# 3D Point Cloud Classification with Deep Learning

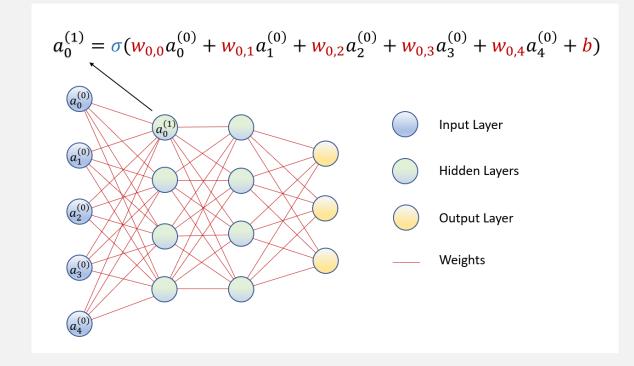
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UCSB's Mathematics Directed Reading Program

## Introduction

Point clouds are sets of points that arise in many situations such as LiDAR data and samplings of 3D meshes. Traditional neural networks struggle with point clouds because their output depends on the order of the input, and sets with *n* points have *n*! permutations to worry about. PointNet [1] solves this problem directly by being permutation invariant by design.

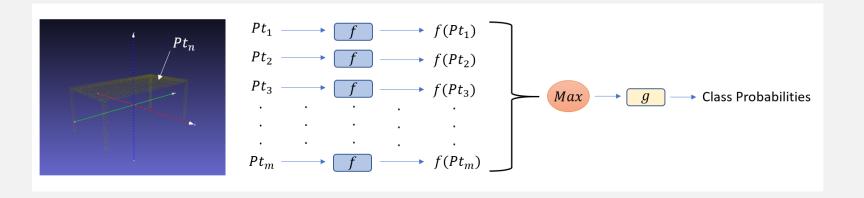
# Feed-Forward Neural Networks



Above is a 2-hidden-layer neural network with activation function  $\sigma$ . In general, a feed-forward neural network applies an alternating sequence of linear transformations  $L_i$  and nonlinear transformations  $\sigma_i$  to an input x:

$$F(x) = \sigma_n(L_n(...(\sigma_1(L_1(x)))))$$

## PointNet



$$F_{PN}(A) = g(\max_{a \in A} f(a))$$

Above, f and g are traditional neural networks and  $F_{PN}$  is a PointNet. By taking the component-wise maximum (a.k.a. max-pooling) of transformed elements of the set, PointNet achieves permutation invariance.

## Theoretical Properties of PointNet

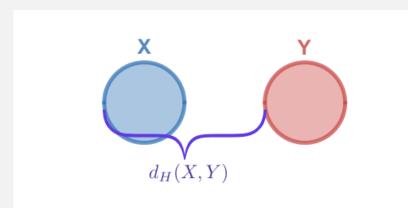
• PointNet is continuous with respect to the Hausdorff distance. The Hausdorff distance  $d_H$  is a metric that measures how different non-empty compact subsets are. For a metric space  $(\Omega, d)$ , it's given by:

$$d_{\mathbb{H}}(X,Y) = \inf\{\epsilon \geq 0 : X \subseteq Y^{\epsilon} \text{ and } Y \subseteq X^{\epsilon}\}$$

where  $X^{\epsilon}$  is  $\epsilon$ -fattening of X, i.e., the set of all points within  $\epsilon$  of X.

# Theoretical Properties (Continued)

This can be visualized in  $(\mathbb{R}^2, d_{Euclidean})$  as:



• Universal Approximation. For any  $\epsilon > 0$  and uniformly  $d_H$ -continuous function F, there's a PointNet  $F_{PN}$  so that  $|F(A) - F_{PN}(A)| < \epsilon$  for all point clouds A in the unit ball.

# Training in General

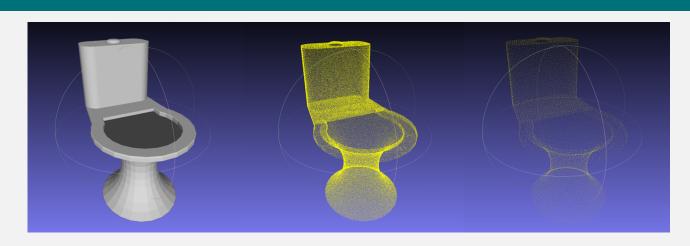
Given some data  $D = \{(x_i, y_i)\}_{i=1}^n \&$  parametric model  $f_w$  with weights w.

- Loss Function / Objective Function: For the machine to know how far predictions are from actual observations we use a loss function  $\ell(y, \hat{y})$ , where  $\hat{y}$  is the predicted value and y is the ground-truth.
- **Gradient Descent (GD):** For a given loss function, GD is an optimization algorithm with the goal of  $\min_{w} \frac{1}{n} \sum_{i=1}^{n} \ell(y_i, f_w(x_i))$ . GD updates the weights by  $w^{i+1} = w^i \alpha \nabla_{w} \frac{1}{n} \sum_{i=1}^{n} \ell(y_i, f_w(x_i))$  where  $\alpha > 0$  is the so-called learning rate.
- Stochastic Gradient Descent (SGD): Similar to GD except the whole-data gradient is estimated using gradients over smaller batches of data. SGD has a reduced computation time and a slightly lower convergence rate than GD. As a result, many epochs (i.e. number of times the algorithm sees every data point) may be needed.
- Backpropagation: An algorithm which efficiently computes the gradient  $\nabla_w(\cdot)$  with respect to network weights via careful use of the chain rule, iterating backwards from the final layer to 'unpack' one layer at a time, thus avoiding calculating anything twice. [2]

# Training a Classifier

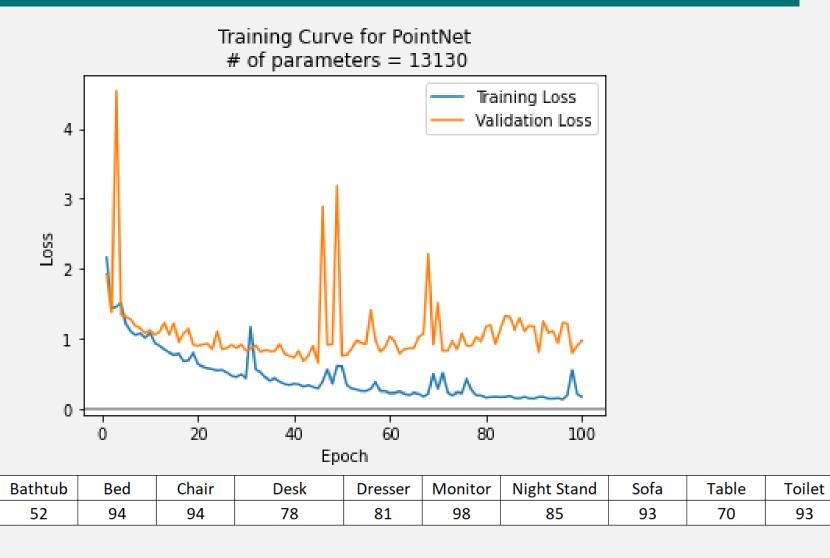
- **Softmax:** A function for transforming  $x = (x_1, ..., x_m) \in \mathbb{R}^m$  into a probability distribution by  $s(x)_i = \frac{e^{x_i}}{\sum_{j=1}^n e^{x_j}}$ . Classification models output the class with the largest associated probability, e.g. 77% toilet.
- Information Entropy: Given by  $H(p) = -\sum_i p_i \log p_i$  for a probability distribution p. It's deeply related to data compression.
- Cross-Entropy Loss: The distance, in bits of information, separating two probability distributions. Cross entropy loss can be mathematically defined as  $H(y, \hat{y}) = -\sum_i y_i \log_e(\hat{y}_i)$ , where  $\hat{y}$  and y are as defined above. Often used in classification problems, including our experiment.

## Sampling Meshes



For this project we use the ModelNet10 data set, 3D meshes broken into 10 classes (bed, chair, desk, etc.). We use Barycentric coordinates to sample 1,024 random points from surface of the mesh. These form the point clouds our model takes as input. Some meshes are sampled multiple times to ensure a balanced data set. After sampling the 3D meshes, we have 1,000 point clouds per class.

## Our Results



We implement PointNet with PyTorch. We tried SGD but found the Adam optimizer better for training and used it instead. We train using: Epochs = 100, Batch Size = 32, Learning Rate =  $10^{-3}$ . We chose the sub-networks of PointNet to be of type  $f: \mathbb{R}^3 \to \mathbb{R}^{32} \to \mathbb{R}^{32}$  and  $g: \mathbb{R}^{32} \to \mathbb{R}^{32} \to \mathbb{R}^{10}$  with Softmax at the end. Our model achieves an accuracy of 80.2% on ModelNet10 (random guessing would give 10%).

#### References

Accuracy(%):

- [1] Charles R Qi, Hao Su, Kaichun Mo, and Leonidas J Guibas.

  Pointnet: Deep learning on point sets for 3d classification and segmentation.

  In Proceedings of the IEEE conference on computer vision and pattern recognition, pages 652–660, 2017.
- [2] Justing Domke. Automatic differentiation and neural networks, 2011.
- [3] Eman Ahmed, Alexandre Saint, Abd El Rahman Shabayek, Kseniya Cherenkova, Rig Das, Gleb Gusev, Djamila Aouada, and Bjorn Ottersten.

  A survey on deep learning advances on different 3d data representations.

  arXiv preprint arXiv:1808.01462, 2018.