# Class Design for Siena 4

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#### 1. Introduction

The purpose of this document is to give an overview of the C++ code for Siena 4. Some notes:

- Names in the code are indicated as name.
- Typewriter font is used for file names, like FileName.cpp.
- Normally, a class named *SomeName* is declared in the file SomeName.h and implemented in the file SomeName.cpp.
- Camel case is used for names of classes, methods, and variables. More specifically, all names but class names start with a lower case letter, and when the name consists of several words, each of the subsequent words starts with an upper case letter. Examples:
  - StatisticCalculator a class name
  - calculateNetworkRateStatistics a method name
  - observationCount a variable name
- The names of pointer variables start with a 'p' followed by an upper case letter, like *pNetworkData*.
- Similarly, the names of reference variables start with an 'r', like in the following declarations of a copy constructor and an assignment operator:

```
Network(const Network & rNetwork);
Network & operator=(const Network & rNetwork);
```

- Moreover, the names of instance variables are prepended with an 'l', e.g.
  - int lobservationCount an instance variable of a non-pointer type,
  - Model \* lpModel an instance variable of a pointer type.

## 2. Library Overview

The code is organised into libraries that correspond to the directory names under **src**. The libraries are briefly explained in the following list in the order of their dependencies, namely, no library depends on any other library listed after it.

- utils contains various general purpose classes and functions.
- network contains the classes Network and OneModeNetwork for storing and manipulating directed two-mode and one-mode networks, respectively, as well as supporting classes like various iterators over ties in a network.
- data contains everything related to the observed data with the class *Data* being the main container storing the observations of network and behavior variables, covariates, etc.
- model contains the tools for specifying and simulating actor-oriented models. The *Model* class can be used to specify an actor-oriented model, which can be subsequently simulated with respect to a specific *Data* object by using an instance of the *EpochSimulation* class. Finally, the *StatisticCalculator* class provides the means for calculating the observed or simulated statistics for effects in the model.

In the next sections, each library is explained in some detail.

# 3. Utils

- Utils.h provides miscellaneous utility functions, macros, and classes.
- Random.h provides functions for drawing random numbers.
- The class NamedObject acts as a base class for anything that has a name.
- The singleton class SqrtTable is used throughout the system to calculate square roots of integers efficiently. Once the root of an integer is calculated, it is stored in a table for later reuse. Example:

```
SqrtTable * pTable = SqrtTable::instance();
double root2 = pTable->sqrt(2);
```

#### 4. Networks

#### 4.1 Network class

The Network class implements directed two-mode networks with valued ties. The number of tie senders n and the number of tie receivers m have to be provided at the construction of a network. Technically, the Network class can be used for storing one-mode networks as well, in which case n=m, however, the derived class OneModeNetwork is recommended for this purpose.

## 4.1.1 Internal Data Representation

The outgoing ties of each sender i are stored in an STL (C++ Standard Template Library) map. The alters of non-zero ties from i act as keys in the map, and the tie values are stored in the map as values corresponding to those keys. The maps themselves are stored in an array lpOutTies, hence the value of a tie (i, j) can be accessed as lpOutTies[i][j]. Similarly, an array of maps lpInTies is used to store the incoming ties of all receivers.

While being much more memory efficient than storing the adjacency matrix of a network explicitly, this representation still provides fast queries of tie values – the number of steps necessary to retrieve the value of a tie (i, j) is

proportional to the logarithm of the out-degree of i. Also, this representation directly provides a fast and convenient way of iterating over all non-zero ties of an actor in the increasing order of the alters.

The users of the *Network* class should not care about its internal representation, though, and use the public interface methods, to which we now turn.

#### 4.1.2 Interface

Some of the more important methods of the *Network* class are explained in the following list.

- Network(int n, int m) constructs a network with n senders, m receivers, and no ties.
- int n() returns the number of actors in the set of tie senders.
- int m() returns the number of actors in the set of tie receivers.
- void setTieValue(int i, int j, int v) sets the specified value of the tie (i, j).
- int tieValue(int i, int j) returns the value of the tie (i, j).
- *Tielterator ties*() returns an iterator over all ties of the network. The ties are ordered according to their senders from smallest to largest, and the ties from the same sender are ordered according to their receivers.

Usage:

```
TieIterator iter = pNetwork->ties();
while (iter.valid())
{
  int ego = iter.ego();
  int alter = iter.alter();
  int value = iter.value();

cout << "The tie from " << ego << " to " << alter <<</pre>
```

```
" has a value " << value << endl;

// Move on to the next tie
  iter.next();
}</pre>
```

 IncidentTielterator outTies(int i) – returns an iterator over the outgoing ties of actor i in the increasing order of the alters.
 Usage:

```
IncidentTieIterator iter = pNetwork->outTies(i);
while (iter.valid())
{
  int alter = iter.actor();
  int value = iter.value();

  cout << "The tie from " << i << " to " << alter << " has a value " << value << endl;

  // Move on to the next tie
  iter.next();
}</pre>
```

- Incident Tielterator in Ties (int i) returns a similar iterator over the incoming ties of actor i.
- int outDegree(int i) returns the number of non-zero outgoing ties for actor i.
- int inDegree(int i) returns the number of non-zero incoming ties for actor i.

#### 4.2 Iterators

We have already seen the usage of supporting classes *Tielterator* and *IncidentTielterator*. Another iterator class, namely *CommonNeighborlterator*, provides convenient means for iterating over actors that are common to two instances of *IncidentTielterator*. For example, one can iterate over reciprocated ties of an actor in a one-mode network as follows:

```
CommonNeighborIterator iter(pNetwork->inTies(i),
    pNetwork->outTies(i));
while (iter.valid())
{
    int neighbor = iter.actor();
    cout << "There is a reciprocated tie from " << i <<
        " to " << neighbor << endl;

    // Move on to the next neighbor
    iter.next();
}</pre>
```

#### 4.3 OneModeNetwork class

A one-mode network can be thought of as a special case of a two-mode network, where the set of tie senders coincides with the set of tie receivers. Hence, the *OneModeNetwork* class is derived from the *Network* class. In addition to the interface inherited from the base class, it maintains the number of reciprocated ties per each actor and provides various methods for counting two-paths in a network. A non-exhaustive list of methods follows:

- OneModeNetwork(int n, bool loopsPermitted) constructs an empty network for n actors. Ties from actors to themselves (which are called loops) can be explicitly forbidden by providing the value false as the second argument.
- int reciprocalDegree(int i) returns the number of reciprocated ties of actor i.
- CommonNeighborIterator reciprocatedTies(int i) returns an iterator over all reciprocated ties of actor i. The usage is similar to that of the method Network::outTies(int i) except that the class CommonNeighborIterator does not have a value() method. In a sense, the network is treated as a boolean network, where the existence/non-existence of ties is of interest, but not the actual values of ties.

• int twoPathCount(int i, int j) – returns the number of two-paths from actor i to actor j.

#### Observed Data

The data library contains classes for storing the observed data subject to actor-oriented modeling. The entire set of observed data for a Siena project (or one group in a multi-group project) should be stored in an instance of the *Data* class. It owns collections of more specific data objects like those storing the observed data for dependent network variables, constant actor covariates, etc. This section will guide you step-by-step through the process of populating a *Data* object. To begin with, an instance of the *Data* class should be created:

```
int observationCount = 4;
Data * pData = new Data(observationCount);
```

Note that the number of observations has to be provided in the very beginning.

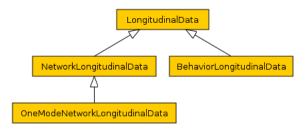
# 5.1 Actor Sets

There may be several sets of actors involved, like a set of students, a set of teachers, and a set of courses, therefore, when specifying dependent variables and covariates, one should be explicit about the relevant actor sets. Each set of actors is represented in the system by an instance of the ActorSet class, which can be created with the factory method Data::createActorSet by providing the name of the set and the number of actors in it.

```
const ActorSet * pStudents =
  pData->createActorSet("students", 50);
const ActorSet * pCourses =
  pData->createActorSet("courses", 20);
```

# 5.2 Observed Data for Dependent Variables

There is a small hierarchy of classes for storing the observed data for dependent variables.



The base class *LongitudinalData* is not supposed to be created directly, however, it provides some useful methods applicable to observed data of all types of dependent variables:

- const ActorSet \* pActorSet() returns the set of actors this dependent variable is defined for.
- int n() returns the size of the set of actors.
- int observationCount() returns the number of observations that can be stored in this data object.
- bool upOnly(int period) returns if only upward changes are observed in the given period.
- void upOnly(int period, bool flag) stores the indicator if only upward changes are observed in the given period. Note that the LongitudinalData class provides just the storage of these flags, and their values have to be computed elsewhere. They are currently passed in from the R part of the system.
- downOnly similar accessor methods for flags indicating that only downward changes are observed.

The derived classes of *LongitudinalData* are created with the factory methods of the *Data* class by providing the name of the variable and the corresponding actor set (or both the set of tie senders and the set of tie receivers in the case of two-mode networks):

one-mode networks

```
OneModeNetworkLongitudinalData * pFriendshipData =
   pData->createOneModeNetworkData("friendship",
        pStudents);
```

• two-mode networks

```
NetworkLongitudinalData * pCourseSelectionData =
   pData->createNetworkData("courses",
        pStudents,
        pCourses);
```

behavior

```
BehaviorLongitudinalData * pAverageGradeData =
   pData->createBehaviorData("grade", pStudents);
```

#### 5.2.1 Two-Mode Network Variables

**Network Structure.** The main purpose of the *NetworkLongitudinalData* class is to store the values of network ties in each of the observations as well as indicators about whether a tie value is missing or structurally determined. This can be done with the following setter methods:

- void *tieValue*(int *i*, int *j*, int *observation*, int *value*) stores the value of the tie between the given actors at the given observation,
- void *missing* (int *i*, int *j*, int *observation*, bool *flag*) stores if the value of the tie between the given actors is missing at the given observation.
- void *structural*(int *i*, int *j*, int *observation*, bool *flag*) stores if the value of the tie between the given actors is structurally determined at the given observation.

There is a corresponding set of methods for accessing the stored values:

• int *tieValue*(int *i*, int *j*, int *observation*)

- bool *missing*(int *i*, int *j*, int *observation*)
- bool *structural*(int *i*, int *j*, int *observation*)

Internally, this information is stored in three arrays of networks, namely, Inetworks for the observed tie values, Imissing TieNetworks for indicators of missing ties, and IstructuralTieNetworks for storing the indicators of structurally determined ties. To enable effective iteration over all ties, the class NetworkLongitudinalData provides constant access to these networks via the following methods:

- const Network \* pNetwork(int observation) returns the network of observed values at the given observation,
- const Network \* pMissingTieNetwork(int observation) returns the network of missing tie indicators for the given observation,
- const Network \* pStructuralTieNetwork(int observation) returns the network of structural tie indicators for the given observation.

For example, the following code snippets demonstrate two ways of iterating over the selected courses of a certain student i, but the second snippet is much more efficient.

```
Example 1
```

```
for (int j = 0; j < pCourses->n(); j++)
{
  if (pCourseSelectionData->tieValue(i, j, observation) != 0)
  {
    cout << "The student " << i <<
        " has selected the course " << j << endl;
  }
}</pre>
```

Example 2

```
const Network * pNetwork =
   pCourseSelectionData->pNetwork(observation);

IncidentTieIterator iter = pNetwork->outTies(i);

while (iter.valid())
{
   int j = iter.actor();
   cout << "The student " << i <<
       " has selected the course " << j << endl;
   iter.next();
}</pre>
```

Calculating Properties. Once a network data object has been populated, it is important to call the *calculateProperties* method that computes important properties of the observed data, which are used by some effects during model simulations:

```
pCourseSelectionData->calculateProperties();

cout << "The average number of courses per student is " <<
   pCourseSelectionData->averageOutDegree() << endl;
cout << "The average number of students " <<
   "attending a course is " <<
   pCourseSelectionData->averageInDegree() << endl;</pre>
```

## Other Methods.

• void maxDegree(int degree) – if there is a restriction on the maximum number of outgoing ties an actor can have, it has to be specified by using this method.

## 5.2.2 One-Mode Network Variables

Since one-mode networks are a special kind of two-mode networks, the class OneModeNetworkLongitudinalData derives from NetworkLongitudinalData and inherits all its methods. The derived class provides some additional methods, though, which are applicable to one-mode networks only:

- void symmetric(bool flag) stores if the network is symmetric,
- void balanceMean(double value) stores the centering constant for the balance effect.

Some of the information that is simply stored in the OneModeNetworkLongitudinalData class could be computed by the class itself, but since this information is already computed in R, we save the effort of computing it again, and simply pass the values in from the R part of the system.

#### 5.2.3 Behavior Variables

Analogous to the data class for network variables, the class BehaviorLongitudinalData stores the observed values of a certain behavior variable and various properties computed from the observed data.

**Observed Values.** The observed values or indications about missing values can be stored with the following methods:

- void value(int observation, int actor, int value)
- void missing(int observation, int actor, bool missing)

The stored values can be accessed with these methods:

- int value(int observation, int actor)
- bool missing(int observation, int actor)

Internally, the observed values are stored in an  $M \times N$  integer array *lvalues* and the missingness indicators are stored in an  $M \times N$  boolean array *lmissing*, where M is the number of observations and N is the number of actors in the corresponding actor set. A read-only access to a whole row of the matrix of values (namely, the values of all actors in a single observation) is provided by the method

• const int \* values(int observation).

Calculating Properties. Again, as soon as the observed values and missingness indicators are stored, and before the data object can be used for model simulations, the method *calculateProperties* should be called:

```
pAverageGradeData->calculateProperties();
```

```
cout << "The average grades of students range from " <<
   pAverageGradeData->min() << " to " <<
   pAverageGradeData->max() << endl;</pre>
```

The method *calculateProperties* calculates some properties of the observed data, which can be subsequently queried with the following methods:

- int min() returns the smallest observed non-missing value,
- int max() returns the largest observed non-missing value,
- int range() returns the range of observed non-missing values, which is simply the difference between the maximum and the minimum values,
- double overallMean() returns the overall mean of the observed non-missing values defined as  $\frac{1}{M} \sum_{k=1}^{M} \frac{\sum_{i \in A_k} v_i^k}{|A_k|}$ , where  $v_i^k$  is the observed behavior for actor i and the observation k and  $A_k$  is the set of actors with non-missing values at the observation k.

### Other Methods.

- void similarityMean(double similarityMean) stores the mean similarity of actor behavior values over all observations, which is calculated in R.
- double similarity (double a, double b) returns the centered similarity score for the given values a and b. The similarity score is defined as  $1 \frac{|a-b|}{\Delta}$ , where  $\Delta$  is the observed range of the behavior variable, and the mean similarity is subtracted from this expression to obtain the centered similarity score.

#### 5.3 Covariates

The classes for storing actor covariates and dyadic covariates are organised in two separate hierarchies:



Since the usage of covariate classes is very similar to that of observed data for behavior variables, we will just briefly list the main methods for working with covariates.

The covariate data classes can be created by the factory methods of the *Data* class:

- ConstantCovariate \* createConstantCovariate(...)
- ChangingCovariate \* createChangingCovariate(...)
- ConstantDyadicCovariate \* createConstantDyadicCovariate(...)
- ChangingDyadicCovariate \* createChangingDyadicCovariate(...)

The name of the covariate and one (for actor covariates) or two (for dyadic covariates) actor sets should be provided as parameters for these methods.

#### 5.3.1 Actor Covariates

The base class *Covariate* for actor covariates provides the following methods:

- void range(double range) stores the observed range of the covariate. Unlike the observed data for behavior variables, it is not computed by the covariate class itself, but passed in from R.
- double range() returns the observed range of the covariate.
- similarityMean(...) and similarity(...) these methods behave precisely as the corresponding methods in the BehaviorLongitudinalData class.

The derived classes ConstantCovariate and ChangingCovariate provide appropriate methods value(...) and missing(...) for storing and retrieving the values of the covariate and the missingness indicators, respectively. Internally, the data is stored in one-dimensional or two-dimensional  $N \times M$  arrays Ivalues and Imissing, where N is the number of actors in the respective set and M is the number of observations.

# 5.3.2 Dyadic Covariates

The interface of the dyadic covariates is very similar to that of actor covariates and should not present any difficulties. The base class <code>DyadicCovariate</code> provides access to both relevant sets of actors (methods <code>pFirstActorSet()</code> and <code>pSecondActorSet()</code>) and a storage of the mean value of the covariate that is passed in from R (<code>mean(...)</code> methods).

Again, the values of the covariate and their missingness indicators can be stored and accessed with methods value(...) and missing(...), which are defined in the derived classes ConstantDyadicCovariate and ChangingDyadicCovariate.

The internal representation of the values is tricky, though. Since storing a sparse  $N_1 \times N_2$  (the sizes of both involved actor sets) matrix explicitly is expensive in terms of memory, we store each row of the matrix as an instance of map<int, double> that maps each column index with a non-zero value in that row to the respective value. The matrix of missings has only 0 and 1 as its entries, so an instance of set<int> is more appropriate for storing the column indices with missings in a certain row. Array of such maps or sets (like IpRowValues and IpRowMissings in Constant Dyadic Covariate), one for each row, then represents the whole matrices. Such a representation is not only space-efficient, but also suitable for fast iteration over non-zero values in a certain row. To facilitate an equally fast iteration over non-zero values in a certain column, we maintain analogous structures for columns in *lpColumnValues* and *lpColumnMissings*. The following methods in ConstantDyadicCovariate exploit this internal representation to provide fast iterators over non-zero non-missing values of in a given row or column:

- DyadicCovariateValueIterator rowValues(int i)
- DyadicCovariateValueIterator columnValues(int j)

# Example

The following example multiplies the row i with the column j.

```
DyadicCovariateValueIterator rowIter =
  pCovariate->rowValues(i);
DyadicCovariateValueIterator columnIter =
  pCovariate->columnValues(j);
double product = 0;
while (rowIter.valid() && columnIter.valid())
{
  if (rowIter.actor() < columnIter.actor())</pre>
    rowIter.next();
  else if (rowIter.actor() > columnIter.actor())
    columnIter.next();
  }
  else
    product += rowIter.value() * columnIter.value();
    rowIter.next();
    columnIter.next();
 }
}
```

Finally, we should note that the *ChangingDyadicCovariate* class has the same functionality as discussed above for constant dyadic covariates, except that the methods expect the observation to be specified as an additional parameter and that the dimensionality of the whole storage increases by one.

# 5.4 Composition Change

If a set of actors is not constant over time because actors join or leave, it has to be specified in the *Data* object. The following methods of the *Data* 

class should be used for this purpose:

- void active(const ActorSet \* pActorSet,
   int actor,
   int observation,
   bool flag) specifies if the given actor of the given set of actors is active at the given observation.
- void addJoiningEvent(int period,
   const ActorSet \* pActorSet,
   int actor,
   double time) stores the time of a period when an actor joins a certain actor set.
- void addLeavingEvent(int period, const ActorSet \* pActorSet, int actor, double time) – stores the time of a period when an actor leaves a certain actor set.

The time values in the above methods have to lie in the range [0, 1] with values 0 and 1 representing the start and end point of the period, respectively. For example, assuming that the length of a period is one year, the following code snippet expresses the fact that and the student i leaves the university 3 months after the second observation and resumes the studies half year after the third observation (remember that the indices of observations start with 0):

```
for (int k = 0; k < observationCount; k++)
{
   if (k == 2)
   {
      pData->active(pStudents, i, k, false);
   }
   else
   {
      // This is not strictly necessary,
      // as the actors are active by default
```

```
pData->active(pStudents, i, k, true);
}

pData->addLeavingEvent(1, pStudents, i, .25);
pData->addJoiningEvent(2, pStudents, i, .5);
```

The details about every exogenous event are collected in instances of the *ExogenousEvent* class, which are stored in sets of type *EventSet*, one for each period. These sets can be accessed with the method *pEventSet*(int *period*).

#### 5.5 Accessor Methods

Once a *Data* object has been populated, its sub-objects can be accessed in two ways. A single object can be looked up by its name, like in the following examples.

```
const ActorSet * pStudents = pData->pActorSet("students");
OneModeNetworkLongitudinalData * pFriendshipData =
    pData->pOneModeNetworkData("friendship");
```

If some operation is to be performed for all sub-objects of a certain type, one can obtain a reference to the vector, where the subobjects of this type are stored by the *Data* class. For example, the values of all constant covariates can be printed as follows:

```
const vector<ConstantCovariate *> & rCovariates =
   pData->rConstantCovariates();

for (unsigned i = 0; i < rCovariates.size(); i++)
{
   ConstantCovariate * pCovariate = rCovariates[i];
   cout << pCovariate->name() << endl;
   for (int j = 0; j < pCovariate->pActorSet()->n(); j++)
   {
```

```
cout << j << " " << pCovariate->value(j) << endl;
}</pre>
```

## 6. Models

#### 6.1 Effects

## 6.1.1 Generic Network Effects

**The Basic Idea.** The class *GenericNetworkEffect* may be used to specify an effect for a network variable  $x^{(r)}$  if its evaluation and endowment statistics can be conveniently defined as

$$\sum_{i \neq j} x_{ij}^{(r)} f_{ij}(y)$$

and

$$\sum_{i \neq j} (1 - x_{ij}^{(r)}) x_{ij}^{(r)\text{obs}}(t_m) f_{ij}(y^{\text{obs}}(t_m)),$$

respectivelly. This function  $f_{ij}(y)$  as well as the change contribution  $\Delta_{kij}^X(y)$  should be specified as instances of the *AlterFunction* class and passed as parameters when creating the effect.

We illustrate the overall process by defining the density effect  $s_{i1}^{\text{net}}(x) = \sum_{i} x_{ij}$  as a generic network effect.

1. First, let us define the change contribution function by creating a subclass of *AlterFunction*. Since in our case  $\Delta_{1ij}^X(y) = 1$ , we will name the new class accordingly:

```
class ConstantOneFunction : public AlterFunction
{
   virtual double value(int alter);
};
```

The method *value* should be overridden to return the value of the function for the given alter j. The ego i is implicit and can be accessed by the method AlterFunction::ego(). Here is the trivial implementation of the value method:

```
double ConstantOneFunction::value(int alter)
{
   return 1;
}
```

- 2. Similarly, the tie statistic  $f_{ij}(y)$  should be defined. However, since in our case  $f_{ij}(y) = \Delta_{1ij}^X(y) = 1$ , we can reuse the same class ConstantOneFunction.
- 3. Now that the necessary alter functions are implemented, we are ready to create the generic effect:

```
AlterFunction * pChangeContribution =
  new ConstantOneFunction();
AlterFunctoin * pTieStatistic =
  new ConstantOneFunction();
Effect * pEffect =
  new GenericNetworkEffect(pEffectInfo,
     pChangeContribution,
     pTieStatistic);
```

If the change contribution and the tie statistic functions are the same (as for the density effect), the alternative constructor with a single function is recommended:

```
Effect * pEffect =
  new GenericNetworkEffect(pEffectInfo,
    new ConstantOneFunction());
```

The Anatomy of Alter Functions. As indicated above, the key method of the *AlterFunction* class is the method *value* that has to be implemented by all concrete functions. However, there is a couple of other methods that may be necessary to override.

• initialize(pData, pState, period, pCache) – This method is called before evaluating the function for a specific period of the observed data and a fixed state of the dependent variables. Also, functions may take advantage of the given cache object to speed up the overall processing

time by avoiding repetitive computation of common values, like the number of two-paths, etc. The following example shows the initialization method in the class *NetworkAlterFunction*, which is the base class for all alter functions defined on a network:

```
void NetworkAlterFunction::initialize(const Data * pData,
  State * pState,
  int period,
  Cache * pCache)OneModeNetworkAlterFunction
{
  // Do not forget to initialize the base class
  AlterFunction::initialize(pData,
    pState,
    period,
    pCache);
  // Obtain the right network from the state
  this->lpNetwork = pState->pNetwork(this->name());
  // Store the corresponding network cache object
  this->lpNetworkCache =
    pCache->pNetworkCache(this->lpNetwork);
}
```

• preprocessEgo(ego) – This method is called before calling the value method for any specific alters. The base implementation simply stores the ego, which can be later accessed by using the ego method. The derived alter functions may override this method to do some other ego-related preprocessing.

Important Alter Functions. There is a whole hierarchy of alter functions implemented in src/model/effects/generic, and one should review the existing functions before writing his or her own.

• NetworkAlterFunction – This is the base class for all functions defined on a network such as InDegreeFunction, InStarFunction, etc. The name of the network should be given as an argument on the construction of

the function. The following methods are defined for convenient use in the actual derived functions:

- Network \* pNetwork() Returns the current network this function is computed for.
- NetworkCache \* pNetworkCache() Returns the corresponding cache object for efficient calculations.
- OneModeNetworkAlterFunction This is the base class for all functions defined on a one-mode network. It is a subclass of NetworkAlterFunction and does nothing more than throwing an exception if the underlying network is not a one-mode network.
- *ProductFunction* A composite function defined as a product of two other alter functions.
- DifferenceFunction A composite function defined as a difference between two other alter functions.
- ConditionalFunction A composite function returning the value of either of two other alter functions depending on the value of a certain predicate.

Composite Functions. Composite functions like ProductFunction and DifferenceFunction may be used to define new alter funtions without having to implement new classes. For example, consider the mutuality effect with the network W on the network X, which is formally defined as  $s_{ik}^{\text{net}}(y) = \sum_j x_{ij} w_{ij} w_{ji}$ . The change contribution is  $\Delta_{kij}^X(y) = w_{ij} w_{ji}$ , which is not implemented directly as an alter function. However, there is a function OutTieFunction that returns the values  $w_{ij}$  of the outgoing ties and an analogous function InTieFunction that returns the values  $w_{ji}$  of the incoming ties. These two atomic functions can be easily combined in a product function. Assuming that W is a friendship network, the complete code defining the mutuality effect looks like this:

```
pEffect = new GenericNetworkEffect(pEffectInfo,
   new ProductFunction(
   new OutTieFunction("friendship"),
   new InTieFunction("friendship")));
```

Conditional Functions. The function ConditionalFunction is another type of composite functions, which takes three parameters in its constructor – a predicate and two alter functions. The value of the conditional function depends on the value of the predicate. If the predicate holds for a certain alter j, the if-function is evaluated and its value is returned as the value of the conditional function. If the predicated does not hold then the else-function is evaluated. The predicate has to be an object of the AlterPredicate class. This class functions very much like AlterFunction except that the type of the value method is bool instead of double.