SML_312 _FInal_Project_2

December 6, 2024

```
[2]: # import statements
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
import pickle
```

0.1 Modelling

```
[3]: # Load the df_merged DataFrame from the pickle file
     with open('df_merged.pkl', 'rb') as f:
         df_merged = pickle.load(f)
     # Print the first few rows of the loaded DataFrame to verify
     print(df_merged.head())
            date
                   vixo
                          vixh
                                 vixl
                                                vxno
                                                       vxnh
                                                              vxnl
                                                                      vxn
                                                                            vxdo
                                          vix
    0 2004-11-18
                 13.22
                         13.29
                                12.96
                                       12.98
                                              18.55
                                                      19.03
                                                             18.44
                                                                    18.79
                                                                           12.12
    1 2004-11-19
                 12.79
                         13.83
                                12.77
                                       13.50
                                              18.63
                                                      19.73
                                                             18.32
                                                                    19.72
                                                                           12.12
    2 2004-11-22 13.71
                         13.71
                                12.94
                                       12.97
                                               19.98
                                                      20.07
                                                             18.72
                                                                    18.77
                                                                           12.39
    3 2004-11-23
                 12.78
                         12.91
                                12.57
                                              18.82
                                                      18.97
                                       12.67
                                                             18.35
                                                                    18.43
                                                                           11.84
    4 2004-11-24 12.58 12.89
                                12.56
                                       12.72
                                             18.22 18.28
                                                             17.73 17.88
                                                                           11.57
            b2ret
                      b2ind
                                b1ret
                                          b1ind
                                                    t90ret
                                                              t90ind
                                                                        t30ret
      ... -0.00572
                  1104.611 -0.002025
                                                                      0.001541
                                       1030.445
                                                 0.001474
                                                            828.7477
    1 ... -0.00572 1104.611 -0.002025
                                       1030.445
                                                  0.001474
                                                            828.7477
                                                                      0.001541
    2 ... -0.00572 1104.611 -0.002025
                                       1030.445
                                                  0.001474
                                                            828.7477
                                                                      0.001541
      ... -0.00572 1104.611 -0.002025
                                       1030.445
                                                 0.001474
                                                            828.7477
                                                                      0.001541
    4 ... -0.00572 1104.611 -0.002025 1030.445 0.001474 828.7477
                                                                      0.001541
         t30ind
                   cpiret
                           cpiind
      689.9246
                 0.000524
                            449.4
       689.9246
                 0.000524
                            449.4
    2 689.9246
                 0.000524
                            449.4
    3 689.9246
                 0.000524
                            449.4
       689.9246
                 0.000524
                            449.4
```

[5 rows x 99 columns]

0.1.1 Feature Engineering

```
[4]: df_merged.columns.tolist()
[4]: ['date',
      'vixo',
      'vixh',
      'vixl',
      'vix',
      'vxno',
      'vxnh',
      'vxnl',
      'vxn',
      'vxdo',
      'vxdh',
      'vxdl',
      'vxd',
      'exratd_fromUSD_df_eur',
      'exratd_toUSD_df_eur',
      'exratd_fromUSD_df_jpy',
      'exratd_toUSD_df_jpy',
      'exratd_fromUSD_df_gbp',
      'exratd_toUSD_df_gbp',
      'exratd_fromUSD_df_chf',
      'exratd_toUSD_df_chf',
      'exratd_fromUSD_df_cny',
      'exratd_toUSD_df_cny',
      'BIDLO_df_spy',
      'ASKHI_df_spy',
      'PRC_df_spy',
      'VOL_df_spy',
      'BID_df_spy',
      'ASK_df_spy',
      'OPENPRC_df_spy',
      'BIDLO_df_qqq',
      'ASKHI_df_qqq',
      'PRC_df_qqq',
      'VOL_df_qqq',
      'BID_df_qqq',
      'ASK_df_qqq',
      'OPENPRC_df_qqq',
      'BIDLO_df_oih',
      'ASKHI_df_oih',
      'PRC_df_oih',
      'VOL_df_oih',
      'BID_df_oih',
      'ASK_df_oih',
```

```
'OPENPRC_df_oih',
'BIDLO_df_iyr',
'ASKHI_df_iyr',
'PRC_df_iyr',
'VOL_df_iyr',
'BID_df_iyr',
'ASK_df_iyr',
'OPENPRC_df_iyr',
'BIDLO_df_lqd',
'ASKHI_df_lqd',
'PRC_df_lqd',
'VOL_df_lqd',
'BID_df_lqd',
'ASK_df_lqd',
'OPENPRC_df_lqd',
'BIDLO_df_tlt',
'ASKHI_df_tlt',
'PRC_df_tlt',
'VOL_df_tlt',
'BID_df_tlt',
'ASK_df_tlt',
'OPENPRC_df_tlt',
'BIDLO_df_tip',
'ASKHI_df_tip',
'PRC_df_tip',
'VOL_df_tip',
'BID_df_tip',
'ASK_df_tip',
'OPENPRC_df_tip',
'BIDLO_df_gld',
'ASKHI_df_gld',
'PRC_df_gld',
'VOL_df_gld',
'BID_df_gld',
'ASK_df_gld',
'OPENPRC_df_gld',
'b30ret',
'b30ind',
'b20ret',
'b20ind',
'b10ret',
'b10ind',
'b7ret',
'b7ind',
'b5ret',
'b5ind',
'b2ret',
```

```
'b1ret',
      'blind',
      't90ret',
      't90ind',
      't30ret',
      't30ind',
      'cpiret',
      'cpiind']
[5]: # Calculate the 7 and 21 day moving averages, daily percent changes, and the
      \hookrightarrow 0, 5, 10, 30, 44-day movements for the ETFs
     columns_to_calculate = ['df_oih', 'df_spy', 'df_qqq', 'df_iyr', 'df_lqd', __

    df_tlt', 'df_tip', 'df_gld']

     for column in columns_to_calculate:
         df merged[f'{column} 7d ma'] = df merged[f'PRC {column}'].rolling(window=7).
      →mean()
         df merged[f'{column} 21d ma'] = df merged[f'PRC {column}'].
      →rolling(window=21).mean()
         df_merged[f'{column}_pct_change'] = (df_merged[f'PRC_{column}'] -__

¬df_merged[f'OPENPRC_{column}']) / df_merged[f'PRC_{column}']

         for days in [0, 5, 10, 30, 44]:
             df_merged[f'{column}_{days}d_movement'] = np.where(
                 df_merged[f'OPENPRC_{column}'].notna() & df_merged[f'PRC_{column}'].
      ⇔shift(-days).notna(),
                 np.where(df_merged[f'OPENPRC_{column}'] <__
      ⇔df_merged[f'PRC_{column}'].shift(-days), 1,0),
                 np.nan
             )
     # Display the first few rows to verify the calculations
     print(df_merged.head())
            date
                   vixo
                          vixh
                                 vixl
                                          vix
                                                vxno
                                                       vxnh
                                                              vxnl
                                                                      vxn
                                                                            vxdo \
    0 2004-11-18 13.22 13.29 12.96 12.98
                                              18.55 19.03
                                                             18.44 18.79
                                                                            12.12
    1 2004-11-19 12.79 13.83 12.77 13.50 18.63 19.73
                                                             18.32 19.72
                                                                            12.12
    2 2004-11-22 13.71 13.71 12.94 12.97
                                               19.98
                                                             18.72 18.77
                                                                            12.39
                                                      20.07
    3 2004-11-23 12.78 12.91
                                12.57 12.67
                                               18.82
                                                      18.97
                                                             18.35 18.43
                                                                            11.84
    4 2004-11-24 12.58 12.89 12.56 12.72 18.22 18.28
                                                             17.73 17.88
                                                                           11.57
          df_tip_30d_movement df_tip_44d_movement df_gld_7d_ma df_gld_21d_ma \
    0
                           1.0
                                                1.0
                                                              NaN
                                                                             NaN
                           0.0
                                                0.0
                                                              NaN
                                                                             NaN
    1
    2 ...
                           0.0
                                                0.0
                                                                             NaN
                                                              NaN
    3
                           0.0
                                                0.0
                                                                             NaN
                                                              NaN
    4
                           0.0
                                                1.0
                                                              NaN
                                                                             NaN
```

'b2ind',

```
df_gld_pct_change df_gld_0d_movement df_gld_5d_movement
    0
                -0.001127
                                           0.0
                                                                1.0
                 0.006476
                                           1.0
                                                                1.0
    1
    2
                 0.004449
                                           1.0
                                                                1.0
    3
                -0.002905
                                           0.0
                                                                1.0
    4
                 0.002664
                                           1.0
                                                                1.0
       df_gld_10d_movement df_gld_30d_movement df_gld_44d_movement
    0
                        1.0
                                              0.0
                        1.0
                                              0.0
                                                                    0.0
    1
    2
                        1.0
                                              0.0
                                                                    0.0
    3
                                                                    0.0
                        0.0
                                              0.0
    4
                        0.0
                                              0.0
                                                                    0.0
    [5 rows x 163 columns]
[6]: # Filter columns containing 'qqq'
     qqq_columns = [col for col in df_merged.columns if 'qqq' in col]
     # Select specific columns
     selected_columns = ['OPENPRC_df_qqq', 'PRC_df_qqq'] + [col for col in_
      ⇒qqq_columns if 'qqq' and 'movement' in col]
     # Print the first 10 rows of these columns
     print(df_merged[selected_columns].tail(30))
          OPENPRC_df_qqq PRC_df_qqq df_qqq_Od_movement df_qqq_5d_movement
                            481.26999
    4957
                475.17001
                                                        1.0
                                                                             1.0
    4958
                480.35001
                            480.26001
                                                        0.0
                                                                             0.0
    4959
                481.04999
                            482.50000
                                                        1.0
                                                                             0.0
    4960
                484.84000
                            474.85001
                                                        0.0
                                                                             0.0
    4961
                479.23999
                                                        1.0
                                                                             0.0
                            480.00000
    4962
                479.45001
                            475.34000
                                                        0.0
                                                                             0.0
    4963
                473.69000
                            476.76001
                                                        1.0
                                                                             0.0
    4964
                476.29001
                            471.35001
                                                       0.0
                                                                            0.0
    4965
                473.28000
                            470.66000
                                                       0.0
                                                                             0.0
                                                        1.0
                                                                             0.0
    4966
                475.04001
                            476.26999
                                                                            0.0
    4967
                473.20001
                            461.81000
                                                        0.0
    4968
                458.67001
                            460.60999
                                                        1.0
                                                                             1.0
    4969
                458.97000
                            461.04001
                                                        1.0
                                                                            1.0
    4970
                460.32999
                            448.69000
                                                        0.0
                                                                            1.0
    4971
                453.06000
                            454.45999
                                                        1.0
                                                                            1.0
    4972
                456.23999
                            458.66000
                                                       1.0
                                                                            1.0
                                                        1.0
                                                                            1.0
    4973
                459.91000
                            468.62000
                468.64999
                            473.22000
                                                        1.0
    4974
                                                                            1.0
    4975
                472.48001
                            475.34000
                                                        1.0
                                                                             1.0
                473.19000
                            473.23999
    4976
                                                        1.0
                                                                             1.0
```

```
0.0
    4977
                 476.29001
                              473.48999
                                                                                  1.0
    4978
                 474.70001
                              471.44000
                                                            0.0
                                                                                  1.0
    4979
                 482.60999
                                                            1.0
                                                                                  1.0
                              483.35999
    4980
                 482.48999
                              482.44000
                                                            0.0
                                                                                  1.0
                 482.95001
                              483.04001
                                                            1.0
                                                                                  1.0
    4981
    4982
                 484.45999
                              485.37000
                                                            1.0
                                                                                  NaN
    4983
                 484.73999
                              485.82001
                                                            1.0
                                                                                  NaN
                                                            0.0
    4984
                 493.37000
                              489.47000
                                                                                  NaN
    4985
                 490.50000
                              486.75000
                                                            0.0
                                                                                  NaN
    4986
                              488.07001
                                                            1.0
                                                                                  NaN
                 485.78000
           df_qqq_10d_movement
                                   df_qqq_30d_movement
                                                           df_qqq_44d_movement
    4957
                             0.0
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    4958
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    4959
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    4969
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    4970
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    4971
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    4972
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                             1.0
    4973
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    4974
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    4975
                                                     NaN
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    4976
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    4978
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    4979
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    4983
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    4984
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                                                                             NaN
    4985
                             {\tt NaN}
                                                     NaN
                                                                             NaN
    4986
                             NaN
                                                     NaN
                                                                             NaN
[7]: # Drop rows with NaN values
     df_merged_cleaned = df_merged.dropna()
     # Display the first few rows to verify the changes
```

```
print(df_merged_cleaned.shape)
      print(df_merged_cleaned.columns)
     (4779, 163)
     Index(['date', 'vixo', 'vixh', 'vixl', 'vix', 'vxno', 'vxnh', 'vxnl', 'vxn',
            'vxdo',
            'df_tip_30d_movement', 'df_tip_44d_movement', 'df_gld_7d_ma',
            'df_gld_21d_ma', 'df_gld_pct_change', 'df_gld_0d_movement',
            'df_gld_5d_movement', 'df_gld_10d_movement', 'df_gld_30d_movement',
            'df_gld_44d_movement'],
           dtype='object', length=163)
[20]: def create_data(df, target_column, price_columns, columns=[], window_size=30):
          Creates data for the past window_size days
          df: DataFrame
          target_column: str
          columns: list
          window_size: int
          return: DataFrame, DataFrame, DataFrame
          X, y = [], []
          for i in range(window_size, len(df)):
              data = []
              for column in columns:
                  data.extend(df[column].values[i-window_size:i])
              X.append(data)
              y.append(df[target_column].values[i])
          # Create column names for X
          column_names = []
          for column in columns:
              column_names.extend([f"{column}_{-j}" for j in range(window_size, 0,_
       →-1)])
          # Convert X and y to DataFrames
          X_df = pd.DataFrame(X, columns=column_names)
          y_df = pd.DataFrame(y, columns=[target_column])
          prices = df[price_columns][window_size:]
          return X_df, y_df, prices
```

0.1.2 QQQ Daily Change as Output

```
[21]: # Get data
      columns = df_merged_cleaned.select_dtypes(exclude=['datetime']).columns.tolist()
      columns = [col for col in columns if 'movement' not in col]
      X, y, prices = create_data(df_merged_cleaned, 'df_qqq_0d_movement',_
       →['OPENPRC_df_qqq', 'PRC_df_qqq'], columns=columns, window_size=30)
[11]: X.head()
Γ11]:
         vixo_-30
                   vixo_-29
                              vixo_-28
                                        vixo_-27 vixo_-26
                                                             vixo_-25
                                                                        vixo_-24 \
            12.34
                       12.26
                                 11.78
                                            11.42
                                                       11.41
                                                                 11.53
                                                                            12.25
      1
            12.26
                       11.78
                                 11.42
                                            11.41
                                                       11.53
                                                                 12.25
                                                                            11.61
      2
            11.78
                       11.42
                                 11.41
                                            11.53
                                                       12.25
                                                                 11.61
                                                                            12.25
      3
            11.42
                       11.41
                                 11.53
                                            12.25
                                                       11.61
                                                                 12.25
                                                                            12.42
      4
            11.41
                       11.53
                                 12.25
                                            11.61
                                                       12.25
                                                                 12.42
                                                                            13.39
         vixo_-23
                   vixo_-22
                              vixo_-21
                                        ... df_gld_pct_change_-10
      0
            11.61
                       12.25
                                 12.42
                                                          0.002363
            12.25
                       12.42
                                 13.39 ...
                                                         -0.009229
      1
      2
            12.42
                       13.39
                                 14.01
                                                          0.003077
      3
            13.39
                       14.01
                                 13.98
                                                          0.009827
            14.01
                       13.98
                                 14.09 ...
                                                          0.000701
         df_gld_pct_change_-9
                                df_gld_pct_change_-8
                                                       df_gld_pct_change_-7 \
                                                                    0.009827
      0
                     -0.009229
                                             0.003077
                      0.003077
                                             0.009827
                                                                    0.000701
      1
      2
                      0.009827
                                             0.000701
                                                                   -0.006866
      3
                      0.000701
                                            -0.006866
                                                                    0.002342
      4
                     -0.006866
                                             0.002342
                                                                    0.003285
         df_gld_pct_change_-6
                                df_gld_pct_change_-5
                                                        df_gld_pct_change_-4
      0
                      0.000701
                                            -0.006866
                                                                    0.002342
      1
                     -0.006866
                                             0.002342
                                                                     0.003285
      2
                      0.002342
                                             0.003285
                                                                   -0.000468
      3
                      0.003285
                                            -0.000468
                                                                    0.000237
                     -0.000468
                                             0.000237
                                                                    0.000238
         df_gld_pct_change_-3
                                df_gld_pct_change_-2
                                                        df_gld_pct_change_-1
      0
                                            -0.000468
                                                                    0.000237
                      0.003285
      1
                     -0.000468
                                             0.000237
                                                                    0.000238
      2
                      0.000237
                                             0.000238
                                                                   -0.001423
      3
                      0.000238
                                            -0.001423
                                                                    0.002879
                     -0.001423
                                             0.002879
                                                                   -0.002894
      [5 rows x 3660 columns]
```

```
[25]: from sklearn.model_selection import train_test_split
      # Split the data into training and temporary sets
      X_train, X_temp, y_train, y_temp = train_test_split(X, y, test_size=0.2,__
       ⇔shuffle=False)
      # Split the temporary set into cross-validation and test sets
      X_cv, X_test, y_cv, y_test = train_test_split(X_temp, y_temp, test_size=0.5,_
       ⇒shuffle=False)
      print(f'Training set size: {X_train.shape[0]}')
      print(f'Cross-validation set size: {X_cv.shape[0]}')
      print(f'Test set size: {X_test.shape[0]}')
     Training set size: 3799
     Cross-validation set size: 475
     Test set size: 475
[34]: print('Training from ' + df_merged_cleaned['date'][30].strftime('%Y-%m-%d') + '__
      -to ' + df merged_cleaned['date'][X_train.shape[0]+30].strftime('\(\frac{\''\}Y-\mathbc{'\''\}M-\'\d'\))
      print('Cross-validation from ' + df_merged_cleaned['date'][X_train.shape[0]+30].
       ⇒strftime('%Y-%m-%d') + ' to ' + df_merged_cleaned['date'][X_train.
       \Rightarrowshape [0] +X_cv.shape [0] +30].strftime('\(\frac{\'}{\'}Y-\\mathbb{m}-\\d'\))
      print('Test from ' + df_merged_cleaned['date'][X_train.shape[0]+X_cv.
       ⇔shape[0]+30].strftime('%Y-%m-%d') + ' to ' +

       df_merged_cleaned['date'][X_train.shape[0]+X_cv.shape[0]+X_test.shape[0]+30].

strftime('%Y-%m-%d'))
     Training from 2005-01-03 to 2020-02-24
     Cross-validation from 2020-02-24 to 2022-01-11
     Test from 2022-01-11 to 2023-12-01
[26]: prices train = prices.iloc[:X train.shape[0]]
      prices_cv = prices.iloc[X_train.shape[0]:X_train.shape[0]+X_cv.shape[0]]
      prices test = prices.iloc[-X test.shape[0]:]
[14]: def calculate_percentage(y):
          unique, counts = np.unique(y, return_counts=True)
          total = len(y)
          percentages = {k: (v / total) * 100 for k, v in zip(unique, counts)}
          return percentages
      \# Calculate percentages for y_train, y_cv, and y_test
      y_train_percentage = calculate_percentage(y_train)
      y_cv_percentage = calculate_percentage(y_cv)
      y_test_percentage = calculate_percentage(y_test)
      print(f'y_train percentages: {y_train_percentage}')
```

```
print(f'y_cv percentages: {y_cv_percentage}')
      print(f'y_test percentages: {y_test_percentage}')
     y train percentages: {0.0: 46.880758094235325, 1.0: 53.11924190576468}
     y_cv percentages: {0.0: 43.78947368421053, 1.0: 56.21052631578948}
     y_test percentages: {0.0: 45.89473684210526, 1.0: 54.10526315789473}
     Let's first get a baseline result by using logistic regression.
[15]: from sklearn.linear model import LogisticRegression
      from sklearn.metrics import accuracy_score
      # Create a logistic regression model
      log_reg = LogisticRegression(max_iter=1000)
      # Fit the model to the data
      log_reg.fit(X_train, y_train)
      # Predict the target values for training and cross-validation sets
      y_train_pred = log_reg.predict(X_train)
      y_cv_pred = log_reg.predict(X_cv)
      # Calculate the accuracy for training and cross-validation sets
      train_accuracy = accuracy_score(y_train, y_train_pred)
      cv_accuracy = accuracy_score(y_cv, y_cv_pred)
      print(f'Training Accuracy: {train accuracy}')
      print(f'Cross-Validation Accuracy: {cv_accuracy}')
     /Users/charlieyang/anaconda3/lib/python3.11/site-
     packages/sklearn/utils/validation.py:1339: DataConversionWarning: A column-
     vector y was passed when a 1d array was expected. Please change the shape of y
     to (n_samples, ), for example using ravel().
       y = column_or_1d(y, warn=True)
     Training Accuracy: 0.6030534351145038
     Cross-Validation Accuracy: 0.4905263157894737
     /Users/charlieyang/anaconda3/lib/python3.11/site-
     packages/sklearn/linear_model/_logistic.py:469: ConvergenceWarning: lbfgs failed
     to converge (status=1):
     STOP: TOTAL NO. of ITERATIONS REACHED LIMIT.
     Increase the number of iterations (max_iter) or scale the data as shown in:
         https://scikit-learn.org/stable/modules/preprocessing.html
     Please also refer to the documentation for alternative solver options:
         https://scikit-learn.org/stable/modules/linear_model.html#logistic-
     regression
```

n_iter_i = _check_optimize_result(

Try more models:

```
[16]: from sklearn.pipeline import make_pipeline
      from sklearn.neighbors import KNeighborsClassifier
      from sklearn.naive_bayes import GaussianNB
      from sklearn.linear_model import LogisticRegression
      from sklearn.preprocessing import StandardScaler
      from sklearn.svm import SVC
      from sklearn.tree import DecisionTreeClassifier
      from sklearn.ensemble import RandomForestClassifier
      knn = make_pipeline(StandardScaler(), KNeighborsClassifier())
      nb = GaussianNB()
      log_reg = make_pipeline(StandardScaler(), LogisticRegression())
      svm = make_pipeline(StandardScaler(), SVC(kernel='linear', random_state=37))
      dt = DecisionTreeClassifier(random_state=37)
      rf = RandomForestClassifier(random_state=37)
      models = {'knn': knn, 'nb': nb, 'log_reg': log_reg, 'svm': svm, 'dt': dt, 'rf':
       ⊶rf}
[24]: from sklearn.metrics import accuracy score, precision score, recall score,
      # Dictionary to store the results
      results = {}
      # Iterate over each model in the models set
      for model_name, model in models.items():
          # Fit the model to the training data
         model.fit(X_train, y_train)
         # Predict the target values for the cross-validation set
         y_cv_pred = model.predict(X_cv)
          # Calculate accuracy, precision, and recall
         accuracy = accuracy_score(y_cv, y_cv_pred)
         precision = precision_score(y_cv, y_cv_pred)
         recall = recall_score(y_cv, y_cv_pred)
          # Store the results in the dictionary
         results[model_name] = {
              'accuracy': accuracy,
              'precision': precision,
              'recall': recall,
              'confusion_matrix': confusion_matrix(y_cv, y_cv_pred)
         }
```

```
/Users/charlieyang/anaconda3/lib/python3.11/site-
     packages/sklearn/neighbors/_classification.py:238: DataConversionWarning: A
     column-vector y was passed when a 1d array was expected. Please change the shape
     of y to (n_samples,), for example using ravel().
       return self. fit(X, y)
     /Users/charlieyang/anaconda3/lib/python3.11/site-
     packages/sklearn/utils/validation.py:1339: DataConversionWarning: A column-
     vector y was passed when a 1d array was expected. Please change the shape of y
     to (n_samples, ), for example using ravel().
       y = column_or_1d(y, warn=True)
     /Users/charlieyang/anaconda3/lib/python3.11/site-
     packages/sklearn/utils/validation.py:1339: DataConversionWarning: A column-
     vector y was passed when a 1d array was expected. Please change the shape of y
     to (n_samples, ), for example using ravel().
       y = column_or_1d(y, warn=True)
     /Users/charlieyang/anaconda3/lib/python3.11/site-
     packages/sklearn/linear_model/_logistic.py:469: ConvergenceWarning: lbfgs failed
     to converge (status=1):
     STOP: TOTAL NO. of ITERATIONS REACHED LIMIT.
     Increase the number of iterations (max_iter) or scale the data as shown in:
         https://scikit-learn.org/stable/modules/preprocessing.html
     Please also refer to the documentation for alternative solver options:
         https://scikit-learn.org/stable/modules/linear model.html#logistic-
     regression
       n_iter_i = _check_optimize_result(
     /Users/charlieyang/anaconda3/lib/python3.11/site-
     packages/sklearn/utils/validation.py:1339: DataConversionWarning: A column-
     vector y was passed when a 1d array was expected. Please change the shape of y
     to (n_samples, ), for example using ravel().
       y = column_or_1d(y, warn=True)
     /Users/charlieyang/anaconda3/lib/python3.11/site-packages/sklearn/base.py:1473:
     DataConversionWarning: A column-vector y was passed when a 1d array was
     expected. Please change the shape of y to (n_samples,), for example using
     ravel().
       return fit_method(estimator, *args, **kwargs)
[27]: # Print the results
      for model name, metrics in results.items():
          print(f"{model_name}:")
          print(f" Accuracy: {metrics['accuracy']:.4f}")
          print(f" Precision: {metrics['precision']:.4f}")
          print(f" Recall: {metrics['recall']:.4f}")
          print(f" Confusion Matrix:")
          print(f"
                           Predicted 0 Predicted 1")
          print(f"Actual 0
                             {metrics['confusion_matrix'][0, 0]}

→{metrics['confusion_matrix'][0, 1]}")
```

```
print(f"Actual 1 {metrics['confusion_matrix'][1, 0]}
  print()
knn:
  Accuracy: 0.4737
 Precision: 0.5612
 Recall: 0.2921
  Confusion Matrix:
        Predicted 0 Predicted 1
Actual 0
           147
                        61
Actual 1
           189
                        78
nb:
  Accuracy: 0.5537
 Precision: 0.5647
 Recall: 0.8989
  Confusion Matrix:
        Predicted 0 Predicted 1
Actual 0
           23
                       185
Actual 1
                       240
           27
log_reg:
  Accuracy: 0.5179
 Precision: 0.5864
 Recall: 0.4831
  Confusion Matrix:
        Predicted 0 Predicted 1
Actual 0
           117
                        91
Actual 1
           138
                        129
svm:
 Accuracy: 0.4400
 Precision: 0.5556
 Recall: 0.0187
  Confusion Matrix:
        Predicted 0 Predicted 1
           204
Actual 0
                        4
                        5
Actual 1
           262
dt:
  Accuracy: 0.4779
 Precision: 0.5333
 Recall: 0.5693
  Confusion Matrix:
        Predicted 0 Predicted 1
Actual 0
           75
                       133
```

152

Actual 1

115

```
rf:
       Accuracy: 0.4526
       Precision: 0.5294
       Recall: 0.2360
       Confusion Matrix:
              Predicted 0 Predicted 1
     Actual 0
                 152
                              56
     Actual 1
                 204
                              63
[28]: import tensorflow as tf
      from tensorflow.keras.models import Sequential
      from tensorflow.keras.layers import Dense, Dropout
      # Define the neural network model
      nn_model = Sequential([
          Dense(128, activation='relu', input_shape=(X_train.shape[1],)),
          Dropout(0.2),
          Dense(64, activation='relu'),
          Dropout(0.2),
          Dense(1, activation='sigmoid')
      ])
      # Compile the model
      nn_model.compile(optimizer='adam', loss='binary_crossentropy',_
       →metrics=['accuracy'])
      # Fit the model to the training data
      nn model.fit(X_train, y_train, epochs=50, batch_size=32, validation_data=(X_cv,_
       -y_cv))
     Epoch 1/50
     /Users/charlieyang/anaconda3/lib/python3.11/site-
     packages/keras/src/layers/core/dense.py:87: UserWarning: Do not pass an
     `input_shape`/`input_dim` argument to a layer. When using Sequential models,
     prefer using an `Input(shape)` object as the first layer in the model instead.
       super().__init__(activity_regularizer=activity_regularizer, **kwargs)
     119/119
                         1s 3ms/step -
     accuracy: 0.5218 - loss: 3066010.5000 - val_accuracy: 0.5095 - val_loss:
     145863.8125
     Epoch 2/50
     119/119
                         Os 2ms/step -
     accuracy: 0.5026 - loss: 315587.6250 - val_accuracy: 0.5642 - val_loss:
     2531.7805
     Epoch 3/50
     119/119
                         Os 2ms/step -
```

```
accuracy: 0.5248 - loss: 1870.0193 - val_accuracy: 0.5621 - val_loss: 0.6869
Epoch 4/50
119/119
                   Os 2ms/step -
accuracy: 0.5322 - loss: 35.4138 - val_accuracy: 0.5621 - val_loss: 0.6859
Epoch 5/50
119/119
                   Os 2ms/step -
accuracy: 0.5397 - loss: 28.0429 - val accuracy: 0.5621 - val loss: 0.6855
Epoch 6/50
119/119
                   Os 2ms/step -
accuracy: 0.5344 - loss: 29.7258 - val_accuracy: 0.5621 - val_loss: 0.6852
Epoch 7/50
119/119
                   0s 3ms/step -
accuracy: 0.5380 - loss: 16.1641 - val_accuracy: 0.5621 - val_loss: 0.6851
Epoch 8/50
119/119
                   Os 2ms/step -
accuracy: 0.5215 - loss: 1.7777 - val_accuracy: 0.5621 - val_loss: 0.6849
Epoch 9/50
119/119
                   0s 2ms/step -
accuracy: 0.5180 - loss: 0.7602 - val_accuracy: 0.5621 - val_loss: 0.6848
Epoch 10/50
                   Os 3ms/step -
119/119
accuracy: 0.5269 - loss: 0.6910 - val accuracy: 0.5621 - val loss: 0.6847
Epoch 11/50
119/119
                   Os 2ms/step -
accuracy: 0.5244 - loss: 0.6913 - val_accuracy: 0.5621 - val_loss: 0.6848
Epoch 12/50
119/119
                   Os 2ms/step -
accuracy: 0.5309 - loss: 49.4529 - val_accuracy: 0.5621 - val_loss: 0.6846
Epoch 13/50
119/119
                   Os 2ms/step -
accuracy: 0.5226 - loss: 162.0076 - val_accuracy: 0.5621 - val_loss: 0.6846
Epoch 14/50
119/119
                   Os 2ms/step -
accuracy: 0.5153 - loss: 0.6925 - val_accuracy: 0.5621 - val_loss: 0.6847
Epoch 15/50
119/119
                   Os 2ms/step -
accuracy: 0.5305 - loss: 0.6907 - val accuracy: 0.5621 - val loss: 0.6846
Epoch 16/50
                   Os 2ms/step -
119/119
accuracy: 0.5377 - loss: 0.6903 - val_accuracy: 0.5621 - val_loss: 0.6847
Epoch 17/50
119/119
                   0s 2ms/step -
accuracy: 0.5317 - loss: 0.6912 - val_accuracy: 0.5621 - val_loss: 0.6846
Epoch 18/50
119/119
                   Os 3ms/step -
accuracy: 0.5198 - loss: 0.9204 - val_accuracy: 0.5621 - val_loss: 0.6847
Epoch 19/50
119/119
                   Os 2ms/step -
```

```
accuracy: 0.5247 - loss: 0.6917 - val_accuracy: 0.5621 - val_loss: 0.6846
Epoch 20/50
119/119
                   Os 2ms/step -
accuracy: 0.5516 - loss: 0.6884 - val_accuracy: 0.5621 - val_loss: 0.6846
Epoch 21/50
119/119
                   Os 2ms/step -
accuracy: 0.5382 - loss: 0.6900 - val accuracy: 0.5621 - val loss: 0.6847
Epoch 22/50
119/119
                   Os 2ms/step -
accuracy: 0.5262 - loss: 1.4543 - val_accuracy: 0.5621 - val_loss: 0.6847
Epoch 23/50
119/119
                   0s 2ms/step -
accuracy: 0.5339 - loss: 0.6910 - val_accuracy: 0.5621 - val_loss: 0.6847
Epoch 24/50
119/119
                   Os 2ms/step -
accuracy: 0.5334 - loss: 0.6900 - val_accuracy: 0.5621 - val_loss: 0.6847
Epoch 25/50
119/119
                   Os 2ms/step -
accuracy: 0.5356 - loss: 0.6908 - val_accuracy: 0.5621 - val_loss: 0.6846
Epoch 26/50
                   Os 2ms/step -
119/119
accuracy: 0.5392 - loss: 0.6901 - val accuracy: 0.5621 - val loss: 0.6848
Epoch 27/50
119/119
                   Os 2ms/step -
accuracy: 0.5394 - loss: 0.6901 - val_accuracy: 0.5621 - val_loss: 0.6846
Epoch 28/50
119/119
                   Os 2ms/step -
accuracy: 0.5289 - loss: 0.6916 - val_accuracy: 0.5621 - val_loss: 0.6847
Epoch 29/50
119/119
                   Os 2ms/step -
accuracy: 0.5303 - loss: 0.6912 - val_accuracy: 0.5621 - val_loss: 0.6846
Epoch 30/50
119/119
                   Os 2ms/step -
accuracy: 0.5392 - loss: 0.6902 - val_accuracy: 0.5621 - val_loss: 0.6848
Epoch 31/50
119/119
                   Os 3ms/step -
accuracy: 0.5314 - loss: 0.6912 - val accuracy: 0.5621 - val loss: 0.6848
Epoch 32/50
                   Os 2ms/step -
119/119
accuracy: 0.5323 - loss: 0.6911 - val_accuracy: 0.5621 - val_loss: 0.6848
Epoch 33/50
119/119
                   0s 2ms/step -
accuracy: 0.5353 - loss: 0.6902 - val_accuracy: 0.5621 - val_loss: 0.6848
Epoch 34/50
119/119
                   Os 2ms/step -
accuracy: 0.5243 - loss: 0.6919 - val_accuracy: 0.5621 - val_loss: 0.6848
Epoch 35/50
119/119
                   Os 2ms/step -
```

```
accuracy: 0.5185 - loss: 0.6929 - val_accuracy: 0.5621 - val_loss: 0.6847
Epoch 36/50
119/119
                   Os 2ms/step -
accuracy: 0.5390 - loss: 0.6904 - val_accuracy: 0.5621 - val_loss: 0.6847
Epoch 37/50
119/119
                   Os 2ms/step -
accuracy: 0.5330 - loss: 0.6910 - val accuracy: 0.5621 - val loss: 0.6848
Epoch 38/50
119/119
                   Os 2ms/step -
accuracy: 0.5362 - loss: 0.6906 - val_accuracy: 0.5621 - val_loss: 0.6848
Epoch 39/50
119/119
                   0s 2ms/step -
accuracy: 0.5397 - loss: 0.6898 - val_accuracy: 0.5621 - val_loss: 0.6847
Epoch 40/50
119/119
                   Os 2ms/step -
accuracy: 0.5336 - loss: 0.6907 - val_accuracy: 0.5621 - val_loss: 0.6847
Epoch 41/50
119/119
                   Os 2ms/step -
accuracy: 0.5314 - loss: 0.6912 - val_accuracy: 0.5621 - val_loss: 0.6848
Epoch 42/50
119/119
                   Os 2ms/step -
accuracy: 0.5362 - loss: 0.6905 - val accuracy: 0.5621 - val loss: 0.6846
Epoch 43/50
119/119
                   Os 3ms/step -
accuracy: 0.5338 - loss: 0.6910 - val_accuracy: 0.5621 - val_loss: 0.6847
Epoch 44/50
119/119
                   Os 2ms/step -
accuracy: 0.5238 - loss: 0.6918 - val_accuracy: 0.5621 - val_loss: 0.6846
Epoch 45/50
119/119
                   Os 2ms/step -
accuracy: 0.5213 - loss: 0.6923 - val_accuracy: 0.5621 - val_loss: 0.6846
Epoch 46/50
119/119
                   Os 2ms/step -
accuracy: 0.5418 - loss: 0.6895 - val_accuracy: 0.5621 - val_loss: 0.6846
Epoch 47/50
119/119
                   Os 2ms/step -
accuracy: 0.5468 - loss: 0.6893 - val accuracy: 0.5621 - val loss: 0.6846
Epoch 48/50
119/119
                   Os 2ms/step -
accuracy: 0.5222 - loss: 0.6923 - val_accuracy: 0.5621 - val_loss: 0.6847
Epoch 49/50
119/119
                   0s 2ms/step -
accuracy: 0.5311 - loss: 0.6913 - val_accuracy: 0.5621 - val_loss: 0.6847
Epoch 50/50
119/119
                   Os 2ms/step -
accuracy: 0.5269 - loss: 0.6915 - val_accuracy: 0.5621 - val_loss: 0.6847
```

[28]: <keras.src.callbacks.history.History at 0x2ff934190>

This is predicting everything as 1, not helpful.

```
[]: from sklearn.discriminant_analysis import LinearDiscriminantAnalysis,_
     →QuadraticDiscriminantAnalysis
     from sklearn.metrics import accuracy_score, precision_score, recall_score,
      ⇔confusion matrix
     # Initialize the models
     lda = LinearDiscriminantAnalysis()
     qda = QuadraticDiscriminantAnalysis()
     # Dictionary to store the models
     discriminant_models = {'LDA': lda, 'QDA': qda}
     # Dictionary to store the results
     discriminant results = {}
     # Fit the models, predict, and calculate metrics
     for model_name, model in discriminant_models.items():
         model.fit(X train, y train)
         y_cv_pred = model.predict(X_cv)
         accuracy = accuracy_score(y_cv, y_cv_pred)
         precision = precision_score(y_cv, y_cv_pred)
         recall = recall_score(y_cv, y_cv_pred)
         conf_matrix = confusion_matrix(y_cv, y_cv_pred)
         discriminant_results[model_name] = {
             'accuracy': accuracy,
             'precision': precision,
             'recall': recall,
             'confusion_matrix': conf_matrix
         }
```

```
print(f"Actual 1 {metrics['confusion_matrix'][1, 0]}

→{metrics['confusion_matrix'][1, 1]}")
          print()
     LDA:
       Accuracy: 0.4442
       Precision: 0.5484
       Recall: 0.0637
       Confusion Matrix:
              Predicted 0 Predicted 1
     Actual 0
                 194
                              14
     Actual 1
                 250
                              17
     QDA:
       Accuracy: 0.5221
       Precision: 0.5641
       Recall: 0.6592
       Confusion Matrix:
              Predicted 0 Predicted 1
     Actual 0
                 72
                             136
     Actual 1
                 91
                              176
     Now, let's select some features:
[29]: rf.feature_importances_.shape
[29]: (3660,)
 []: # Get feature importances from the RandomForestClassifier
      feature_importances = rf.feature_importances_
      # Create a DataFrame to display the feature importances
      feature_importance_df = pd.DataFrame({
          'Feature': X.columns,
          'Importance': feature_importances
      })
      # Sort the DataFrame by importance in descending order
      feature_importance_df = feature_importance_df.sort_values(by='Importance',__
       →ascending=False)
      # Display the top 10 most important features
      print(feature_importance_df.head(50))
                         Feature Importance
     3553 df_tip_pct_change_-17
                                     0.001485
     3006 df_oih_pct_change_-24
                                     0.001450
     3378 df_lqd_pct_change_-12
                                    0.001423
```

```
3558
      df_tip_pct_change_-12
                                0.001415
3387
       df_lqd_pct_change_-3
                                0.001372
3282
      df_iyr_pct_change_-18
                                0.001311
3641
      df_gld_pct_change_-19
                                0.001276
3548
      df tip pct change -22
                                0.001254
3281
      df_iyr_pct_change_-19
                                0.001245
      df_spy_pct_change_-25
3095
                                0.001223
3289
      df_iyr_pct_change_-11
                                0.001216
3009
      df oih pct change -21
                                0.001213
                                0.001211
3379
      df_lqd_pct_change_-11
      df_oih_pct_change_-11
3019
                                0.001209
3451
      df_tlt_pct_change_-29
                                0.001207
3564
       df_tip_pct_change_-6
                                0.001193
3295
       df_iyr_pct_change_-5
                                0.001179
3118
       df_spy_pct_change_-2
                                0.001169
3381
       df_lqd_pct_change_-9
                                0.001165
3643
      df_gld_pct_change_-17
                                0.001163
3372
      df_lqd_pct_change_-18
                                0.001162
      df_gld_pct_change_-21
3639
                                0.001161
757
             VOL df spy -23
                                0.001150
3279
      df_iyr_pct_change_-21
                                0.001149
3108
      df spy pct change -12
                                0.001137
3368
      df_lqd_pct_change_-22
                                0.001136
3013
      df_oih_pct_change_-17
                                0.001132
3186
      df_qqq_pct_change_-24
                                0.001132
3187
      df_qqq_pct_change_-23
                                0.001112
1173
             VOL_df_oih_-27
                                0.001099
3545
      df_tip_pct_change_-25
                                0.001099
      df_lqd_pct_change_-16
3374
                                0.001095
3630
      df_gld_pct_change_-30
                                0.001094
3105
      df_spy_pct_change_-15
                                0.001091
3471
       df_tlt_pct_change_-9
                                0.001091
3461
      df_tlt_pct_change_-19
                                0.001088
3199
      df_qqq_pct_change_-11
                                0.001080
3650
      df gld pct change -10
                                0.001076
      df lqd pct change -29
3361
                                0.001075
3563
       df tip pct change -7
                                0.001072
3092
      df_spy_pct_change_-28
                                0.001068
      df_iyr_pct_change_-24
3276
                                0.001064
3191
                                0.001061
      df_qqq_pct_change_-19
3363
      df_lqd_pct_change_-27
                                0.001057
3463
      df_tlt_pct_change_-17
                                0.001056
2237
             VOL_df_gld_-13
                                0.001054
3638
      df_gld_pct_change_-22
                                0.001053
3015
      df_oih_pct_change_-15
                                0.001051
3453
      df_tlt_pct_change_-27
                                0.001050
3457
      df_tlt_pct_change_-23
                                0.001047
```

```
[37]: # Remove the last 4 characters from the feature names to group them
      feature_importance_df['Grouped_Feature'] = feature_importance_df['Feature'].
       ⇔str[:-4]
      # Group by the new feature names and sum the importances
      grouped_feature_importance_df = feature_importance_df.
       ⇒groupby('Grouped_Feature')['Importance'].sum().reset_index()
      # Sort the DataFrame by importance in descending order
      grouped_feature_importance_df = grouped_feature_importance_df.
       sort_values(by='Importance', ascending=False)
      # Display the top 10 most important grouped features
      print(grouped_feature_importance_df.head(20))
            Grouped_Feature Importance
     230
                               0.020284
                        vxn
     155 df_iyr_pct_change
                               0.019724
     149 df_gld_pct_change
                              0.019229
         df_tip_pct_change
     185
                              0.019136
     161 df_lqd_pct_change
                              0.019101
     226
                              0.019029
                        vxd
     167 df_oih_pct_change
                              0.018711
     191 df_tlt_pct_change
                              0.018677
     173 df_qqq_pct_change
                              0.018224
     221
                        vix
                               0.018163
     179 df_spy_pct_change
                              0.017930
     103
                 VOL_df_oih
                             0.014378
     97
                 VOL_df_gld
                              0.013865
                 VOL_df_tip
     109
                              0.013256
     111
                 VOL_df_tlt
                              0.013107
     107
                 VOL_df_spy
                              0.012717
                 VOL df iyr
     99
                               0.012299
     105
                 VOL_df_qqq
                               0.011846
     101
                 VOL df lqd
                               0.011439
     228
                       vxdl
                               0.009299
[46]: # Keep the top 19 grouped features
      top_19_grouped_features = grouped_feature_importance_df.
       ⇔head(19)['Grouped_Feature'].tolist()
      # Filter the columns in X based on the top 19 grouped features
      top_19_columns = [col for col in X.columns if any(feature in col for feature in_
       →top_19_grouped_features)]
      # Create a new DataFrame with only the top 19 columns
```

X_top_19 = X[top_19_columns]

```
X_train_top_19 = X_train[top_19_columns]
      X_cv_{top_19} = X_cv[top_19_columns]
      # Display the first few rows to verify
     print(X_top_19.head())
        vixo_-30 vixo_-29 vixo_-28 vixo_-27 vixo_-26 vixo_-25 vixo_-24
     0
           12.34
                      12.26
                                11.78
                                          11.42
                                                     11.41
                                                               11.53
                                                                         12.25
     1
           12.26
                      11.78
                                11.42
                                          11.41
                                                     11.53
                                                               12.25
                                                                         11.61
     2
           11.78
                     11.42
                                          11.53
                                                     12.25
                                                               11.61
                                                                         12.25
                                11.41
     3
           11.42
                     11.41
                               11.53
                                          12.25
                                                    11.61
                                                               12.25
                                                                         12.42
                                          11.61
                                12.25
                                                     12.25
                                                                         13.39
     4
           11.41
                     11.53
                                                               12.42
        vixo_-23 vixo_-22 vixo_-21 ... df_gld_pct_change_-10
     0
           11.61
                      12.25
                                12.42 ...
                                                        0.002363
     1
           12.25
                      12.42
                                13.39 ...
                                                       -0.009229
     2
           12.42
                      13.39
                                14.01 ...
                                                        0.003077
     3
           13.39
                     14.01
                                13.98 ...
                                                        0.009827
     4
           14.01
                      13.98
                                14.09
                                                        0.000701
        df_gld_pct_change_-9 df_gld_pct_change_-8 df_gld_pct_change_-7 \
     0
                   -0.009229
                                           0.003077
                                                                  0.009827
                                           0.009827
                                                                  0.000701
     1
                     0.003077
     2
                     0.009827
                                           0.000701
                                                                 -0.006866
     3
                     0.000701
                                          -0.006866
                                                                  0.002342
     4
                    -0.006866
                                           0.002342
                                                                  0.003285
        df_gld_pct_change_-6
                               df_gld_pct_change_-5 df_gld_pct_change_-4
     0
                     0.000701
                                          -0.006866
                                                                  0.002342
     1
                    -0.006866
                                           0.002342
                                                                  0.003285
     2
                     0.002342
                                           0.003285
                                                                 -0.000468
     3
                     0.003285
                                          -0.000468
                                                                  0.000237
     4
                    -0.000468
                                           0.000237
                                                                  0.000238
        df_gld_pct_change_-3 df_gld_pct_change_-2 df_gld_pct_change_-1
     0
                                                                  0.000237
                     0.003285
                                          -0.000468
     1
                    -0.000468
                                           0.000237
                                                                  0.000238
     2
                     0.000237
                                           0.000238
                                                                 -0.001423
     3
                     0.000238
                                          -0.001423
                                                                  0.002879
                    -0.001423
                                           0.002879
                                                                 -0.002894
     [5 rows x 840 columns]
[47]: knn2 = make pipeline(StandardScaler(), KNeighborsClassifier())
      nb2 = GaussianNB()
      log_reg2 = make_pipeline(StandardScaler(), LogisticRegression())
      svm2 = make_pipeline(StandardScaler(), SVC(kernel='linear', random_state=37))
```

```
dt2 = DecisionTreeClassifier(random_state=37)
rf2 = RandomForestClassifier(random_state=37)
models2= {'knn': knn2, 'nb': nb2, 'log_reg': log_reg2, 'svm': svm2, 'dt': dt2, \( \to \'rf': rf2\)}
```

```
[48]: # Dictionary to store the results
      results2 = {}
      # Iterate over each model in the models set
      for model name, model in models2.items():
          # Fit the model to the training data
          model.fit(X_train_top_19, y_train)
          # Predict the target values for the cross-validation set
          y_cv_pred = model.predict(X_cv_top_19)
          # Calculate accuracy, precision, and recall
          accuracy = accuracy_score(y_cv, y_cv_pred)
          precision = precision_score(y_cv, y_cv_pred)
          recall = recall_score(y_cv, y_cv_pred)
          # Store the results in the dictionary
          results2[model name] = {
              'accuracy': accuracy,
              'precision': precision,
              'recall': recall,
              'confusion_matrix': confusion_matrix(y_cv, y_cv_pred)
          }
```

```
/Users/charlieyang/anaconda3/lib/python3.11/site-
packages/sklearn/neighbors/_classification.py:238: DataConversionWarning: A
column-vector y was passed when a 1d array was expected. Please change the shape
of y to (n_samples,), for example using ravel().
  return self._fit(X, y)
/Users/charlieyang/anaconda3/lib/python3.11/site-
packages/sklearn/utils/validation.py:1339: DataConversionWarning: A column-
vector y was passed when a 1d array was expected. Please change the shape of y
to (n_samples, ), for example using ravel().
  y = column_or_1d(y, warn=True)
/Users/charlieyang/anaconda3/lib/python3.11/site-
packages/sklearn/utils/validation.py:1339: DataConversionWarning: A column-
vector y was passed when a 1d array was expected. Please change the shape of y
to (n_samples, ), for example using ravel().
 y = column_or_1d(y, warn=True)
/Users/charlieyang/anaconda3/lib/python3.11/site-
packages/sklearn/linear_model/_logistic.py:469: ConvergenceWarning: lbfgs failed
to converge (status=1):
```

```
STOP: TOTAL NO. of ITERATIONS REACHED LIMIT.
     Increase the number of iterations (max_iter) or scale the data as shown in:
         https://scikit-learn.org/stable/modules/preprocessing.html
     Please also refer to the documentation for alternative solver options:
         https://scikit-learn.org/stable/modules/linear_model.html#logistic-
     regression
       n_iter_i = _check_optimize_result(
     /Users/charlieyang/anaconda3/lib/python3.11/site-
     packages/sklearn/utils/validation.py:1339: DataConversionWarning: A column-
     vector y was passed when a 1d array was expected. Please change the shape of y
     to (n_samples, ), for example using ravel().
       y = column_or_1d(y, warn=True)
     /Users/charlieyang/anaconda3/lib/python3.11/site-packages/sklearn/base.py:1473:
     DataConversionWarning: A column-vector y was passed when a 1d array was
     expected. Please change the shape of y to (n_samples,), for example using
     ravel().
       return fit_method(estimator, *args, **kwargs)
[57]: # Print the results
      for (model_name, metrics), (model_name2, metrics2) in zip(results.items(),__
       →results2.items()):
          print(f"{model_name}:")
          print(f" Accuracy: {metrics['accuracy']:.4f} -> {metrics2['accuracy']:.

4f}")

          print(f" Precision: {metrics['precision']:.4f} -> {metrics2['precision']:.
       <4f}")
          print(f" Recall: {metrics['recall']:.4f} -> {metrics2['recall']:.4f}")
          print(f" Confusion Matrix:")
                           Predicted 0 Predicted 1")
          print(f"
          print(f"Actual 0
                             {metrics['confusion_matrix'][0, 0]} ->__
       →{metrics2['confusion matrix'][0, 0]} {metrics['confusion matrix'][0, 1]} ->⊔

¬{metrics2['confusion_matrix'][0, 1]}")
          print(f"Actual 1
                             {metrics['confusion_matrix'][1, 0]} ->__
       →{metrics2['confusion_matrix'][1, 0]} {metrics['confusion_matrix'][1, 1]} ->_

→{metrics2['confusion_matrix'][1, 1]}")
          print()
     knn:
       Accuracy: 0.4737 -> 0.5053
       Precision: 0.5612 -> 0.5734
       Recall: 0.2921 -> 0.4682
       Confusion Matrix:
               Predicted 0 Predicted 1
     Actual 0 147 -> 115 61 -> 93
     Actual 1
                189 -> 142 78 -> 125
```

nb:

Accuracy: 0.5537 -> 0.5537 Precision: 0.5647 -> 0.5653 Recall: 0.8989 -> 0.8914

Confusion Matrix:

Predicted 0 Predicted 1
Actual 0 23 -> 25 185 -> 183
Actual 1 27 -> 29 240 -> 238

log_reg:

Accuracy: 0.5179 -> 0.4926 Precision: 0.5864 -> 0.5551 Recall: 0.4831 -> 0.4906

Confusion Matrix:

Predicted 0 Predicted 1
Actual 0 117 -> 103 91 -> 105
Actual 1 138 -> 136 129 -> 131

svm:

Accuracy: 0.4400 -> 0.4842 Precision: 0.5556 -> 0.5478 Recall: 0.0187 -> 0.4719

Confusion Matrix:

Predicted 0 Predicted 1
Actual 0 204 -> 104 4 -> 104
Actual 1 262 -> 141 5 -> 126

dt:

Accuracy: 0.4779 -> 0.4842 Precision: 0.5333 -> 0.5724 Recall: 0.5693 -> 0.3258

Confusion Matrix:

Predicted 0 Predicted 1
Actual 0 75 -> 143 133 -> 65
Actual 1 115 -> 180 152 -> 87

rf:

Accuracy: 0.4526 -> 0.4884 Precision: 0.5294 -> 0.5411 Recall: 0.2360 -> 0.5918

Confusion Matrix:

Predicted 0 Predicted 1
Actual 0 152 -> 74 56 -> 134
Actual 1 204 -> 109 63 -> 158

Improvement is minimal or non-exisiting.

```
[]: # Save the DataFrames to pickle files

X.to_pickle('X.pkl')

X_train.to_pickle('X_train.pkl')

X_cv.to_pickle('X_cv.pkl')

X_test.to_pickle('X_test.pkl')

y.to_pickle('y.pkl')

y_train.to_pickle('y_train.pkl')

y_cv.to_pickle('y_cv.pkl')

y_test.to_pickle('y_test.pkl')

[28]: prices.to_pickle('prices.pkl')

prices_train.to_pickle('prices_train.pkl')

prices_cv.to_pickle('prices_cv.pkl')

prices_test.to_pickle('prices_test.pkl')
```