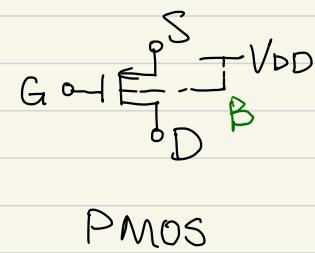
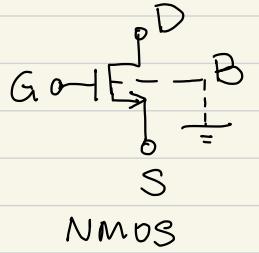
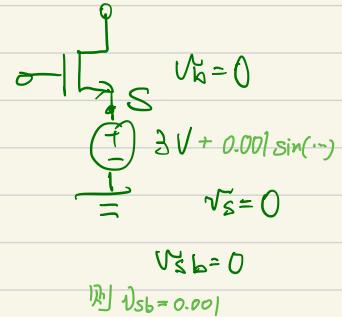
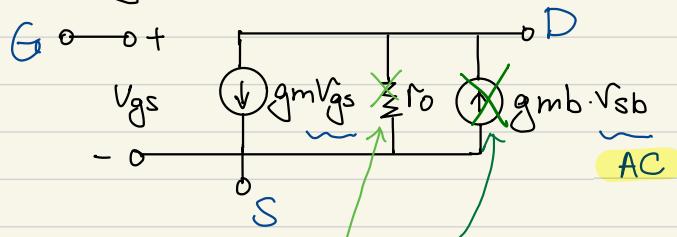


Single-Stage Amplifier RC

Recap from last RC:



Small-signal model:



Note: ① No body effect: $1^{\circ} \gamma = 0 \Rightarrow gmb = 0$
2^o $\sqrt{s_b} = 0$

② No channel length: $\lambda = 0 \Rightarrow r_0 = \infty$

$$r_0 = \frac{1}{2 \mu_0 \epsilon_0 \frac{w}{2} (V_{GS} - V_{TH})^2 \cdot \lambda}$$

$$g_m = \mu_n (C_{ox} \frac{W}{L}) (V_{GS} - V_{TH})$$

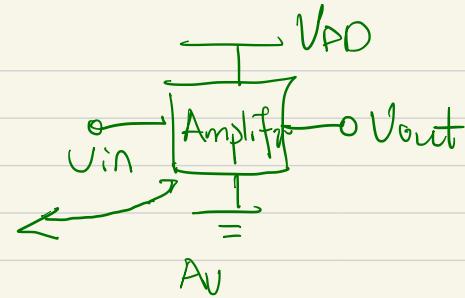
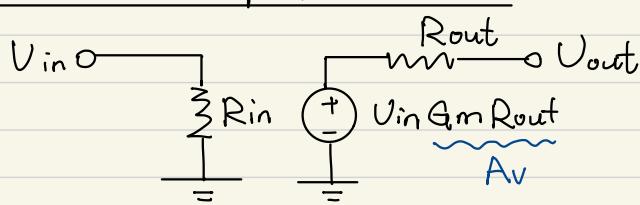
$$= \frac{I_D}{V_{GS} - V_{TH}}$$

$$g_m b = -\mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH}) \frac{\gamma}{2} \cdot \frac{1}{\sqrt{2\phi_F + V_{SB}}}$$

$$L: L_{\text{eff}}$$

$$L': L_{\text{eff}}(1 + \lambda V_{DS}).$$

General Amplifier Model:

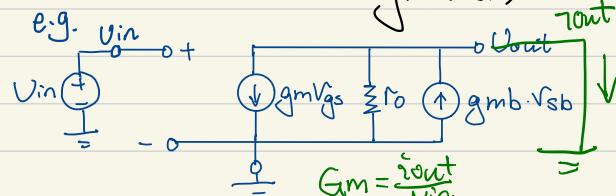


① To get G_m :

$$V_{out} = V_{in} G_m \cdot R_{out}$$

1° short V_{out} to small-signal ground. (i_{out} goes into ground)

$$2° G_m = \frac{i_{out}}{V_{in}}$$

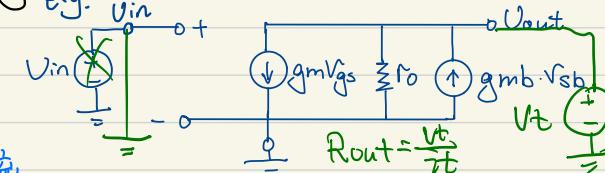


② To get R_{out} :

1° Put V_t at V_{out} (it goes into circuit)

2° Short V_{in} to ground

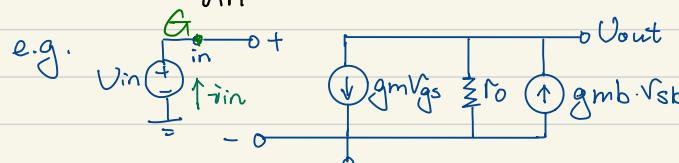
$$3° R_{out} = \frac{V_t}{i_t}$$



③ To get R_{in} :

1° Denote i_{in} goes into circuit (Do nothing else to current circuit)

$$2° R_{in} = \frac{V_{in}}{i_{in}}$$

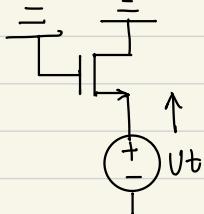


$$R_{in} = \frac{V_{in}}{i_{in}} = \infty$$

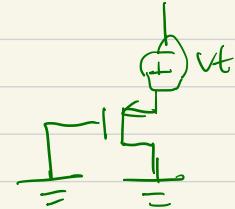
* How to obtain R_{out} for different circuit efficiently?

* 记住以下几个基本模型: (熟练运用!)

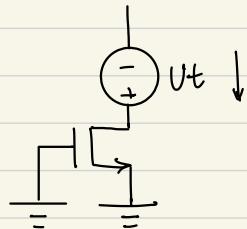
①



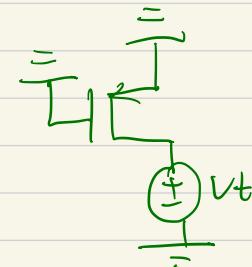
$$R_{out} = \frac{1}{gm} \parallel \frac{1}{gmb} \parallel R_0$$



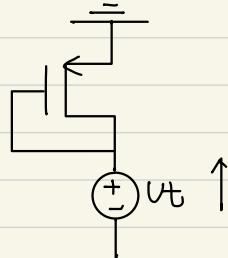
②



$$R_{out} = R_0$$



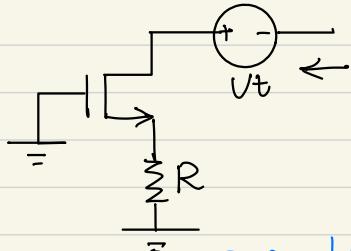
③



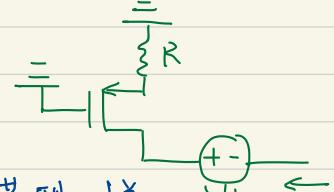
$$R_{out} = \frac{1}{gm} \parallel R_0$$



④



$$R_{out} = (gm + gmb)R_0 + R_0 + R$$

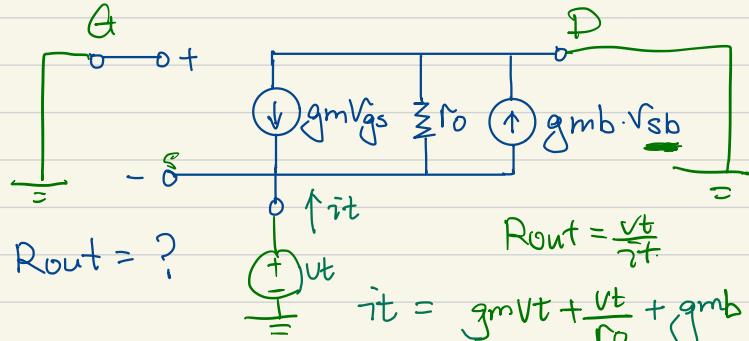
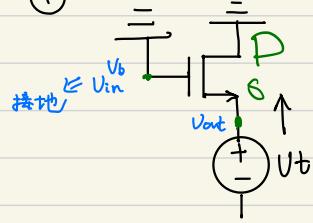


Source degeneration: source有电阻

* PMOS 和 NMOS “上下翻转一样” 则模型一样

Analysis:

①



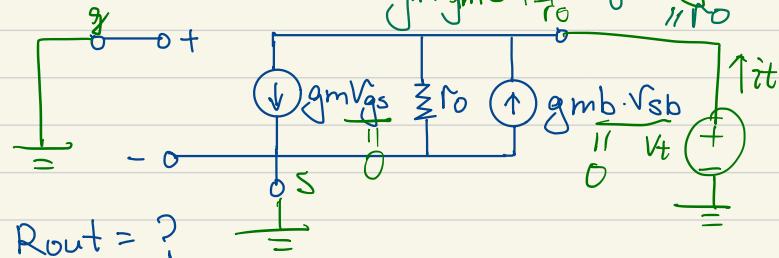
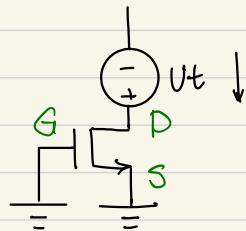
$$R_{out} = \frac{Vt}{it}$$

$$R_{out} = ?$$

$$it = gmVt + \frac{Vt}{R_0} + gmbVt$$

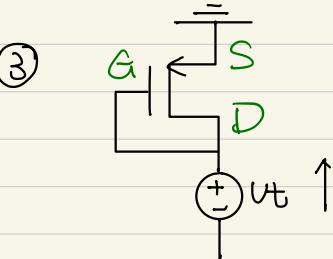
$$R_{out} = \frac{1}{gm + gmb + \frac{1}{R_0}} = \frac{1}{gm} \parallel \frac{1}{gmb} \parallel \frac{1}{R_0}$$

②

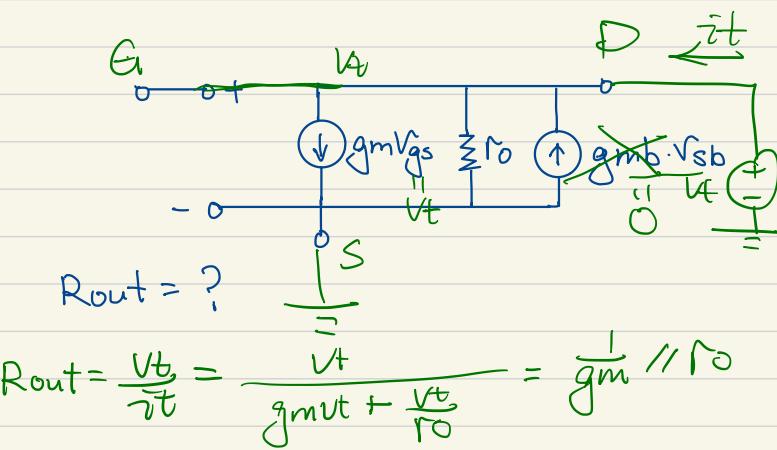


$$R_{out} = \frac{Vt}{it} = \frac{Vt}{\frac{Vt}{R_0}} = R_0$$

③



PMOS 默认接VDD
小信号中 $V_b = 0$.



$$R_{out} = \frac{Vt}{it} = \frac{Vt}{gmVt + \frac{Vt}{R_0}} = \frac{1}{gm} \parallel R_0$$

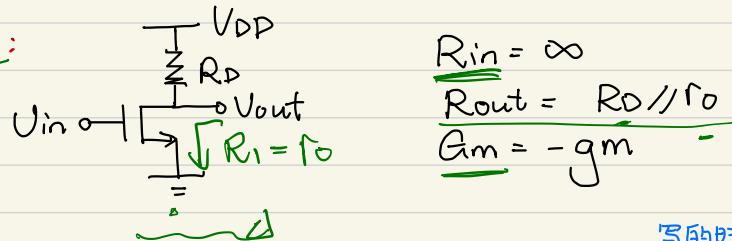
区别 Common Source, Source Follower, Common Gate :

看 signal path! (V_{in} 到 V_{out} 通过 path)



Common Source: Gate 进 Drain 出

* 记:



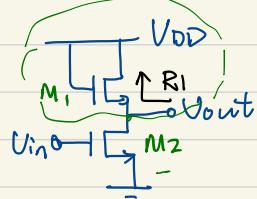
$$R_{in} = \infty$$

$$R_{out} = R_D // r_o$$

$$G_m = -g_m$$

写的时候注意 J_{sb} .

* 变型: 2° with diode-connected load



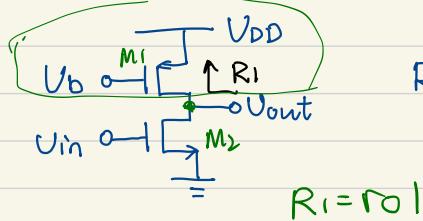
$$R_1 = \frac{1}{g_m} // \frac{1}{g_{mb}} // r_o$$

$$G_m = ? - g_m$$

$$R_{out} = ? \frac{1}{g_m} \left[\frac{1}{g_{mb}} \right] \left[r_o // r_o \right]$$

$$[\lambda=0] \quad [\gamma=0]$$

3° with current source load

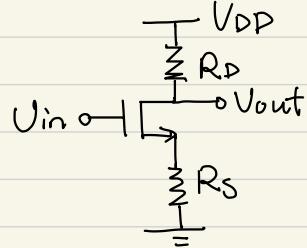


$$G_m = -g_m$$

$$R_{out} = ? r_o // r_o$$

$$R_1 = r_o$$

* 记: 4° with source degraduation



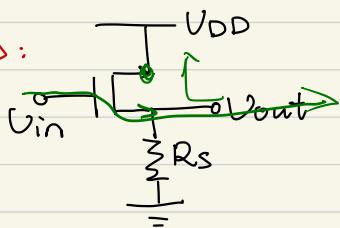
$$R_{in} = \infty$$

$$* G_m = \frac{-g_m r_o}{R_s + r_o + (g_m + g_{mb}) r_o R_s}$$

$$R_{out} = [R_s + r_o + (g_m + g_{mb}) r_o R_s] // R_D$$

Source Follower: Gate to source 出

* 记:

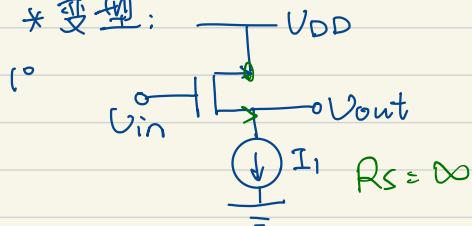


$$R_{in} = \infty$$

$$G_m = g_m$$

$$R_{out} = r_o // R_s // \frac{1}{g_m} // \frac{1}{g_{mb}}$$

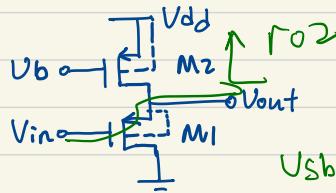
* 变型:



$$G_m = ? \quad g_m$$

$$R_{out} = ? \quad r_o // \frac{1}{g_m} // \frac{1}{g_{mb}}$$

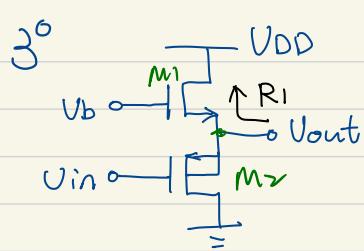
2° with current source load



$$R_{out} = ? \quad r_o1 // r_o2 // \frac{1}{g_{m1}}$$

$$U_{sb} = 0 \Rightarrow g_{mb}, r_o^3$$

SF

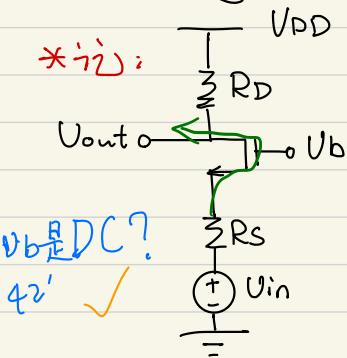


$$R_1 = \frac{1}{g_m1} \parallel \frac{1}{gmb1} \parallel r_o1$$

$$R_{out} = ? \quad \left(\frac{1}{g_m1} \parallel \frac{1}{gmb1} \parallel r_o1 \parallel r_s \right) \parallel r_o2 \parallel \frac{1}{g_m2}$$

Common-gate:

Source 进 Drain 出.



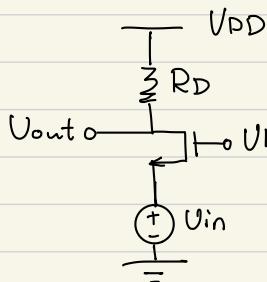
Vb 是 DC?

42' ✓

$$G_m = \frac{(g_m + g_{mb})r_o + 1}{r_o + R_s + (g_m + g_{mb})r_o R_s}$$

$$R_{out} = R_D \parallel [r_o + R_s + (g_m + g_{mb})r_o R_s]$$

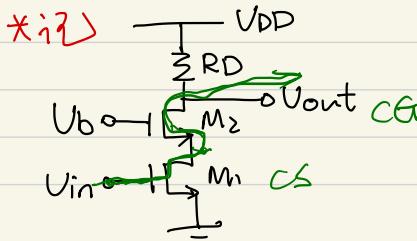
$$R_{in} = \frac{1 + R_s(g_m + g_{mb}) + \frac{1}{r_o}(R_s + R_D)}{g_m + g_{mb} + \frac{1}{r_o}}$$



$$* R_{in} = \frac{R_D + r_o}{1 + (g_m + g_{mb})r_o}$$

P133?

Cascode CS + CE:



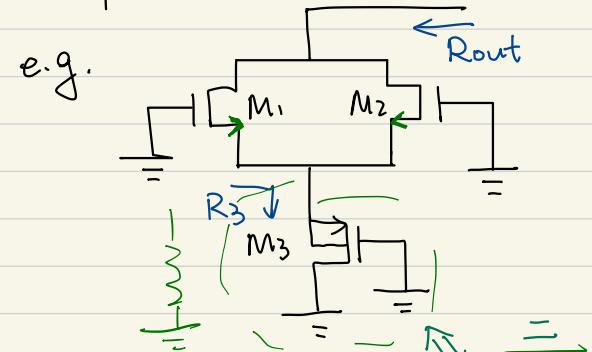
$$G_m = -g_m1 \frac{r_o1}{r_o1 + (r_o2 \parallel \frac{1}{g_m2 \parallel g_{mb2}})}$$

$$R_{out} = [r_o1 + r_o2 + (g_m2 + g_{mb2})r_o1 r_o2] \parallel R_D$$

$$R_{in} = \infty$$

并联 MOS :

e.g.



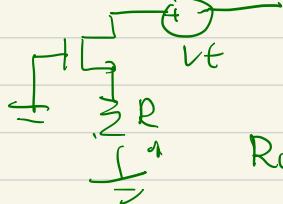
* 两个 MOS 并联:

$$g_m = g_{m1} + g_{m2}$$

$$g_{mb} = g_{mb1} + g_{mb2}$$

$$R_o = R_{o1} // R_{o2}$$

$$R_{out} = ?$$

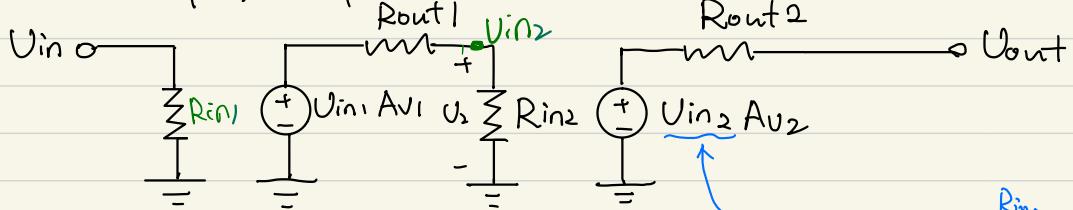


$$R_3 = \frac{1}{g_{m3}} // R_3$$

$$R_{out} = (g_m + g_{mb}) R_o R + R_o + R$$

$$R_3$$

多个 Amplifier 串联:



$$A_V = \frac{V_{out}}{V_{in}} = A_{V1} \cdot \frac{R_{in2}}{R_{out1} + R_{in2}} \cdot A_{V2}$$

$$V_2 = V_{in1} \cdot A_{V1} \cdot \frac{R_{in2}}{R_{out1} + R_{in2}}$$

$$\cdot A_{V2} = V_{out}$$

$$\text{其中 } A_{V1} = G_{m1} \cdot R_{out1}$$

$$A_{V2} = G_{m2} \cdot R_{out2}$$

假設 100 个 Amplifier 连在一起, R_{in} , G_m , R_{out} 均相等

$$A_V = A_{V1} \cdot \frac{R_{in}}{R_{out} + R_{in}} \cdot A_{V2} \cdot \frac{R_{in}}{R_{out} + R_{in}} \cdots A_{V100}$$

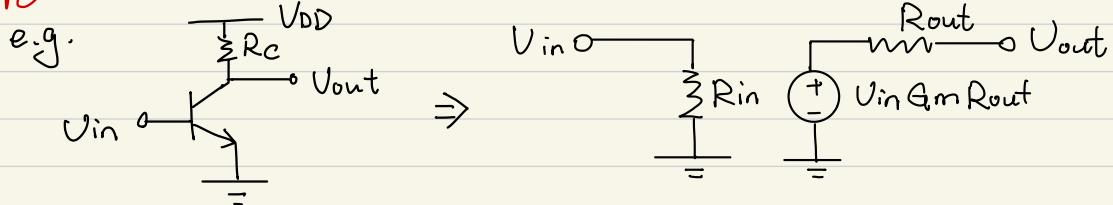
$$= G_m^{100} \frac{R_{out}^{100} \cdot R_{in}^{99}}{(R_{out} + R_{in})^{99}}$$

$$= G_m^{100} (R_{out} \parallel R_{in})^{99} R_{out}$$

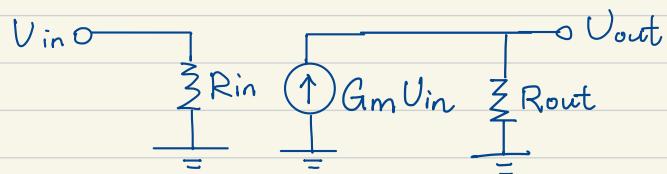
if $R_{in} = \infty$, $A_V = A_{V1} \cdot A_{V2} \cdots A_{V100}$

* **BJT Amplifier**

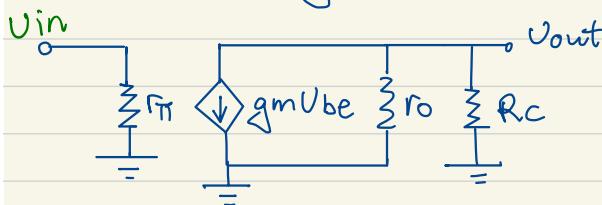
記



equivalent general amplifier model:



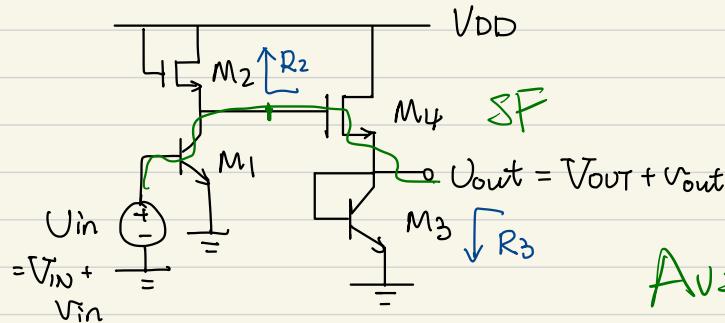
BJT's small-signal model:



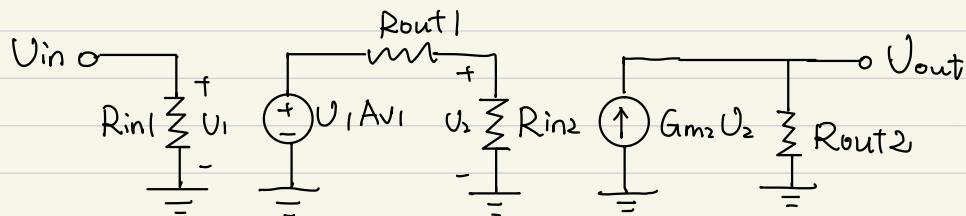
$R_{in} = r_{\pi}$
 $R_{out} = r_o \parallel R_C$
 $G_m = -gm$

$$M_2 : R_{out}$$

Ex. (2020 SU Final Exam)



$$A_V = A_{V1} \cdot \frac{R_{in2}}{R_{out1} + R_{in2}} \cdot A_{V2}$$



Derive analytical expressions for R_{in1} , R_{out1} , A_{V1} , R_{in2} , R_{out2} , G_{m2}

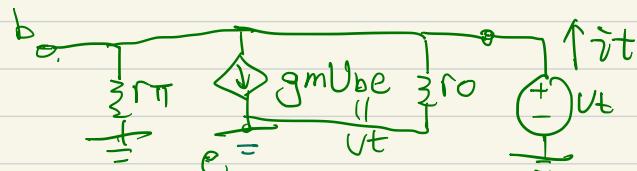
$$R_2 = \frac{1}{g_{m2}} \parallel \frac{1}{g_{mb2}} \parallel \frac{1}{f_02}$$

$$R_{out1} = f_01 \parallel R_2 = f_01 \parallel f_02 \parallel \frac{1}{g_{m2}} \parallel \frac{1}{g_{mb2}}$$

$$R_{in1} = f_1 \parallel 1$$

$$G_{m1} = -g_{m1}$$

$$A_{V1} = G_{m1} \cdot R_{out1} = -g_{m1} (f_01 \parallel f_02 \parallel \frac{1}{g_{m2}} \parallel \frac{1}{g_{mb2}})$$



$$R_3 = \frac{V_t}{i_t} =$$

$$i_t = \frac{V_b}{R_1} + \frac{V_t}{R_2} + g_m V_t$$

$$R_3 = \frac{1}{g_{m3}} \parallel f_03 \parallel \frac{1}{f_3}$$

$$SF: R_{in2} = \infty$$

$$G_{m2} = g_{m4}$$

$$R_{out2} = R_3 \parallel f_04 \parallel \frac{1}{g_{m4}} \parallel \frac{1}{g_{mb4}}$$

Solution:

① 1st stage (M_1)

$$R_2 = \frac{1}{gm_2} \parallel \frac{1}{gm_{b2}} \parallel r_{o2}$$

$$R_{in1} = r_{T1}$$

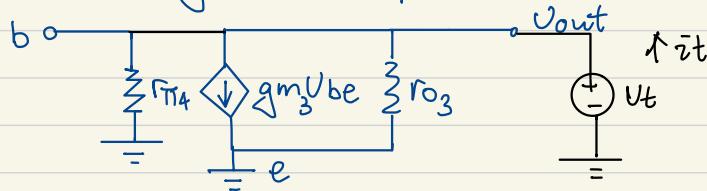
$$R_{out1} = r_{o1} \parallel R_2 = r_{o1} \parallel \frac{1}{gm_2} \parallel \frac{1}{gm_{b2}} \parallel r_{o2}$$

$$Gm_1 = -gm_1$$

$$A_V = Gm_1 \cdot R_{out1} = -gm_1 \cdot (r_{o1} \parallel r_{o2} \parallel \frac{1}{gm_2} \parallel \frac{1}{gm_{b2}})$$

② 2nd stage (M_4)

1° R_3 用 small-signal model 画 (沒有模型可以套):



$$R_3 = \frac{Vt}{it} \quad it = gm_3 Vt + \frac{Vt}{r_{T3}} + \frac{Vt}{r_{o3}}$$

$$R_3 = \frac{1}{gm_3} \parallel r_{T3} \parallel r_{o3}$$

2° M_4 is Source Follower

$$R_{in2} = \infty$$

$$Gm_2 = gm_4$$

$$R_{out2} = r_{o4} \parallel \frac{1}{gm_4} \parallel \frac{1}{gm_{b4}} \parallel R_3$$

$$= r_{o4} \parallel \frac{1}{gm_4} \parallel \frac{1}{gm_{b4}} \parallel \frac{1}{gm_3} \parallel r_{T3} \parallel r_{o3}$$

$$A_V = ?$$