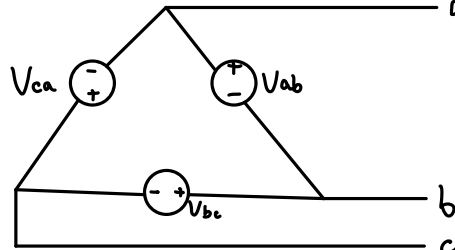


a) Y形联结



b) Δ形联结

$Z_{\Delta} = 3Z_Y$, $Z_Y = \frac{1}{3}Z_{\Delta}$ 进行 Y形联结负载与Δ形负载转换

联结方式	相电压/电流	线电压/电流
<p>Y-Y</p>	$V_{an} = V_p \angle 0^\circ$ $V_{bn} = V_p \angle -120^\circ$ $V_{cn} = V_p \angle +120^\circ$ 同线电流	$V_{ab} = \sqrt{3} V_p \angle 30^\circ$ $V_{bc} = V_{ab} \angle -120^\circ$ $V_{ca} = V_{ab} \angle 120^\circ$ $I_a = V_{an} / Z_Y$ $I_b = I_a \angle -120^\circ$ $I_c = I_a \angle 120^\circ$ <p><small>指电源/负载 ↓ 线电压V_L幅度是相电压V_p的$\sqrt{3}$倍,超前相电压30°</small></p> <p><small>$I_a + I_b + I_c = 0$ $I_n = 0$ $V_{NN} = 0$</small></p>
<p>Y-Δ</p>	$V_{an} = V_p \angle 0^\circ$ $V_{bn} = V_p \angle -120^\circ$ $V_{cn} = V_p \angle +120^\circ$ $I_{AB} = V_{AB} / Z_{\Delta}$ $I_{BC} = V_{BC} / Z_{\Delta}$ $I_{CA} = V_{CA} / Z_{\Delta}$	$V_{ab} = \sqrt{3} V_p \angle 30^\circ = V_{AB}$ $V_{bc} = V_{ab} \angle -120^\circ = V_{BC}$ $V_{ca} = V_{ab} \angle 120^\circ = V_{CA}$ $I_a = I_{AB} \sqrt{3} \angle -30^\circ$ $I_b = I_a \angle -120^\circ$ $I_c = I_a \angle 120^\circ$ 同相电压 <p><small>线电流I_L幅度是相电流I_p的$\sqrt{3}$倍,滞后相电流30°</small></p>
<p>Δ-Δ</p>	$V_{ab} = V_p \angle 0^\circ$ $V_{bc} = V_p \angle -120^\circ$ $V_{ca} = V_p \angle 120^\circ$ $I_{AB} = V_{ab} / Z_{\Delta}$ $I_{BC} = V_{bc} / Z_{\Delta}$ $I_{CA} = V_{ca} / Z_{\Delta}$	$I_a = I_{AB} \sqrt{3} \angle -30^\circ$ $I_b = I_a \angle 120^\circ$ $I_c = I_a \angle 120^\circ$ 同相电压 <p><small>线电流I_L幅度是相电流I_p的$\sqrt{3}$倍,滞后相电流30°</small></p>
<p>Δ-Y</p>	$V_{ab} = V_p \angle 0^\circ$ $V_{bc} = V_p \angle -120^\circ$ $V_{ca} = V_p \angle 120^\circ$ 同线电流	$I_a = \frac{V_p \angle -30^\circ}{\sqrt{3} Z_Y}$ $I_b = I_a \angle -120^\circ$ $I_c = I_a \angle 120^\circ$ 同相电压

• 对称系统中的功率

$$U_{AN} = \sqrt{2} V_p \cos \omega t, \quad U_{BN} = \sqrt{2} V_p \cos (\omega t - 120^\circ), \quad U_{CN} = \sqrt{2} V_p \cos (\omega t + 120^\circ) \quad (V_p \text{ 定义是相电压有效值})$$

若 $Z_Y = Z \angle \theta$.

$$i_a = \sqrt{2} I_p \cos (\omega t - \theta), \quad i_b = \sqrt{2} I_p \cos (\omega t - \theta - 120^\circ), \quad i_c = \sqrt{2} I_p \cos (\omega t - \theta + 120^\circ)$$

$$P = P_a + P_b + P_c = 3 V_p I_p \cos \theta. \quad \text{各项平均功率 } p/3$$

负载平均功率 $P_p = V_p I_p \cos \theta$.

视在功率 $S_p = V_p I_p$.

无功功率 $Q_p = V_p I_p \sin \theta$.

复功率 $\tilde{S}_p = P_p + Q_p j = \tilde{V}_p \tilde{I}_p^*$

又有 $P = \sqrt{3} V_L I_L \cos \theta$ $\therefore \begin{cases} Y \text{ 接 } I_L = I_p, V_L = \sqrt{3} V_p \\ \Delta \text{ 接 } V_L = V_p, I_L = \sqrt{3} I_p \end{cases}$

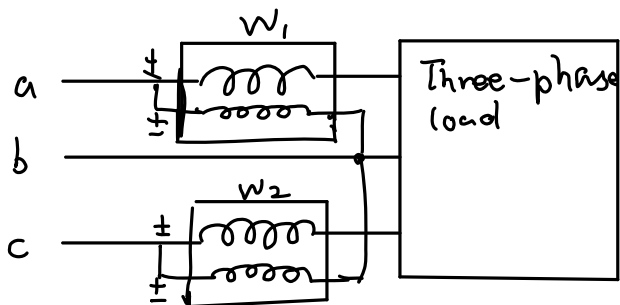
$\therefore Q = \sqrt{3} V_L I_L \sin \theta = 3 V_p I_p \sin \theta$

总复功率 $S = 3 S_p = 3 \tilde{V}_p \tilde{I}_p^* = 3 I_p^2 \tilde{Z}_p = \frac{3 V_p^2}{\tilde{Z}_p^*} = \sqrt{3} V_L I_L \angle \theta$.

The material (transmission line) to deliver the same power and to tolerate the same loss needed is 3/4 times less.

滞后 lagging $\Rightarrow \sin \theta$ 为正.

$C = \frac{|Q_c|}{\omega V_L^2}$



$P_T = P_1 + P_2$

$P_1 = V_L I_L \cos(\theta + 30^\circ)$

$P_2 = V_L I_L \cos(\theta - 30^\circ)$

$P_1 + P_2 = P_T$ $P_1 - P_2 = V_L I_L \sin \theta = \frac{Q_T}{\sqrt{3}}$

$\therefore \tan \theta = \frac{Q_T}{P_T} = \sqrt{3} \frac{P_2 - P_1}{P_2 + P_1}$