

I) $d \ll r$ $\phi(r, \theta, t) = \frac{1}{4\pi\epsilon_0} \left\{ \frac{q_0 \cos(\omega(t + \frac{r_+}{c}))}{r_+} - \frac{q_0 \cos(\omega(t + \frac{r_-}{c}))}{r_-} \right\}$ (1)

$$r_+ = \sqrt{r^2 - rd \cos \theta + \frac{d^2}{4}} \approx \sqrt{r^2 \left(1 - \frac{d}{r} \cos \theta\right)} = r \sqrt{1 - \frac{d}{r} \cos \theta} =$$

use McLaurin expansion of Small

$$\sqrt{1+x} \approx 1 + \frac{x}{2} - \frac{x^2}{8} + \frac{x^3}{16} \dots ; x = -\frac{d}{r} \cos \theta$$

$$= \left(\text{McLaurin expansion} \right) = r \left(1 + \frac{1}{2} \left(-\frac{d}{r} \cos \theta \right) - \frac{1}{8} \left(-\frac{d}{r} \cos \theta \right)^2 + \frac{1}{16} \left(-\frac{d}{r} \cos \theta \right)^3 \right) \approx r \left(1 + \frac{1}{2} \left(-\frac{d}{r} \cos \theta \right) \right) = r \left(1 - \frac{d}{2r} \cos \theta \right)$$

$$\frac{1}{r_+} = \frac{1}{r \left(1 - \frac{d}{2r} \cos \theta \right)} = \left(\text{McLaurin expansion} \right) \approx \frac{1}{r} \left(1 + \frac{d \cos \theta}{2r} + \left(\frac{d \cos \theta}{2r} \right)^2 + \dots \right)$$

Use McLaurin expansion of

$$\frac{1}{1-x} = 1 + x + x^2 + x^3 \dots ; x = \frac{d \cos \theta}{2r}$$

$$= \frac{1}{r} \left(1 + \frac{d \cos \theta}{2r} \right)$$

