# MINI PROJECT II: IMPLEMENTATION OF PYTORCH MODULES

### 1 Implementation of Modules: Base class

All Modules in our implementation are based on the following base class Module structure:

```
class Module(object):
    def __init__(self) -> None:
        pass
    def forward(self, *input):
        raise NotImplementedError
    def backward(self, *gradwrtoutput):
        raise NotImplementedError
    def param(self):
        return []
    def to(self, device):
        return self
    def load_param(self, *param):
        return None
```

Listing 1: Base class.

- param() function returns the list of parameters in a module, e.g. for Conv2d and Upsampling, the parameters are [(self.weight, self.dl\_dw), (self.bias, self.dl\_db)].
- to(self, device) function moves the module to the specified device, possible devices are 'cpu' and 'cuda'. We used 'cuda' during training to increase matrix calculation speed (about 30× faster, takes about 5 second per epoch to train our models in Section 8).
- For each module, we also provide a load\_param(self, \*param) to load saved weights back to the modules.

#### 2 Conv2d Module

The major tools we use in this implementation are: torch.nn.functional.unfold/fold and torch.einsum for multidimensional tensor multiplication. Here we illustrate the forward/backward pass of Conv2d.

The forward pass of our Conv2d module is in the following order:

- 1. Reshape kernel weights:  $[C_{out}, C_{in}, ks, ks] \rightarrow [C_{out}, C_{in} \times ks^2]$ . Where  $C_{in/out}$  stands for numbers of in/output channels and ks stands for kernel\_size.
- 2. Unfold input tensor:  $[bz, C_{in}, H_{in}, W_{in}] \rightarrow [bz, C_{in} \times ks^2, H_{out} \times W_{out}]$ . Where bz stands for batch size, and H, W stands for height and width of in/output images. The output of this step is saved in the model class as self.unfolded for later use in backpropagation. And the relationship between input and output widths and heights are (we assume hyperparameter inputs are int instead of tuple):

$$\begin{split} H_{out} &= \left\lfloor \frac{H_{\text{in}} + 2 \times \text{ padding } - \text{ dilation } \times (\text{kernel\_size} - 1) - 1}{\text{stride}} + 1 \right\rfloor \\ W_{out} &= \left\lfloor \frac{W_{\text{in}} + 2 \times \text{ padding } - \text{ dilation } \times (\text{kernel\_size} - 1) - 1}{\text{stride}} + 1 \right\rfloor \end{split}$$

3. Matrix Multiplication  $\mathbf{Y} = \mathbf{X}\mathbf{W} + \mathbf{b}$ :  $[bz, C_{in} \times ks^2, H_{out} \times W_{out}] \times [C_{out}, C_{in} \times ks^2] + [C_{out}] = [bz, C_{out}, H_{out} \times W_{out}].$ 

4. Reshape output:  $[bz, C_{out}, H_{out} \times W_{out}] \rightarrow [bz, C_{out}, H_{out}, W_{out}]$ 

The entire forward pass could be done within a few lines of code (only the relevant parts are kept):

```
self.unfolded = unfold(x, kernel_size = self.kernel_size, dilation=self.dilation, padding=self.padding, stride=self.stride)
weight = self.weight.reshape(self.out_channels, -1)
wxb = einsum('ow,bws->bso', weight, self.unfolded)
if self.use_bias: wxb += self.bias
wxb = einsum('bso->bos', wxb)
out_h = math.floor((x.shape[-2]-(self.kernel_size-1)*self.dilation+2*self.padding-1)/self.stride+1)
out_w = math.floor((x.shape[-1]-(self.kernel_size-1)*self.dilation+2*self.padding-1)/self.stride+1)
ret = wxb.reshape(-1, self.out_channels, out_h, out_w)
```

Listing 2: Forward pass of Conv2d.

The backward pass of our Conv2d module is in the following order:

1. Reshape upstream gradients  $\partial L/\partial Y$ :

$$[bz, C_{out}, H_{out}, W_{out}] \rightarrow [bz, C_{out}, H_{out} \times W_{out}].$$

2. Reshape kernel weights:

$$[C_{out}, C_{in}, ks, ks] \rightarrow [C_{out}, C_{in} \times ks^2].$$

3. Apply chain rule 
$$\frac{\partial \mathbf{L}}{\partial \mathbf{X}} = \frac{\partial \mathbf{L}}{\partial \mathbf{Y}} \mathbf{W}^T$$
:
$$[C_{out}, C_{in} \times ks^2] \times [bz, C_{out}, H_{out} \times W_{out}] \rightarrow [bz, C_{in} \times ks^2, H_{out} \times W_{out}].$$

4. Apply fold to recover shape of  $\frac{\partial \mathbf{L}}{\partial \mathbf{X}}$  to  $\mathbf{X}$ :

$$[bz, C_{in} \times ks^2, H_{out} \times W_{out}] \xrightarrow{\text{fold}} [bz, C_{in}, H_{in}, W_{in}]$$

5. Acquire gradients w.r.t weights in self .unfolded  $\frac{\partial L}{\partial W} = X^T \frac{\partial L}{\partial Y}$  and transform to the original weight

$$[bz, C_{in} \times ks^2, H_{out} \times W_{out}] \times [bz, C_{out}, H_{out} \times W_{out}] = [C_{out}, C_{in} \times ks^2] \rightarrow [C_{out}, C_{in}, ks, ks]$$

6. Acquire gradients w.r.t bias: 
$$\frac{\partial \mathbf{L}}{\partial \mathbf{b}} = \frac{\partial \mathbf{L}}{\partial \mathbf{Y}}$$
: 
$$[bz, C_{out}, H_{out}, W_{out}] \xrightarrow{\text{transpose+flatten}} [C_{out}, bz \times H_{out} \times W_{out}] \xrightarrow{\text{mean}} [C_{out}, ]$$

In terms of initialization, we use the same method as in the reset\_parameters (self) function in PyTorch repository. Entire implementation of Conv2d module is shown in Section 8.

#### **Upsampling Module** 3

In our implementation, the Upsampling module is implemented in the way of nearest neighbor sampling (NN Sample) + convolution. Two tricky parts in this implementation are: 1) implement nearest neighbor sampling efficiently. 2) implement backward gradient pass of nearest neighbor sampling.

In terms of nearest neighbor sampling, we implement it with torch.repeat\_interleave as follows (simplified due to paragraph limit):

```
def nearest_neighbor_sampling(self, inp, scale_factor):
    inter = repeat_interleave(inp, repeats=scale_factor, dim=-1)
    ret = repeat_interleave(inter, repeats=scale_factor, dim=-2)
   return ret
```

Listing 3: Nearest neighbor sampling.

The back propagation of Upsampling consists of two parts: 1) backprop the upstream gradients from output to convolution layer input  $\partial \mathbf{L}/\partial \mathbf{X}_{up}$ , and 2) back prop from convolution input to input  $\partial \mathbf{X}_{up}/\partial \mathbf{X}$  (passing the NN Sample module). Where 1) can simply be achieved by backpropagating the convolution layer in Upsampling, whereas, the second requires a special type of gradient accumulation way which depends on the scale\_factor in the NN Sample part. An example of this type of accumulation is shown in Eq. (1) (with scale\_factor=2):

$$\underbrace{\begin{bmatrix}
1 & 0 & 0 & 2 \\
-3 & 4 & 2 & 1 \\
\hline
-2 & 0 & 0 & 1 \\
0 & 3 & 0 & 1
\end{bmatrix}}_{\partial \mathbf{L}/\partial \mathbf{X}_{up}} \rightarrow \underbrace{\begin{bmatrix} 2 & 5 \\ 1 & 2 \end{bmatrix}}_{\partial \mathbf{L}/\partial \mathbf{X}} \tag{1}$$

This is implemented with two for loops, we use tensor operations to accelerate on GPU:

```
def backward(self, grdwrtoutput):
    dl_dw = self.conv.backward(grdwrtoutput)
   N, C, H, W = dl_dw.size()
   out_h, out_w = H // self.scale_factor, W // self.scale_factor
   rows = arange(0, H, self.scale_factor).repeat(out_h)
    cols = arange(0, W, self.scale_factor).repeat_interleave(out_w)
    dl_dx = zeros(dl_dw[..., cols+0, rows+0].size()).to(grdwrtoutput.device)
    for i in range(self.scale_factor):
       for j in range(self.scale_factor):
            dl_dx = dl_dx + dl_dw[..., cols+i, rows+j]
   dl_dx = dl_dx.reshape(N, C, out_h, out_w)
    return dl_dx
```

Listing 4: Backprop of Upsampling module.

#### 4 ReLU Module

torch.clamp and torch.sign are mainly used to implement ReLU module. Module implement main steps: clamp input  $\rightarrow$  output 0 or input itself  $\rightarrow$  sign input and then clamp  $\rightarrow$  1 or 0, notice this module has no parameters.

#### 5 Sigmoid Module

torch. exp is used to implement sigmoid module with following equations. Sigmoid(x) =  $\frac{1}{1+e^{-x}}$ , Sigmoid'(x) =  $\frac{(e^{-x}+1)-1}{1+e^{-x}}\frac{1}{1+e^{-x}} = (1-\text{Sigmoid}(x))$  Sigmoid(x), this module also has no parameters.

## **6** Mean Squared Error Loss Function Module

MSELoss module is implemented with torch.pow, torch.mean, and torch.size with the following equations.  $\text{MSELoss}(y,t) = \frac{1}{N} \sum_{i=0}^{N} (y_i - t_i)^2$ ,  $\text{MSELoss}'(y,t) = \frac{2}{N} \sum_{i=0}^{N} (y_i - t_i)$ , where N is total elements in y and t. The module does following things: initialize the prediction y and target  $t \Rightarrow$  compute the loss and compute the gradient w.r.t prediction y.

## 7 Stochastic Gradient Descent optimizer Module

SGD module is mainly implemented with torch.add and torch.Tensor.zero\_. SGD module has zero\_grad() to set all grad parameters in the input parameters to 0, and step() to update grad parameters in the input parameters by w += -grad \* lr.

These are done with the following code:

```
def zero_grad(self):
    for modules in self.params:
        weight, grad = modules
        if grad != None: grad.zero_()
```

```
Listing 5: SGD zero_grad() part.
```

```
def step(self):
    for modules in self.params:
        weight, grad = modules
        if weight != None and (grad != None): weight.add_(-self.lr * grad)
```

Listing 6: SGD step() part.

# 8 Sequential Module

Sequential module needs to make sure that both forward inputs and backward gradients as well as backward gradients could flow smoothly during training. Morever, the Sequential module also needs to take care of gathering parameters from all sub modules and loading back the parameters to its sub modules. All these are done by:

```
class Sequential(Module):
   def __init__(self, *layers) -> None:
       super().__init__()
        self.modules = []
       for layer in layers:
           self.modules.append(layer)
   def forward(self, x):
       ret = x
       for layer in self.modules:
           ret = layer.forward(ret)
       return ret
   def backward(self, gradwrtoutput):
       grad_from_back = gradwrtoutput
        for layer in reversed(self.modules):
           grad_from_back = layer.backward(
     grad_from_back)
   def __call__(self, input):
       return self.forward(input)
```

Listing 7: Sequential functioning part.

```
def to(self, device):
    for i, module in enumerate(self.modules):
       self.modules[i] = module.to(device)
    return self
def param(self):
    for layer in self.modules:
        ret.append(layer.param()[0])
        if len(layer.param()) > 1:
            ret.append(layer.param()[1])
   return ret
def load_param(self, param):
   model_idx = param_idx = 0
    while model_idx < len(self.modules) and (param_idx < len(param)):</pre>
        required_length = len(self.modules[model_idx].param())
        self.modules[model_idx].load_param(param[param_idx:
     required_length+param_idx])
        param_idx += required_length
        model_idx += 1
```

Listing 8: Auxiliary: switch device save/load parameters.

# Appendix 1: Experiment

In terms of experiment design, we implement several *Noise2Noise-*like model structures to test our modules' performance. Due to space limitation, we report validation performance on the given dataset of two typical models and their training curves as well as final visualizations.

```
model = Sequential(
    Conv2d(3, 32, 3, stride=1),
    ReLU(),
    Conv2d(32, 64, 3, stride=1, padding=3),
    ReLU(),
    Upsampling(2, 64, 32, stride=2),
    ReLU(),
    Upsampling(2, 32, 3, stride=2),
    Sigmoid()
)
```

```
model = Sequential(
    Conv2d(3, 10, 3, stride=2, padding=2),
    ReLU(),
    Conv2d(10, 10, 3, stride=2, padding=2),
    ReLU(),
    Upsampling(2, 10, 10, kernel_size=4, stride=1),
    ReLU(),
    Upsampling(2, 10, 3, kernel_size=3, stride=1),
    Sigmoid()
)
```

Listing 9: Best performance model 1.

Listing 10: Model 2: Conv2d stride 2.

We trained both models for 500 epochs with batch size 16 and SGD of learning rate 6e-2. The best performances they achieved were **24.85dB** for model 1 and **22.73dB** for model 2 (we submitted model 2 as per requirements). The training/validation curves are shown in Fig. 1.

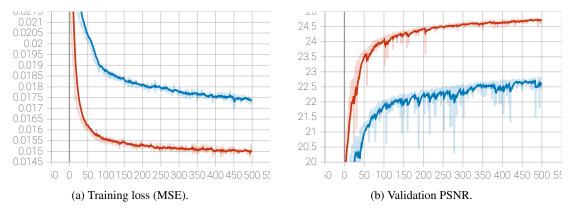


Figure 1: Training/Validation curves of Model 1 and Model 2.

The result visualizations are shown in Fig. 2.

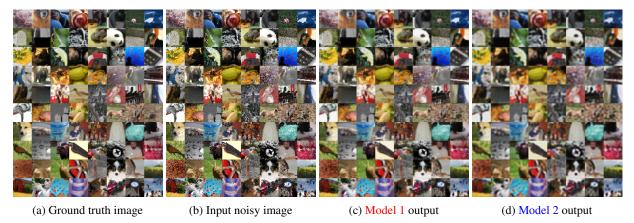


Figure 2: Visualization results at validation.

## **Appendix 2: Conv2d Implementation**

```
class Conv2d(Module):
    def __init__(self, in_channels, out_channels, kernel_size=3, bias=True, dilation=1, stride=1, padding=0):
        self.in_channels = in_channels
        self.out_channels = out_channels
        self.kernel_size = kernel_size
        self.dilation = dilation
        self.stride = stride
        self.padding = padding
        self.use_bias = bias
        # torch initialization
        n = in_channels * kernel_size**2
        stdv = 1. / math.sqrt(n)
        self.weight = empty(out_channels, in_channels, kernel_size, kernel_size).uniform_(-stdv, stdv)
        self.bias = empty(out_channels).uniform_(-stdv, stdv)
        self.dilation = dilation
        self.padding = padding
        self.stride = stride
        self.unfolded = None
        self.x = None
        # gradients
        self.dl_dw = empty(self.weight.size())
self.dl_db = empty(self.bias.size())
    def forward(self, x):
        self.x = x
        self.unfolded = unfold(x, kernel_size = self.kernel_size, dilation=self.dilation, padding=self.padding, stride=self.
      stride)
        weight = self.weight.reshape(self.out_channels, -1)
        wxb = einsum('ow,bws->bso', weight, self.unfolded)
        if self.use_bias:
            wxb += self.bias
        wxb = einsum('bso->bos', wxb)
        out_h = math.floor((x.shape[-2] - (self.kernel_size-1)*self.dilation + 2*self.padding - 1) / self.stride + 1)
out_w = math.floor((x.shape[-1] - (self.kernel_size-1)*self.dilation + 2*self.padding - 1) / self.stride + 1)
        ret = wxb.reshape(-1, self.out_channels, out_h, out_w)
    def backward(self, grdwrtoutput):
        grdwrtoutput = grdwrtoutput.flatten(2, -1)
        weight = self.weight.reshape(self.out_channels, -1)
        # here x is cin*kernelsize^2 and s is Hout*Wout
        dl_dx = einsum('ox,nos->nxs', weight, grdwrtoutput)
        out_size = (self.x.size(-2), self.x.size(-1))
        dl_dx = fold(dl_dx, output_size=out_size, kernel_size=self.kernel_size, dilation=self.dilation, padding=self.padding,
      stride=self.stride)
         self.dl_dw.add_(einsum('nos,nxs->ox', grdwrtoutput, self.unfolded).reshape(self.weight.size()))
        self.dl_db.add_(grdwrtoutput.transpose(0, 1).flatten(1, -1).mean(1))
        return dl_dx
        return [(self.weight, self.dl_dw), (self.bias, self.dl_db)]
    def __call__(self, input):
        return self.forward(input)
    def to(self, device):
        self.dl_dw = self.dl_dw.to(device)
        self.dl_db = self.dl_db.to(device)
        self.weight = self.weight.to(device)
        self.bias = self.bias.to(device)
        return self
    def load_param(self, param):
    self.weight, _ = param[0]
    self.bias, _ = param[1]
```

Listing 11: Implementation of Conv2d.