This problem set has 10 questions, for a total of 100 points. Please carefully read the guidelines below:

- Provide your final answers <u>only</u> within the designated spaces on each of the questions. We use automatic grading for some questions answers outside these spaces will not be graded.
- You may annotate your answers digitally on the PDF, or alternatively, you can print the PDF and write your answers by hand. If you choose the second option, please ensure that your handwriting is legible, and the software/hardware used for scanning the document does not change the original format of the PDF, keeping the same structure, orientation, and page size. Once you are done, submit your file through Gradescope.
- We expect you to focus on <u>fully understanding</u> how to solve each problem, not just on obtaining the final answer. This is important not only for your learning, but also for your performance in the course, as similar questions may appear in your exams. Do not hesitate to ask for help if you have any questions.

## Your Name:

## Queues

1. (10 points) Which of the following descriptions best describes what mystery does?

```
int mystery(int *arr, int n) {
    if(n == 1) {
        return arr[0];
    }
    int val = mystery(arr + 1, n - 1)
    return (arr[0] < val) ? arr[0] : val;
}</pre>
```

- A. find the minimum element in arr
- B. find the maximum element in arr
- C. find the the sum of all elements of arr
- D. sort all elements of arr

1. \_\_\_\_\_

3. (10 points) Assume the sequence of elements 1, 3, 6, 7, 10 has been pushed into a queue Q in that order. Determine the output of the mystery function below, when called with Q as the argument.

```
int mystery(std::queue < int > & Q) {
    int result = 0;
    int loop = Q.size();
    for(int i = 0 ; i < loop ; i++) {
        if(!(i % 2)) {
            result += Q.front();
        }
        else {
            result *= Q.front();
        }
        Q.pop();
    }
    return result;
}</pre>
```

3. \_\_\_\_\_

Due: Apr 3, 2025

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## Priority Queues

|  | ray', 'string', 'map', 'set']. Draw | ray', 'string', 'map', 'set']. Draw the tree represen | the following sequence and apply the buildHeap algorithm: ['stack' ray', 'string', 'map', 'set']. Draw the tree representation of a Min-Egorithm. |
|--|-------------------------------------|-------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------|

Due: Apr 3, 2025

## Linked Lists

| 6. | Assume each pointer uses 8 bytes, each integer uses 4 bytes, all linked lists are implemented with a head and a tail pointer, and each node in a linked list stores an integer.                                                                                                                                             |
|----|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
|    | (a) (5 points) How many bytes are necessary to store a Singly-Linked List of length 100?                                                                                                                                                                                                                                    |
|    | (a)                                                                                                                                                                                                                                                                                                                         |
|    | (b) (5 points) How many bytes are necessary to store a Doubly-Linked List (DLL) of length 100?                                                                                                                                                                                                                              |
|    | (b)                                                                                                                                                                                                                                                                                                                         |
| 7. | (10 points) Write a function (use C++) that counts the number of triplets (three adjacent elements) whose sum is equal to 0. The function should match the following signature: int count_triplets(Node *head). where head is a pointer to the first node of a doubly linked list. Assume the list has at least 3 elements. |
|    |                                                                                                                                                                                                                                                                                                                             |
|    |                                                                                                                                                                                                                                                                                                                             |
|    |                                                                                                                                                                                                                                                                                                                             |
|    |                                                                                                                                                                                                                                                                                                                             |
|    | Recursion                                                                                                                                                                                                                                                                                                                   |
| 8. | (10 points) Write a recursive function (use C++) that returns the sum of all even numbers of an input array. The function should match the following signature: int sum_array(std::vector <int>&amp; arr, int n) where n indicates the number of elements in the array.</int>                                               |
|    |                                                                                                                                                                                                                                                                                                                             |
|    |                                                                                                                                                                                                                                                                                                                             |
|    |                                                                                                                                                                                                                                                                                                                             |

| 9. | (10 points) Write a recursive function (use C++) that reverses the elements of an input array in place.         |
|----|-----------------------------------------------------------------------------------------------------------------|
|    | The function should match the following signature: void reverse_array(std::vector <int>&amp; arr, int n)</int>  |
|    | where <b>n</b> indicates the number of elements in the array. The function should modify the array in place and |
|    | perform no more than $n/2$ swaps.                                                                               |

Due: Apr 3, 2025

10. (10 points) Given the following recursive function. Draw the recursion call tree (graphic representation of all the calls), for an initial call of this algorithm with m=14 and n=4. The function is a recursive implementation of Dijkstra's algorithm for finding the greatest common divisor (GCD) of two numbers.

```
int gcd(int m, int n) {
   if (m == n) return m;
   else if (m > n) return gcd(n, m - n);
   else return gcd(m, n - m);
}
```