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journal homepage: www.elsevier.com/locate/calphad

Assessment of the ternary Fe–Si–B phase diagram

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ARTICLE INFO

Article history:

Received 10 May 2013

Received in revised form

3 August 2013

Accepted 5 August 2013

Available online 24 August 2013

Keywords:

Iron–Silicon–Boron phase diagram

Amorphous metals

Metastable eutectic

Glass transition

ABSTRACT

An improvement of the thermodynamic description of the ternary Fe–Si–B system by means of Calphad method has been carried out in this work considering not only the equilibria involving the stable Fe_2B phase but also the metastable ternary equilibria in which the Fe_3B phase occurs. Furthermore, the glass transition is introduced in the Calphad framework as a second-order one using the tools provided by the Hillert–Jarl formalism of the ferromagnetic transitions not yet applied to Fe–B and Fe–Si–B. The assessments have been made using data available in the literature regarding both the amorphous and crystalline phases. The results improve the previous ones for the glassy phase while keeping the agreement with experimental data concerning stable equilibria.

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1. Introduction

The most recent thermodynamic assessments of the Fe–B and Fe–Si–B glass forming systems were performed, respectively, by Palumbo and Tokunaga [1,2].

Fe–Si–B amorphous alloys are attractive technological materials both for their good magnetic properties and outstanding mechanical behavior [3]. $\text{Fe}_{78}\text{Si}_{13}\text{B}_9$ is one of the commercially available amorphous alloys [4] used as a core material in distribution transformers. A promising application of these materials concerns also the exploitation of their magnetoelastic properties to be employed in sensors [5,6] and bio-sensors [7]. Moreover the properties can be improved by tuning the composition of the alloy with the addition of other elements, therefore this ternary system is an important basis for more complex glass-forming alloys [8]. Examples include FINEMET, a nanocrystalline alloy with good soft magnetic properties obtained by adding to the Fe–Si–B system Copper and Niobium, while amorphous steels [9] are promising non magnetic Bulk Metallic Glasses with exceptional strength.

Amorphous alloys are metastable and it is well known that Fe–Si–B metallic glasses, similarly to binary Fe–B ones, crystallize in two different ways forming a mixture of *bcc* Fe with either the metastable Fe_3B phase or the stable Fe_2B one according to the metalloid content [10]. Moreover it is worthwhile to underline that Fe_3B can nucleate during quenching and competes with the formation of the glass. The ability of the alloy to glass formation is highest in the composition range where a metastable ternary eutectic is supposed to occur [11]. The above reasons motivate the interest in the metastable equilibria of this ternary system exploiting the potential of the Calphad method.

In the literature the most recent assessment of the ternary Fe–Si–B system has been provided, also using own experimental data, by Tokunaga [1] comparing the results with the ternary equilibria found experimentally by Aronsson [12], Efimov [13] and Chaban [14]. Although the issue of glass formation is clearly raised in [1], the metastable Fe_3B phase was not taken into account. On the other hand, Palumbo [2] provided an assessment of the binary Fe–B system comprehensive of both the stable and the metastable phase diagrams involving either Fe_2B or Fe_3B . In this work we propose an improvement of the description of the Fe–Si–B proposed by Tokunaga introducing the metastable Fe_3B compound in the Calphad description of the ternary system.

Furthermore, a treatment of the glass transition has been implemented both in the binary Fe–B and in the ternary Fe–Si–B systems according to the model proposed by Shao [15] where the amorphous phase is described by using the formalism developed by Hillert and Jarl [16] for the ferromagnetic transitions. This model also allows to consider the composition dependence of the glass transition temperature, T_g , and the introduction of experimental data on crystallization in the assessment process. In [2] the glass transition was already treated fixing the T_g at 800 K for every composition while in [1] the glass transition was not dealt with. Shao's model allows, although with some limitations, to model the heat capacity of the undercooled liquid in the region above T_g , reflecting the increase in short range order in the undercooled liquid needed for the formation of the glass.

2. Thermodynamic model

2.1. Solution phases and stoichiometric compounds

Aronsson [12], Efimov [13] and Chaban [14] studied the Fe–Si–B equilibria finding three ternary compounds: $\text{Fe}_5\text{Si}_2\text{B}$, $\text{Fe}_{4.7}\text{SiB}_2$ and

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Table 1

Calculated and experimental thermodynamic properties of intermetallic compounds in the Fe–B system obtained in this optimization and in [2].

Comp.	Property	Reference phase		T (°C)	Calculated (J/mol of atoms)	Palumbo [2] (J/mol of atoms)	Experimental (J/mol of atoms)	Ref.
		Fe	B					
Fe ₂ B	Enthalpy of formation	α	β	25	–20,970	–21,000	–22,300	[46]
	Enthalpy of formation	γ	β	1112	–26,300	–26,344	–22,600	[47]
	Gibbs energy of formation	α	β	900	–25,580	–25,600	–26,000	[48]
	Gibbs Energy of formation	α	β	827	–25,600	–25,600	–26,400	[49]
FeB	Enthalpy of formation	α	β	25	–32,400	–29,600	–35,600	[46]
	Enthalpy of formation	γ	β	1112	–36,400	–33,600	–32,300	[47]
	Gibbs energy of formation	α	β	900	–32,700	–31,600	–31,800	[48]
	Gibbs Energy of formation	α	β	827	–32,940	–31,700	–33,300	[42]
	Enthalpy of fusion	–	–	1590	37,600	38,600	31,600	[50]
	Entropy of formation	–	–	25	17.96 (J/mol of atoms °C)	19.4 (J/mol of atoms °C)	18.1 (J/mol of atoms °C)	[50]
Fe ₃ B	Enthalpy of formation	γ	β	1112	–18,500	–18,300	–17,840	[37]

Fe₂Si_{0.4}B_{0.6}. In this study all these are described as stoichiometric phases expressing their free energy according to the formula

$$G_{\text{Fe}_a\text{Si}_b\text{B}_c}^{\text{ref}} = a {}^0G_{\text{Fe}}^{\text{bcc}} + b {}^0G_{\text{Si}}^{\text{diamond}} + c {}^0G_{\text{B}}^{\beta\text{-rhombohedral}} + \Delta G_{\text{Fe}_a\text{Si}_b\text{B}_c}^f \quad (1)$$

where ${}^0G_{\text{Fe}}^{\text{bcc}}$, ${}^0G_{\text{Si}}^{\text{diamond}}$ and ${}^0G_{\text{B}}^{\beta\text{-rhombohedral}}$ are the lattice stability of the reference state respectively for Fe, Si and B.

The formation energy per mole of unit formula, $\Delta G_{\text{Fe}_a\text{Si}_b\text{B}_c}^f$, is expressed by

$$\Delta G_{\text{Fe}_a\text{Si}_b\text{B}_c}^f = A + BT \quad (2)$$

being A and B the enthalpy and the entropy of formation.

The Gibbs free energy of *fcc* and the *bcc* solid solutions and of the liquid are treated according to the conventional sub-regular solution model

$$G = {}^{\text{ref}}G + {}^{\text{id}}G + {}^{\text{ex}}G \quad (3)$$

$${}^{\text{ref}}G = x_{\text{B}} {}^0G_{\text{B}}^{\phi} + x_{\text{Fe}} {}^0G_{\text{Fe}}^{\phi} + x_{\text{Si}} {}^0G_{\text{Si}}^{\phi} \quad (4)$$

$${}^{\text{id}}G = RT(x_{\text{B}} \ln x_{\text{B}} + x_{\text{Fe}} \ln x_{\text{Fe}} + x_{\text{Si}} \ln x_{\text{Si}}) \quad (5)$$

$${}^{\text{ex}}G = x_{\text{B}}x_{\text{Fe}}\phi_{\text{L,B,Fe}} + x_{\text{Fe}}x_{\text{Si}}\phi_{\text{L,Fe,Si}} + x_{\text{B}}x_{\text{Si}}\phi_{\text{L,B,Si}} + x_{\text{B}}x_{\text{Fe}}x_{\text{Si}}\phi_{\text{L,B,Fe,Si}} \quad (6)$$

where 0G_i denotes the Gibbs free energy of the element i in the ϕ phase, x_i the molar fraction of the element i and R is the gas constant. The excess free energy ${}^{\text{ex}}G$ has been expressed with the Redlich–Kister–Muggianu polynomial and $\phi_{\text{L,A,B}}$, $\phi_{\text{L,A,B,C}}$ (Table 3) stand for the interaction parameters for the binary and ternary systems. The 0G_i has been taken from SGTE data file [17]. A parameter of ternary interaction has been used in the description of the liquid but not for the ternary *fcc* and *bcc* solid solutions.

2.2. Accounting for the glass transition

In the temperature range from the glass transition temperature up to the melting point glass-formers display an excess heat capacity related to ordering at short range in the undercooling regime (expressed by both the associate solution model and the two state model [18,19]). Palumbo [2] proposed to model the glass transition as a second order one; this can be justified by the consideration that the behavior of the extensive and differential thermodynamic properties during it agree with Ehrenfest's classification of thermodynamic transitions [20]. Of course the amorphous phase cannot be considered as sitting in a single minimum in the free energy landscape of a multicomponent system but a wealth of local minima must be envisaged. Therefore, the glass transition temperature depends on the cooling rate and can be better defined as a range of temperatures where the formation of a glassy state occurs. With the aim to build a

Table 2

Enthalpy and temperature of crystallization of the amorphous Fe–Si–B phase calculated in this work and experimental [41–43].

$x(\text{Fe})$	$x(\text{B})$	$x(\text{Si})$	Exp. ΔH (J/mol)	Calc. ΔH (J/mol)	Exp. T_x (°C)	Ref.
0.75	0.1	0.15	5629	5763	548	[41]
0.78	0.13	0.09	7470	7370	542	[42]
0.8	0.18	0.02	6653	6749	493	[41]
0.8	0.16	0.04	7463	8057	515	[41]
0.8	0.12	0.08	7330	7309	538	[41]
0.8	0.1	0.1	6896	7263	539	[41]
0.8	0.14	0.06	7612	7580	532	[41]
0.805	0.173	0.022	6900	6805	487	[43]
0.805	0.129	0.066	8700	8518	517	[43]
0.81	0.106	0.084	7790	7312	537	[43]
0.81	0.085	0.105	7700	7625	527	[43]

Table 3

Assessed parameters of the ternary Fe–Si–B system.

Phase	Parameter (J/mol)	Amorphous phase parameter
Liquid	${}^0L_{\text{B,Fe}}^{\text{L}}$	$-122861 + 14.59T$
	${}^1L_{\text{B,Fe}}^{\text{L}}$	394
	${}^2L_{\text{B,Fe}}^{\text{L}}$	1152
	${}^0L_{\text{B,Fe}}^{\text{L}}$	870
	${}^1L_{\text{B,Fe}}^{\text{L}}$	–2039
	${}^2L_{\text{B,Fe}}^{\text{L}}$	662
	${}^0L_{\text{B,Fe,Si}}^{\text{L}}$	–3483
	${}^1L_{\text{B,Fe,Si}}^{\text{L}}$	$\Omega_0^{\text{B,Fe}}$ 471.06.00
	${}^2L_{\text{B,Fe,Si}}^{\text{L}}$	$\Omega_0^{\text{B,Fe,Si}}$ –77049
		$\Omega_1^{\text{B,Fe,Si}}$ 40437
Fe ₅ SiB ₂	A	–269801
	B	23.59
Fe _{4.7} Si ₂ B	A	–248130
	B	5
Fe ₂ Si _{0.4} B _{0.6}	A	–92665
	B	0.296527778
BCC	${}^0L_{\text{B,Fe}}^{\text{bcc}}$	–33092 + 15.6T
FeB	A	–73933
	B	0.307638889
Fe ₂ B	A	–81226
	B	3.01
Fe ₃ B	A	–77749
	B	2.59

model capable of fitting experimental data in an assessment process, it can be assumed that the ordering in the undercooled liquid occurs until the entropy of the solid phase and that of the liquid are the same (Kauzmann paradox) at the Kauzmann temperature, T_K . Although this temperature point cannot be detected in experiments, it provides a thermodynamic definition of the glass transition temperature. In the framework of CALPHAD a formalism is used since long to represent

second order transitions of the ferromagnetic type. Shao first proposed to employ such formalism as a tool to deal with the amorphous phase in an assessment process and applied it successfully to several systems [21,22]. Also Abe [18] and Palumbo [23] described the glass transition with this model, in association with, respectively, the associate solution model and an excess heat capacity parameter for the undercooled liquid.

In Calphad the ferromagnetic transition is based on the work of Inden [24] who found a good interpolation function of the magnetic contribution to experimental heat capacity C_p^{mag}

$$C_p^{mag} = K^{LRO} \ln\left(\frac{1+\tau^3}{1-\tau^3}\right) \quad \tau = \frac{T}{T_C} \leq 1 \quad (7)$$

$$C_p^{mag} = K^{SRO} \ln\left(\frac{1+\tau^{-5}}{1-\tau^{-5}}\right) \quad \tau = \frac{T}{T_C} > 1 \quad (8)$$

with T_C the Curie temperature and K^{LRO} , K^{SRO} empirically derived constants.

Hillert and Jarl [16] later proposed an expression for the magnetic contribution by a series expansion of Inden formulae according to which the magnetic contribution to free energy, G_{mag} , due to the stabilization of ferromagnetic state with respect to the paramagnetic one is expressed through two interpolation functions, one below and the other above the Curie temperature

$$G_{mag} = RT \ln(\alpha + 1) g(\tau) \quad (9)$$

$$g(\tau) = \left\{ 1 - \left[\frac{79\tau^{-1}}{140p} + \frac{474}{497} \right] \left(\frac{1}{p} - 1 \right) \left(\frac{\tau^3}{6} + \frac{\tau^9}{135} + \frac{\tau^{15}}{600} \right) \right\} / D \quad \tau = \frac{T}{T_C} \leq 1 \quad (10)$$

$$g(\tau) = \left\{ \left(\frac{\tau^{-5}}{10} + \frac{\tau^{-15}}{315} + \frac{\tau^{-25}}{1500} \right) \right\} / D \quad \tau = \frac{T}{T_C} > 1 \quad (11)$$

$$D = \frac{518}{1125} + \frac{11692}{159575} \left(\frac{1}{p} - 1 \right) \quad (12)$$

The value of the function $g(\tau)$ depends on the Curie temperature, T_C , and the parameter p represents the fraction of magnetic enthalpy absorbed above T_C [25]. Its value is structure dependent and was given the value 0.43 for a bcc structure, otherwise it was taken as 0.28.

According to the model proposed by Shao the glass transition temperature is assimilated to the Curie temperature and the free energy difference between the liquid and the amorphous phase as the stabilization due to the ferromagnetic-paramagnetic state. Following the above discussion, here T_C is set at the Kauzmann temperature. The Kauzmann temperature and the α stabilization parameter are obtained through a Redlich-Kister expansion using the PARROT module

$$T_K^{ij} = x_i T_K^j + x^j T_K^i + x^i x^j [\Omega_0^{ij} + \Omega_1^{ij}(x^i - x^j) + \Omega_2^{ij}(x^i - x^j)^2] \quad (13)$$

$$\alpha^{ij} = x_i \alpha^j + x^j \alpha^i + x^i x^j [\Lambda_0^{ij} + \Lambda_1^{ij}(x^i - x^j) + \Lambda_2^{ij}(x^i - x^j)^2] \quad (14)$$

where Ω_v^{ij} and Λ_v^{ij} are the binary interaction parameters to describe the concentration dependence of the stabilization parameter α and T_K .

The values of the stabilization parameter α for the pure elements have been obtained from Eqs. (9)–(11) considering the maximum change in entropy due to the amorphous phase formation

$$\Delta S^{liquid-amo} = -R \ln(1 + \alpha) \quad (15)$$

approximating the maximum change in entropy of pure components with the entropy of melting while T_K of pure elements is approximated as $T_K = 0.25 T_m$. Data on and correlations of the Kauzmann temperature of several amorphous alloys with the glass transition temperature and other thermophysical parameters have

been recently collected for inorganic, organic and metallic glasses [26]. A relationship between T_K and T_g can be proposed as $T_K = 0.8 T_g$. This average value disregards differences in glass forming ability and glass stability of different substances. It, however, provides a simple estimate for T_K and will be justified *a posteriori* by the results of assessment.

The choice of the p parameter in the ferromagnetic formalism influences the shape of the heat capacity and weights the relative importance of the two interpolation function $g(\tau)$ below and above T_C : an high value of p means enhancing the role of the function that expresses the heat capacity above T_C . In our study the value of p is set to 0.99 to exploit the influence of this parameter on the shape of the heat capacity curve with an abrupt jump at the glass transition. In Fig. 1 supposed heat capacity, C_p , curves of a binary Fe₈₀B₂₀ system for the liquid-amorphous state according to Shao's model are shown for different values of p : 0.28, as in a generic ferromagnetic transition, $p = 0.43$, for a ferromagnetic transition in a bcc structure, $p = 0.6$, as used by Shao and $p = 0.99$, as used in this work.

In the binary and ternary system optimized in this study the amorphous phase has been introduced using as experimental data the enthalpy of crystallization ΔH_x . This quantity refers to the difference of enthalpy between amorphous and crystalline phases at T_x , the crystallization temperature. Considering the heat capacity of the amorphous phase equal to that of the crystal phase between T_x and T_K we associated the experimental ΔH_x to the calculated Kauzmann temperature.

3. Optimized results and discussion

3.1. Fe–B, Si–B and Fe–Si binary systems

The thermodynamic parameters for the binary Fe–Si and Si–B systems were taken from [27] and [28], respectively. The Fe–B system has been assessed several times [2,29–31,34], however the amorphous and metastable phases have been treated only by Palumbo [2] although without resorting to Shao's model for the former. Recently, this work has been used as a starting point to predict the devitrification kinetics of amorphous steel [35]. The Fe–B system used here derives from [2] employing Shao's model of the glass transition. In the literature the equilibria between Fe₂B, FeB and liquid in the region near the Fe₂B boride have been thoroughly discussed. Some authors [36] proposed the occurrence of a eutectic reaction between FeB and Fe₂B at $x_B = 0.38$ while most of the optimizations [2,29–31] of the binary system have been done considering a peritectic, although the results look uncertain because of the closeness in the free energy of the phases. The work by Palumbo has been reassessed not only introducing the amorphous phase through the Shao model but also trying to obtain a clear peritectic behavior of Fe₂B re-assessing the parameters for the liquid, FeB, bcc solid solution and Fe₃B using as experimental data those given in Table 1 and the Fe enthalpy of mixing from [50]. In [2] the amorphous phase has been introduced by operating on the interaction parameter of the liquid at the same Kauzmann temperature for all compositions: below T_K the parameter relates to the amorphous phase with no excess contribution to the heat capacity; above T_K the undercooled liquid is described with an excess coefficient for the heat capacity. The parameters of the liquid and the amorphous phases were linked considering the glass transition as a second order transition. In our work the parameters for the liquid have been re-assessed by treating the undercooled liquid according to the model by Shao and accounting for a composition dependence of T_K . The stabilization parameter of the amorphous phase has been obtained, by means of the PARROT module, using the heats of crystallization.

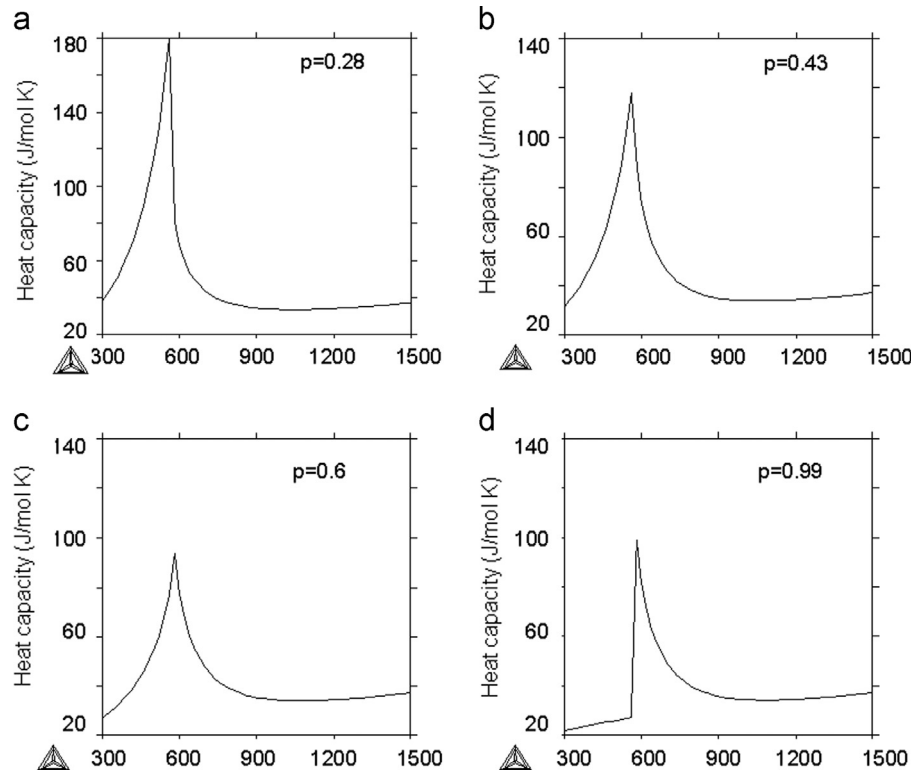


Fig. 1. Heat capacity trend of a binary liquid $\text{Fe}_{80}\text{B}_{20}$ alloy according to Shao's model with different values of the p parameter.

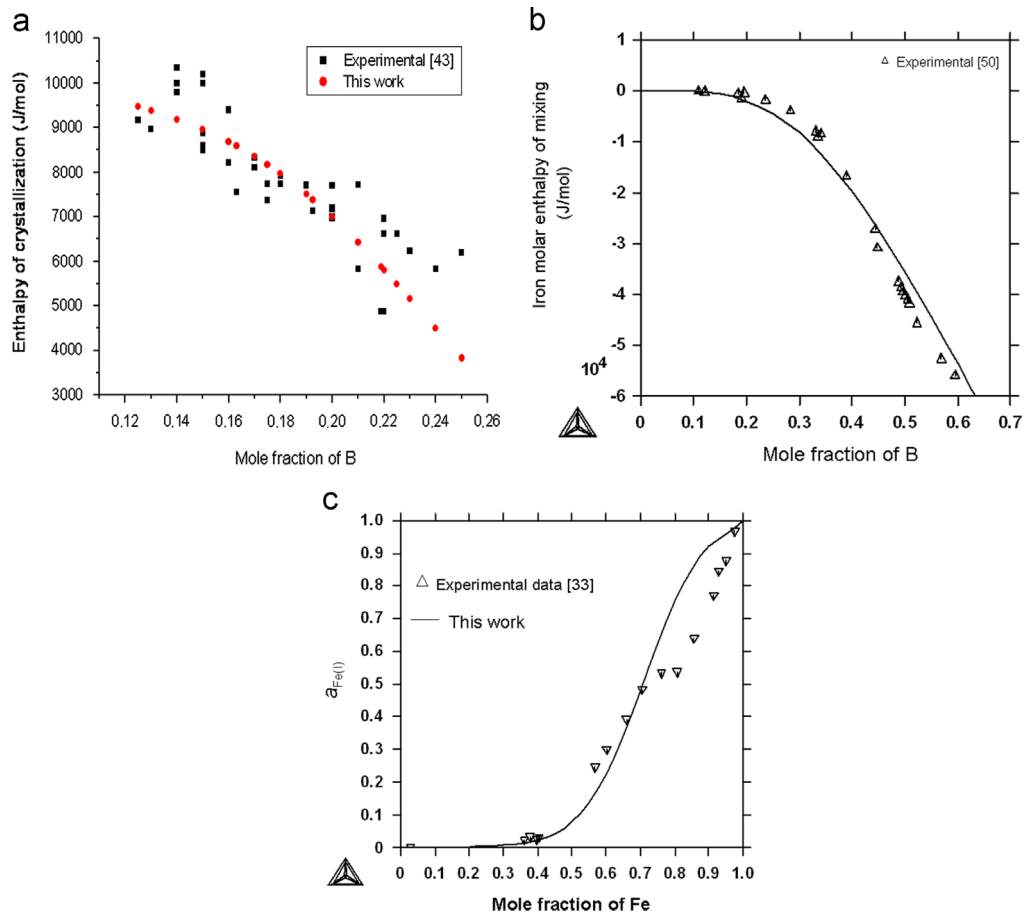


Fig. 2. Heats of crystallization of Fe-B amorphous alloys (a), partial molar enthalpy of mixing of Fe at 1677 °C (b) and activity of Fe in the liquid at 1600 °C [33] (c).

In Fig. 2 and in Fig. 3 results of the re-assessment are presented: in Fig. 2a the calculated and experimental heat of crystallization versus composition are shown; we can see that the calculated data reproduce the trend of the experimental value within the scatter. Also the mixing properties in the liquid phase are in good accordance with the experimental data [32] as shown in Fig. 2b where the calculated and experimental partial molar enthalpies of Fe as a function of x_B are shown. The thermodynamic properties of the liquid at high temperature obtained in this re-assessment are compared in Fig. 2c with the activity of Fe in the Fe–B liquid at 1600 °C determined by Miki et al. [33]; at x_{Fe} higher than 0.7 our assessment overestimates the experimental values similarly to [33], while at lower Fe content the agreement is good. The binary phase diagrams, both stable and metastable are shown in Fig. 3a and b. They are in good accordance with the previous one. In Table 1 the calculated and experimental thermodynamic properties used in the optimization in comparison with the results obtained by Palumbo [2] are given. In our assessment the eutectic between Fe_2B and fcc Fe has been found at $x_B=0.176$ and 1166 °C, very close to the experimental data obtained in [37] ($x_B=0.170$ and 1164 °C). The peritectic equilibrium between Fe_2B , liquid and FeB has been obtained at 1383 °C and $x_B=0.333$ closer to the experimental data obtained by [38] ($x_B=0.325$ and 1389 °C) than that in [39] ($x_B=0.333$ and 1410 °C). The metastable eutectic between

Fe_3B and fcc Fe has been obtained at $x_B=0.188$ and 1393 °C close to the experimental data obtained in [37] ($x_B=0.186$ and 1114 °C).

3.2. Optimization of the ternary Fe–Si–B phase diagram

The Fe–Si and Si–B binaries are taken, respectively, from the work of [27] and [28] in addition to the binary Fe–B just obtained. In the assessment procedure we optimized the parameters relative to the ternary compounds Fe_5Si_2B , $Fe_{4.7}SiB_2$ and $Fe_2Si_{0.4}B_{0.6}$ and those relative to the ternary interaction parameter of the liquid. The experimental data used are the DSC melting temperatures provided by Tokunaga, the activity measured by Zaitsev [40] and some our DSC data (Table 4). The aim of this initial optimization procedure is to obtain the stable ternary phase diagram which results comparable to that obtained by Tokunaga as shown in the isothermal section at 1000 °C (Fig. 4); we just find a smaller two phase $Fe_2Si_{0.4}B_{0.6}$ –bcc region with respect to [1]. A good accordance has been obtained also in the isopleth at $x_B=0.10$ where DSC data were available from Tokunaga, as can be seen in Fig. 5a. On the other hand the section at $x_{Fe}=0.65$ (Fig. 5b) at low silicon content is quite different with respect to [1], for concentrations up to $x_{Si}=0.15$: a better description of the liquidus points has been obtained whereas the differences with respect to experimental DSC points regarding the solidus are higher. In Fig. 5c the section at $x_{Fe}=0.80$ is shown together with our DSC data: also in this region a good fit to the experimental data has been achieved. In Fig. 6 the calculated and experimental enthalpy of mixing of liquid are presented at $x_B=0.25$ and 1650 °C. The agreement is reasonable up to $x_{Si}=0.20$ whereas a larger deviation is found at higher silicon content.

Once the parameters for representing the ternary phase equilibria have been obtained, we introduced the Shao's model for the amorphous and undercooled liquid and optimized the α and T_K

Table 4
Experimental DSC data of the Fe–Si–B (heating rate 10 K/min).

Composition	Transf.	T (°C)	ΔH (J/mol)
$Fe_{78}Si_{2}B_{20}$	Eutectic	1166	15666
	Liquidus	1289	
$Fe_{80}Si_{15}B_{15}$	Melting	1168.5	16293
$Fe_{80}Si_{7.5}B_{12.5}$	Eutectic	1144	14892
	Liquidus	1272	
$Fe_{80}Si_{10}B_{10}$	Eutectic	1148	13384
	Liquidus	1236	

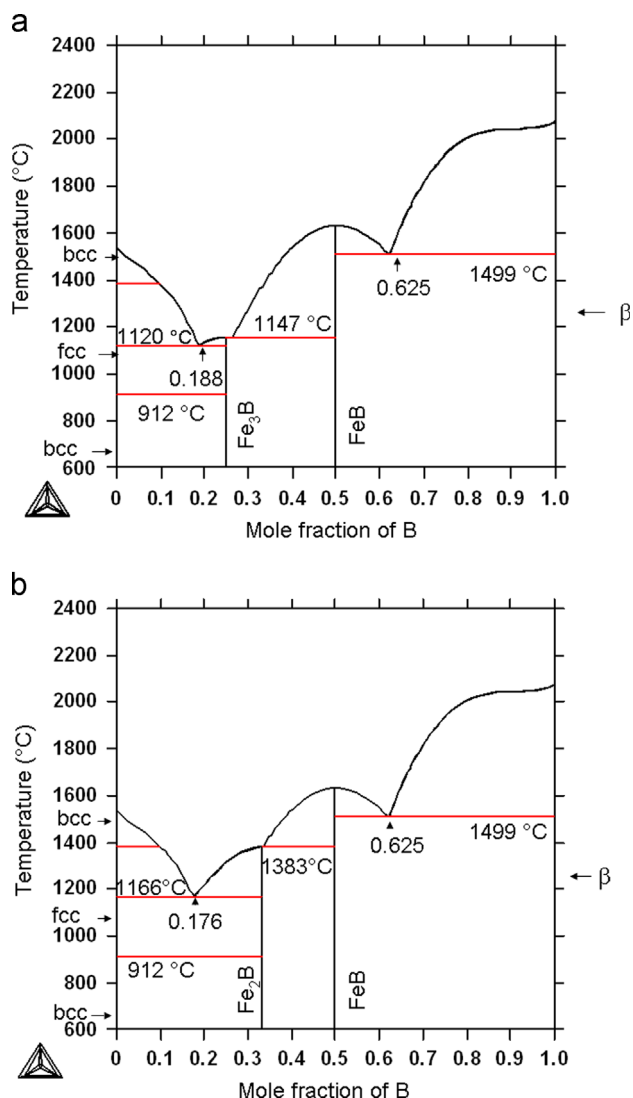


Fig. 3. Optimized metastable (a) and stable (b) Fe–B phase diagrams.

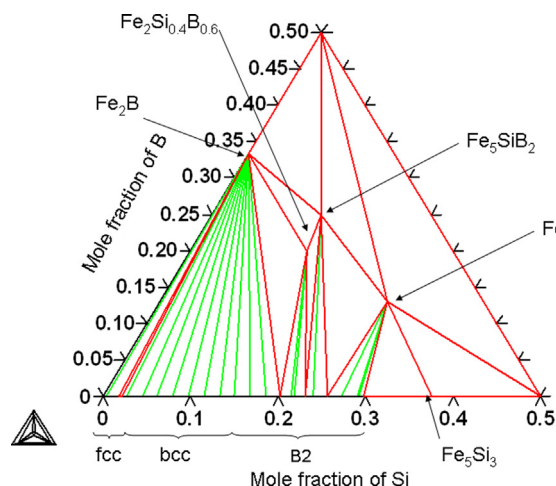


Fig. 4. Isothermal section of the stable Fe–Si–B phase diagram at 1000 °C.

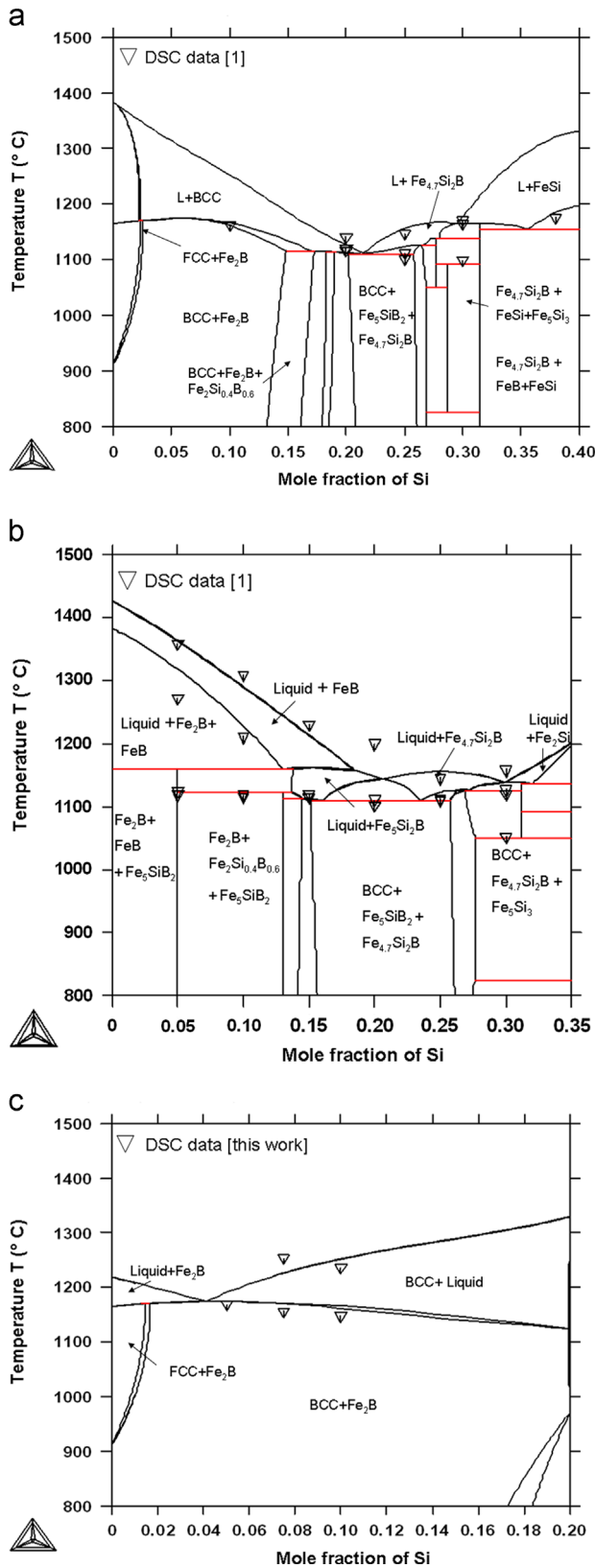


Fig. 5. Calculated isopleths at $x_B=0.10$ (a), at $x_{Fe}=0.65$ (b) with DSC data by [1]. Isopleth at $x_{Fe}=0.80$ (c) with our DSC data.

parameters (Eqs. (13) and (14)) as above on the basis of experimental data of the heats and temperatures of crystallization [41–43]. For this step accounting for the Fe_3B phase is important because of its occurrence as a product of crystallization.

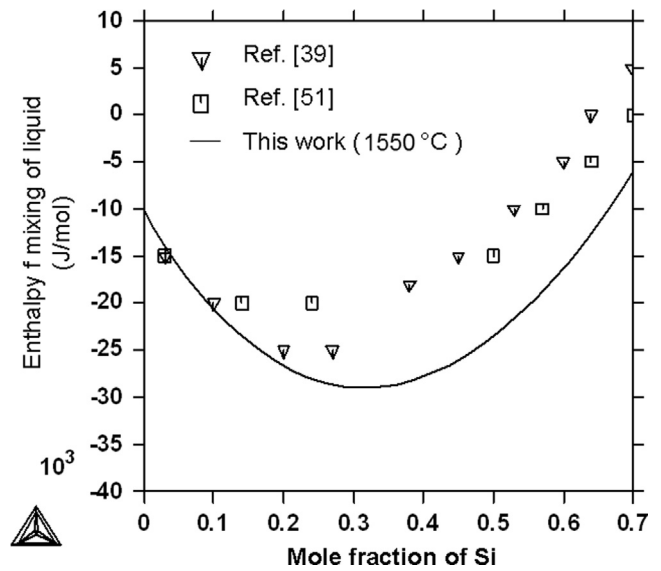


Fig. 6. Enthalpy of mixing of the liquid at $x_B=0.25$ and 1550 °C and experimental data (reference for boron is β rhombohedral).

For the Fe–Si–B system there is complete lack of experimental data on the heat capacity in the undercooled liquid region and also the glass transition temperature has never been detected because it is preceded by the crystallization of the amorphous phase. Therefore, the Kauzmann temperature has been approximated as in the case of the Fe–B system, using the temperature of crystallization T_K i.e. $T_K=0.8 T_x$. Only in quaternary Fe–Al–Si–B alloys glass transition is detectable and the heat capacity for the $Fe_{65}Al_{7}B_{18}Si_{10}$ composition has been measured [44]. A value of C_p^{Liquid} of 43.4 J/mol °C has been obtained at 572 °C in the undercooling regime; the calculated value of C_p^{Liquid} for the $Fe_{72}B_{18}Si_{10}$ alloy at the same temperature in this work is 49.9 J/mol °C, of the same order of the experimental value. Since in most alloys crystallization occurs as a two steps process to a *bcc* solid solution first and a compound at higher temperature, the use of the heat of crystallization in the assessment required special care. Two procedures were attempted to obtain the heats of crystallization

- in the first one we tried to calculate the partial heats of crystallization associated to each step relating them to the respective DSC peak temperature and
- in the second one the overall heat of crystallization was computed assuming an average crystallization temperature in between the two DSC peaks, in view also of the relative proximity of the two peaks.

Although the first procedure would be conceptually more satisfactory, it was not possible to obtain a reasonable fit of the partial heat of crystallization, therefore, we resolved to employ the latter procedure.

In Table 2 calculated and experimental heat of crystallization are given for ternary alloys with variable amount of Fe; in general the accordance between experimental and calculated data are good and differences are mostly within 600 J/mol, i.e. close to the scatter for experimental points. It is important to note that the introduction of the amorphous phase does not change the description of equilibria at high temperature, infact the ternary phase diagrams shown in Figs. 4 and 5 refer to the case where the amorphous phase has already been considered.

The predicted metastable Fe–Si–B phase diagram, obtained by suspending the Fe_2B phase, is shown in Fig. 7 for the isothermal section at 1000 °C.

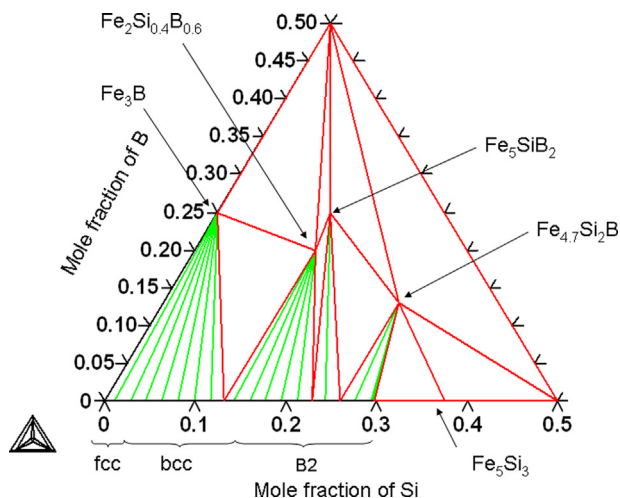


Fig. 7. Isothermal section of the metastable ternary Fe-Si-B phase diagram at 1000 °C.

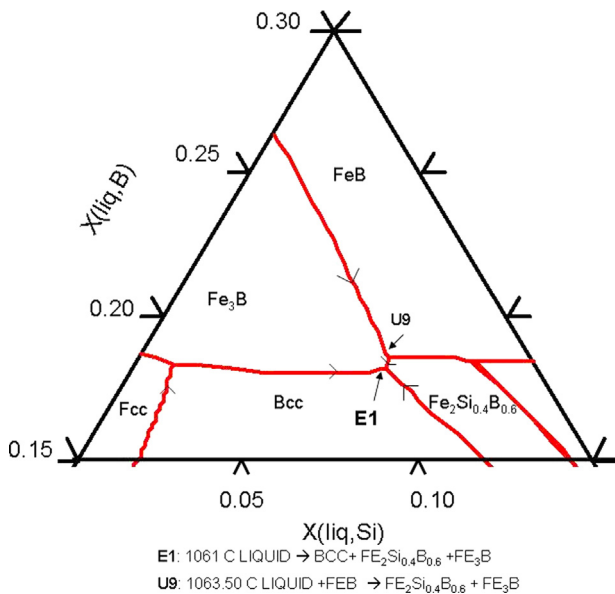


Fig. 8. Liquid surface projection of the metastable Fe-Si-B system in the zone near the ternary eutectic (E1).

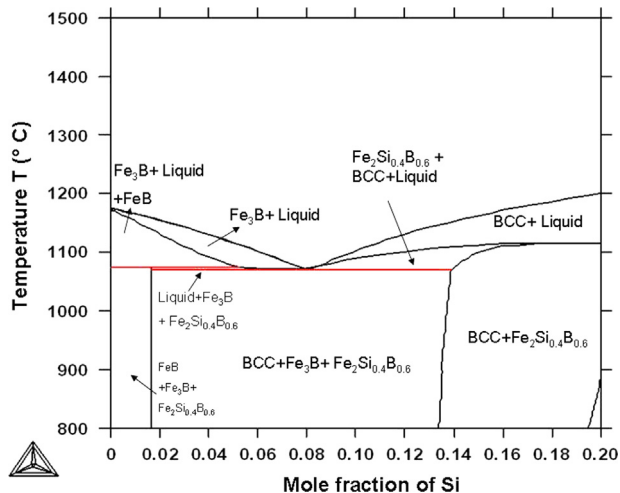


Fig. 9. Calculated isopleth at $x_{Fe}=0.74$ where the ternary metastable eutectic is evidenced at 1061 °C, $x_B=0.18$ and $x_{Si}=0.08$.

The metastable eutectic of the ternary Fe-Si-B is evidenced in the liquid surface projection of Fig. 8; the region around it is expected to correlate with the easy glass formation by rapid quenching. Actually Hagiwara [45] studied the critical ribbon thickness of Fe-Si-B in a wide range of concentrations finding higher values along the 25% line with 14–19% of B. Fig. 9 shows the isopleth at $x_{Fe}=0.76$ comprising the ternary eutectic which occurs at the concentration $Fe_{74}Si_8B_{18}$.

4. Conclusions

This paper improves previous assessments of Fe-B and Fe-Si-B systems on two grounds

- the liquid C_p down to the glass transition has been modeled by means of Shao's model with a dependence on both temperature and concentration contrary to [1] and [2],
- the metastable Fe_3B compound, a major product of glass crystallization, has been introduced in both binary Fe-B and ternary Fe-Si-B systems.

The main results of this work are

- the metastable equilibria involving the Fe_3B phase in the ternary system have been established finding the ternary metastable eutectic in a concentration range where the highest glass formability has been reported in literature,
- the thermodynamic quantities (partial molar enthalpy of mixing, heat of mixing, heat of crystallization) are well reproduced and the functional shape of the liquid C_p curve has been adopted to the actual trend down to T_g by tuning the p parameter of Shao's model.

Acknowledgments

This work has been performed in the frame of the EU-7FP project 'ACCMET'.

Appendix A. Supporting information

Supplementary data associated with this article can be found in the online version at <http://dx.doi.org/10.1016/j.calphad.2013.08.001>.

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