

$$I) d \ll r \quad \phi(r, \theta, t) = \frac{1}{4\pi\epsilon_0} \left\{ \frac{q_0 \cos(\omega(t + \frac{r_+}{c}))}{r_+} - \frac{q_0 \cos(\omega(t + \frac{r_-}{c}))}{r_-} \right\}$$

$$\phi(r, \theta, t) = \frac{q_0}{4\pi\epsilon_0} \left\{ \frac{1}{r} \left( 1 + \frac{d \cos \theta}{2r} \right) \left[ \cos\left(\omega\left(t + \frac{r}{c}\right)\right) \cos\left(\frac{\omega d}{c} \frac{1}{2} \cos \theta\right) - \sin\left(\omega\left(t + \frac{r}{c}\right)\right) \sin\left(\frac{\omega d}{c} \frac{1}{2} \sin \theta\right) \right] - \right.$$

$$\left. - \frac{1}{r} \left( 1 - \frac{d \cos \theta}{2r} \right) \left[ \cos\left(\omega\left(t + \frac{r}{c}\right)\right) \cos\left(\frac{\omega d}{c} \frac{1}{2} \cos \theta\right) + \sin\left(\omega\left(t + \frac{r}{c}\right)\right) \sin\left(\frac{\omega d}{c} \frac{1}{2} \sin \theta\right) \right] \right\}$$

$$= \frac{q_0}{4\pi\epsilon_0} \frac{1}{r} \left\{ \left[ \cos\left(\omega\left(t + \frac{r}{c}\right)\right) \cos\left(\frac{\omega d}{c} \frac{1}{2} \cos \theta\right) - \sin\left(\omega\left(t + \frac{r}{c}\right)\right) \sin\left(\frac{\omega d}{c} \frac{1}{2} \cos \theta\right) - \right.$$

$$\left. - \cos\left(\omega\left(t + \frac{r}{c}\right)\right) \cos\left(\frac{\omega d}{c} \frac{1}{2} \cos \theta\right) - \sin\left(\omega\left(t + \frac{r}{c}\right)\right) \sin\left(\frac{\omega d}{c} \frac{1}{2} \cos \theta\right) \right] +$$

$$+ \frac{d \cos \theta}{2r} \left[ \cos\left(\omega\left(t + \frac{r}{c}\right)\right) \cos\left(\frac{\omega d}{c} \frac{1}{2} \cos \theta\right) - \sin\left(\omega\left(t + \frac{r}{c}\right)\right) \sin\left(\frac{\omega d}{c} \frac{1}{2} \cos \theta\right) + \right.$$

$$\left. + \cos\left(\omega\left(t + \frac{r}{c}\right)\right) \cos\left(\frac{\omega d}{c} \frac{1}{2} \cos \theta\right) + \sin\left(\omega\left(t + \frac{r}{c}\right)\right) \sin\left(\frac{\omega d}{c} \frac{1}{2} \cos \theta\right) \right] \right\}$$

$$= \frac{q_0}{4\pi\epsilon_0} \frac{1}{r} \left\{ - 2 \sin\left(\omega\left(t + \frac{r}{c}\right)\right) \sin\left(\frac{\omega d}{c} \frac{1}{2} \cos \theta\right) + \frac{2d \cos \theta}{2r} \right.$$

$$\left. \cos\left(\omega\left(t + \frac{r}{c}\right)\right) \cos\left(\frac{\omega d}{c} \frac{1}{2} \cos \theta\right) \right\} =$$

$$= \frac{q_0}{4\pi\epsilon_0} \frac{1}{r} \left\{ \frac{d \cos \theta}{r} \cos\left(\omega\left(t + \frac{r}{c}\right)\right) \cos\left(\frac{\omega d}{c} \frac{1}{2} \cos \theta\right) - 2 \sin\left(\omega\left(t + \frac{r}{c}\right)\right) \sin\left(\frac{\omega d}{c} \frac{1}{2} \cos \theta\right) \right\}$$

