is particularly useful in addressing multicollinearity among the features in a dataset.

Ε

Since principal components are linear combinations of the original features, they often do not have a direct or easily interpretable relationship to the original variables. This makes models using PCA less interpretable in terms of the original features.

Question 4 (MapReduce).

What is true about MapReduce:

- A. MapReduce is a Python module enabling parallel computing
- B. Using MapReduce approach makes the code more suitable for parallel computing.
- C. MapReduce code always runs faster compared to the code using more traditional approaches, like loops or list comprehensions.
- D. MapReduce code will always efficiently run on multiple cores of your CPU or multiple machines within your cluster if available.
- E. Multiprocessing and PySpark efficient alternatives to MapReduce.

Your answer:

B

The MapReduce programming model is designed to process large data sets across a distributed cluster in a parallel manner. It breaks down the job into smaller chunks (Map phase) and then consolidates the results (Reduce phase), making the code inherently suitable for parallel computing.

Practice part: Taxi ridership from JFK to other taxi zones prediction.

This project is an example of applying PCA to predict hourly yellow taxi ridership at the taxi zone level. Modeling taxi ridership at a fine spatial and temporal granularity is challenging due to the low signal-to-noise ratio and high dimensionality. In this case, dimension reduction essential in feature engineering. This project has five steps: data downloading, data preprocessing, baseline modeling, feature engineering, and RandomForest modeling.

Let's start with data downloading.

1. Data downloading

Design a function to download yellow taxi data from 2017-01-01 to 2018-12-31 at https://www1.nyc.gov/site/tlc/about/tlc-trip-record-data.page.

```
In [2]:
    dataDir = 'taxidata'
    if os.path.exists(dataDir):
        pass
    else:
        os.mkdir(dataDir)
    Years = [2017,2018]
    Months = range(1,13)
    VehicleTypes = ['yellow']

    def getUrl(cabtype,year,month):
        baseUrl = 'https://d37ci6vzurychx.cloudfront.net/trip-data/'
        month = str(month).zfill(2)
        fileName = '%s_tripdata_%s-%s.parquet'%(cabtype,year,month)
        return baseUrl + fileName, fileName
```

```
In [3]: for year in Years:
    for month in Months:
        for cabtype in VehicleTypes:
            url, fileName = getUrl(cabtype, year, month)

            print("Downloading: "+str(fileName))

            if fileName in os.listdir(dataDir):
                print("file exists")
                 continue

            filePath = os.path.join(dataDir, fileName)
            try:
                 urllib.request.urlretrieve(url, filePath)
            except:
                 # if fails remove the incomplete file
                  os.remove(filePath)
                  try:
```

```
# start again after a delay of 2 min
time.sleep(60*2)
urllib.request.urlretrieve(url, filePath)
except:
    print("Download this file later!")
pass
```

```
Downloading: yellow_tripdata_2017-01.parquet
file exists
Downloading: yellow tripdata 2017-02.parguet
file exists
Downloading: yellow_tripdata_2017-03.parquet
file exists
Downloading: yellow tripdata 2017-04.parguet
file exists
Downloading: yellow_tripdata_2017-05.parquet
file exists
Downloading: yellow_tripdata_2017-06.parquet
file exists
Downloading: yellow tripdata 2017-07.parguet
file exists
Downloading: yellow_tripdata_2017-08.parquet
file exists
Downloading: yellow_tripdata_2017-09.parquet
file exists
Downloading: yellow_tripdata_2017-10.parquet
file exists
Downloading: yellow tripdata 2017-11.parguet
file exists
Downloading: yellow_tripdata_2017-12.parquet
file exists
Downloading: yellow_tripdata_2018-01.parquet
file exists
Downloading: yellow_tripdata_2018-02.parquet
file exists
Downloading: yellow_tripdata_2018-03.parquet
file exists
Downloading: yellow tripdata 2018-04.parguet
file exists
Downloading: yellow_tripdata_2018-05.parquet
file exists
Downloading: yellow tripdata 2018-06.parguet
file exists
Downloading: yellow_tripdata_2018-07.parquet
file exists
Downloading: yellow_tripdata_2018-08.parquet
file exists
Downloading: yellow_tripdata_2018-09.parquet
file exists
Downloading: yellow_tripdata_2018-10.parquet
file exists
Downloading: yellow tripdata 2018-11.parguet
file exists
Downloading: yellow_tripdata_2018-12.parquet
file exists
```

2. Data Preprocessing

Use dask to aggregate all months' records into one dataframe, and aggregate dataset by date and hour to get the ridership from JFK to each taxi zone each hour. The expected output has columns: date, hour, drop-off location 1, drop-off location 2, etc.

Hint:

- 1. JFK taxi zone id is 132.
- 2. time column should be the pickup time, and ridership is passenger count.
- 3. Try read_parquet("*.parquet") to read all parquet file in a folder
- 4. files in 2017 and 2018 have different columns; apply argument usecols to select desired columns.
- 5. using .compute() function to convert processed dask dataframe to pandas dataframe for further modeling.

2.1 Data loading

```
In [4]: #your answer here
directory = 'taxidata'
df_list = []
desired_columns = ['tpep_pickup_datetime', 'tpep_dropoff_datetime', 'passenger_of for filename in os.listdir(directory):
    if filename.endswith(".parquet"):
        filepath = os.path.join(directory, filename)
        df = pd.read_parquet(filepath, columns=desired_columns)
        df_list.append(df)
```

In [5]: df_list

```
tpep_pickup_datetime tpep_dropoff_datetime
                                                                  passenger_count
Out[5]:
          0
                   2018-09-01 00:01:35
                                           2018-09-01 00:09:48
                                                                               2.0
          1
                    2018-09-01 00:22:22
                                           2018-09-01 00:28:55
                                                                               1.0
          2
                   2018-09-01 00:38:10
                                           2018-09-01 00:44:42
                                                                               1.0
          3
                   2018-09-01 00:46:36
                                           2018-09-01 00:54:49
                                                                               1.0
          4
                   2018-09-01 00:59:46
                                           2018-09-01 01:02:41
                                                                               1.0
                                                                               . . .
          8049089
                   2018-09-30 23:04:00
                                           2018-09-30 23:37:00
                                                                               NaN
          8049090
                   2018-09-30 23:02:00
                                           2018-09-30 23:31:00
                                                                               NaN
                   2018-09-30 23:21:00
                                           2018-09-30 23:35:00
                                                                               NaN
          8049091
          8049092
                   2018-09-30 23:14:00
                                           2018-09-30 23:36:00
                                                                               NaN
                                           2018-09-30 23:29:00
                                                                               NaN
          8049093
                   2018-09-30 23:17:00
                                   PULocationID
                                                  DOLocationID
                   trip_distance
          0
                             1.50
                                             161
                                                             107
          1
                             1.00
                                             233
                                                             100
          2
                             1.00
                                             164
                                                            163
          3
                             1.90
                                              48
                                                            140
          4
                             0.60
                                             262
                                                             263
                              . . .
                                                             . . .
          8049089
                            18.81
                                             177
                                                             69
                             6.27
                                             225
                                                             226
          8049090
          8049091
                             3.93
                                             170
                                                            238
                                             226
          8049092
                             8.04
                                                            159
          8049093
                             3.63
                                               7
                                                            230
          [8049094 \text{ rows } \times 6 \text{ columns}]
                    tpep_pickup_datetime tpep_dropoff_datetime passenger_count
          0
                    2017-03-01 00:38:16
                                            2017-03-01 00:59:21
                                                                                  1
          1
                                                                                  1
                    2017-03-01 00:25:01
                                            2017-03-01 00:31:36
          2
                                                                                  1
                    2017-03-01 00:43:48
                                            2017-03-01 00:44:17
          3
                    2017-03-01 00:47:17
                                            2017-03-01 00:47:33
                                                                                  1
          4
                    2017-03-01 00:13:37
                                            2017-03-01 00:13:46
                                                                                  1
                                                                                . . .
          . . .
                    2017-03-31 23:38:53
                                            2017-04-01 00:05:17
                                                                                  1
          10295436
          10295437
                    2017-03-31 23:06:11
                                            2017-03-31 23:12:46
                                                                                  1
          10295438
                    2017-03-31 23:14:00
                                            2017-03-31 23:14:11
                                                                                  1
          10295439
                    2017-03-31 23:22:28
                                            2017-03-31 23:39:02
                                                                                  1
          10295440
                    2017-03-31 23:40:59
                                            2017-03-31 23:55:37
                                                                                  1
                    trip_distance PULocationID DOLocationID
          0
                             10.50
                                              231
                                                              42
          1
                              1.40
                                              239
                                                              262
          2
                              0.00
                                              145
                                                              145
          3
                              0.00
                                              145
                                                              145
          4
                              0.00
                                              145
                                                              145
                               . . .
                                               . . .
                                                              . . .
                                              237
                                                              116
          10295436
                              5.80
          10295437
                              1.05
                                               48
                                                              50
                                               50
                                                              143
          10295438
                              0.01
                              1.44
                                               48
                                                              100
          10295439
          10295440
                                              100
                                                              236
                              3.12
          [10295441 \text{ rows x 6 columns}],
                  tpep_pickup_datetime tpep_dropoff_datetime
                                                                  passenger_count \
          0
                    2018-10-01 00:23:34
                                           2018-10-01 00:44:50
                                                                               1.0
          1
                   2018-10-01 00:40:05
                                           2018-10-01 01:01:56
                                                                               1.0
          2
                                           2018-10-01 00:19:38
                   2018-10-01 00:05:35
                                                                               1.0
          3
                   2018-10-01 00:42:56
                                           2018-10-01 00:49:00
                                                                               1.0
                   2018-10-01 00:19:14
                                           2018-10-01 00:31:54
                                                                               1.0
```

```
. . .
8834515
         2018-10-31 23:36:00
                                2018-10-31 23:55:00
                                                                   NaN
8834516
         2018-10-31 23:09:00
                                2018-10-31 23:38:00
                                                                   NaN
8834517
         2018-10-31 23:35:16
                                2018-11-01 00:07:43
                                                                   NaN
8834518 2018-10-31 23:01:00
                                2018-10-31 23:34:00
                                                                   NaN
8834519 2018-10-31 23:07:53
                                2018-10-31 23:37:20
                                                                   NaN
         trip_distance PULocationID DOLocationID
0
                  6.20
                                   68
                                                   7
1
                 12.60
                                  132
                                                   9
2
                  6.10
                                  50
                                                 244
3
                  1.30
                                  151
                                                 239
4
                  2.60
                                  233
                                                 143
                   . . .
                                  . . .
                  9.38
                                  235
                                                 246
8834515
8834516
                 13.29
                                  225
                                                 53
                 19.58
                                  79
                                                 222
8834517
8834518
                 11.43
                                  158
                                                  69
                                  140
8834519
                  12.84
                                                 102
[8834520 \text{ rows } \times 6 \text{ columns}]
        tpep_pickup_datetime tpep_dropoff_datetime passenger_count
0
         2017-02-01 00:19:20 2017-02-01 00:25:56
                                                                     1
1
                                                                     1
         2017-02-01 00:19:55
                                2017-02-01 00:33:06
2
         2017-02-01 00:01:15
                                2017-02-01 00:09:03
                                                                     2
3
                                                                     5
         2017-02-01 00:06:36
                                2017-02-01 00:14:50
                                2017-02-01 00:14:36
4
         2017-02-01 00:07:53
                                                                     1
9169770
         2017-02-28 23:35:01
                                2017-02-28 23:56:25
                                                                     2
9169771 2017-02-28 23:58:55
                                2017-03-01 00:17:41
                                                                     1
                                                                     1
9169772 2017-02-28 23:26:41
                                2017-02-28 23:26:45
         2017-02-28 23:27:31
                                                                     1
9169773
                                2017-02-28 23:27:33
9169774 2017-02-28 23:28:08
                                2017-02-28 23:28:10
                                                                     1
         trip distance PULocationID DOLocationID
0
                  2.90
                                   75
                                                 162
1
                  4.90
                                  246
                                                 166
2
                  1.50
                                  237
                                                 170
                  1.51
3
                                  137
                                                 236
4
                  1.40
                                 112
                                                 112
                   . . .
                  5.40
9169770
                                  114
                                                  43
                                  43
                                                  79
9169771
                  5.80
9169772
                  0.00
                                  264
                                                 193
                                  264
                                                 193
9169773
                  0.00
9169774
                  0.00
                                  264
                                                 193
[9169775 \text{ rows } \times 6 \text{ columns}]
        tpep_pickup_datetime tpep_dropoff_datetime
                                                      passenger_count \
0
         2017-12-01 00:12:00 2017-12-01 00:12:51
1
         2017-12-01 00:13:37
                                2017-12-01 00:13:47
                                                                     1
2
                                2017-12-01 00:15:05
                                                                     1
         2017-12-01 00:14:15
3
         2017-12-01 00:15:33
                                2017-12-01 00:15:37
                                                                     1
4
         2017-12-01 00:50:03
                                2017-12-01 00:53:35
                                                                     1
. . .
9508496 2017-12-31 23:31:57
                                2017-12-31 23:55:59
                                                                     1
9508497
         2017-12-31 22:53:16
                                2017-12-31 22:57:03
                                                                     1
                                                                     1
         2017-12-31 23:05:23
                                2017-12-31 23:14:30
9508498
                                                                     1
9508499
         2017-12-31 23:22:29
                                2017-12-31 23:31:47
         2017-12-31 23:34:49
                                2017-12-31 23:40:29
9508500
```

```
PULocationID
                                          DOLocationID
          trip distance
0
                    0.00
                                    226
                                                    226
1
                    0.00
                                    226
                                                    226
2
                    0.00
                                    226
                                                    226
3
                    0.00
                                    226
                                                    226
4
                    0.00
                                    145
                                                    145
                     . . .
                                     . . .
                                                    . . .
. . .
9508496
                    9.80
                                    186
                                                    127
9508497
                    0.63
                                     74
                                                     74
                    3.05
                                    236
                                                     42
9508498
9508499
                    1.76
                                     74
                                                    152
9508500
                    0.91
                                    152
                                                     41
[9508501 \text{ rows } \times 6 \text{ columns}],
         tpep pickup datetime tpep dropoff datetime
                                                          passenger count \
0
          2018-11-01 00:51:36
                                  2018-11-01 00:52:36
                                                                       1.0
1
          2018-11-01 00:07:47
                                  2018-11-01 00:21:43
                                                                       1.0
2
          2018-11-01 00:24:27
                                  2018-11-01 00:34:29
                                                                       1.0
3
          2018-11-01 00:35:27
                                  2018-11-01 00:47:02
                                                                       1.0
4
          2018-11-01 00:16:46
                                  2018-11-01 00:22:50
                                                                       1.0
. . .
                                                                       . . .
8155444
         2018-11-30 23:28:00
                                  2018-12-01 00:00:00
                                                                       NaN
          2018-11-30 23:07:00
                                  2018-11-30 23:51:00
                                                                       NaN
8155445
8155446
         2018-11-30 23:07:00
                                  2018-11-30 23:27:00
                                                                       NaN
8155447
          2018-11-30 23:36:00
                                  2018-12-01 00:09:00
                                                                       NaN
         2018-11-30 23:17:53
                                  2018-11-30 23:45:06
                                                                       NaN
8155448
          trip_distance
                          PULocationID
                                          DOLocationID
0
                    0.00
                                    145
                                                    145
1
                    2.30
                                    142
                                                    164
2
                    1.80
                                    164
                                                     48
3
                    2.30
                                     48
                                                    107
4
                    1.00
                                    163
                                                    170
. . .
                     . . .
                                     . . .
                                                    . . .
                    9.95
8155444
                                    151
                                                    196
8155445
                   15.80
                                    107
                                                    191
8155446
                    9.40
                                    226
                                                     42
8155447
                   10.52
                                      68
                                                    169
8155448
                                      25
                                                     21
                    7.75
[8155449 \text{ rows } \times 6 \text{ columns}],
         tpep pickup datetime tpep dropoff datetime
                                                          passenger count
0
          2018-01-01 00:21:05
                                  2018-01-01 00:24:23
1
          2018-01-01 00:44:55
                                  2018-01-01 01:03:05
                                                                         1
2
                                                                         2
          2018-01-01 00:08:26
                                  2018-01-01 00:14:21
3
                                                                         1
          2018-01-01 00:20:22
                                  2018-01-01 00:52:51
4
                                                                         2
          2018-01-01 00:09:18
                                  2018-01-01 00:27:06
. . .
         2018-01-31 23:21:35
                                  2018-01-31 23:34:20
                                                                         2
8760682
         2018-01-31 23:35:51
                                  2018-01-31 23:38:57
                                                                         1
8760683
                                  2018-01-31 23:37:09
                                                                         1
8760684
         2018-01-31 23:28:00
                                                                         1
8760685
         2018-01-31 23:24:40
                                  2018-01-31 23:25:28
8760686
         2018-01-31 23:28:16
                                  2018-01-31 23:28:38
                                                                         1
                          PULocationID
                                          DOLocationID
          trip_distance
0
                    0.50
                                     41
                                                     24
1
                    2.70
                                    239
                                                    140
2
                    0.80
                                    262
                                                    141
3
                   10.20
                                     140
                                                    257
```

```
4
                   2.50
                                   246
                                                   239
                    . . .
                                   . . .
                                                   . . .
. . .
8760682
                   2.80
                                   158
                                                   163
                   0.60
                                   163
8760683
                                                   162
8760684
                   2.95
                                    74
                                                   69
8760685
                   0.00
                                      7
                                                   193
                                      7
8760686
                   0.00
                                                   193
[8760687 rows \times 6 columns],
        tpep_pickup_datetime tpep_dropoff_datetime
                                                        passenger_count \
0
          2018-08-01 00:44:35
                                 2018-08-01 01:03:22
         2018-08-01 00:02:19
1
                                 2018-08-01 00:02:31
                                                                     1.0
2
          2018-08-01 00:13:25
                                 2018-08-01 00:24:40
                                                                     1.0
3
         2018-08-01 00:10:37
                                 2018-08-01 00:49:10
                                                                     1.0
4
         2018-08-01 00:02:18
                                 2018-08-01 00:07:32
                                                                     2.0
                                                                     . . .
. . .
7855035
         2018-08-31 23:19:00
                                 2018-08-31 23:38:00
                                                                     NaN
7855036
         2018-08-31 23:46:00
                                 2018-08-31 23:46:00
                                                                     NaN
         2018-08-31 23:09:51
                                 2018-08-31 23:14:33
7855037
                                                                     NaN
7855038
         2018-08-31 23:30:00
                                 2018-08-31 23:35:00
                                                                     NaN
7855039 2018-08-31 23:05:00
                                 2018-08-31 23:31:00
                                                                     NaN
                         PULocationID DOLocationID
         trip_distance
0
                   5.60
                                   238
                                                   79
                   0.00
                                   145
                                                   145
1
2
                   2.90
                                   138
                                                     7
3
                                                     7
                                   231
                   8.40
4
                   0.70
                                    79
                                                   148
                    . . .
                                   . . .
                                                   . . .
. . .
                  10.25
                                                   75
7855035
                                   183
                   0.00
                                   232
                                                   232
7855036
7855037
                   0.54
                                    79
                                                   79
7855038
                   0.91
                                    48
                                                   163
                  12.60
                                   246
                                                   213
7855039
[7855040 \text{ rows } \times 6 \text{ columns}],
        tpep pickup datetime tpep dropoff datetime
                                                        passenger count
0
         2017-10-01 00:01:50
                                 2017-10-01 00:14:13
                                                                       1
                                                                       2
1
         2017-10-01 00:02:43
                                 2017-10-01 00:08:35
2
                                                                       3
         2017-10-01 00:12:08
                                 2017-10-01 00:25:49
3
         2017-10-01 00:00:25
                                 2017-10-01 00:11:24
                                                                       1
4
         2017-10-01 00:15:30
                                 2017-10-01 00:25:11
                                                                        1
9768667
         2017-10-31 23:05:37
                                 2017-10-31 23:14:07
                                                                       1
9768668
         2017-10-31 23:45:12
                                 2017-10-31 23:50:51
                                                                       1
                                                                       2
9768669
         2017-10-31 23:33:17
                                 2017-11-01 00:02:51
                                                                       1
9768670
         2017-10-31 23:25:32
                                 2017-10-31 23:31:22
                                 2017-11-01 00:16:14
                                                                       1
9768671
         2017-10-31 23:34:55
                                         DOLocationID
          trip distance
                         PULocationID
0
                   2.00
                                   142
                                                   233
1
                   2.30
                                   142
                                                   166
2
                   2.80
                                   151
                                                   262
3
                   1.97
                                                   229
                                   100
4
                   2.17
                                   141
                                                   142
                    . . .
9768667
                   4.67
                                    13
                                                   257
                   1.54
                                                   33
9768668
                                   181
                   6.20
                                   100
                                                   255
9768669
9768670
                   0.82
                                   264
                                                   264
```

```
[9768672 rows x 6 columns].
        tpep_pickup_datetime tpep_dropoff_datetime passenger_count
         2018-03-01 00:01:34
                                2018-03-01 00:01:43
1
         2018-03-01 00:14:34
                                2018-03-01 00:28:13
                                                                      1
2
         2018-03-01 00:51:25
                                2018-03-01 00:59:54
                                                                      1
3
                                                                      1
         2018-03-01 00:00:01
                                2018-03-01 00:00:17
4
         2018-03-01 00:55:10
                                 2018-03-01 00:56:36
                                                                      1
. . .
                                                                      5
         2018-03-31 23:34:47
                                 2018-03-31 23:55:17
9431284
9431285
         2018-03-31 23:02:38
                                2018-03-31 23:13:10
                                                                      6
9431286
         2018-03-31 23:15:58
                                 2018-03-31 23:30:29
                                                                      6
9431287
         2018-03-31 23:05:37
                                 2018-03-31 23:18:31
                                                                      2
9431288 2018-03-31 23:37:11
                                2018-03-31 23:56:53
                                                                      1
         trip_distance PULocationID DOLocationID
0
                   0.00
                                   145
                                                  145
1
                   3.30
                                   151
                                                  244
2
                   2.70
                                   238
                                                 152
3
                   0.00
                                   145
                                                  145
4
                   3.70
                                   145
                                                 145
                   . . .
                                                  . . .
9431284
                   4.11
                                   186
                                                 263
9431285
                   1.50
                                   100
                                                 107
9431286
                   2.07
                                   107
                                                  170
                   1.60
9431287
                                   163
                                                  164
9431288
                   3.90
                                   144
                                                  161
[9431289 \text{ rows } \times 6 \text{ columns}],
        tpep_pickup_datetime tpep_dropoff_datetime
                                                       passenger_count
0
         2017-09-01 00:17:17
                                2017-09-01 00:18:49
                                                                      2
1
         2017-09-01 00:22:08
                                2017-09-01 00:25:22
2
                                                                      1
         2017-09-01 00:30:43
                                2017-09-01 00:33:47
3
         2017-09-01 00:37:57
                                2017-09-01 00:42:24
         2017-09-01 00:15:56
                                2017-09-01 00:28:28
                                                                      1
8945416 2017-09-30 23:03:35
                                 2017-09-30 23:14:56
                                                                      1
8945417
         2017-09-30 23:15:53
                                2017-09-30 23:20:33
                                                                      1
8945418 2017-09-30 23:05:20
                                2017-09-30 23:23:22
                                                                      1
8945419 2017-09-30 23:28:39
                                2017-10-01 00:24:39
                                                                      1
8945420 2017-09-30 23:36:10
                                 2017-10-01 00:03:27
                                                                      1
         trip_distance PULocationID DOLocationID
0
                   0.40
                                   161
                                                  161
                   0.90
                                   164
                                                 234
1
2
                   0.52
                                                 193
                                   193
3
                   1.50
                                   246
                                                  50
4
                   1.30
                                   143
                                                  143
                   . . .
                                   . . .
                                                  . . .
                   2.22
                                   48
                                                  141
8945416
                   1.50
                                   141
                                                 263
8945417
8945418
                   4.98
                                   164
                                                  87
                  13.98
                                   87
                                                 258
8945419
8945420
                   5.26
                                   148
                                                  140
[8945421 rows \times 6 columns],
        tpep pickup datetime tpep dropoff datetime
                                                       passenger count
0
         2017-08-01 00:29:45
                                2017-08-01 00:29:51
                                                                      1
                                                                      2
1
         2017-08-01 00:06:34
                                 2017-08-01 00:19:23
```

```
2
         2017-08-01 00:07:46
                               2017-08-01 00:14:51
                                                                   1
3
                               2017-08-01 00:35:36
                                                                   1
         2017-08-01 00:16:03
4
                                                                   1
         2017-08-01 00:21:14
                                2017-08-01 00:22:40
8422148 2017-08-31 23:39:07
                                2017-09-01 00:08:22
                                                                   1
8422149 2017-08-31 23:04:26
                               2017-08-31 23:44:33
                                                                   1
                                                                   2
8422150 2017-08-31 23:09:33
                               2017-08-31 23:15:32
                                                                  1
8422151 2017-08-31 23:37:20
                                2017-08-31 23:53:32
8422152 2017-08-31 23:55:14
                               2017-09-01 00:02:22
                                                                   1
         trip_distance PULocationID D0LocationID
0
                  0.00
                                 145
                                                145
1
                  1.20
                                  140
                                                237
2
                  3.80
                                 223
                                                 70
3
                                  79
                  3.30
                                                230
4
                  0.50
                                 162
                                                237
                  . . .
8422148
                 10.10
                                 138
                                                 61
                                 50
                                                196
8422149
                 10.72
                                  41
                                                116
8422150
                 1.70
8422151
                  3.89
                                  68
                                                263
8422152
                  1.91
                                  263
                                                233
[8422153 rows x 6 columns],
        tpep pickup datetime tpep dropoff datetime
                                                     passenger_count
0
         2017-01-01 00:32:05 2017-01-01 00:37:48
                                                                   1
1
                                                                   2
         2017-01-01 00:43:25
                               2017-01-01 00:47:42
2
                                                                   2
         2017-01-01 00:49:10
                               2017-01-01 00:53:53
3
         2017-01-01 00:36:42
                                2017-01-01 00:41:09
                                                                   1
4
         2017-01-01 00:07:41
                               2017-01-01 00:18:16
                                                                   1
9710815 2017-01-31 23:04:11
                               2017-01-31 23:10:56
                                                                   2
9710816 2017-01-31 23:32:46
                               2017-01-31 23:40:14
                                                                   4
                                                                   1
9710817 2017-01-31 23:23:22
                               2017-01-31 23:38:38
         2017-01-31 23:48:10
                               2017-01-31 23:57:15
                                                                   1
9710818
9710819 2017-01-31 23:57:58
                               2017-02-01 00:11:16
         trip_distance PULocationID D0LocationID
0
                  1.20
                                 140
                                                236
1
                  0.70
                                 237
                                                140
2
                  0.80
                                 140
                                                237
3
                                 41
                  1.10
                                                42
4
                  3.00
                                 48
                                                263
                  . . .
                                 . . .
                                                . . .
9710815
                                                 45
                  1.04
                                  148
9710816
                  1.60
                                 264
                                                264
9710817
                  3.65
                                 148
                                                 48
                                                 79
                                  249
9710818
                  0.93
                  2.71
9710819
                                  79
                                                256
[9710820 rows x 6 columns],
        tpep_pickup_datetime tpep_dropoff_datetime
                                                     passenger_count
0
         2017-11-01 00:01:48
                               2017-11-01 00:03:47
1
                                                                   1
         2017-11-01 00:18:22
                               2017-11-01 00:40:32
2
         2017-11-01 00:01:58
                                2017-11-01 00:15:57
                                                                   1
3
                                                                   1
         2017-11-01 00:18:53
                               2017-11-01 00:25:23
         2017-11-01 00:28:56
                                2017-11-01 00:38:22
                                                                   1
                                                                  . . .
         2017-11-30 23:27:24
9284798
                                2017-11-30 23:48:15
                                                                   1
9284799
        2017-11-30 23:59:05
                                2017-11-30 23:59:14
```

```
1
9284800 2017-11-30 23:17:20
                                 2017-11-30 23:39:33
9284801 2017-11-30 22:52:40
                                 2017-11-30 23:27:26
                                                                      1
                                                                      1
9284802 2017-11-30 23:33:39
                                 2017-11-30 23:42:54
         trip_distance
                        PULocationID DOLocationID
0
                   0.40
                                   151
                                                  151
1
                   4.80
                                   142
                                                  144
2
                   3.70
                                   151
                                                  140
3
                   1.90
                                   140
                                                  233
4
                   2.00
                                   229
                                                   50
                   . . . .
                                   . . .
                                                  . . .
9284798
                   3.16
                                    90
                                                  141
9284799
                   0.00
                                    25
                                                   25
9284800
                  10.28
                                                  127
                                   161
9284801
                   5.80
                                   113
                                                  181
9284802
                   1.68
                                   181
                                                   25
[9284803 rows x 6 columns],
        tpep_pickup_datetime tpep_dropoff_datetime
                                                       passenger count
0
         2018-12-01 00:28:22
                                 2018-12-01 00:44:07
                                                                    2.0
1
         2018-12-01 00:52:29
                                 2018-12-01 01:11:37
                                                                    3.0
2
         2018-12-01 00:12:52
                                 2018-12-01 00:36:23
                                                                    1.0
3
         2018-12-01 00:35:08
                                 2018-12-01 00:43:11
                                                                    1.0
4
         2018-12-01 00:21:54
                                 2018-12-01 01:15:13
                                                                    1.0
                                                                    . . .
8195670 2018-12-31 23:25:00
                                 2018-12-31 23:40:00
                                                                    NaN
8195671
         2018-12-31 23:04:00
                                 2018-12-31 23:30:00
                                                                    NaN
8195672
         2018-12-31 23:02:00
                                 2018-12-31 23:35:00
                                                                    NaN
                                 2018-12-31 23:43:00
8195673
         2018-12-31 23:17:00
                                                                    NaN
8195674 2018-12-31 23:01:26
                                 2018-12-31 23:43:42
                                                                    NaN
         trip_distance PULocationID DOLocationID
0
                   2.50
                                   148
                                                  234
1
                   2.30
                                   170
                                                  144
2
                                                  193
                   0.00
                                   113
3
                   3.90
                                   95
                                                   92
4
                  12.80
                                   163
                                                  228
                    . . .
                                   . . .
                                                  . . .
                   9.32
8195670
                                    50
                                                  265
8195671
                  9.06
                                   243
                                                  182
8195672
                  11.70
                                   236
                                                  254
                   7.82
                                   146
                                                   78
8195673
                   9.92
                                    95
                                                   48
8195674
[8195675 \text{ rows } \times 6 \text{ columns}]
        tpep_pickup_datetime tpep_dropoff_datetime
                                                       passenger_count
0
         2018-02-01 00:01:58
                                 2018-02-01 00:04:03
                                                                      1
                                                                      1
1
         2018-02-01 00:56:48
                                 2018-02-01 00:57:42
2
         2018-02-01 00:04:42
                                 2018-02-01 00:19:32
                                                                      1
3
                                                                      1
         2018-02-01 00:38:10
                                 2018-02-01 00:40:16
4
                                                                      2
         2018-02-01 00:43:03
                                 2018-02-01 00:59:26
                                                                    . . .
. . .
8492814
         2018-02-28 23:21:56
                                 2018-02-28 23:47:43
                                                                      6
         2018-02-28 23:54:07
8492815
                                 2018-03-01 00:24:56
                                                                      6
8492816
         2018-02-28 23:17:42
                                 2018-02-28 23:53:11
                                                                      1
                                                                      2
         2018-03-01 13:39:17
                                 2018-03-01 13:49:08
8492817
8492818 2018-02-28 23:03:18
                                 2018-02-28 23:03:24
                                        DOLocationID
         trip distance
                         PULocationID
                   0.00
                                   145
                                                  145
```

```
2.90
1
                                    145
                                                    145
2
                   5.80
                                    236
                                                    119
3
                   0.30
                                     82
                                                     82
4
                   2.60
                                     82
                                                      7
                    . . .
                                     . . .
                                                    . . .
8492814
                    9.61
                                    138
                                                    163
8492815
                   4.20
                                    230
                                                    230
                    0.00
8492816
                                    193
                                                    193
8492817
                    0.00
                                    264
                                                    264
8492818
                    0.00
                                    264
                                                    193
[8492819 \text{ rows } \times 6 \text{ columns}],
        tpep_pickup_datetime tpep_dropoff_datetime
                                                         passenger count
0
          2018-07-01 00:28:09
                                  2018-07-01 00:28:51
                                                                       1.0
1
                                                                       1.0
          2018-07-01 00:29:27
                                  2018-07-01 00:30:17
2
          2018-07-01 00:04:19
                                  2018-07-01 00:08:29
                                                                       2.0
3
          2018-07-01 00:14:26
                                  2018-07-01 00:36:35
                                                                       1.0
4
          2018-07-01 00:41:56
                                  2018-07-01 00:50:54
                                                                       1.0
                                                                       . . .
. . .
7851138
         2018-07-31 19:02:00
                                  2018-07-31 19:33:00
                                                                       NaN
7851139
         2018-07-31 19:12:00
                                  2018-07-31 19:13:00
                                                                       NaN
                                                                       NaN
7851140
         2018-07-31 20:57:00
                                  2018-07-31 21:47:00
7851141
         2018-07-31 22:50:00
                                  2018-07-31 22:50:00
                                                                       NaN
                                                                       NaN
7851142
         2018-07-31 23:02:00
                                  2018-07-31 23:20:00
         trip distance
                          PULocationID
                                          D0LocationID
0
                    5.30
                                    145
                                                    145
1
                   5.30
                                    145
                                                    145
2
                   0.70
                                    211
                                                    144
3
                   4.80
                                    144
                                                    142
4
                   1.80
                                    142
                                                    141
                     . . .
                                    . . .
                                                    . . .
. . .
7851138
                   17.15
                                    158
                                                    265
7851139
                   0.00
                                    132
                                                    132
                   33.54
                                     48
                                                    265
7851140
                                     79
                                                     79
7851141
                    0.00
7851142
                    4.68
                                    249
                                                    265
[7851143 \text{ rows } \times 6 \text{ columns}]
          tpep pickup datetime tpep dropoff datetime
                                                           passenger count
0
           2017-04-01 00:51:24
                                   2017-04-01 00:51:49
                                                                          1
1
           2017-04-01 00:41:17
                                   2017-04-01 00:55:36
                                                                          1
2
                                                                          1
           2017-04-01 00:23:31
                                   2017-04-01 00:35:17
3
           2017-04-01 00:05:31
                                   2017-04-01 00:35:30
                                                                          1
                                                                          2
4
           2017-04-01 00:38:13
                                   2017-04-01 00:54:48
                                                                        . . .
10047130 2017-04-30 23:42:01
                                   2017-04-30 23:56:39
                                                                          1
          2017-04-30 23:18:36
                                   2017-04-30 23:24:55
                                                                          1
10047131
                                                                          2
10047132
          2017-04-30 23:33:25
                                   2017-04-30 23:39:30
                                                                          1
10047133
          2017-04-30 23:54:53
                                   2017-04-30 23:56:16
          2017-04-30 23:58:57
                                                                          1
10047134
                                   2017-05-01 00:00:45
           trip_distance PULocationID DOLocationID
0
                     0.00
                                     145
                                                     145
1
                     3.40
                                     249
                                                      87
2
                     2.50
                                                     263
                                     163
3
                     4.50
                                     163
                                                       7
4
                     4.90
                                        7
                                                     262
                                                     . . .
10047130
                     3.39
                                      186
                                                     263
```

| | | ADS_midterm_ | spring2024 | |
|----------------------|--|--------------------------|------------|-------------------|
| 10047131 | | 68 | 107 | |
| 10047132 | | 170 | 229 | |
| 10047133 10047134 | | 7 193 | 7 193 | |
| 1004/134 | 0.00 | 193 | 195 | |
| | 5 rows x 6 columns], | | | |
| | tpep_pickup_datetime | | | passenger_count \ |
| 0 1 | 2018-06-01 00:15:40 2018-06-01 00:04:18 | 2018-06-01 2018-06-01 | | 1 1 |
| 2 | 2018-06-01 00:14:39 | | | 1 |
| 3 | 2018-06-01 00:51:25 | | | 3 |
| 4 | 2018-06-01 00:55:06 | 2018-06-01 | 00:55:10 | 1 |
| 8714662 | 2018-06-30 23:09:48 | 2018-06-30 | 23:21:09 | 1 |
| 8714663 | 2018-06-30 23:39:24 | 2018-06-30 | 23:45:02 | 3 |
| 8714664 | 2018-06-30 23:24:13 | 2018-06-30 | | 2 |
| 8714665 8714666 | 2018-06-30 23:46:15 2018-06-30 23:43:59 | | | 1 1 |
| 0714000 | 2010-00-30 23:43:39 | 2010-00-30 | 23.43.39 | 1 |
| | · | | cationID | |
| 0 | 0.00 | 145 | 145 | |
| 1 2 | 1.00 3.30 | 230 100 | 161 263 | |
| 3 | 0.00 | 145 | 145 | |
| 4 | 0.00 | 145 | 145 | |
| 0714662 | F 00 | 120 | | |
| 8714662 8714663 | 5.00 0.70 | 138 230 | 92 230 | |
| 8714664 | 1.88 | 166 | 239 | |
| 8714665 | 2.40 | 142 | 68 | |
| 8714666 | 0.00 | 264 | 7 | |
| [8714667 | rows x 6 columns], | | | |
| | tpep_pickup_datetime | | | |
| 0 | 2017-05-01 00:02:54 | | | 1 |
| 1 2 | 2017-05-01 00:03:52 2017-05-01 00:00:10 | | | 1 1 |
| 3 | 2017-05-01 00:48:58 | | | 1 |
| 4 | 2017-05-01 00:27:37 | 2017-05-01 | L 00:39:40 | 1 |
| 10102122 | 2017-05-31 23:19:41 | 2017-05-31 | | 1 |
| 10102122 | | | | 1 |
| 10102124 | | | | 1 |
| 10102125 | | | | 1 |
| 10102126 | 2017-05-31 23:52:58 | 2017-06-01 | 1 00:0/:15 | 1 |
| | trip_distance PULo | cationID DOL | ocationID | |
| 0 | 0.00 | 260 | 260 | |
| 1 | 0.00 | 145 | 145 | |
| 2 | 2.50 7.20 | 68 230 | 79 160 | |
| 4 | 2.70 | 138 | 223 | |
| 10102122 | 2.10 | 224 | 40 | |
| 10102122 10102123 | | 234 186 | 48 164 | |
| 10102123 | | 261 | 231 | |
| 10102125 | 0.61 | 141 | 140 | |
| 10102126 | 2.38 | 141 | 170 | |
| | | | | |

[10102127 rows x 6 columns],

```
tpep_pickup_datetime tpep_dropoff_datetime
                                                        passenger_count
0
         2018-04-01 00:22:20
                                 2018-04-01 00:22:26
                                                                       1
1
                                                                       1
         2018-04-01 00:47:37
                                 2018-04-01 01:08:42
2
                                                                       2
         2018-04-01 00:02:13
                                 2018-04-01 00:17:52
3
         2018-04-01 00:46:49
                                 2018-04-01 00:52:05
                                                                       1
4
                                                                       1
         2018-04-01 00:19:04
                                 2018-04-01 00:19:09
9306211
         2018-04-30 23:15:20
                                 2018-04-30 23:32:58
                                                                       1
9306212
         2018-04-30 23:02:02
                                 2018-04-30 23:03:37
                                                                       5
         2018-04-30 23:38:18
                                                                       1
9306213
                                 2018-04-30 23:44:57
                                                                       1
9306214
         2018-04-30 23:07:08
                                 2018-04-30 23:23:04
                                                                       1
9306215 2018-04-30 23:26:50
                                 2018-04-30 23:44:54
                         PULocationID
                                        DOLocationID
         trip_distance
0
                   0.00
                                                  145
                                   145
1
                   6.70
                                   152
                                                   90
2
                   4.10
                                   239
                                                  158
3
                   0.70
                                    90
                                                  249
4
                   0.00
                                   145
                                                  145
                    . . .
                                                  . . .
9306211
                   3.60
                                   148
                                                  112
9306212
                                                  151
                   0.01
                                   151
9306213
                   1.62
                                   186
                                                  125
                   6.36
9306214
                                   261
                                                  162
9306215
                   7.17
                                   162
                                                   65
[9306216 \text{ rows } \times 6 \text{ columns}],
        tpep_pickup_datetime tpep_dropoff_datetime
                                                        passenger_count
0
         2017-07-01 00:06:25
                                 2017-07-01 00:10:50
                                                                       1
1
                                                                       2
         2017-07-01 00:20:04
                                 2017-07-01 00:21:38
2
                                                                       1
         2017-07-01 00:44:10
                                 2017-07-01 00:59:29
3
                                                                       1
         2017-07-01 00:07:33
                                 2017-07-01 00:31:30
4
         2017-07-01 00:01:17
                                 2017-07-01 00:16:18
                                                                       1
. . .
         2017-07-31 23:57:40
                                 2017-08-01 00:07:49
8588481
                                                                       1
8588482
         2017-07-31 23:04:41
                                 2017-07-31 23:10:18
                                                                       1
8588483
         2017-07-31 23:35:47
                                 2017-07-31 23:46:01
                                                                       3
8588484
         2017-07-31 23:50:49
                                 2017-08-01 00:00:59
                                                                       3
8588485
         2017-07-31 23:44:14
                                 2017-07-31 23:50:21
         trip_distance
                         PULocationID
                                        DOLocationID
0
                                                   90
                   1.20
                                   249
1
                   0.20
                                   249
                                                  158
2
                   4.30
                                                   45
                                   100
3
                   8.30
                                   138
                                                  162
4
                   1.90
                                   107
                                                  158
                    . . .
                                   . . .
                                                  . . .
8588481
                   2.21
                                   170
                                                  142
8588482
                   1.41
                                   262
                                                  141
                   1.66
8588483
                                   113
                                                  148
                   3.02
                                   148
                                                   80
8588484
                                                  107
8588485
                   1.40
                                   162
[8588486 rows x 6 columns],
        tpep_pickup_datetime tpep_dropoff_datetime
                                                        passenger_count
0
         2018-05-01 00:13:56
                                 2018-05-01 00:22:46
                                                                       1
1
         2018-05-01 00:23:26
                                 2018-05-01 00:29:56
                                                                       1
2
                                                                       2
         2018-05-01 00:36:23
                                 2018-05-01 00:48:26
3
                                                                       1
         2018-05-01 00:26:12
                                 2018-05-01 00:27:05
         2018-05-01 00:29:51
                                 2018-05-01 00:30:02
```

```
9224783
         2018-05-31 23:25:13
                                 2018-05-31 23:27:46
                                                                       2
                                 2018-05-31 23:19:39
                                                                       1
9224784
         2018-05-31 23:15:24
                                                                       1
9224785
         2018-05-31 23:46:26
                                 2018-05-31 23:52:55
9224786
         2018-05-31 23:59:33
                                 2018-06-01 00:11:58
                                                                      1
9224787
         2018-05-31 23:27:40
                                 2018-06-01 00:14:39
                                                                       1
         trip_distance PULocationID DOLocationID
0
                   1.60
                                   230
                                                   50
1
                   1.70
                                   263
                                                  239
2
                   2.60
                                   239
                                                  152
3
                   0.00
                                   145
                                                  145
4
                   0.00
                                   145
                                                  145
                    . . .
                                   . . .
                                                  . . .
9224783
                   0.70
                                   140
                                                  262
9224784
                   0.91
                                   263
                                                  237
9224785
                   1.29
                                   230
                                                  237
9224786
                   2.42
                                   163
                                                   90
9224787
                   9.10
                                   142
                                                  158
[9224788 \text{ rows } \times 6 \text{ columns}]
        tpep_pickup_datetime tpep_dropoff_datetime passenger_count
0
         2017-06-01 00:02:36
                                 2017-06-01 00:10:02
                                                                       1
                                                                       1
1
         2017-06-01 00:14:14
                                 2017-06-01 00:16:50
2
         2017-06-01 00:47:11
                                 2017-06-01 00:57:47
                                                                       1
3
                                                                       1
         2017-06-01 00:14:38
                                 2017-06-01 00:19:49
                                 2017-06-01 00:57:09
                                                                       1
4
         2017-06-01 00:03:41
         2017-06-30 23:07:15
                                 2017-06-30 23:33:18
9656988
                                                                       1
         2017-06-30 23:35:12
                                 2017-06-30 23:44:46
                                                                       1
9656989
9656990
         2017-06-30 23:59:15
                                 2017-07-01 00:09:35
                                                                       1
9656991
         2017-06-30 23:12:25
                                 2017-06-30 23:25:50
                                                                       1
         2017-06-30 23:34:04
                                                                       3
9656992
                                 2017-06-30 23:47:26
         trip distance PULocationID DOLocationID
0
                   1.80
                                   161
                                                  263
1
                   0.80
                                   237
                                                  237
2
                   1.70
                                    48
                                                  233
3
                   1.10
                                   246
                                                  249
4
                  14.80
                                   166
                                                   61
                    . . .
                                   . . .
                                                  . . .
                                                  238
9656988
                   6.76
                                   232
                   4.51
                                   238
                                                  244
9656989
                   2.49
                                    42
                                                  238
9656990
9656991
                   2.50
                                   161
                                                  141
9656992
                   3.60
                                   264
                                                   41
[9656993 rows x 6 columns]]
```

```
In [6]: combined_df = pd.concat(df_list, ignore_index=True)
    combined_df
```

| Out[6]: | | tpep_pickup_datetime | tpep_dropoff_datetime | passenger_count | trip_distance | PUL |
|---------|-----------|----------------------|-----------------------|-----------------|---------------|-----|
| | 0 | 2018-09-01 00:01:35 | 2018-09-01 00:09:48 | 2.0 | 1.50 | |
| | 1 | 2018-09-01 00:22:22 | 2018-09-01 00:28:55 | 1.0 | 1.00 | |
| | 2 | 2018-09-01 00:38:10 | 2018-09-01 00:44:42 | 1.0 | 1.00 | |
| | 3 | 2018-09-01 00:46:36 | 2018-09-01 00:54:49 | 1.0 | 1.90 | |
| | 4 | 2018-09-01 00:59:46 | 2018-09-01 01:02:41 | 1.0 | 0.60 | |
| | | | | | | |
| | 216371709 | 2017-06-30 23:07:15 | 2017-06-30 23:33:18 | 1.0 | 6.76 | |
| | 216371710 | 2017-06-30 23:35:12 | 2017-06-30 23:44:46 | 1.0 | 4.51 | |
| | 216371711 | 2017-06-30 23:59:15 | 2017-07-01 00:09:35 | 1.0 | 2.49 | |
| | 216371712 | 2017-06-30 23:12:25 | 2017-06-30 23:25:50 | 1.0 | 2.50 | |
| | 216371713 | 2017-06-30 23:34:04 | 2017-06-30 23:47:26 | 3.0 | 3.60 | |

216371714 rows × 6 columns

```
In [7]: jfk_df = combined_df.loc[combined_df['PULocationID']==132]
jfk_df.size
```

Out[7]: 31822620

```
in [8]: jfk_df['hours']=jfk_df['tpep_pickup_datetime'].dt.hour
    jfk_df['days']=jfk_df['tpep_pickup_datetime'].dt.dayofyear
    jfk_df['year']=jfk_df['tpep_pickup_datetime'].dt.year
    jfk_df['date'] = jfk_df['tpep_pickup_datetime'].dt.date
```

```
In [9]: jfk_df
```

| Out[9]: | | tpep_pickup_datetime | tpep_dropoff_datetime | passenger_count | trip_distance | PUL |
|---------|--------------------------------------|----------------------|-----------------------|-----------------|---------------|-----|
| | 25 | 2018-09-01 00:05:17 | 2018-09-01 00:28:45 | 5.0 | 16.55 | |
| | 26 | 2018-09-01 00:41:28 | 2018-09-01 01:15:36 | 1.0 | 11.99 | |
| | 130 | 2018-09-01 00:16:45 | 2018-09-01 00:23:58 | 1.0 | 4.00 | |
| | 143 | 2018-09-01 00:15:27 | 2018-09-01 01:11:59 | 3.0 | 17.30 | |
| | 144 | 2018-09-01 00:09:51 | 2018-09-01 00:33:27 | 1.0 | 8.47 | |
| | ••• | | | | ••• | |
| | 216371511 | 2017-06-30 23:16:33 | 2017-07-01 00:14:36 | 1.0 | 29.20 | |
| | 216371525 | 2017-06-30 23:44:28 | 2017-07-01 00:22:47 | 1.0 | 13.60 | |
| | 216371577 2017-06-30 23:40:53 | | 2017-07-01 00:09:37 | 1.0 | 15.33 | |
| | 216371587 | 2017-06-30 23:47:12 | 2017-07-01 00:26:56 | 2.0 | 17.10 | |
| | 216371689 | 2017-06-30 23:43:51 | 2017-06-30 23:57:27 | 3.0 | 4.90 | |

5303770 rows × 10 columns

2.2 Sanity check

Then, we need to do some basic sanity checks. It is possible that in a particular hour, completely dispatched no yellow taxis from JFK. Check does each day has 24-hour records and add missing records back to the dataframe. The final output should have 17520 rows ($365 \times 2 \times 24$)

```
In [10]: #your answer here
grouped = jfk_df.loc[(jfk_df['year']== 2017) | (jfk_df['year'] == 2018)]
grouped = grouped.groupby(['date', 'hours', 'DOLocationID']).agg({'passenger_continued})
grouped
```

Out[10]:

passenger_count

| date | hours | DOLocationID | |
|------------|-------|--------------|------|
| 2017-01-01 | 0 | 4 | 1.0 |
| | | 7 | 2.0 |
| | | 10 | 7.0 |
| | | 12 | 1.0 |
| | | 13 | 13.0 |
| ••• | ••• | | |
| 2018-12-31 | 23 | 260 | 1.0 |
| | | 261 | 1.0 |
| | | 262 | 8.0 |
| | | 263 | 13.0 |
| | | 265 | 25.0 |

1848572 rows × 1 columns

```
pivot = grouped.pivot_table(values='passenger_count',
In [11]:
                                                index=['date', 'hours'],
                                                columns='DOLocationID',
                                                aggfunc='sum',fill value=0)
         pivot=pivot.reset_index()
In [12]: pivot['date'] = pd.to_datetime(pivot['date'])
In [13]: date_range = pd.date_range(start="2017-01-01", end="2019-01-01", freq='H')
         # Create a DataFrame with the date range
         df = pd.DataFrame({
             'date': date_range,
             'hours': date range.hour, # Correctly extract hour from each datetime
         })
         # edit the formate to match with the result dataframe
         df['date'] = pd.to datetime(df['date'])
         df['hours'] = df['hours'].astype('int64')
         df['date'] = df['date'].dt.date
         df['date'] = pd.to datetime(df['date'])
         for col in range(1, 266): # Python range stops before the second number, so us
             df[f'DO{col}'] = 0.0
         df
```

| Out[13]: | | date | hours | DO1 | DO2 | DO3 | DO4 | DO5 | D06 | D07 | D08 | ••• | DO256 | DO257 | DO25 |
|----------|-------|----------------|-------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-------|-------|------|
| | 0 | 2017- 01-01 | 0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | | 0.0 | 0.0 | 0. |
| | 1 | 2017- 01-01 | 1 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | | 0.0 | 0.0 | 0. |
| | 2 | 2017- 01-01 | 2 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | | 0.0 | 0.0 | 0. |
| | 3 | 2017- 01-01 | 3 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | | 0.0 | 0.0 | 0. |
| | 4 | 2017- 01-01 | 4 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | | 0.0 | 0.0 | 0. |
| | ••• | | | | | ••• | ••• | ••• | | ••• | ••• | | | | |
| | 17516 | 2018- 12-31 | 20 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | | 0.0 | 0.0 | 0. |
| | 17517 | 2018- 12-31 | 21 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | ••• | 0.0 | 0.0 | 0. |
| | 17518 | 2018- 12-31 | 22 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | | 0.0 | 0.0 | 0. |
| | 17519 | 2018- 12-31 | 23 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | | 0.0 | 0.0 | 0. |
| | 17520 | 2019- 01-01 | 0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | | 0.0 | 0.0 | 0. |

17521 rows × 267 columns

```
In [14]: merged_df = pd.merge(df, pivot, on=['date', 'hours'], how='left')
    merged_df = merged_df.fillna(0)
    merged_df
```

| Out[14]: | | date | hours | DO1 | DO2 | DO3 | DO4 | DO5 | D06 | D07 | D08 | ••• | 256 | 257 | 258 | 259 |
|----------|-------|----------------|-------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|------|-----|-----|
| | 0 | 2017- 01-01 | 0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | | 0.0 | 3.0 | 0.0 | 0.0 |
| | 1 | 2017- 01-01 | 1 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | | 6.0 | 0.0 | 0.0 | 0.0 |
| | 2 | 2017- 01-01 | 2 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | ••• | 0.0 | 0.0 | 2.0 | 0.0 |
| | 3 | 2017- 01-01 | 3 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | | 1.0 | 0.0 | 2.0 | 0.0 |
| | 4 | 2017- 01-01 | 4 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | | 0.0 | 0.0 | 0.0 | 0.0 |
| | ••• | | | ••• | | | ••• | | ••• | ••• | ••• | | | ••• | ••• | |
| | 17516 | 2018- 12-31 | 20 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | | 6.0 | 4.0 | 0.0 | 0.0 |
| | 17517 | 2018- 12-31 | 21 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | ••• | 4.0 | 5.0 | 5.0 | 0.0 |
| | 17518 | 2018- 12-31 | 22 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | | 1.0 | 11.0 | 0.0 | 1.0 |
| | 17519 | 2018- 12-31 | 23 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | | 0.0 | 11.0 | 0.0 | 0.0 |
| | 17520 | 2019- 01-01 | 0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | | 0.0 | 0.0 | 0.0 | 0.0 |

17521 rows × 530 columns

```
In [15]: merged_df = merged_df.drop(merged_df.index[-1])
    merged_df = merged_df.drop(merged_df.columns[2:267], axis=1)
    merged_df
```

| Out[15]: | | date | hours | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | ••• | 256 | 257 | 258 | 259 | 260 | 261 |
|----------|-------|----------------|-------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|------|-----|-----|-----|-----|
| | 0 | 2017- 01-01 | 0 | 0.0 | 0.0 | 0.0 | 1.0 | 0.0 | 0.0 | 2.0 | 0.0 | | 0.0 | 3.0 | 0.0 | 0.0 | 1.0 | 0.0 |
| | 1 | 2017- 01-01 | 1 | 0.0 | 0.0 | 0.0 | 2.0 | 0.0 | 0.0 | 5.0 | 0.0 | | 6.0 | 0.0 | 0.0 | 0.0 | 0.0 | 5.0 |
| | 2 | 2017- 01-01 | 2 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | | 0.0 | 0.0 | 2.0 | 0.0 | 0.0 | 0.0 |
| | 3 | 2017- 01-01 | 3 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 1.0 | 0.0 | | 1.0 | 0.0 | 2.0 | 0.0 | 0.0 | 0.0 |
| | 4 | 2017- 01-01 | 4 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| | ••• | | | | | | | | | | | ••• | | | | | | |
| | 17515 | 2018- 12-31 | 19 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 4.0 | 0.0 | | 3.0 | 1.0 | 5.0 | 0.0 | 2.0 | 5.0 |
| | 17516 | 2018- 12-31 | 20 | 1.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 7.0 | 0.0 | | 6.0 | 4.0 | 0.0 | 0.0 | 8.0 | 1.0 |
| | 17517 | 2018- 12-31 | 21 | 0.0 | 0.0 | 0.0 | 2.0 | 0.0 | 0.0 | 9.0 | 0.0 | | 4.0 | 5.0 | 5.0 | 0.0 | 1.0 | 1.0 |
| | 17518 | 2018- 12-31 | 22 | 0.0 | 0.0 | 2.0 | 2.0 | 0.0 | 0.0 | 2.0 | 0.0 | | 1.0 | 11.0 | 0.0 | 1.0 | 0.0 | 5.0 |
| | 17519 | 2018- 12-31 | 23 | 5.0 | 0.0 | 0.0 | 7.0 | 0.0 | 0.0 | 6.0 | 0.0 | | 0.0 | 11.0 | 0.0 | 0.0 | 1.0 | 1.0 |

17520 rows × 265 columns

3. Time-series exploratory analysis

Apply exploratory analysis over the daily aggregated dataset at first.

3.1 aggregate the ridership from each dropoff location and sum it to get daily records.

```
In [16]: #your answer here
# Assuming 'result' is your DataFrame and it has a column named 'date'
daily = merged_df.groupby(by=merged_df['date']).sum()
daily = daily.drop(columns='hours')
daily.reset_index()
```

| Out[16]: | | date | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | ••• | 256 | 257 | 258 | 259 | 260 | 2 |
|----------|-----|--------------------|------|-----|-----|------|-----|-----|-------|-----|------|-----|-------|------|------|------|------|-----|
| | 0 | 2017- 01-01 | 15.0 | 1.0 | 0.0 | 72.0 | 0.0 | 4.0 | 136.0 | 0.0 | 27.0 | | 127.0 | 55.0 | 38.0 | 10.0 | 36.0 | 3 |
| | 1 | 2017- 01-02 | 13.0 | 0.0 | 4.0 | 74.0 | 0.0 | 0.0 | 192.0 | 0.0 | 11.0 | | 135.0 | 35.0 | 41.0 | 8.0 | 50.0 | 6! |
| | 2 | 2017- 01- 03 | 26.0 | 0.0 | 9.0 | 47.0 | 0.0 | 0.0 | 171.0 | 2.0 | 17.0 | ••• | 123.0 | 50.0 | 45.0 | 16.0 | 55.0 | 61 |
| | 3 | 2017- 01- 04 | 21.0 | 0.0 | 3.0 | 43.0 | 0.0 | 5.0 | 142.0 | 0.0 | 3.0 | | 125.0 | 36.0 | 32.0 | 9.0 | 12.0 | 6: |
| | 4 | 2017- 01- 05 | 8.0 | 1.0 | 3.0 | 58.0 | 0.0 | 0.0 | 83.0 | 0.0 | 8.0 | ••• | 115.0 | 8.0 | 23.0 | 4.0 | 38.0 | 4! |
| | ••• | | | | | | | | | | | | | | | | | |
| | 725 | 2018- 12-27 | 8.0 | 0.0 | 2.0 | 33.0 | 0.0 | 0.0 | 116.0 | 1.0 | 5.0 | | 109.0 | 21.0 | 14.0 | 5.0 | 45.0 | 10: |
| | 726 | 2018- 12-28 | 5.0 | 0.0 | 4.0 | 58.0 | 0.0 | 1.0 | 67.0 | 0.0 | 4.0 | | 89.0 | 37.0 | 28.0 | 6.0 | 16.0 | 84 |
| | 727 | 2018- 12-29 | 8.0 | 0.0 | 3.0 | 21.0 | 0.0 | 1.0 | 99.0 | 0.0 | 11.0 | | 109.0 | 33.0 | 27.0 | 6.0 | 26.0 | 6: |
| | 728 | 2018- 12-30 | 12.0 | 0.0 | 2.0 | 35.0 | 1.0 | 2.0 | 128.0 | 0.0 | 15.0 | ••• | 87.0 | 56.0 | 25.0 | 5.0 | 32.0 | 6, |
| | 729 | 2018- 12-31 | 10.0 | 0.0 | 2.0 | 29.0 | 0.0 | 0.0 | 106.0 | 0.0 | 17.0 | | 66.0 | 49.0 | 26.0 | 13.0 | 36.0 | 3 |

730 rows × 264 columns

3.2 Period detection and report the strongest period length on the 2017 data.

Hint: using periodogram or acf plot.

```
In [17]: grouped_2017 = merged_df.loc[merged_df['date'].dt.year==2017]
    grouped_2017
```

| Out[17]: | | date | hours | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | ••• | 256 | 257 | 258 | 259 | 260 | 261 |
|----------|------|----------------|-------|-----|-----|-----|-----|-----|-----|------|-----|-----|-----|-----|-----|-----|-----|-----|
| | 0 | 2017- 01-01 | 0 | 0.0 | 0.0 | 0.0 | 1.0 | 0.0 | 0.0 | 2.0 | 0.0 | | 0.0 | 3.0 | 0.0 | 0.0 | 1.0 | 0.0 |
| | 1 | 2017- 01-01 | 1 | 0.0 | 0.0 | 0.0 | 2.0 | 0.0 | 0.0 | 5.0 | 0.0 | | 6.0 | 0.0 | 0.0 | 0.0 | 0.0 | 5.0 |
| | 2 | 2017- 01-01 | 2 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | | 0.0 | 0.0 | 2.0 | 0.0 | 0.0 | 0.0 |
| | 3 | 2017- 01-01 | 3 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 1.0 | 0.0 | | 1.0 | 0.0 | 2.0 | 0.0 | 0.0 | 0.0 |
| ; | 4 | 2017- 01-01 | 4 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| | ••• | | | | | | | | | | | | | | | | | |
| | 8755 | 2017- 12-31 | 19 | 1.0 | 0.0 | 1.0 | 0.0 | 0.0 | 0.0 | 3.0 | 0.0 | | 6.0 | 2.0 | 0.0 | 0.0 | 1.0 | 5.0 |
| | 8756 | 2017- 12-31 | 20 | 0.0 | 0.0 | 4.0 | 2.0 | 0.0 | 0.0 | 14.0 | 0.0 | | 5.0 | 4.0 | 3.0 | 0.0 | 9.0 | 1.0 |
| | 8757 | 2017- 12-31 | 21 | 1.0 | 0.0 | 0.0 | 1.0 | 1.0 | 0.0 | 2.0 | 0.0 | | 3.0 | 2.0 | 3.0 | 0.0 | 0.0 | 4.0 |
| | 8758 | 2017- 12-31 | 22 | 1.0 | 0.0 | 0.0 | 1.0 | 0.0 | 0.0 | 7.0 | 0.0 | | 2.0 | 0.0 | 0.0 | 0.0 | 0.0 | 2.0 |
| | 8759 | 2017- 12-31 | 23 | 0.0 | 0.0 | 1.0 | 1.0 | 0.0 | 0.0 | 6.0 | 0.0 | | 3.0 | 9.0 | 0.0 | 0.0 | 3.0 | 2.0 |

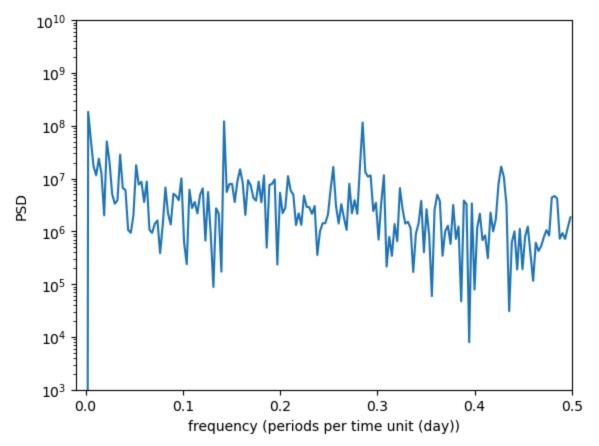
8760 rows × 265 columns

```
In [18]: d17= grouped_2017.groupby(by=grouped_2017['date']).sum()
d17 = d17.drop(columns='hours')
d17 = d17.reset_index()
d17
```

| Out[18]: | | date | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | ••• | 256 | 257 | 258 | 259 | 260 | 2 |
|----------|-----|--------------------|------|-----|------|------|-----|-----|-------|-----|------|-----|-------|------|------|------|------|----|
| | 0 | 2017- 01-01 | 15.0 | 1.0 | 0.0 | 72.0 | 0.0 | 4.0 | 136.0 | 0.0 | 27.0 | | 127.0 | 55.0 | 38.0 | 10.0 | 36.0 | 3 |
| | 1 | 2017- 01- 02 | 13.0 | 0.0 | 4.0 | 74.0 | 0.0 | 0.0 | 192.0 | 0.0 | 11.0 | ••• | 135.0 | 35.0 | 41.0 | 8.0 | 50.0 | 6 |
| | 2 | 2017- 01- 03 | 26.0 | 0.0 | 9.0 | 47.0 | 0.0 | 0.0 | 171.0 | 2.0 | 17.0 | ••• | 123.0 | 50.0 | 45.0 | 16.0 | 55.0 | 61 |
| | 3 | 2017- 01- 04 | 21.0 | 0.0 | 3.0 | 43.0 | 0.0 | 5.0 | 142.0 | 0.0 | 3.0 | | 125.0 | 36.0 | 32.0 | 9.0 | 12.0 | 6 |
| | 4 | 2017- 01- 05 | 8.0 | 1.0 | 3.0 | 58.0 | 0.0 | 0.0 | 83.0 | 0.0 | 8.0 | ••• | 115.0 | 8.0 | 23.0 | 4.0 | 38.0 | 4: |
| | ••• | ••• | | | | | | | | | | | | | | | | |
| | 360 | 2017- 12-27 | 5.0 | 0.0 | 4.0 | 41.0 | 0.0 | 1.0 | 125.0 | 0.0 | 13.0 | | 101.0 | 31.0 | 32.0 | 4.0 | 43.0 | 7! |
| | 361 | 2017- 12- 28 | 13.0 | 1.0 | 3.0 | 30.0 | 0.0 | 0.0 | 79.0 | 0.0 | 5.0 | ••• | 89.0 | 33.0 | 20.0 | 9.0 | 45.0 | 7 |
| | 362 | 2017- 12- 29 | 21.0 | 0.0 | 2.0 | 40.0 | 0.0 | 4.0 | 119.0 | 0.0 | 7.0 | ••• | 132.0 | 59.0 | 21.0 | 4.0 | 33.0 | 7: |
| | 363 | 2017- 12- 30 | 8.0 | 0.0 | 10.0 | 37.0 | 0.0 | 0.0 | 119.0 | 0.0 | 5.0 | | 103.0 | 54.0 | 37.0 | 6.0 | 28.0 | 6 |
| | 364 | 2017- 12-31 | 13.0 | 0.0 | 12.0 | 34.0 | 1.0 | 0.0 | 143.0 | 0.0 | 6.0 | | 65.0 | 49.0 | 15.0 | 2.0 | 38.0 | 5 |

365 rows × 264 columns

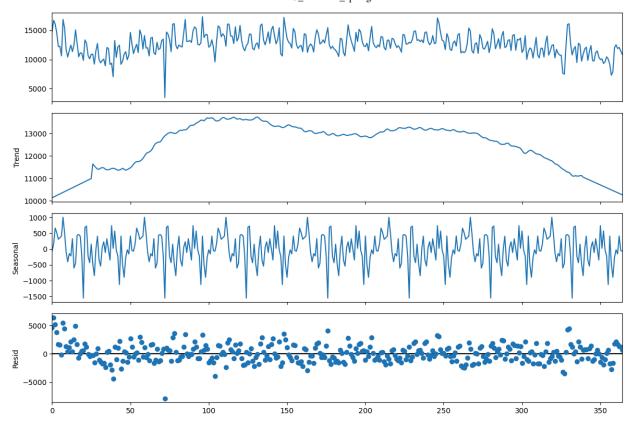
```
In [19]: #your answer here
import scipy
f, PSD = scipy.signal.periodogram(d17.sum(axis=1))
plt.semilogy(f, PSD)
plt.xlabel('frequency (periods per time unit (day))')
plt.ylabel('PSD')
plt.xlim(-0.01,0.5)
plt.ylim(1e3,1e10)
#filter outputs - periods shorter than 2 years (approx 100 weeks)
PSD = PSD[f>0.01]
f = f[f>0.01]
plt.show()
print('Strongest period length = {}'.format(1/f[np.argmax(PSD)])) #report the
```



Strongest period length = 7.019230769230769

3.3 Trend, seasonality, noise decomposition (using additive model) on 2017 data, .

```
In [20]: #your answer here
import matplotlib.pyplot as plt
plt.rcParams['figure.figsize'] = [12, 8]
daily17 = sm.tsa.seasonal_decompose(d17.sum(axis=1), model='additive', period = fig = daily17.plot()
```



4. Predict the total daily ridership from JFK using ARIMA.

ARIMA is a common method to predict taxi ridership. Before we predict taxi zone level hourly ridership, let's try to predict the aggregated daily ridership using ARIMA.

4.1 Using adfuller test to test the stability of the aggregated dataset. If not stable, apply differencing method until the p-value from adfuller test is smaller than 0.05.

```
#your answer here
In [21]:
         from statsmodels.tsa.stattools import adfuller
         series=daily.sum(axis=1)
         result = adfuller(series)
         print('ADF Statistic: %f' % result[0])
         print('p-value: %f' % result[1])
         print('Critical Values:')
         for key, value in result[4].items():
             print('\t%s: %.3f' % (key, value))
             # first order differencing
         series=daily.sum(axis=1).diff()
         result = adfuller(series.dropna())
         print('\n1st order differencing:')
                  ADF Statistic: %f' % result[0])
                  p-value: %f' % result[1])
         # second order differencing
```

```
series=daily.sum(axis=1).diff().diff()
result = adfuller(series.dropna())
print('\n2nd order differencing:')
print(' ADF Statistic: %f' % result[0])
print(' p-value: %f' % result[1])
ADF Statistic: -2.153742
p-value: 0.223460
Critical Values:
        1%: -3.440
        5%: -2.866
        10%: -2.569
1st order differencing:
 ADF Statistic: -8.181998
  p-value: 0.000000
2nd order differencing:
  ADF Statistic: -12.229794
  p-value: 0.000000
```

So we need the D=1 to get p-value smaller than 0.05

4.2 build an ARIMA model using terms [P=0, D=1, Q=1], training on the first 700 days, forecast on the last 31 days. Print ARIMA model results and plot in-sample and out-of-sample prediction in different colors.

```
In [22]: P=0
         D=1
         0 = 1
         # fit model
         N = 700
         #your answer here
         series = daily.sum(axis=1)#.values
         #model = sm.tsa.SARIMAX(series[:N], order=(Q,D,P))
         model = sm.tsa.ARIMA(series[:N], order=(Q,D,P))
         model_fit = model.fit()
         print(model_fit.summary())
         # plot residual errors
         residuals = pd.DataFrame(model fit.resid)
         plt.plot(residuals)
         plt.title('Residual at each data point')
         plot acf(residuals)
         plt.title('Residual autocorrelation')
         plt.show()
         residuals.plot(kind='kde', legend=False)
         plt.title('Residual kernel density estimation')
         plt.show()
         print(residuals.describe())
         k2, p = scipy.stats.normaltest(residuals)
         alpha = 0.1
```

```
print('p value is ',p[0])

print('null hypothesis: residuals come from a normal distribution')
if p < alpha:
    print("The null hypothesis can be rejected")
else:
    print("The null hypothesis cannot be rejected")

print("Ljung-Box:")
print(sm.stats.acorr_ljungbox(residuals))</pre>
```

SARIMAX Results

| ============= | | | |
|----------------|------------------|-------------------|-----------|
| Dep. Variable: | у | No. Observations: | 700 |
| Model: | ARIMA(1, 1, 0) | Log Likelihood | -6251.498 |
| Date: | Sat, 16 Mar 2024 | AIC | 12506.996 |
| Time: | 13:47:06 | BIC | 12516.095 |
| Sample: | 01-01-2017 | HQIC | 12510.513 |
| | - 12-01-2018 | | |

Covariance Type: opg

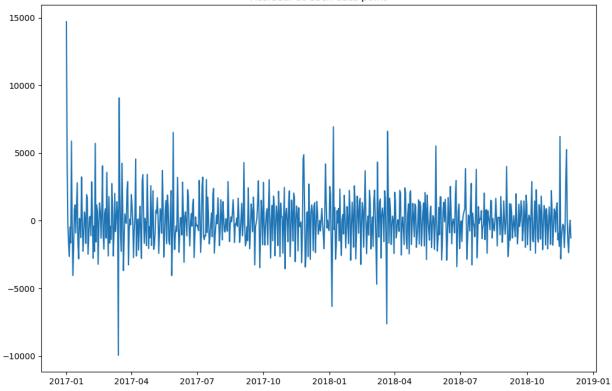
| COVALIANCE | i ype. | | opg | | | |
|--|----------------------|-------------------|-------------------------------|---|--------------------|--------------------|
| ======= | coef | std err | Z | P> z | [0.025 | 0.975] |
| ar.L1 sigma2 | -0.2136 3.409e+06 | 0.025 1.23e+05 | -8.587 27.620 | 0.000 | -0.262 3.17e+06 | -0.165 3.65e+06 |
| Ljung-Box 20.75 Prob(Q): 0.00 Heterosked 0.28 Prob(H) (t | asticity (H) | : | 10.08 0.00 0.60 0.00 | Jarque-Ber Prob(JB): Skew: Kurtosis: | a (JB): | 2 |
| ======= | :======== | ======== | | | ======== | ======== |

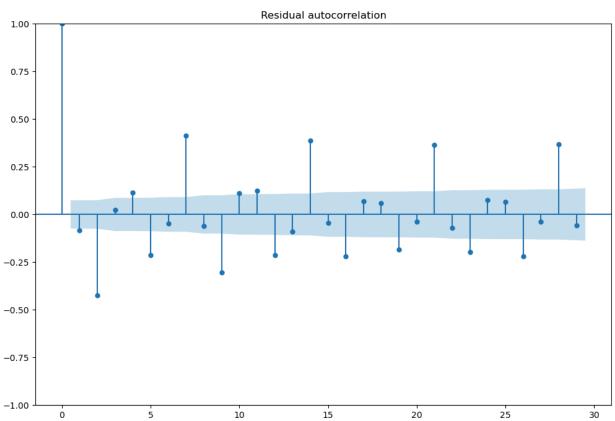
=====

Warnings:

[1] Covariance matrix calculated using the outer product of gradients (complex -step).







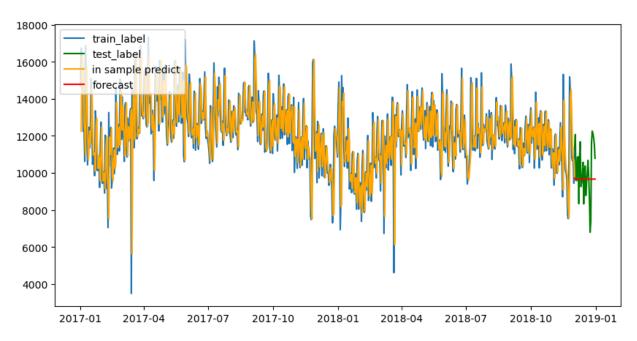
Residual kernel density estimation

```
0.00020
  0.00015
Density
  0.00010
  0.00005
  0.00000
            -20000
                          -10000
                                                       10000
                                                                     20000
count
          700.000000
           15.775769
mean
std
         1934.681591
min
        -9938.582960
25%
        -1263.293712
50%
            9.805882
75%
         1053.734335
        14710.000000
max
p value is 3.2878940825612855e-37
null hypothesis: residuals come from a normal distribution
The null hypothesis can be rejected
Ljung-Box:
        lb_stat
                     lb_pvalue
1
       5.048784
                 2.464323e-02
2
    132.110656 2.053693e-29
    132.512758 1.554284e-28
3
4
    141.578676
                 1.296108e-29
5
    173.663858 1.205690e-35
6
    175.299494 3.377372e-35
7
    295.979051 4.368333e-60
8
    298.632974 8.046372e-60
9
    364.719770
                4.550781e-73
                 3.760209e-74
10
    373.662225
# Forecast
fcast = model_fit.forecast(steps=len(series)-N) # 95% conf
fc = model_fit.get_forecast(steps=len(series)-N).summary_frame()
```

```
In [23]:
         fc_series = pd.Series(fc['mean'])
         #mean_series = pd.Series(fc['mean'], index=range(N,len(series)))
         lower_series = pd.Series(fc.mean_ci_lower, index=range(N,len(series)))
         upper_series = pd.Series(fc.mean_ci_upper, index=range(N,len(series)))
```

```
plt.rcParams.update({'figure.figsize':(10,5)})
fig, ax = plt.subplots()
ax.plot(daily.index[:N+1],series[:N+1],label='train_label') # train
ax.plot(daily.index[N:],series[N:],color='green',label='test_label') # test
ax.plot(daily.iloc[1:N+1].index,model_fit.predict(start=1,end=N,dynamic=False,color='orange',label='in sample predict') # in-sample
ax.plot(fc_series, label='forecast', color='red') # forecast
ax.fill_between(daily.iloc[N:].index, lower_series, upper_series, color='k', accepted ax.legend(loc='upper left')
```

Out[23]: <matplotlib.legend.Legend at 0x14e0dddd0>



Taxi zone level prediction

This project aims to predict hourly yellow taxi ridership volume from JFK to each taxi zone. The ARIMA experiment in section 3 forecasts the total ridership amount from JFK. However, based on the reported R^2 , this model is not a good fit. ARIMA model has four main shortcomings: 1) they rely heavily on stationarity assumption which does not hold in real-world traffic systems 2) they do not consider spatial and structural dependencies that traffic networks exhibit and forecast each sensor as an individual time series 3) they are unable to model non-linear temporal dynamics 4) they suffer from the curse of dimensionality. Due to the limitation of ARIMA, we need to apply another method to predict taxi zone level ridership.

5. Feature engineering

Our workflow is first standardizing the dataset, then using PCA to compress the dataset. As we predict future ridership, PCA should be learned from historical data (2017) then apply to the following year (2018). Next, add lag features (PCA components) from the past 12 hours and apply a Random Forest regressor to predict each PCA component's values in the next hour. After we had the PCA component prediction, inverse PCA, and inverse standardization

to retrieve taxi ridership prediction in its original scale and dimension, in other words, we are predicting the PCA components instead of taxi zone level ridership and then using the inverse PCA method to reconstruct

your answer here

ok

5.1. standardization.

The standardscaler stores information of this standardization process, including the mean and standard deviation values required when converting the prediction back to the raw scale. Split the whole dataset into two parts: 2017 and 2018, standardize each separately.

| In [24]: | #your answer here grouped_2017 | | | | | | | | | | | | | | | | | |
|----------|--------------------------------|----------------|-------|-----|-----|-----|-----|-----|-----|------|-----|-----|-----|-----|-----|-----|-----|-----|
| Out[24]: | | date | hours | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | ••• | 256 | 257 | 258 | 259 | 260 | 261 |
| | 0 | 2017- 01-01 | 0 | 0.0 | 0.0 | 0.0 | 1.0 | 0.0 | 0.0 | 2.0 | 0.0 | ••• | 0.0 | 3.0 | 0.0 | 0.0 | 1.0 | 0.0 |
| | 1 | 2017- 01-01 | 1 | 0.0 | 0.0 | 0.0 | 2.0 | 0.0 | 0.0 | 5.0 | 0.0 | ••• | 6.0 | 0.0 | 0.0 | 0.0 | 0.0 | 5.0 |
| | 2 | 2017- 01-01 | 2 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | ••• | 0.0 | 0.0 | 2.0 | 0.0 | 0.0 | 0.0 |
| | 3 | 2017- 01-01 | 3 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 1.0 | 0.0 | ••• | 1.0 | 0.0 | 2.0 | 0.0 | 0.0 | 0.0 |
| | 4 | 2017- 01-01 | 4 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | ••• | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| | ••• | | | | | | | | | ••• | | | | | | | | ••• |
| | 8755 | 2017- 12-31 | 19 | 1.0 | 0.0 | 1.0 | 0.0 | 0.0 | 0.0 | 3.0 | 0.0 | | 6.0 | 2.0 | 0.0 | 0.0 | 1.0 | 5.0 |
| | 8756 | 2017- 12-31 | 20 | 0.0 | 0.0 | 4.0 | 2.0 | 0.0 | 0.0 | 14.0 | 0.0 | | 5.0 | 4.0 | 3.0 | 0.0 | 9.0 | 1.0 |
| | 8757 | 2017- 12-31 | 21 | 1.0 | 0.0 | 0.0 | 1.0 | 1.0 | 0.0 | 2.0 | 0.0 | ••• | 3.0 | 2.0 | 3.0 | 0.0 | 0.0 | 4.0 |
| | 8758 | 2017- 12-31 | 22 | 1.0 | 0.0 | 0.0 | 1.0 | 0.0 | 0.0 | 7.0 | 0.0 | ••• | 2.0 | 0.0 | 0.0 | 0.0 | 0.0 | 2.0 |
| | 8759 | 2017- 12-31 | 23 | 0.0 | 0.0 | 1.0 | 1.0 | 0.0 | 0.0 | 6.0 | 0.0 | | 3.0 | 9.0 | 0.0 | 0.0 | 3.0 | 2.0 |

8760 rows × 265 columns

```
In [25]: grouped_2018 = merged_df.loc[merged_df['date'].dt.year==2018]
grouped_2018
```

Out[25]:

| | date | hours | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | ••• | 256 | 257 | 258 | 259 | 260 | 261 |
|-------|----------------|-------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|------|-----|-----|-----|-----|
| 8760 | 2018- 01-01 | 0 | 1.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 3.0 | 0.0 | | 1.0 | 0.0 | 0.0 | 8.0 | 5.0 | 0.0 |
| 8761 | 2018- 01-01 | 1 | 0.0 | 0.0 | 1.0 | 0.0 | 0.0 | 0.0 | 1.0 | 0.0 | | 4.0 | 2.0 | 0.0 | 0.0 | 2.0 | 0.0 |
| 8762 | 2018- 01-01 | 2 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 1.0 | 0.0 | | 1.0 | 0.0 | 0.0 | 0.0 | 2.0 | 0.0 |
| 8763 | 2018- 01-01 | 3 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | | 0.0 | 0.0 | 2.0 | 0.0 | 0.0 | 0.0 |
| 8764 | 2018- 01-01 | 4 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | | 0.0 | 0.0 | 1.0 | 0.0 | 0.0 | 0.0 |
| ••• | ••• | ••• | | | | | | | | | | | | | | | |
| 17515 | 2018- 12-31 | 19 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 4.0 | 0.0 | | 3.0 | 1.0 | 5.0 | 0.0 | 2.0 | 5.0 |
| 17516 | 2018- 12-31 | 20 | 1.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 7.0 | 0.0 | | 6.0 | 4.0 | 0.0 | 0.0 | 8.0 | 1.0 |
| 17517 | 2018- 12-31 | 21 | 0.0 | 0.0 | 0.0 | 2.0 | 0.0 | 0.0 | 9.0 | 0.0 | | 4.0 | 5.0 | 5.0 | 0.0 | 1.0 | 1.0 |
| 17518 | 2018- 12-31 | 22 | 0.0 | 0.0 | 2.0 | 2.0 | 0.0 | 0.0 | 2.0 | 0.0 | | 1.0 | 11.0 | 0.0 | 1.0 | 0.0 | 5.0 |
| 17519 | 2018- 12-31 | 23 | 5.0 | 0.0 | 0.0 | 7.0 | 0.0 | 0.0 | 6.0 | 0.0 | | 0.0 | 11.0 | 0.0 | 0.0 | 1.0 | 1.0 |

8760 rows × 265 columns

| In [26]: | grouped_2017.iloc[:,2:] | | | | | | | | | | | | | | | | | | |
|----------|-------------------------|-----|-----|-----|-----|-----|-----|------|-----|-----|------|-----|-----|-----|-----|-----|-----|-----|------|
| Out[26]: | | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | ••• | 256 | 257 | 258 | 259 | 260 | 261 | 262 |
| | 0 | 0.0 | 0.0 | 0.0 | 1.0 | 0.0 | 0.0 | 2.0 | 0.0 | 0.0 | 7.0 | | 0.0 | 3.0 | 0.0 | 0.0 | 1.0 | 0.0 | 3.0 |
| | 1 | 0.0 | 0.0 | 0.0 | 2.0 | 0.0 | 0.0 | 5.0 | 0.0 | 0.0 | 8.0 | | 6.0 | 0.0 | 0.0 | 0.0 | 0.0 | 5.0 | 7.0 |
| | 2 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 1.0 | 3.0 | | 0.0 | 0.0 | 2.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| | 3 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 1.0 | 0.0 | 0.0 | 0.0 | | 1.0 | 0.0 | 2.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| | 4 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| | ••• | | ••• | | ••• | | | ••• | | | ••• | | ••• | | | ••• | ••• | | ••• |
| | 8755 | 1.0 | 0.0 | 1.0 | 0.0 | 0.0 | 0.0 | 3.0 | 0.0 | 1.0 | 8.0 | | 6.0 | 2.0 | 0.0 | 0.0 | 1.0 | 5.0 | 3.0 |
| | 8756 | 0.0 | 0.0 | 4.0 | 2.0 | 0.0 | 0.0 | 14.0 | 0.0 | 0.0 | 12.0 | | 5.0 | 4.0 | 3.0 | 0.0 | 9.0 | 1.0 | 5.0 |
| | 8757 | 1.0 | 0.0 | 0.0 | 1.0 | 1.0 | 0.0 | 2.0 | 0.0 | 0.0 | 11.0 | | 3.0 | 2.0 | 3.0 | 0.0 | 0.0 | 4.0 | 17.0 |
| | 8758 | 1.0 | 0.0 | 0.0 | 1.0 | 0.0 | 0.0 | 7.0 | 0.0 | 1.0 | 24.0 | | 2.0 | 0.0 | 0.0 | 0.0 | 0.0 | 2.0 | 11.0 |
| | 8759 | 0.0 | 0.0 | 1.0 | 1.0 | 0.0 | 0.0 | 6.0 | 0.0 | 0.0 | 8.0 | | 3.0 | 9.0 | 0.0 | 0.0 | 3.0 | 2.0 | 6.0 |

8760 rows × 263 columns

```
st 17 = StandardScaler().fit transform(grouped 2017.iloc[:,2:])
In [27]:
         st_18= StandardScaler().fit_transform(grouped_2018.iloc[:,2:])
         st_18
         array([[ 0.31612173, -0.0286809 , -0.28145419, ..., -0.33416569,
Out[27]:
                 -0.68309719, -0.18582689],
                [-0.43454955, -0.0286809, 0.99668924, ..., -0.96396162,
                 -0.68309719, -0.06607968],
                [-0.43454955, -0.0286809, -0.28145419, ..., -0.96396162,
                 -0.68309719, -1.26355178],
                [-0.43454955, -0.0286809, -0.28145419, ..., 1.76515406,
                  1.71888228, 1.37088683],
                [-0.43454955, -0.0286809, 2.27483267, ..., 0.92542616,
                 -0.68309719, 1.61038125],
                [ 3.31880687, -0.0286809 , -0.28145419, ..., 1.76515406,
                 -0.68309719, 1.61038125]])
```

5.2. PCA

Train PCA on the standardized 2018 dataset. Set PCA components as 5, and gamma is None, use kernel 'linear'. Report the mean squared error between the standardized data and reconstructed data. Hint: fit the PCA on 2017 data and apply it to transform 2018 data. (5 pts)

5.3 Add lag

add 12 lags of each component (pca_comps=5) (compressed 2018 data only). The expected output should have 65 dimensions. In the further modeling step, we will apply the 60 lag variables to predict the 5 components.

```
In [31]: # Placeholder for demonstration: Converting the placeholder PCA transformed data
pca_components = pd.DataFrame(transform_2018)

# Add 12 lags for each PCA component
for component in pca_components.columns[:5]: # Only the first 5 columns are ac
    for lag in range(1, 13):
        pca_components[f'{component}_lag_{lag}'] = pca_components[component].sl
```

```
# Show the DataFrame
pca_components
```

| Out[31]: | | 0 | 1 | 2 | 3 | 4 | 0_lag_1 | 0_lag_2 | 0_lag_3 |
|----------|------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| | 0 | -2.720164 | -4.312002 | -0.554225 | 1.372271 | 0.879431 | NaN | NaN | NaN |
| | 1 | -4.799956 | -3.612092 | -1.400683 | -0.201888 | -2.080059 | -2.720164 | NaN | NaN |
| | 2 | -8.787469 | -0.853776 | 0.814226 | -0.168481 | -0.313817 | -4.799956 | -2.720164 | NaN |
| | 3 | -8.658432 | -1.091070 | 0.500887 | 0.579890 | 0.425699 | -8.787469 | -4.799956 | -2.720164 |
| | 4 | -7.905044 | -1.693033 | -0.752052 | -0.783431 | -0.666292 | -8.658432 | -8.787469 | -4.799956 |
| | ••• | | | | | | | | |
| | 8755 | 7.454186 | -4.539786 | 0.579454 | 0.888912 | 0.146922 | -1.390830 | 5.546593 | 7.323307 |
| | 8756 | 6.112123 | -5.409046 | 3.829655 | 0.542472 | 1.232248 | 7.454186 | -1.390830 | 5.546593 |
| | 8757 | 8.619792 | -8.059970 | 3.858406 | 0.955377 | 0.822999 | 6.112123 | 7.454186 | -1.390830 |
| | 8758 | 7.935406 | -7.058935 | 0.783922 | 2.268200 | -0.374162 | 8.619792 | 6.112123 | 7.454186 |
| | 8759 | 3.239251 | -6.747190 | -1.182133 | 1.897086 | 0.040660 | 7.935406 | 8.619792 | 6.112123 |

8760 rows × 65 columns

6. RandomForest modeling

We aim at predicting compressed daily ridership (5 PCA components values) from 12-hour lag variables. Parameter tuning is required in this section, including min_samples_split, min_samples_leaf, and n_estimators. First 80% days for training, test on the rest 20%. And in the training dataset, validate the model on the bottom 20%.

6.1 train test split

Please keep in mind that random train test split is not applicable in this case.

```
In [34]: grouped_2018=grouped_2018.reset_index()
grouped_2018
```

| Out[34]: | | index | date | hours | 1 | 2 | 3 | 4 | 5 | 6 | 7 | ••• | 256 | 257 | 258 | 259 | 260 | 261 |
|----------|------|-------|----------------|-------|-----|-----|-----|-----|-----|-----|-----|-----|-----|------|-----|-----|-----|-----|
| | 0 | 8760 | 2018- 01-01 | 0 | 1.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 3.0 | | 1.0 | 0.0 | 0.0 | 8.0 | 5.0 | 0.0 |
| | 1 | 8761 | 2018- 01-01 | 1 | 0.0 | 0.0 | 1.0 | 0.0 | 0.0 | 0.0 | 1.0 | | 4.0 | 2.0 | 0.0 | 0.0 | 2.0 | 0.0 |
| | 2 | 8762 | 2018- 01-01 | 2 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 1.0 | | 1.0 | 0.0 | 0.0 | 0.0 | 2.0 | 0.0 |
| | 3 | 8763 | 2018- 01-01 | 3 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | | 0.0 | 0.0 | 2.0 | 0.0 | 0.0 | 0.0 |
| | 4 | 8764 | 2018- 01-01 | 4 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | | 0.0 | 0.0 | 1.0 | 0.0 | 0.0 | 0.0 |
| | ••• | | | | | | | | | | | | | | | | | |
| | 8755 | 17515 | 2018- 12-31 | 19 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 4.0 | | 3.0 | 1.0 | 5.0 | 0.0 | 2.0 | 5.0 |
| | 8756 | 17516 | 2018- 12-31 | 20 | 1.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 7.0 | | 6.0 | 4.0 | 0.0 | 0.0 | 8.0 | 1.0 |
| | 8757 | 17517 | 2018- 12-31 | 21 | 0.0 | 0.0 | 0.0 | 2.0 | 0.0 | 0.0 | 9.0 | ••• | 4.0 | 5.0 | 5.0 | 0.0 | 1.0 | 1.0 |
| | 8758 | 17518 | 2018- 12-31 | 22 | 0.0 | 0.0 | 2.0 | 2.0 | 0.0 | 0.0 | 2.0 | | 1.0 | 11.0 | 0.0 | 1.0 | 0.0 | 5.0 |
| | 8759 | 17519 | 2018- 12-31 | 23 | 5.0 | 0.0 | 0.0 | 7.0 | 0.0 | 0.0 | 6.0 | | 0.0 | 11.0 | 0.0 | 0.0 | 1.0 | 1.0 |

8760 rows × 266 columns

In [35]: pca_components_hour =pd.concat([pca_components, grouped_2018['date'],grouped_20
 pca_components_hour

| Out[35]: | | 0 | 1 | 2 | 3 | 4 | 0_lag_1 | 0_lag_2 | 0_lag_3 |
|----------|------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| | 0 | -2.720164 | -4.312002 | -0.554225 | 1.372271 | 0.879431 | NaN | NaN | NaN |
| | 1 | -4.799956 | -3.612092 | -1.400683 | -0.201888 | -2.080059 | -2.720164 | NaN | NaN |
| | 2 | -8.787469 | -0.853776 | 0.814226 | -0.168481 | -0.313817 | -4.799956 | -2.720164 | NaN |
| | 3 | -8.658432 | -1.091070 | 0.500887 | 0.579890 | 0.425699 | -8.787469 | -4.799956 | -2.720164 |
| | 4 | -7.905044 | -1.693033 | -0.752052 | -0.783431 | -0.666292 | -8.658432 | -8.787469 | -4.799956 |
| | ••• | | | | | | | | |
| | 8755 | 7.454186 | -4.539786 | 0.579454 | 0.888912 | 0.146922 | -1.390830 | 5.546593 | 7.323307 |
| | 8756 | 6.112123 | -5.409046 | 3.829655 | 0.542472 | 1.232248 | 7.454186 | -1.390830 | 5.546593 |
| | 8757 | 8.619792 | -8.059970 | 3.858406 | 0.955377 | 0.822999 | 6.112123 | 7.454186 | -1.390830 |
| | 8758 | 7.935406 | -7.058935 | 0.783922 | 2.268200 | -0.374162 | 8.619792 | 6.112123 | 7.454186 |
| | 8759 | 3.239251 | -6.747190 | -1.182133 | 1.897086 | 0.040660 | 7.935406 | 8.619792 | 6.112123 |

8760 rows × 67 columns

```
In []: #Train test split by daily
In [36]: pca_components_day = pca_components_hour.groupby(by='date').sum()
    pca_components_day
```

Out[36]:

0

1

3

4

0_lag_1

0_lag_2

2

| 00.01001. | | | | | | | | | | | | | |
|-----------|--|---------------|---------------------------|------------|------------|------------------------|-------------|-------------|----|--|--|--|--|
| | date | | | | | | | | | | | | |
| | 2018- 01-01 | 62.612008 | -44.743105 | 56.586062 | 12.557598 | 15.442216 | 50.702225 | 32.286296 | 1 | | | | |
| | 2018- 01-02 | 84.746868 | -36.094098 | 48.962733 | -5.429675 | 6.205125 | 84.035248 | 87.515499 | 8 | | | | |
| | 2018- 01- 03 | 36.192284 | -33.511065 | 12.888260 | -0.544993 | 1.960686 | 44.014725 | 51.802227 | Ę | | | | |
| | 2018- 01- 04 | -97.724889 | -26.879326 | -26.503198 | -7.222360 | -1.293627 | -88.734585 | -83.050344 | -7 | | | | |
| | 2018- 01- 05 | -62.179944 | -13.214626 | -11.778107 | -8.513691 | 8.028394 | -71.182692 | -75.780830 | -7 | | | | |
| | ••• | ••• | ••• | ••• | | ••• | | | | | | | |
| | 2018- 12-27 | 20.203439 | -14.794486 | 13.172488 | -8.506571 | -8.976869 | 18.597803 | 22.622436 | 2 | | | | |
| | 2018- 12-28 | 16.833980 | -21.837957 | 9.738549 | -13.645406 | -11.357192 | 16.258343 | 20.525324 | 2 | | | | |
| | 2018- 12-29 | 14.601693 | -17.897182 | 23.583924 | -21.560275 | -6.514834 | 20.235056 | 15.426699 | 1 | | | | |
| | 2018- 12-30 | 14.322982 | -41.932620 | 30.016178 | -1.490065 | 1.213039 | 9.204234 | 12.175358 | 1 | | | | |
| | 2018- 12-31 | 8.457661 | -61.072147 | 35.693456 | 7.389496 | 14.416576 | 14.271713 | 11.427241 | | | | | |
| | 365 rov | vs × 66 coluı | mns | | | | | | | | | | |
| In [37]: | <pre>train_size = int(len(pca_components_day) * 0.8) X = pca_components_day X = X.iloc[:, 5:] X_train = X.iloc[:train_size, :] X_test = X.iloc[train_size:, :] Y = pca_components_day.iloc[:, :5] y_train = Y.iloc[:train_size, :] y_test = Y.iloc[train_size:, :]</pre> | | | | | | | | | | | | |
| In [38]: | rf = F # <i>Fit</i> | | stRegressor on the tra | _ | | n_samples __ | _leaf=10, m | nin_samples | _S | | | | |
| Out[38]: | V | | Rando | omForestRe | aressor | | | | | | | | |
| | | mForestReg | ressor(mi | | | n_estimat | ors=50) | | | | | | |
| In [39]: | y_pred | | dict(X_test | :) | | | | | | | | | |

```
array([[-9.02778188e+00, 1.04451065e+01,
                                                     6.33736429e+00,
Out[39]:
                 -2.38673860e+00, -3.16662986e+00],
                 [ 2.77861125e+01, 6.51562148e+00,
                                                     1.58456016e+01,
                 -1.55860500e+00, -1.17810381e+00],
                 [ 3.86719418e+01, 6.73886438e+00,
                                                     2.28635067e+00,
                 -1.16326741e+00, -2.92566006e+00],
                 [-7.24392170e+00, 1.23544372e+01,
                                                     1.43239146e+00,
                 -1.19054791e+00, -4.71156047e+00],
                 [-1.04868544e+01, 1.05800233e+01,
                                                     6.80143025e+00,
                  2.07550942e-01, -4.21131934e+00],
                 [ 1.12520562e+01, 9.41663768e+00,
                                                     1.16099219e+01.
                 -1.53076869e+00, -2.76137608e+00],
                 [ 2.63117285e+01, 7.21191753e+00,
                                                     1.76516395e+01,
                 -1.68691163e+00, -1.43078881e+00],
                 [-1.68324697e+01, 6.00887243e+00,
                                                     9.88502972e+00,
                 -6.21723141e+00. 4.63871733e-01].
                 [ 8.50501078e+00, 1.05472371e+01,
                                                     7.42108582e+00,
                 -1.16010478e+00, -3.55414681e+00],
                 [ 2.23092537e+01, 4.22007876e+00,
                                                    8.81888672e-01,
                 -6.27557973e+00, -1.47086787e-01],
                 [-1.62670925e+01, -3.55899907e+00, -7.10704970e+00,
                 -4.28295850e-01, 1.25954168e+00],
                 [-2.67100704e+01, 2.91715588e+00, 4.66657911e+00,
                  2.73269062e+00, -2.20148315e+00],
                 [-1.42420225e+01, 6.03401527e+00, -7.63055319e-01,
                  1.45404689e+00, -3.12583218e+00],
                                                     9.62085311e+00,
                 [-1.42706374e+01, 7.39456162e+00,
                  8.25728389e+00, -5.93396293e+00],
                 [-3.06870811e+01, -1.50400710e+00,
                                                     1.00911714e+01,
                 -2.80366436e+00, 2.55081470e+00],
                                                     4.95160399e+00,
                [-8.34875636e+00, 8.33573133e+00,
                  5.14970136e+00, -5.33908531e+00],
                 [ 7.68535335e+00, 5.52947363e+00, -6.03702022e+00,
                 -2.55678855e+00, -1.06067291e+00],
                 [-2.28943415e+01, -2.73835708e+00, -1.28679609e+00,
                 -4.01897005e-02, 1.36278424e+00],
                 [-2.72798878e+01, 2.86711058e+00,
                                                     8.37957567e+00,
                 -1.39404125e+00, -2.77636507e-01],
                 [-1.47627132e+01, 6.69392203e+00,
                                                     9.16530181e+00,
                  6.22521681e+00, -4.70945043e+00],
                 [-1.59023756e+01, 5.74753114e+00,
                                                     1.00427925e+01,
                 -5.77443047e+00, 8.12964103e-01],
                 [-1.56595857e+01, 2.68922867e+00,
                                                    8.91188236e+00,
                 -7.80255463e+00, 2.49320951e+00],
                                                     7.14471041e+00,
                 [-9.83217624e+00, 3.86804512e+00,
                 -1.21064551e+00, -1.03217368e+00],
                [ 2.67013184e+01, 9.02713344e+00.
                                                     6.10503143e+00,
                 -2.33619728e+00, -2.05998745e+00],
                 [-1.11820284e+01, 3.19573932e+00, -5.17655563e+00,
                  7.42933480e+00, -4.20018713e+00],
                 [-1.96455671e+01, 5.16100154e+00,
                                                     4.98193280e+00,
                  3.63411470e+00, -3.56641829e+00],
                                                     5.66704055e+00,
                 [-7.12752867e+01, -4.26075033e+00,
                  4.21957134e+00, -8.42169210e-02],
                [ 5.11677616e+01, 3.49937278e+00,
                                                     7.20233314e-01,
                  6.81877682e-01, -3.33778335e+00],
                [ 1.33743800e+01, 2.48986240e+00,
                                                     1.34538175e+01,
                 -5.00833926e+00, 6.01286881e-01],
                 [-1.65447794e+01, -2.53789583e+00,
                                                     8.33106726e+00,
                  7.39308577e+00, -9.17268883e-01],
```

```
[-2.22129820e+01, -5.85741498e+00,
                                    4.54528047e+00,
 5.16150350e+00, 1.48369614e+00],
[-2.51918811e+01, -5.35507871e+00,
                                    2.79591961e+00,
 7.52857621e+00, -1.52498703e-02],
[-5.06944021e+01, -2.73033700e+00,
                                    5.69125604e+00,
 2.32650824e+00, 6.17590202e-01],
[-7.11713966e+01, -4.01786441e+00,
                                    5.82800735e+00,
 4.54471442e+00, -3.32282709e-01],
[-7.11713966e+01, -4.01786441e+00,
                                    5.82800735e+00,
 4.54471442e+00, -3.32282709e-01],
[-2.38760212e+01. -3.76495577e+00.
                                    1.03781457e+01.
-6.39594783e+00, 5.56275591e+00],
[ 5.87153417e+01, -1.55938332e+01,
                                    1.88585088e+01,
 4.90976070e+00, 4.18553117e+00],
[ 5.05329261e+01, 2.23809620e+00,
                                    9.34635798e+00,
 1.66001350e+00, -3.11917003e+00],
[ 3.02550221e+01, -2.38633383e+00, -8.83868360e+00,
 2.86827699e+00, -1.20171751e+00],
[-1.11018157e+01, 3.16053064e+00,
                                    2.06554934e-01,
 9.94588109e+00, -5.35132949e+00],
[-2.59722185e+01, 3.67946279e+00,
                                    9.14777553e+00,
 6.40205162e+00, -3.70657370e+00],
[-1.72456192e+01, 5.69066364e+00,
                                    1.03920052e+01,
-5.09223006e+00, 3.93451392e-01],
[-5.13262183e+01, -2.41979333e+00,
                                    7.91830078e+00,
 4.30843130e-01, 1.31365137e+00],
[-1.73245104e+01,
                   5.61060021e+00,
                                    7.89147324e+00,
-5.14792996e+00,
                   5.03005729e-01],
[ 8.44291111e+00, 7.60929964e+00,
                                    7.74607719e-02,
-4.74154987e+00, -1.60287014e+00],
[-5.01816896e+01, -2.28737407e+00,
                                    5.67446745e+00,
 1.44166623e+00, 6.98709180e-01],
[-6.44665654e+01, -2.93749608e+00,
                                    6.46509773e+00,
 3.98499931e+00, 7.08635114e-02],
[-2.24466176e+01,
                   4.17181324e+00.
                                    9.46949105e+00,
-3.38244124e+00,
                  6.84601516e-02],
[-1.33002705e+01, 8.69711261e+00,
                                    8.60384711e+00,
-3.36626538e+00, -2.03119460e+00],
[-7.05828442e+01, -3.87958645e+00,
                                    5.89458216e+00,
 4.47094234e+00, -2.58921436e-01],
[-2.26529871e+01, 3.78371283e+00,
                                    9.15477517e+00,
-1.35038173e+00, -5.78580940e-01],
[-6.81163872e+00, 9.37131110e+00,
                                    6.04559492e-01,
 9.00348588e+00, -7.41445325e+00],
[-6.59515340e+01, -3.03013875e+00,
                                    6.35266660e+00,
 4.17102463e+00, 1.06678116e-02],
[-6.44155603e+01, -3.08588306e+00]
                                    6.12941112e+00,
 4.84536874e+00, -1.93453542e-01],
[-5.69963925e+01, -2.49876760e+00,
                                    7.13237772e+00,
 4.93194469e+00, -4.53696703e-01],
[-2.33913178e+01, 1.66798110e+00,
                                    1.12360441e+01,
-3.90377153e+00, 2.11532821e+00],
                                    5.66704055e+00,
[-7.12752867e+01, -4.26075033e+00,
 4.21957134e+00, -8.42169210e-02],
[-6.08421079e+01, -3.66903817e+00,
                                    5.28352507e+00,
 4.86822693e+00, -1.72893514e-01],
[-1.89234409e+01, -3.26007260e+00, -4.36217164e+00,
 6.88489101e+00, -1.43224924e+00],
[-6.99033419e+01, -3.78144925e+00,
                                    5.81343288e+00,
 5.67941704e+00, -6.48208419e-01],
```

```
[-6.33051295e+01, -3.20747950e+00,
                                    6.45007562e+00,
 3.66540782e+00, 4.02141538e-01],
[-3.17119753e+01. 3.08239776e-01.
                                    6.02439452e+00,
-1.37316393e+00, 1.15616296e+00],
[-1.78448673e+01, -9.78007907e-01, -4.10535513e+00,
-5.73275601e+00, 2.93620129e+00],
[-3.00957742e+01, -6.84905100e-01,
                                    5.81114160e+00,
-4.44224964e+00, 2.87955703e+00],
[-7.12752867e+01, -4.26075033e+00,
                                    5.66704055e+00,
 4.21957134e+00, -8.42169210e-02],
[-7.11713966e+01. -4.01786441e+00.
                                    5.82800735e+00.
 4.54471442e+00, -3.32282709e-01],
[-7.11713966e+01, -4.01786441e+00,
                                    5.82800735e+00,
 4.54471442e+00, -3.32282709e-01],
[ 5.83877051e-01, 5.06821298e+00,
                                    9.84308199e+00,
-3.94653198e+00, -3.38981003e-01],
[ 2.20567001e+01, -5.67115697e-01,
                                    1.34789934e+01,
-2.39852438e+00, 1.01773110e+00],
[ 2.68105869e+01, -5.27603900e+00,
                                    1.39349178e+01,
-1.27313810e+00, 2.70553332e+00],
[ 3.24707854e+01, -5.35564955e+00,
                                    2.03848237e+01.
 1.31784139e+00, 2.50805772e+00],
[ 2.23014193e+01, -4.02365932e+00,
                                    1.70823509e+01,
-2.78766422e-01, 1.85725785e+00],
[ 2.68071151e+01, -5.48319617e+00,
                                    1.78458541e+01,
 9.93962038e-01, 2.35542478e+00]])
```

```
In [40]: y_test = np.array(y_test)
y_test
```

```
array([[-1.44477741e+01, 8.85239245e+00,
                                                    6.60857916e+00,
Out[40]:
                 -2.03718957e+01, -9.15451211e+00],
                                                   1.63290479e+01,
                 [ 3.38072659e+01, 6.97369108e+00,
                 -6.95258656e+00, -5.15849112e+00],
                 [ 3.35800333e+01, 8.15555495e+00, -6.01034607e+00,
                 -2.2223603e+00, -8.03020081e+00],
                 [-1.29783287e+01, 1.96959167e+01,
                                                    1.69311625e+00,
                 -7.78363802e+00, -1.06841967e+01],
                 [-1.41107690e+01, 2.25421435e+01,
                                                    5.94742058e+00,
                 -6.30449296e-02, -7.16490355e+00],
                [ 1.14042773e+01, 2.83988479e+01,
                                                    1.91867250e+01.
                  5.81192844e-01, -1.14936558e+01],
                 [ 1.61751945e+01, 3.07758288e+01,
                                                     1.57854057e+01,
                 -9.91301486e+00, -8.44936709e+00],
                 [-2.01390666e+01, 1.36577090e+01,
                                                    1.09627459e+01,
                 -1.96322922e+01, -5.81567926e+00],
                 [ 9.27858818e+00, 1.49387968e+01, 1.27462299e+01,
                 -2.03152889e+00, -6.33558046e+00],
                [ 1.81652514e+01, -7.87950821e-01, -3.69387087e+00,
                 -1.06395871e+01, -6.11530218e+00],
                [-2.80614796e+01, -6.09427047e+00, -1.24965974e+01,
                 -1.85424102e+00, -3.40170743e+00],
                [-3.76693009e+01, 2.45539241e+01, -4.57224005e+00,
                  4.27519750e+00, -1.71150423e+01],
                 [-1.98196983e+01, 4.28413667e+01, -5.38507431e+00,
                  2.93765599e+00, -1.70217805e+01],
                 [-2.05642078e+01, 2.81399241e+01,
                                                    1.09974498e+01,
                  7.46240888e-01, -1.54673640e+01],
                 [-4.61692868e+01, -5.19439278e+00, 8.94446314e+00,
                 -1.32964520e+01, -9.22402215e-01],
                [-4.41322106e-01, 1.26266719e+01, 6.20274469e+00,
                  2.36011995e+00, -3.86530497e+00],
                 [ 5.34236596e+00, 9.10694518e+00, -1.06621842e+01,
                 -4.84402527e+00, -7.88256080e+00],
                 [-3.15047321e+01, 1.29229462e+00, -2.12437683e+00,
                  3.08659645e+00, -2.02223294e+00],
                 [-3.91416728e+01, 1.53919606e+01,
                                                    5.87606601e+00,
                 -8.53025419e+00, -8.49479103e+00],
                 [-1.98964460e+01, 2.60180540e+01,
                                                    1.48930189e+01,
                  5.97075809e+00, -5.94885577e+00],
                 [-9.32563610e+00, 2.29228538e+01,
                                                    2.38046332e+01,
                 -6.29390873e+00, -2.74609467e+00],
                 [-2.75448456e+01, 3.03832236e+00,
                                                    9.06149357e+00,
                 -1.57928162e+01, 1.88608796e+00],
                 [-1.12776125e+00, 6.49578582e+00,
                                                    1.91373811e+01,
                 -3.31146840e+00, -7.65679913e+00],
                                                    2.39531276e+00,
                [ 1.89152056e+01, 1.50521067e+01,
                  5.09613578e+00, 1.50195585e+00],
                [-1.75156926e+01, 1.02252664e+01, -1.33383522e+01,
                  6.22512374e+00, -1.72229914e+00],
                 [-2.87502105e+01, 1.24294745e+01,
                                                    3.08804344e-01,
                  4.81564016e+00, -5.32208458e+00],
                 [-6.96817705e+01, 2.30962556e+01, -8.43987008e+00,
                 -3.06798530e+00, 9.04050212e+00],
                 [ 7.49345985e+01, 1.06001596e+01,
                                                    1.21795874e+00,
                  4.14880715e+00, 1.45502945e+01],
                [-9.12654909e+00, -1.49741604e+00,
                                                    2.04262135e+01,
                 -8.53347075e+00, 6.56647951e+00],
                 [-1.49402063e+01, -1.17677267e+01,
                                                    1.45397696e+01,
                  6.28573812e+00, -1.21966831e+00],
```

```
[-2.63227951e+01, -1.39691904e+01, 2.56479886e+00,
 9.61881993e+00, 5.73128267e+00],
[-3.33012216e+01, -1.02192871e+01, -4.49626411e+00,
 8.81434781e+00, -1.71812139e+00],
[-4.31426238e+01, 4.38313081e+00, -2.66390776e+00,
-2.72537364e+00, -7.81183704e+00],
[-8.53768754e+01, 5.32432305e+00, -9.33867011e+00,
-3.79805984e+00, -1.22714644e+01],
[-8.84812634e+01, -3.77973935e+00, 7.74968131e-01,
 3.12783225e+00, -6.43713015e+00],
[-1.29420853e+01. -2.02691422e+01.
                                   4.56698124e+01,
-5.43244165e+00, 5.11945059e+00],
[ 9.04979454e+01, -1.26409422e+01,
                                   7.53080681e+01.
 9.62446644e+00, 4.38506151e+00],
[ 5.97019084e+01, 6.10386039e+00, 1.02215276e+01,
  1.16343760e+01, -4.26809486e+00],
[ 2.93007891e+01, -1.30464086e+01, -8.24016558e+00,
 2.40543228e+01, -1.70448149e+01],
[-1.98854346e+01, 8.52488259e+00, -9.10064152e-01,
 8.35224601e+00, -1.15223603e+01],
[-2.89859645e+01, 3.45068068e+01,
                                   1.01840004e+01.
 4.08314738e+00, -1.06133655e+01],
[-2.39096635e+01, 2.30138336e+01,
                                   1.75130508e+01,
-6.53319086e+00, -1.81199978e+00],
[-4.47801558e+01, 1.18791376e+01,
                                   2.30607338e+01,
-1.52653321e+01, 7.80188408e-01],
[-1.46131097e+01, 2.07180797e+01, 8.34724344e+00,
-2.35517769e+00, -3.53759195e+00],
[ 1.46170011e+00, 2.30648476e+01, -9.96405971e+00,
-9.69664479e+00, -1.23024959e+01],
[-4.78747557e+01, 1.39074144e+01, -3.04210163e+00,
-1.13962474e+01, -9.96971438e+00],
[-4.98538923e+01, 2.83402111e+01,
                                   1.04834821e+01,
-7.31405489e+00, -8.30197104e+00],
[-2.52827349e+01, 3.72317594e+01,
                                   8.84924310e+00,
-2.84829493e+00, -6.52175819e+00],
[-1.88846368e+01, 2.67855190e+01,
                                   2.37329154e+01,
-1.13321758e+01, -8.75018339e+00],
[-6.97175337e+01, 4.43733234e+00,
                                    1.55678836e+01.
-1.33047486e+01, 2.51524622e+00],
[-2.06373217e+01, 1.61151597e+01,
                                   1.24290181e+01,
 1.61776659e+00, -8.03835098e+00],
[-7.33274923e+00, 2.31000958e+01, -8.82496982e+00,
 8.55633605e+00, -9.86132489e+00],
[-5.44806140e+01, 1.16922455e+01, -5.25862808e+00,
-2.21188798e+00, -8.11892142e+00],
[-5.14728868e+01, 2.01020580e+01, 2.62631252e+00,
  1.45703820e+00, -1.50272927e+01],
[-4.46681690e+01, 2.79118647e+01, 6.67270908e+00,
 9.06814389e+00, -6.87311859e+00],
[-2.55738891e+01, 1.85104215e+01,
                                    1.90374584e+01,
-9.47620122e-01, 7.30945554e+00],
[-6.99016583e+01, 5.73170859e+00,
                                   1.80994839e+01.
-1.13232023e+01, 7.93918580e+00],
[-3.46699677e+01, -3.22050333e+00, -2.66615045e+00,
 5.27696797e+00, -4.23234559e+00],
[-2.87390265e+01, -1.79773029e+00, -2.10428206e+01,
 9.44911655e+00, -3.64924003e+00],
[-6.36362521e+01, 1.47989273e+00, -1.13846712e+01,
 7.40666530e+00, 6.10161764e+00],
```

```
4.99641710e+00],
                 -1.30165471e+00,
                                   6.57934894e+00, -9.20094950e-02,
                 [-3.78197232e+01,
                 -1.44526396e+00, -2.50100987e+00],
                 [-2.77590637e+01, 2.14931125e+01, -1.12295128e+01,
                 -1.42858446e+01, 2.78641531e+00],
                 [-3.90284406e+01, 6.86091347e+00, -1.23541883e+00,
                 -2.05430470e+01, 9.61788752e+00],
                                   5.43408870e+00, -5.49536812e+00,
                 [-6.79245953e+01,
                 -4.69016121e+00, -3.17411573e+00],
                 [-1.02268754e+02. -3.34927159e+00. -8.53939423e+00.
                  4.70943991e+00, -3.53178145e+00],
                 [-8.88345937e+01, -8.50630233e-01,
                                                     2.19008124e+00,
                  9.32977329e+00, -1.08110838e+01],
                 [ 3.20841817e+00, 9.78597526e-01,
                                                     1.74328508e+01,
                 -9.06419044e+00, -2.74005391e+00],
                 [ 2.02034387e+01, -1.47944860e+01,
                                                     1.31724880e+01,
                 -8.50657080e+00, -8.97686887e+00],
                 [ 1.68339799e+01, -2.18379571e+01,
                                                     9.73854931e+00,
                 -1.36454055e+01, -1.13571922e+01],
                 [ 1.46016931e+01, -1.78971820e+01,
                                                     2.35839237e+01,
                 -2.15602752e+01, -6.51483383e+00],
                [ 1.43229824e+01, -4.19326201e+01,
                                                     3.00161777e+01,
                 -1.49006498e+00, 1.21303948e+00],
                [ 8.45766075e+00, -6.10721467e+01,
                                                    3.56934558e+01,
                  7.38949554e+00, 1.44165764e+01]])
In [41]: from sklearn.metrics import r2_score
         r2 = r2_score(y_test, y_pred)
In [42]: r2
         0.3331655559345308
Out[42]:
 In [ ]: # Train test split by hours
In [43]: train_size = int(len(pca_components) * 0.8)
         X = pca_components.iloc[13:,]
         X = X.iloc[:, 5:]
         X_train = X.iloc[:train_size, :]
         X test = X.iloc[train size:, :]
         Y = pca_components.iloc[13:,].iloc[:, :5]
         y_train = Y.iloc[:train_size, :]
         y test =Y .iloc[train size:, :]
```

6.2 model performance measurement

[-4.72232485e+01,

Use the RandomForest model with the provided parameters (min_samples_split: 2, min_samples_leaf: 10, and n_estimators equal to 50.) to predict the compressed daily ridership. Prediction results are PCA components instead of taxi zone level ridership. To reconstruct the data back to its original size and scale, we need to inverse PCA and inverse standardization. report the taxi zone level R² value.

```
In [44]:
         #your answer here
         rf = RandomForestRegressor(n_estimators=50, min_samples_leaf=10, min_samples_s
         # Fit the model on the training data
         rf.fit(X_train, y_train)
Out[44]:
                              RandomForestRegressor
         RandomForestRegressor(min samples leaf=10, n estimators=50)
In [45]: y_pred = rf.predict(X_test)
         y_pred
         array([[ 1.22742426, 2.44893175, -0.03127481, 0.02336949,
                                                                     0.04823541],
Out[45]:
                [4.04410323, 3.00525498, -0.77888339, -0.30251751,
                                                                     0.13231062],
                [ 4.59584928, 2.40853006, -0.44148399, -0.20524202, 0.17279652],
                [3.45775339, -2.98143902, -0.11226782, -0.05467581, -0.05032933],
                [4.67589206, -3.27699673, -0.12082895, 0.00972545, -0.19545674],
                [ 3.5982126 , -3.20680853, -0.56601796, -0.06323277, -0.32466589]])
In [46]: y_test = np.array(y_test)
         y_test
Out[46]: array([[-1.304949
                              2.98961347, -0.608941 , -0.09891158, 0.49470123],
                              2.69846343, 0.3365104, -0.65082308, -0.19725592],
                [ 2.95845202,
                              3.55936594, 0.32574949, -0.1090164, -1.27846526],
                [ 2.90441484,
                [8.61979218, -8.05996965, 3.85840615, 0.95537746, 0.82299888],
                [7.9354065, -7.05893474, 0.78392213, 2.26819964, -0.37416232],
                [ 3.23925122, -6.7471905 , -1.18213258, 1.89708569, 0.04066047]])
In [47]: from sklearn.metrics import r2 score
         r2 = r2_score(y_test, y_pred)
In [48]:
         0.37744672969744325
Out[48]:
 In []:
```