



# Multilabel Classification and Deep Learning

Zachary Chase Lipton

**Critical Review of RNNs:**

<http://arxiv.org/abs/1506.00019>

**Learning to Diagnose:**

<http://arxiv.org/abs/1511.03677>

**Conditional Generative RNNS:**

<http://arxiv.org/abs/1511.03683>

# Outline

- **Introduction to Multilabel Learning**
- Evaluation
- Efficient Learning & Sparse Models
- Deep Learning for Multilabel Classification
- Classifying Multilabel Time Series with RNNs

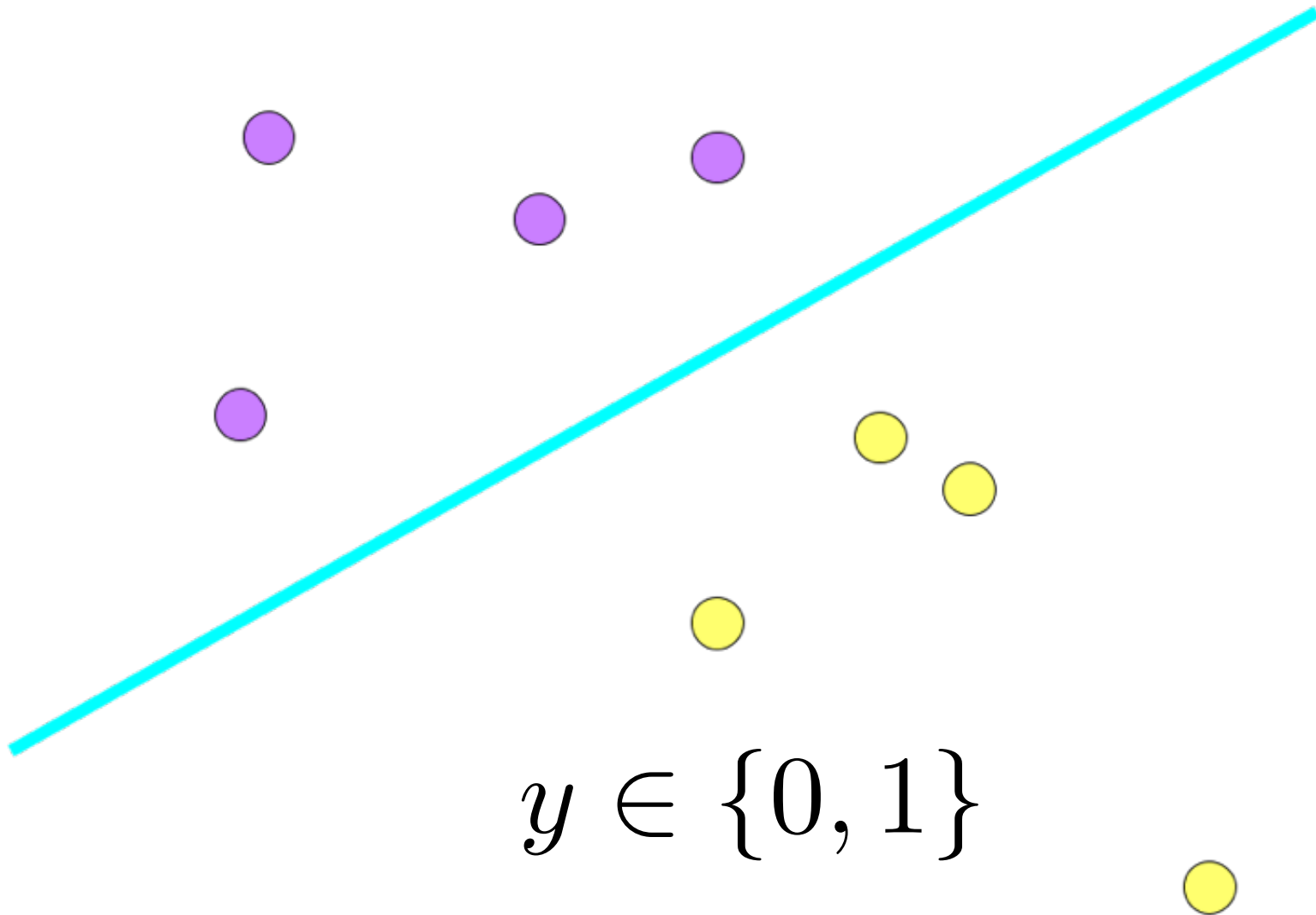
# Supervised Learning

- General problem, desire a labeling function

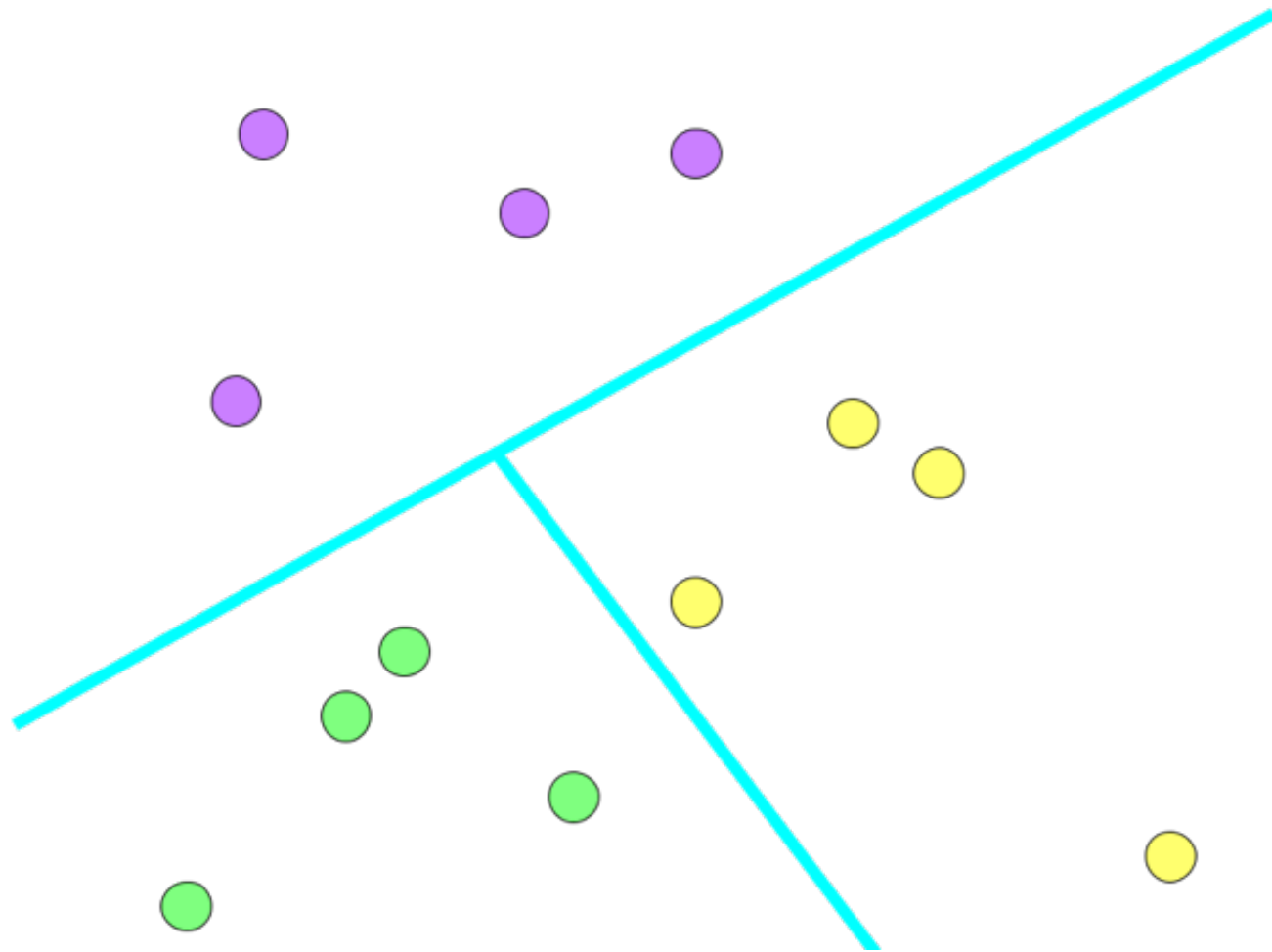
$$f : \mathcal{X} \rightarrow \mathcal{Y}$$

- ERM principle - choose the model  $\hat{f}$  in hypothesis class  $\mathcal{H}$  that minimizes loss on the training sample  $S \in \{\mathcal{X} \times \mathcal{Y}\}^n$
- Most research assumes simplest case  
 $\mathcal{X} = \mathcal{R}^d, \mathcal{Y} = \{0, 1\}$
- Real world much messier

# Binary Classification

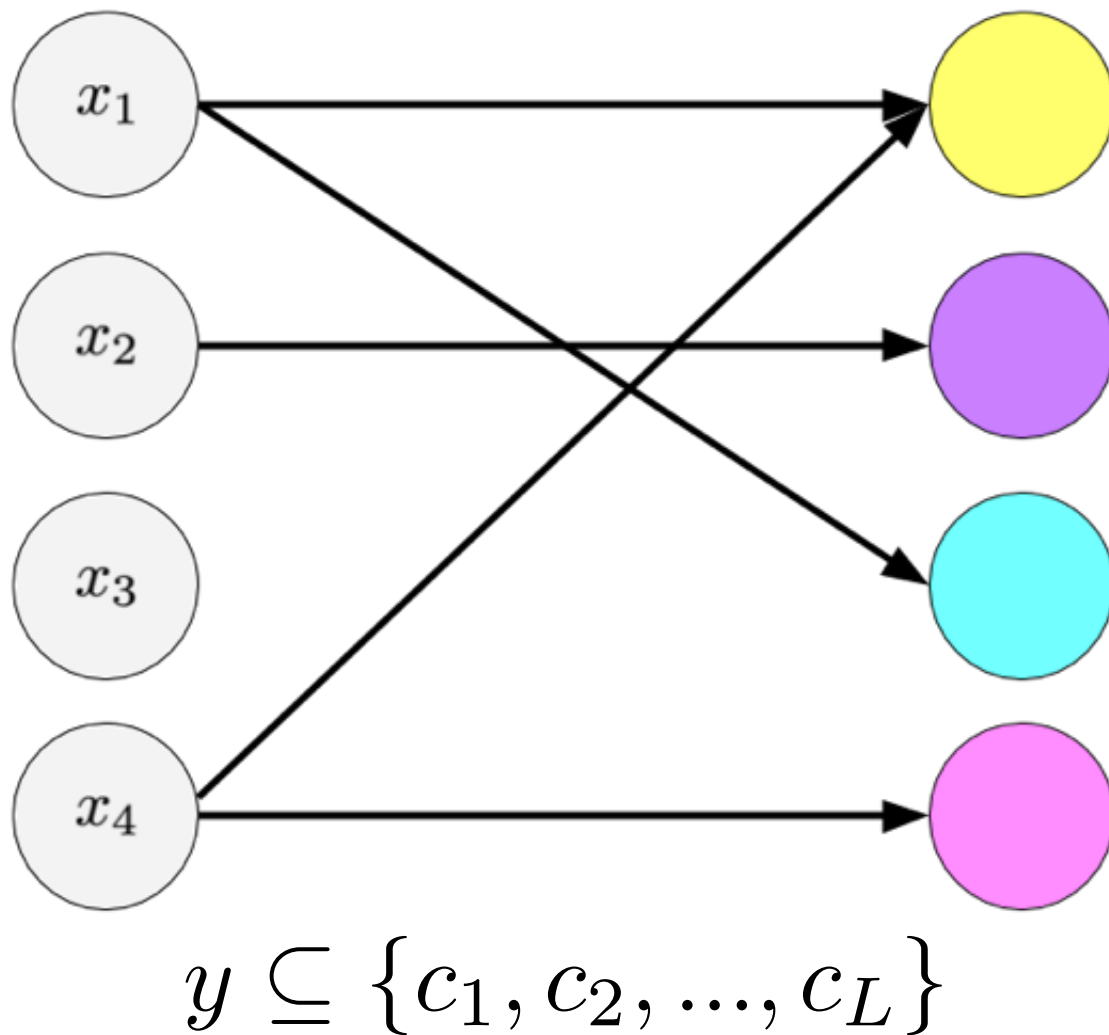


# Multiclass Classification



$$y \in \{c_1, c_2, \dots, c_L\}$$

# Multilabel Classification



# Why Multilabel?

- **Superset of both BC and MC:**  
BC when  $|L| = 1$ , MC when  $y \in L$
- **Natural for many real problems:**  
Clinical diagnosis  
Predicting purchases  
Auto-tagging news articles  
Activity recognition  
Object detection
- **Easy to formulate:**  
Take  $L$  tasks and slap them together

# Naive Baseline

- **Binary relevance:**

Separately train  $|L|$  classifiers  $f_l : \mathcal{X} \rightarrow \{0, 1\}$

- **Pros:**

Simple to execute, easy to understand  
strong baseline

- **Cons:**

Computational cost:  $|L| \times$

Leaves some information on the table (correlation betw. labels)



# Challenges

- **Efficiency**

Develop classifiers that do not scale in time or space complexity with the number of labels

- **Performance**

Make use of the extra labels to achieve better accuracy, generalization

- **Evaluation**

How do we evaluate a multilabel classifier's performance across 10s, 100s, 1000s, or even 1M labels?

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# Why not accuracy?

- **Often extreme class imbalance**

When blind classifier gets 99.99%,  
can be optimal to be uninformative

- **Varying base rates across labels**

E.g.: MeSH dataset: Human applies to 71% of  
articles, platypus in  $<.0001\%$

# F1 Score

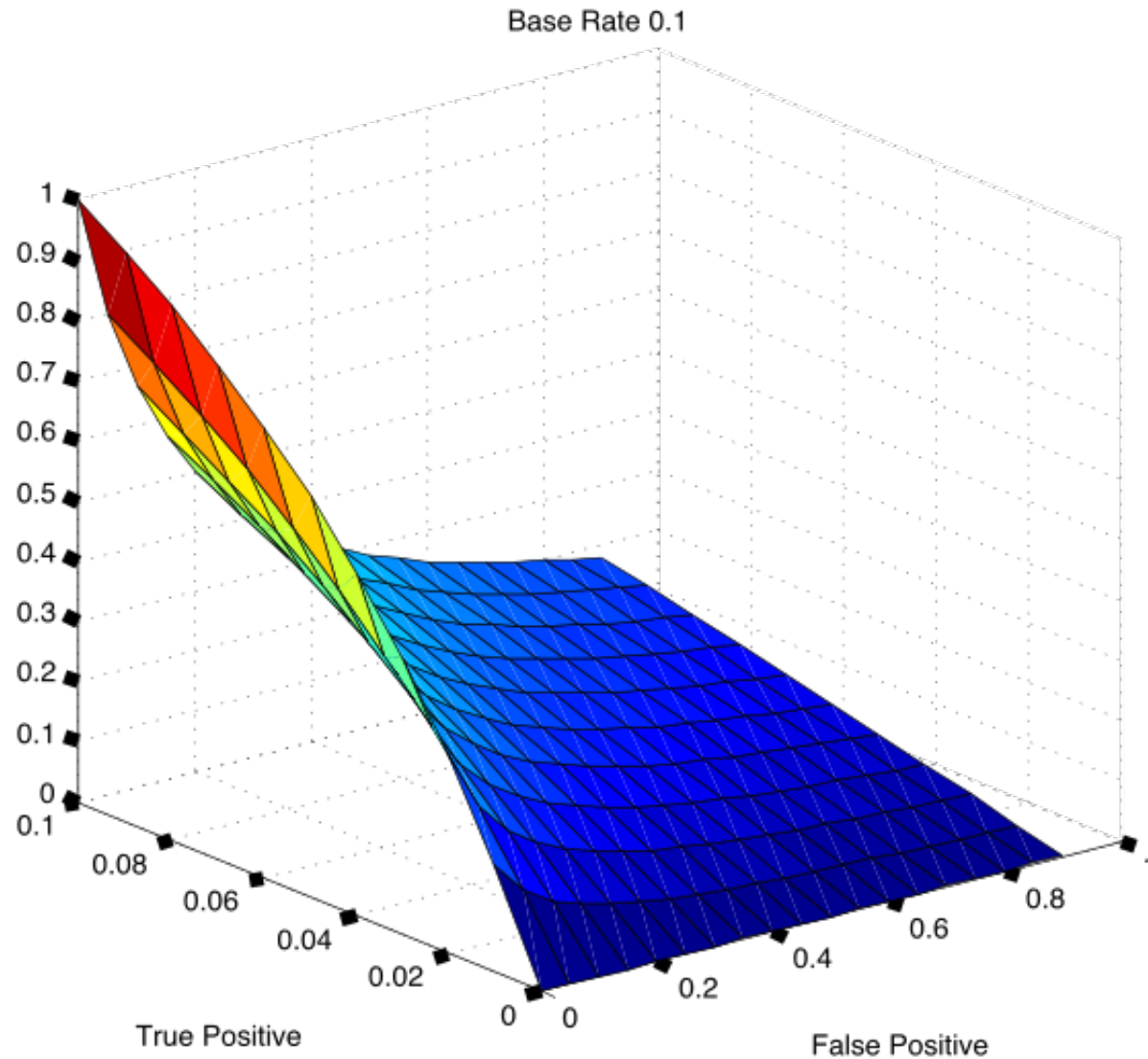
- Easy to calculate from confusion matrix

|             | Actual + | Actual - |
|-------------|----------|----------|
| Predicted + | $tp$     | $fp$     |
| Predicted - | $fn$     | $tn$     |

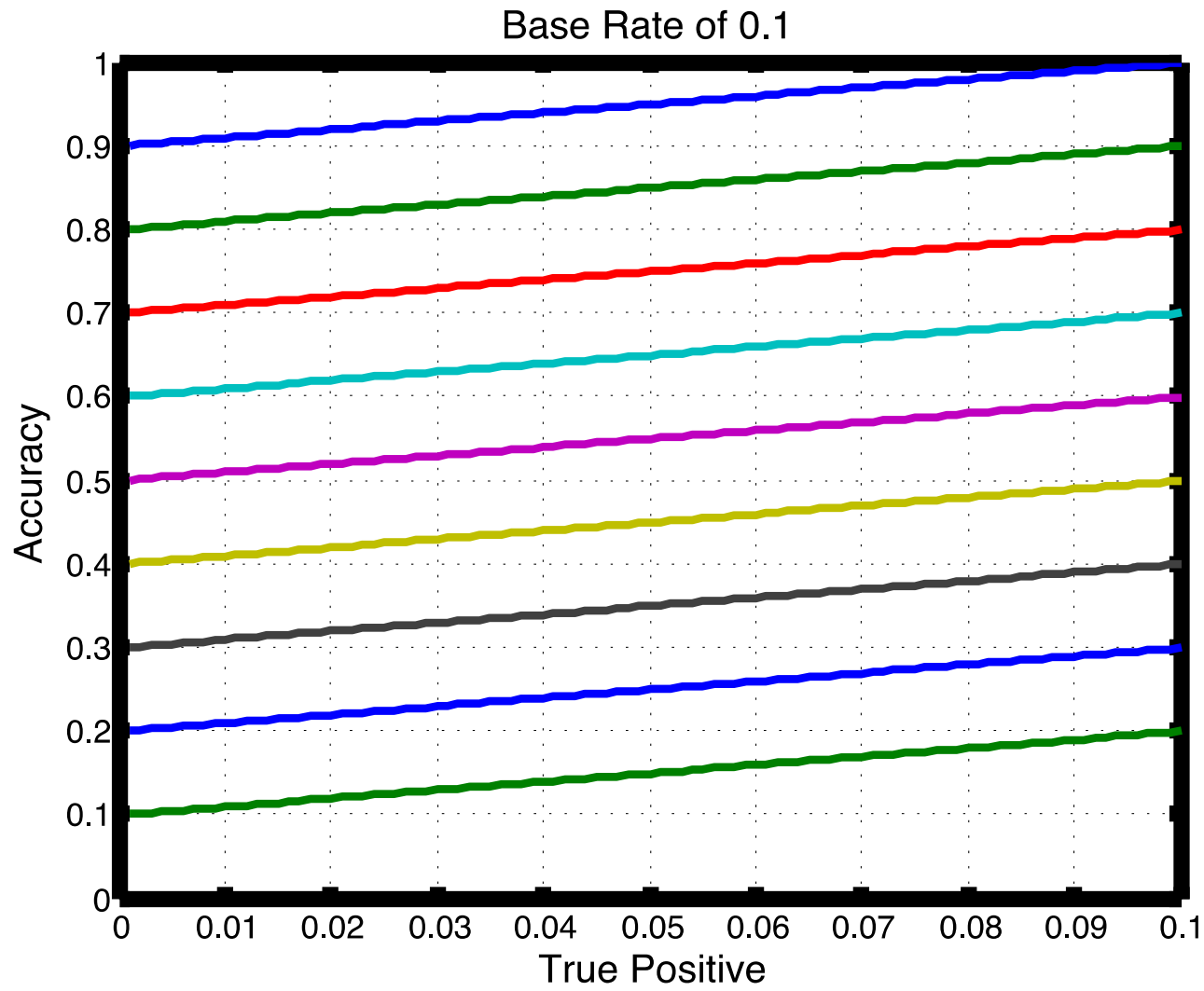
- Harmonic mean of precision  $\frac{tp}{tp + fp}$  and recall  $\frac{tp}{tp + fn}$

$$F1 = \frac{2 \cdot tp}{2 \cdot tp + fp + fn}$$

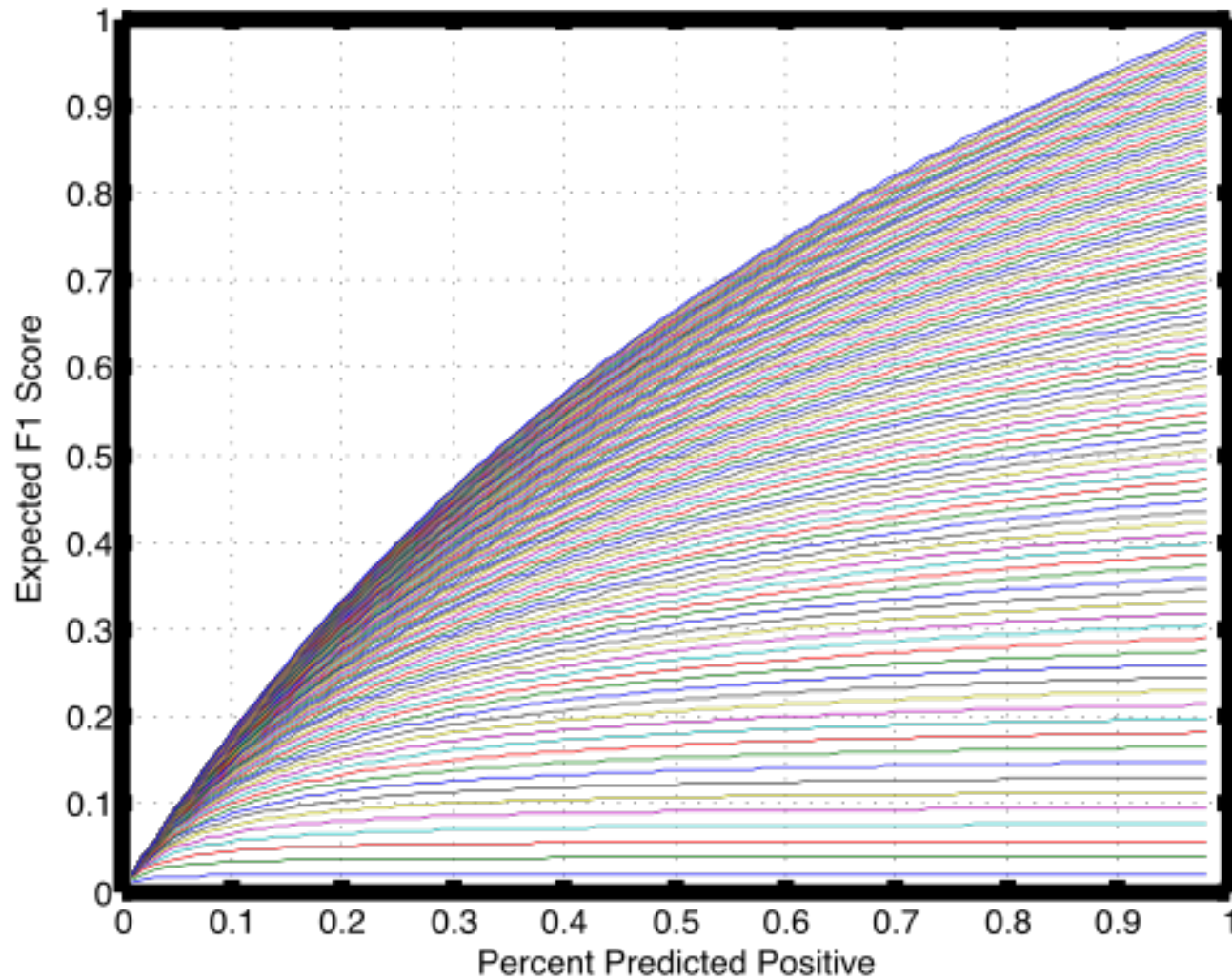
# F1 given fixed base rate



# Compared to Accuracy



# Expected F1 for Uninformative Classifier



# Multilabel Variations

Micro F1 calculated over all entries

| Example 1 | TP | FP | FN | TN |
|-----------|----|----|----|----|
| Example 2 | FP | FP | FN | TP |
| Example 3 | FN | TP | FN | FP |
| ...       | TN | TP | TP | TN |



# Macro F1

- Macro: F1 calculated separately for each label and averaged

|           | Label 1 | Label 2 | Label 3 | Label 4 |
|-----------|---------|---------|---------|---------|
| Example 1 | TP      | FP      | FN      | TN      |
| Example 2 | FP      | FP      | FN      | TP      |
| Example 3 | FN      | TP      | FN      | FP      |
| ...       | TN      | TP      | TP      | TN      |

# Characterizing the Optimal Threshold

- Threshold can be expressed in terms of the conditional probabilities of scores given labels

$$\frac{b \cdot p(s|t = 1)}{(1 - b) \cdot p(s|t = 0)} \geq J$$

- When scores are calibrated probabilities, optimal threshold is precisely half the F1 it achieves.

$$s \geq \frac{tp}{2tp + fn + fp} = \frac{F}{2}$$

# Problems with F1

- Sensitive to thresholding strategy
- Hard to tell who has the best algorithms and who is smart about thresholding
- Micro-F1 biased towards common labels
- Macro-F1 biased against them

# Some alternatives

- Any threshold indicates a cost sensitivity:  
When you know the cost, specify it and use weighted accuracy
- AUC exhibits same dynamic range for every label  
(blind classifier gets 0, perfect is 1)
- Macro-averaged AUC scores may give a better sense of performance across all labels

**\*\*high AUC for rare labels can be misleading.  
can achieve AUC of .99 produce useless results for IR**

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# The problem

- With many labels, binary relevance models can be huge and slow
- 10k labels + 1M features = 80GB of parameters
- We want compact models  
Fast to train and evaluate, cheap to store

# Linear Regression

- The bulk of computation is label agnostic (compute inverse  $(X^T X)^{-1}$ )

$$\theta = (X^T X)^{-1} X^T b$$

$$\theta = (X^T X)^{-1} X^T B$$

- Can do this especially fast when we reduce dimensionality of  $X$  via SVD.
- Problem: Unsupervised dim reduction -> lose signal of rare features -> mess up rare labels

# Sparsity

- For auto-tagging tasks, features are often high-dimensional sparse bag-of-words or n-grams



- Datasets for web-scale information retrieval tasks are large in the number of examples, thus SGD is the default optimization procedure
- Absent regularization, the gradient is sparse and training is fast
- Regularization destroys the sparsity of the gradient
- Number of features and labels are large, dense stochastic updates are computationally infeasible



# Regularization

- Goals: achieve model sparsity, prevent overfitting
- $\ell_1$  regularization induces sparse models
- $\ell_2^2$  regularization is thought to achieve more accurate models in practice
- Elastic net, balances the two

$$F(\mathbf{w}) = L(\mathbf{w}) + \lambda_1 \cdot |\mathbf{w}|_1 + \frac{1}{2} \lambda_2 \cdot |\mathbf{w}|_2^2$$

# Balancing Regularization with Efficiency

- To regularize while maintaining efficiency, can use a lazy updating scheme, first described by Carpenter (2008)
- For each feature, remember the last time it was nonzero
- When a feature is nonzero at some step  $t+k$ , perform a closed form update
- We derive lazy updates for elastic net regularization on both standard SGD and FoBoS (Duchi & Singer)

# Lazy Updates for Elastic Net

**Theorem 1** *To bring the weight  $w_j$  current from time  $\psi_j$  to time  $k$  using SGD, the constant time update is*

$$w_j^{(k)} = \text{sgn}(w_j^{(\psi_j)}) \left[ |w_j^{(\psi_j)}| \frac{P(k-1)}{P(\psi_j-1)} - P(k-1) \cdot (B(k-1) - B(\psi_j-1)) \right]_+ \quad (1)$$

where  $P(t) = (1 - \eta^{(t)}\lambda_2) \cdot P(t-1)$  with base case  $P(-1) = 1$  and  $B(t) = \sum_{\tau=0}^t \eta^{(\tau)} / P(\tau-1)$  with base case  $B(-1) = 0$ .

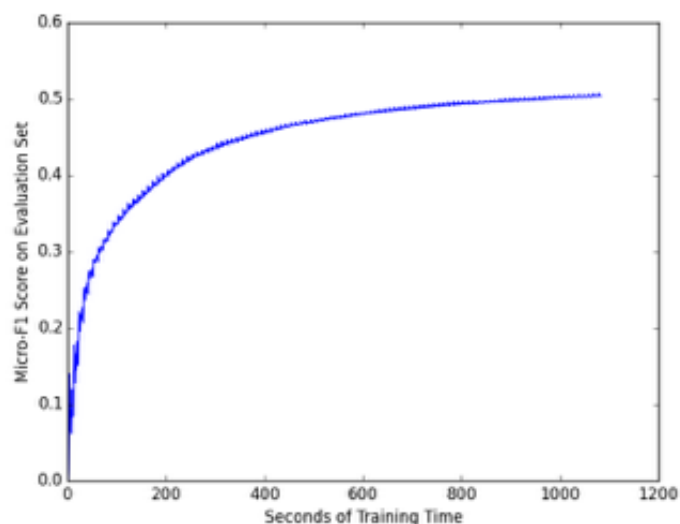
**Theorem 2** *A constant-time lazy update for FoBoS with elastic net regularization and decreasing learning rate to bring a weight current at time  $k$  from time  $\psi_j$  is*

$$w_j^{(k)} = \text{sgn}(w_j^{(\psi_j)}) \left[ |w_j^{(\psi_j)}| \frac{\Phi(k-1)}{\Phi(\psi_j-1)} - \Phi(k-1) \cdot \lambda_1 (\beta(k-1) - \beta(\psi_j-1)) \right]_+ \quad (2)$$

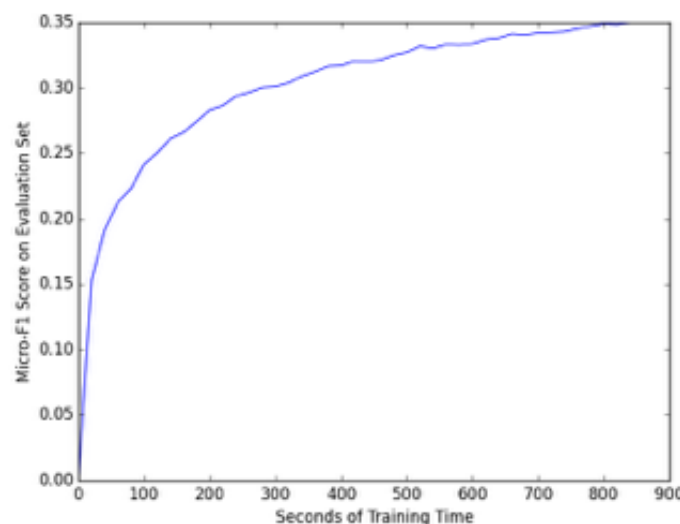
where  $\Phi(t) = \Phi(t-1) \cdot \frac{1}{1+\eta^t\lambda_2}$  with base case  $\Phi(-1) = 1$  and  $\beta(t) = \beta(t-1) + \frac{\eta^{(t)}}{\Phi(t-1)}$  with base case  $\beta(-1) = 0$ .

# Empirical Validation

- On two largest datasets in Mulan repository of multilabel datasets, we can train to convergence on a laptop in just minutes
- *rcv1*: 490x speedup, *bookmarks*: 20x speedup



rcv1



bookmarks

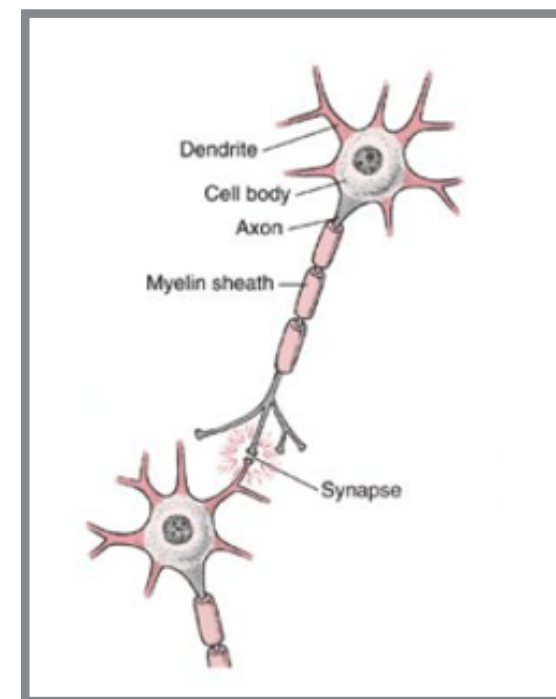
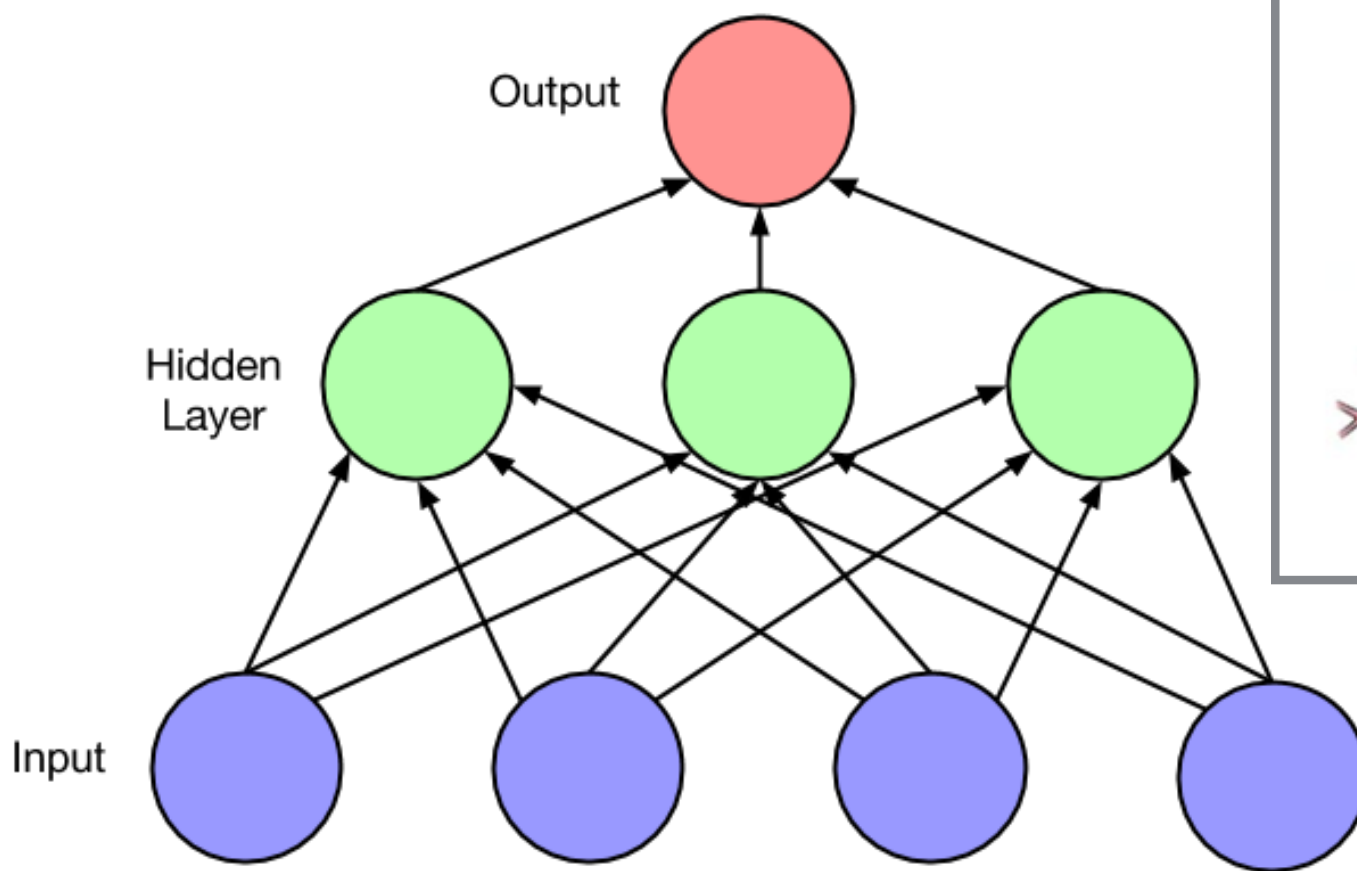
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# Performance

- Efficiency is nice, but we'd also like performance
- Neural networks can learn *shared representations* across labels.
- Both regularizes each label's model and exploits correlations between labels
- In extreme multilabel, may use significantly less parameters than logistic regression

# Neural Network



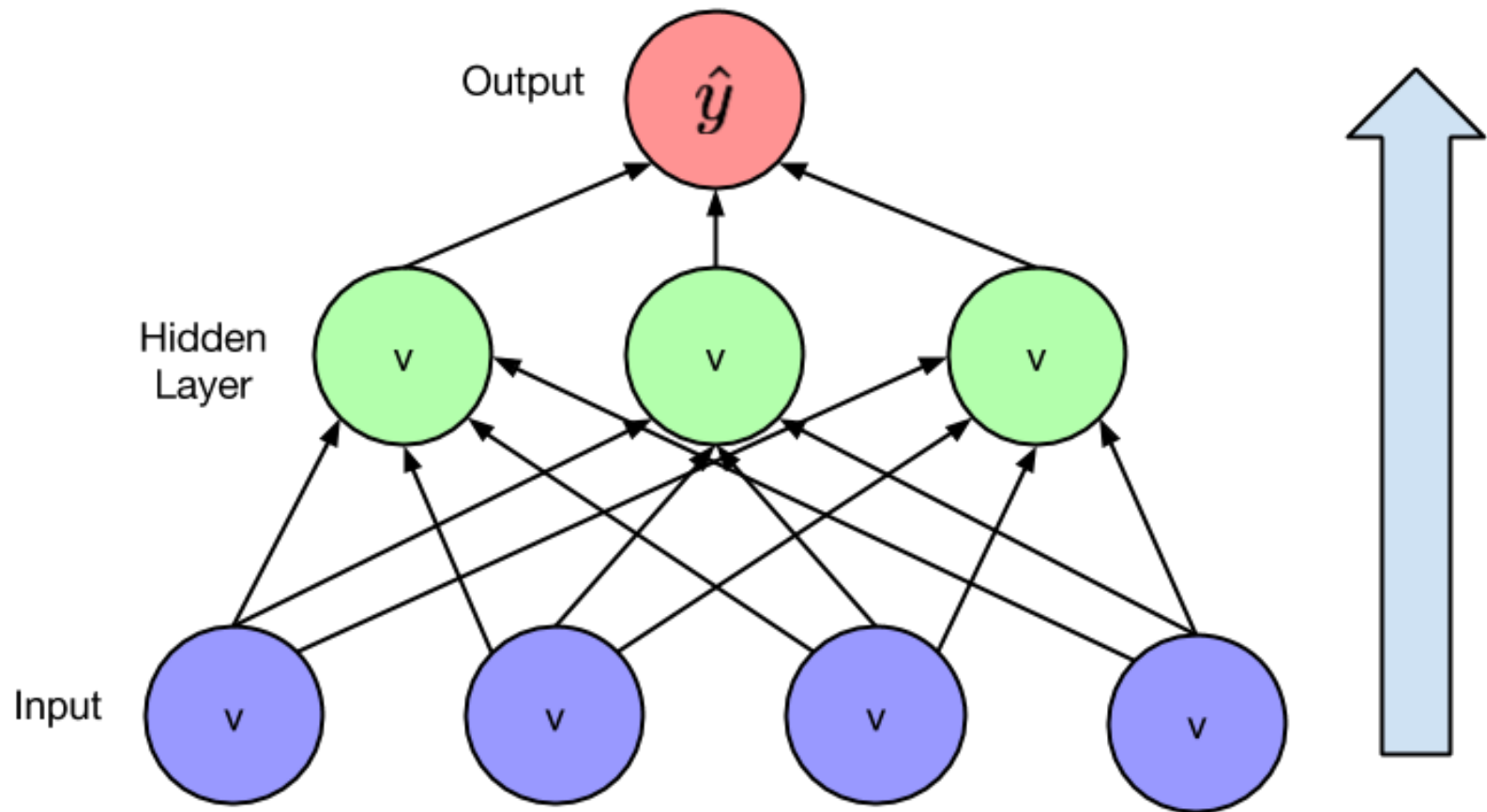
# Training w Backpropagation

- Goal: calculate the derivative of loss function with respect to each parameter (weight) in the model
- Update the weights by gradient following:

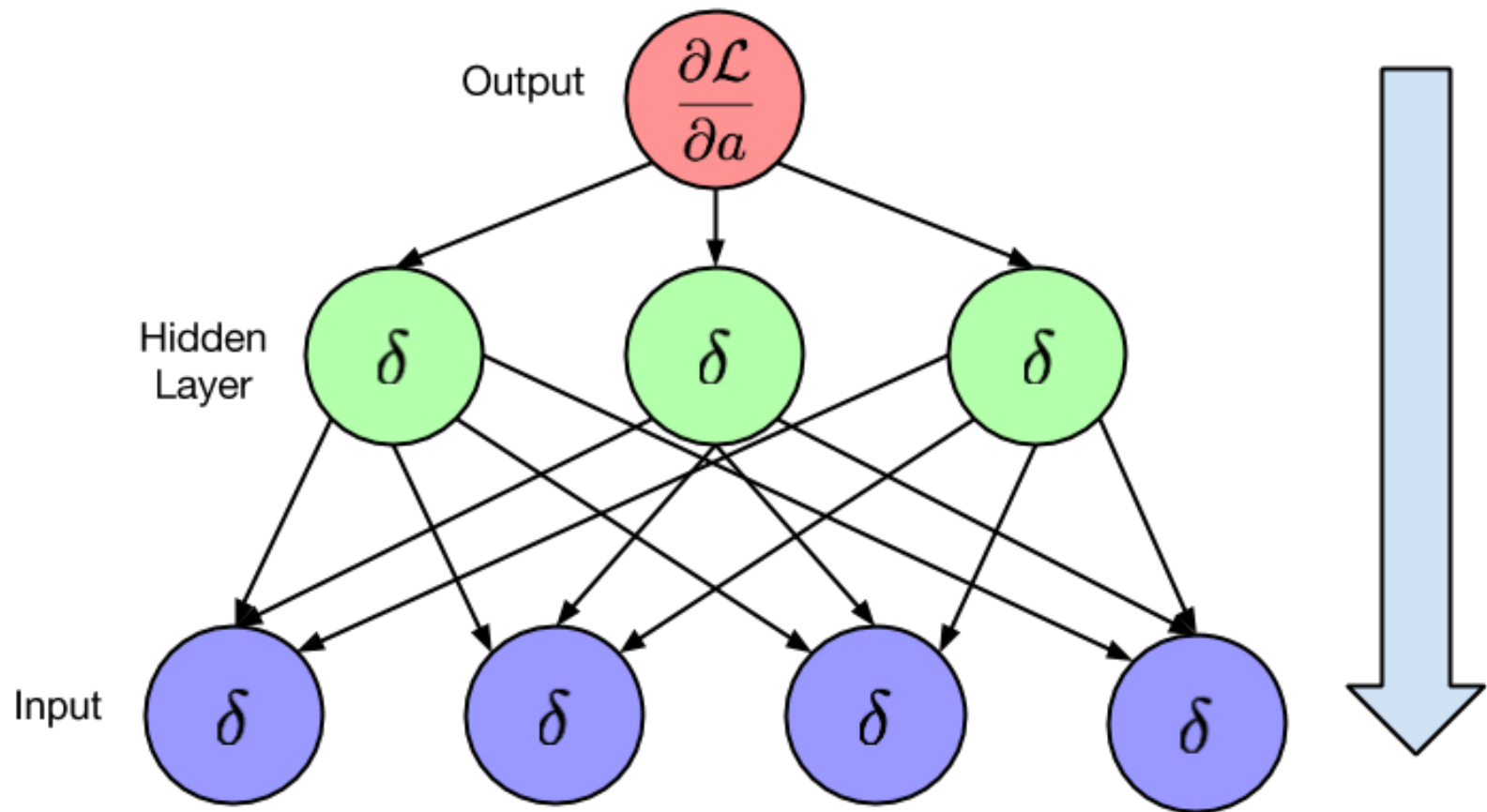
$$\boldsymbol{w} \leftarrow \boldsymbol{w} - \eta \nabla_{\boldsymbol{w}} \mathcal{L}_i$$



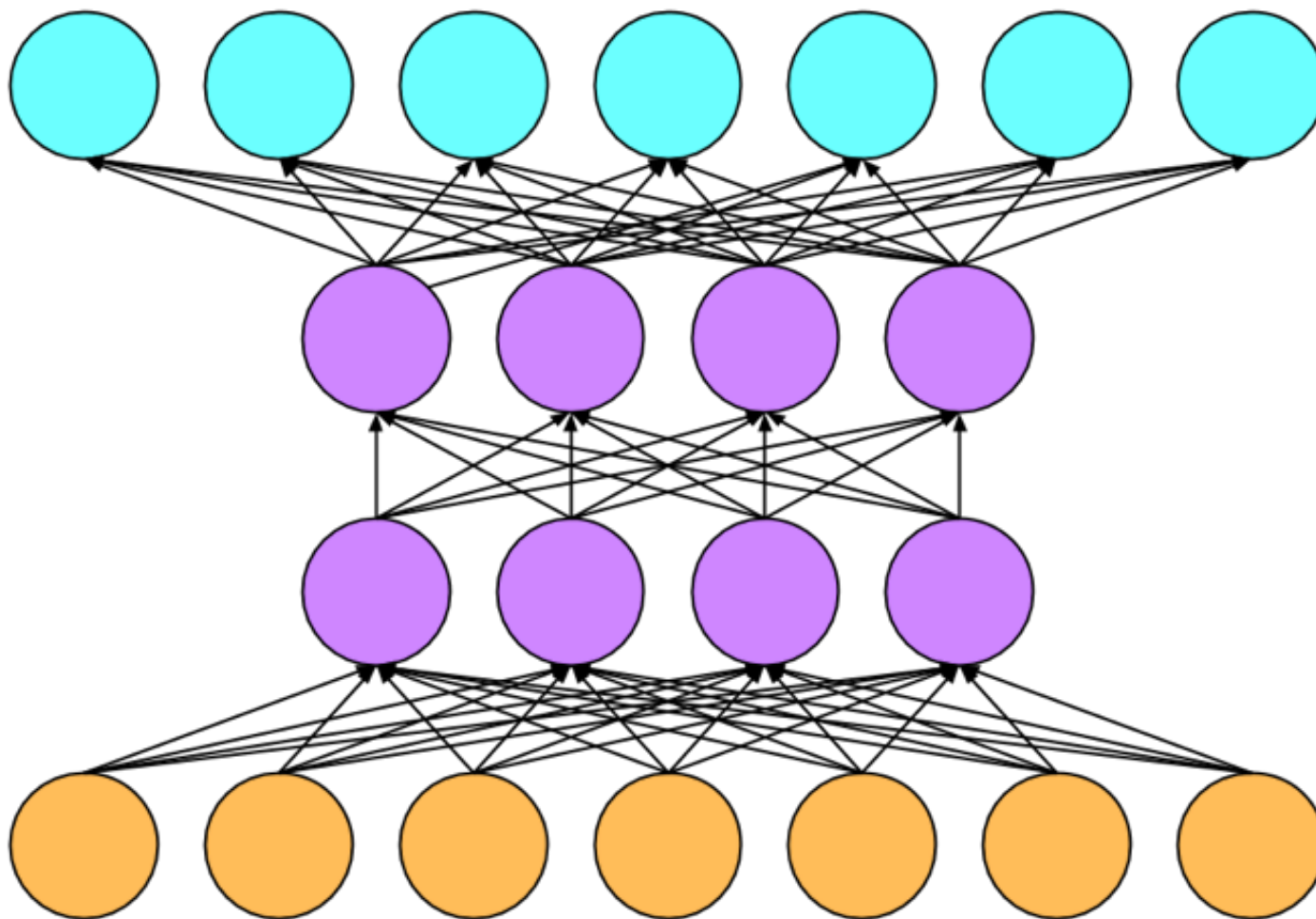
# Forward Pass



# Backward Pass



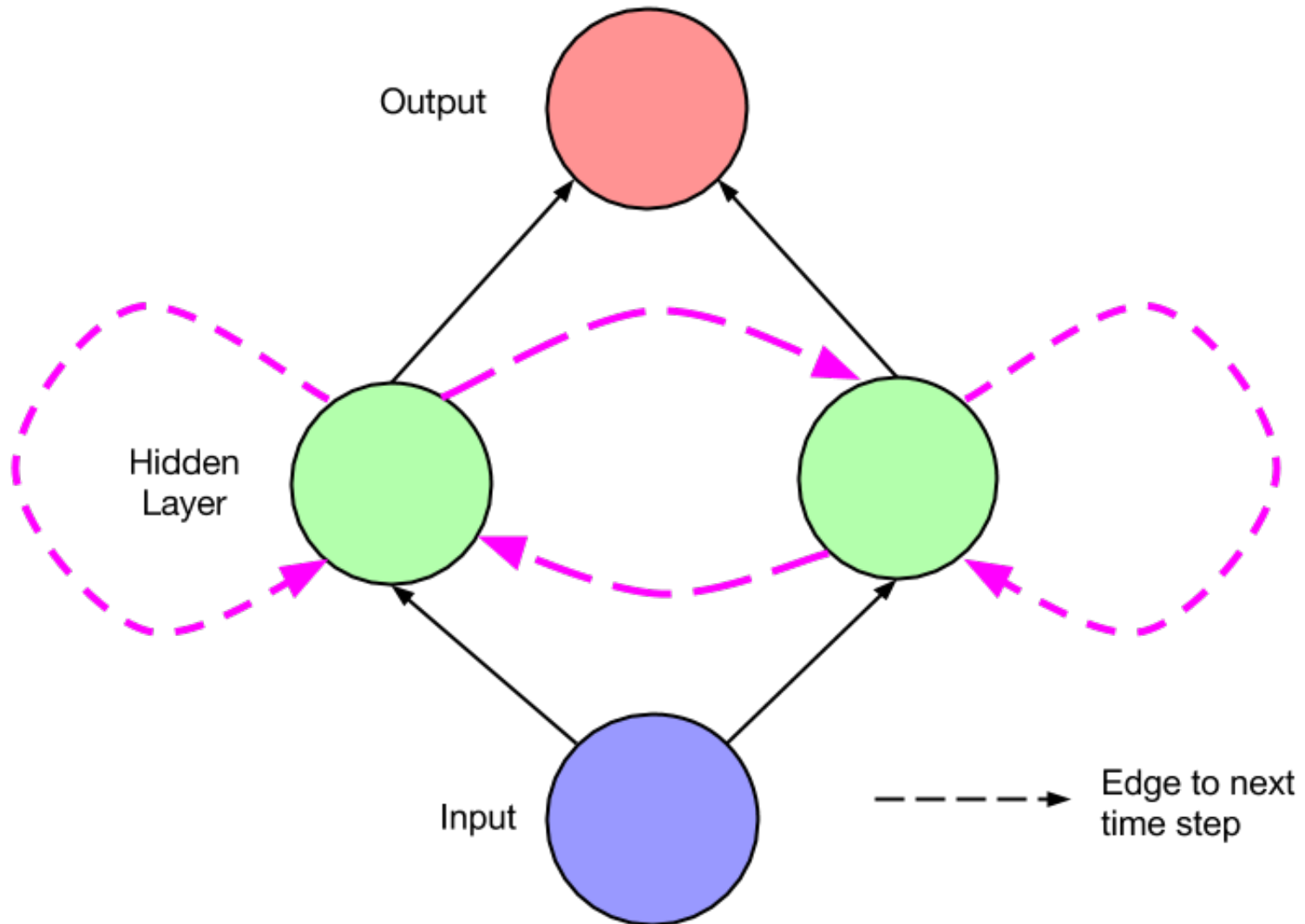
# Multilabel MLP



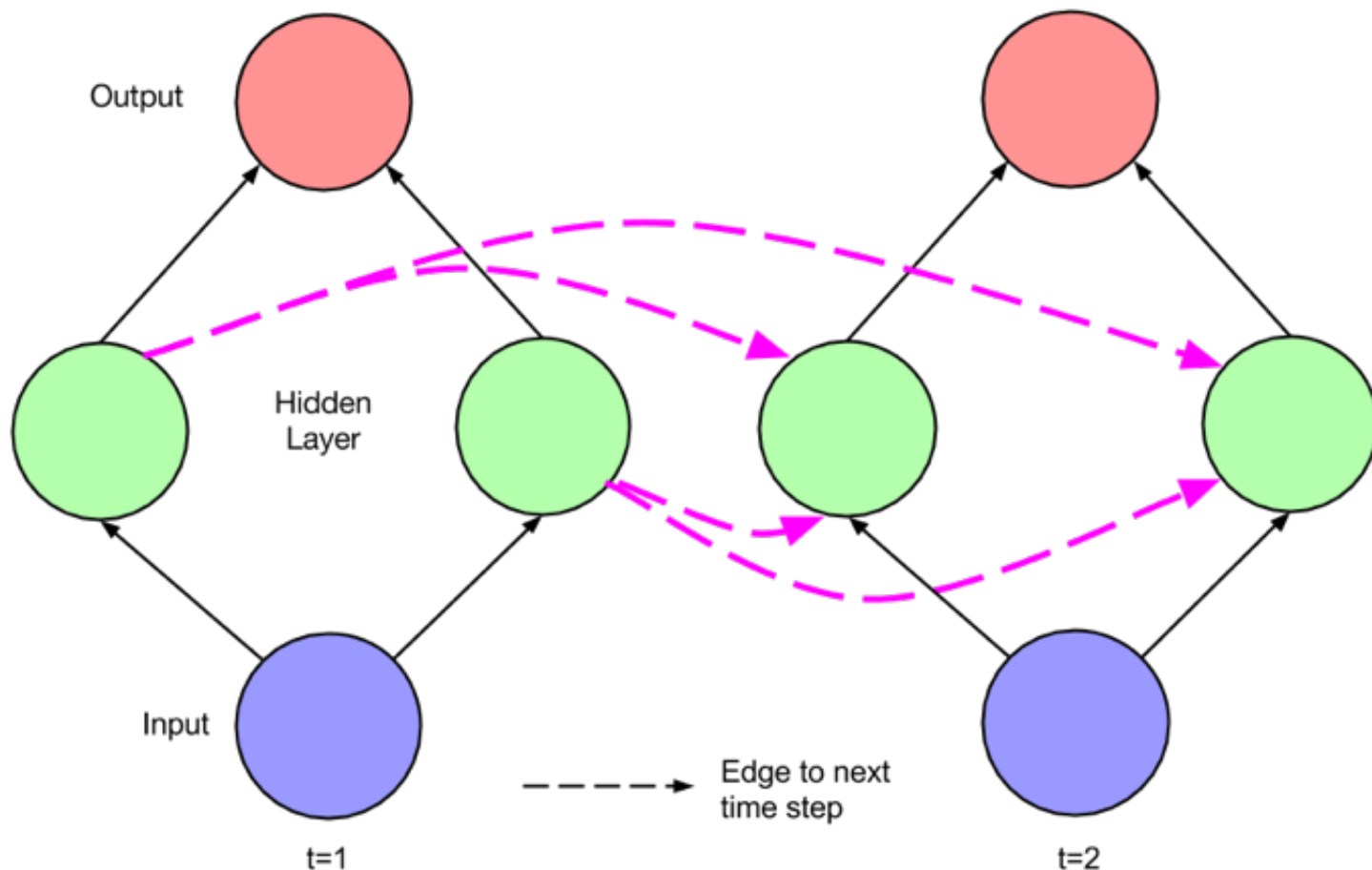
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# To Model Sequential Data: Recurrent Neural Networks



# Recurrent Net (Unfolded)

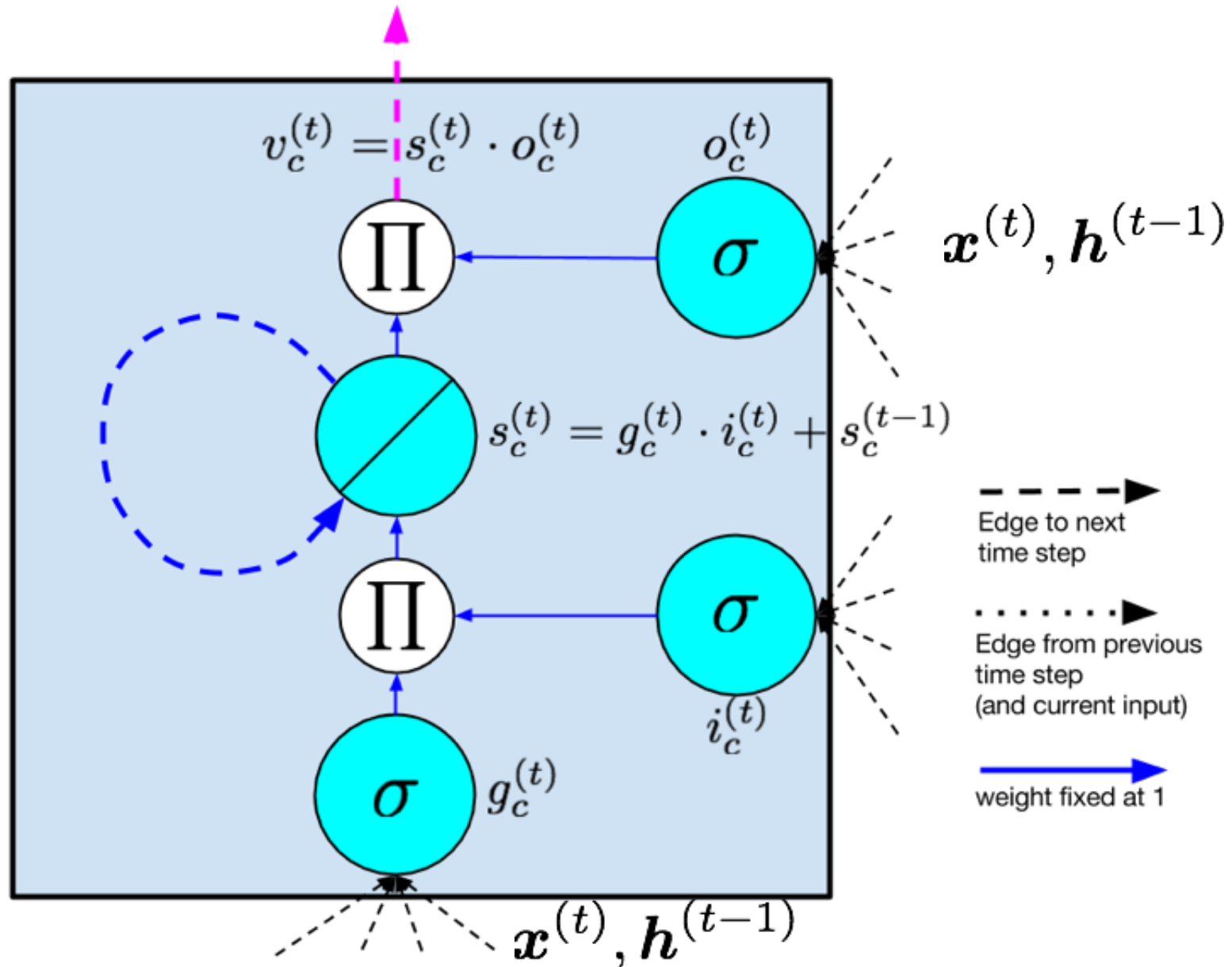


$$h^{(t)} = \sigma(W_{hx}\mathbf{x}^{(t)} + W_{hh}\mathbf{h}^{(t-1)} + \mathbf{b}_h)$$

$$\hat{\mathbf{y}}^{(t)} = \text{softmax}(W_{yh}\mathbf{h}^{(t)} + \mathbf{b}_y)$$

# LSTM Memory Cell

(Hochreiter & Schmidhuber, 1997)



# LSTM Forward Pass

$$\mathbf{g}^{(t)} = \phi(W_{gx}\mathbf{x}^{(t)} + W_{gh}\mathbf{h}^{(t-1)} + \mathbf{b}_g)$$

$$\mathbf{i}^{(t)} = \sigma(W_{ix}\mathbf{x}^{(t)} + W_{ih}\mathbf{h}^{(t-1)} + \mathbf{b}_i)$$

$$\mathbf{f}^{(t)} = \sigma(W_{fx}\mathbf{x}^{(t)} + W_{fh}\mathbf{h}^{(t-1)} + \mathbf{b}_f)$$

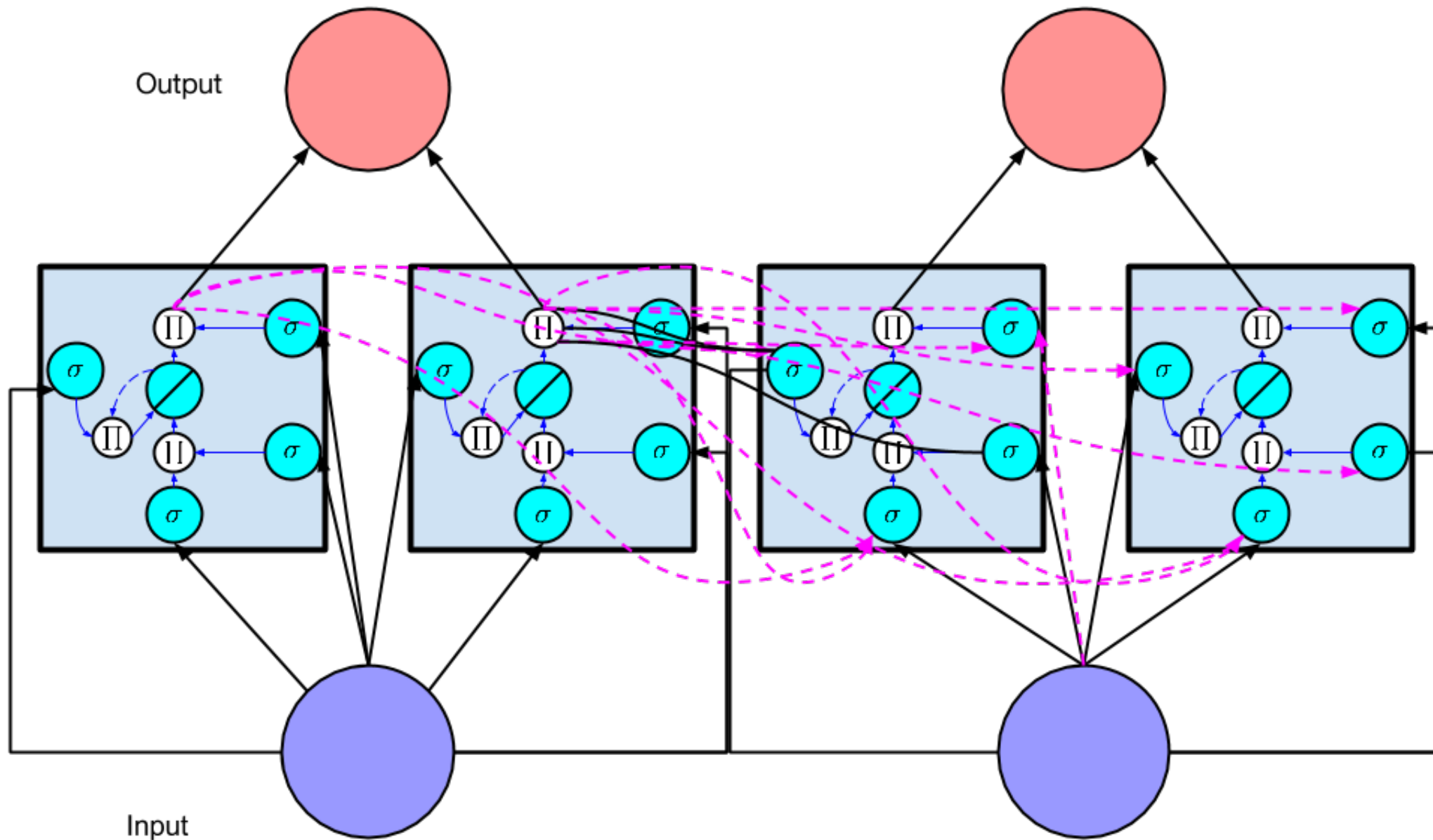
$$\mathbf{o}^{(t)} = \sigma(W_{ox}\mathbf{x}^{(t)} + W_{oh}\mathbf{h}^{(t-1)} + \mathbf{b}_o)$$

$$\mathbf{s}^{(t)} = \mathbf{g}^{(t)} \odot \mathbf{i}^{(t)} + \mathbf{s}^{(t-1)} \odot \mathbf{f}^{(t)}$$

$$\mathbf{h}^{(t)} = \mathbf{s}^{(t)} \odot \mathbf{o}^{(t)}$$



# LSTM (full network)



# Unstructured Input

$x_i =$



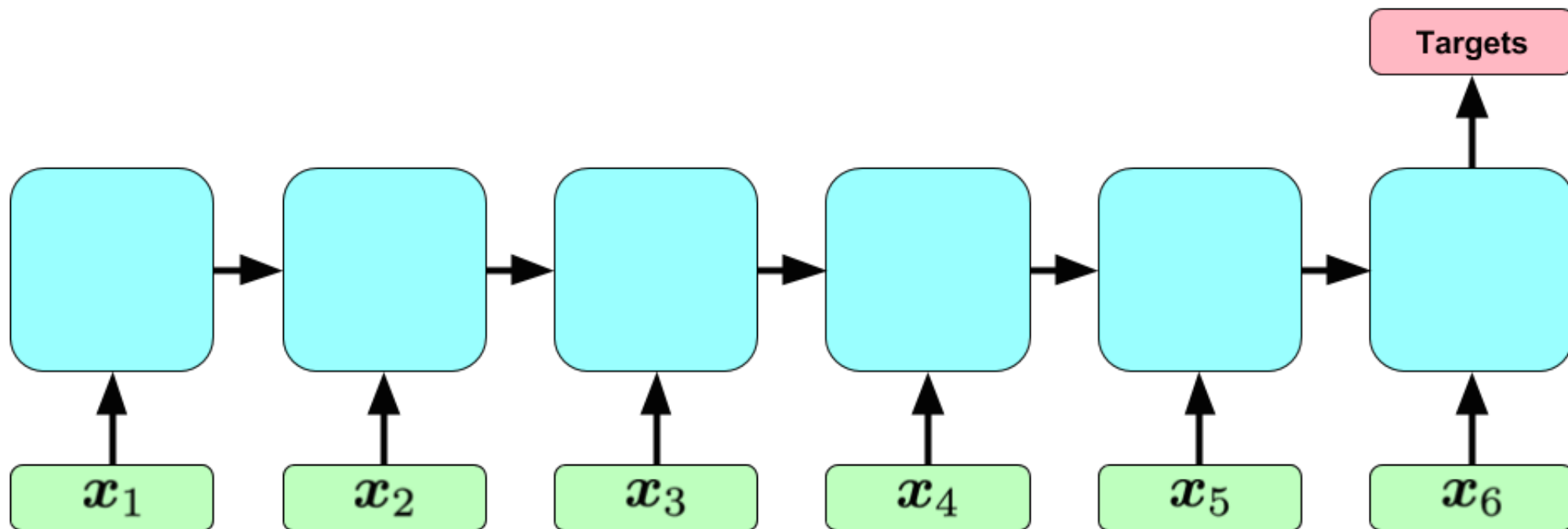
# Modeling Problems

- **Examples:** 10,401 episodes
- **Features:** 13 time series (sensor data, lab tests)
- **Complications:** Irregular sampling, missing values, varying-length sequences

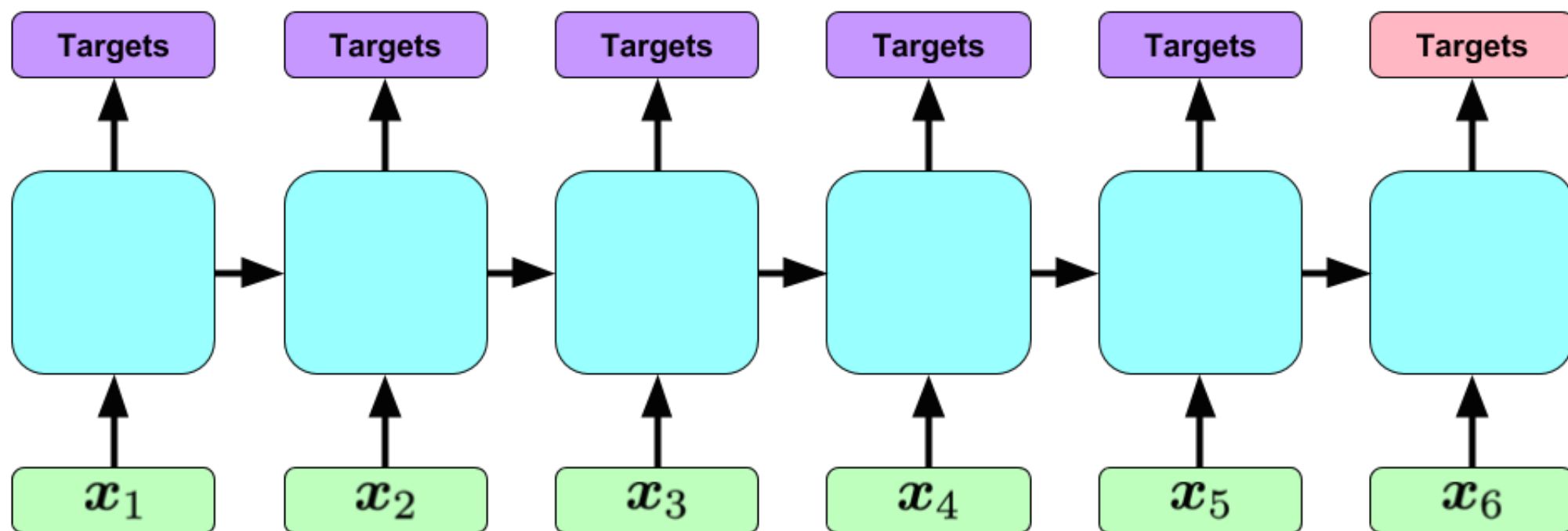
# How to model sequences?

- Markov models
- Conditional Random Fields
- **Problem: Cannot model long range dependencies**

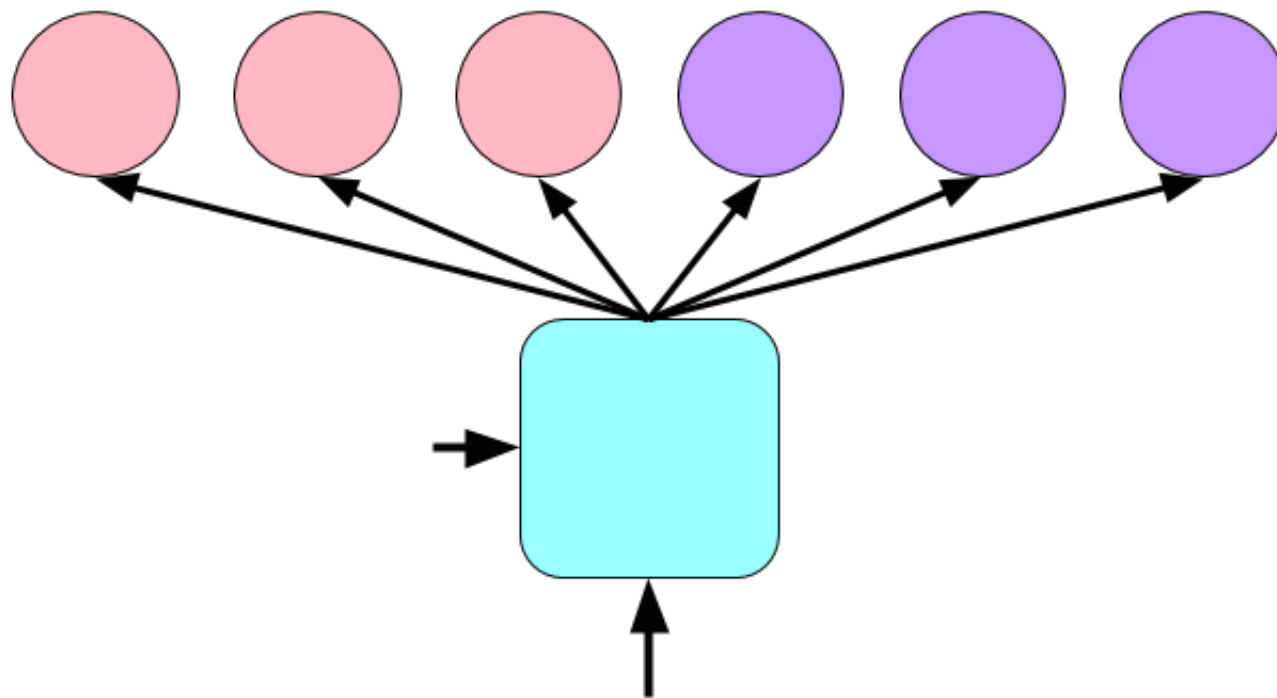
# Simple Formulation



# Target Replication



# Auxiliary Targets



# Results

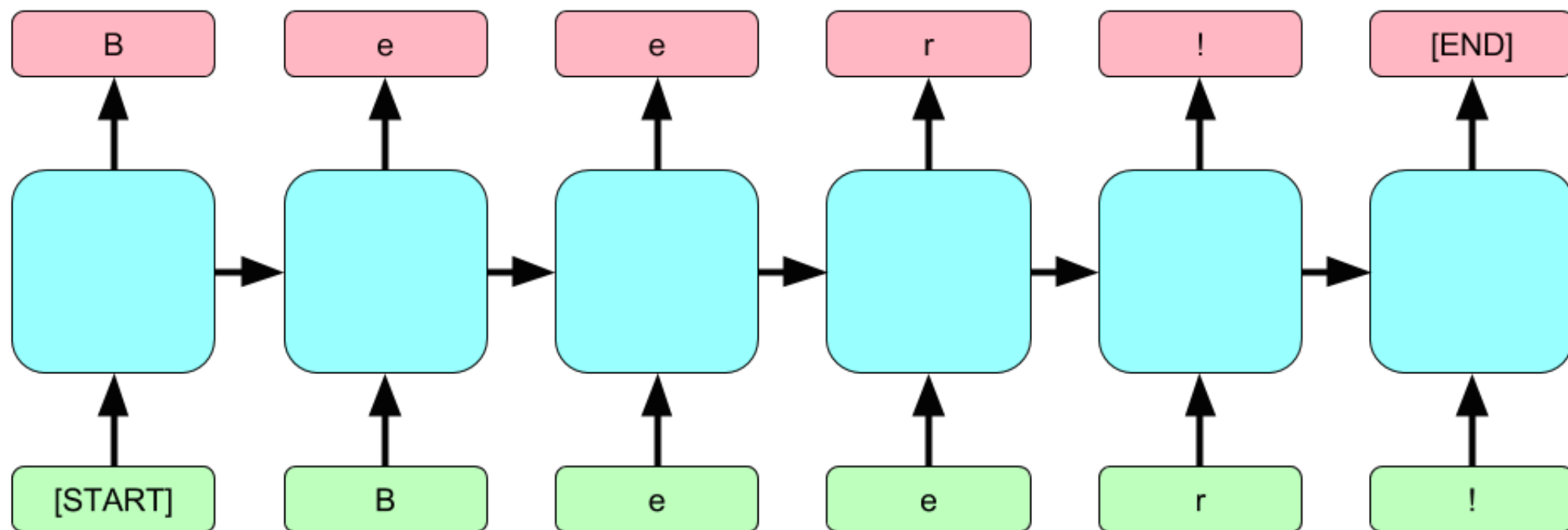
| Classification performance for 128 ICU phenotypes                         |               |               |               |               |               |
|---|---------------|---------------|---------------|---------------|---------------|
| Model   | Micro AUC     | Macro AUC     | Micro F1      | Macro F1      | Prec. at 10   |
| Base Rate   | 0.7128        | 0.5           | 0.1346        | 0.0343        | 0.0788        |
| Logistic Regression, First 6 + Last 6                                     | 0.8122        | 0.7404        | 0.2324        | 0.1081        | 0.1016        |
| Logistic Regression, Expert features                                      | 0.8285        | 0.7644        | 0.2502        | 0.1373        | 0.1087        |
| MLP, First 6 + Last 6   | 0.8375        | 0.7770        | 0.2698        | 0.1286        | 0.1096        |
| MLP, Expert features  | <b>0.8551</b> | <b>0.8030</b> | <b>0.2930</b> | <b>0.1475</b> | <b>0.1170</b> |
| LSTM Models with two 64-cell hidden layers                                |               |               |               |               |               |
| LSTM  | 0.8241        | 0.7573        | 0.2450        | 0.1170        | 0.1047        |
| LSTM, AuxOut (Diagnoses)  | 0.8351        | 0.7746        | 0.2627        | 0.1309        | 0.1110        |
| LSTM-AO (Categories)  | 0.8382        | 0.7748        | 0.2651        | 0.1351        | 0.1099        |
| LSTM-TR   | 0.8429        | 0.7870        | 0.2702        | 0.1348        | 0.1115        |
| LSTM-TR-AO (Diagnoses)  | 0.8391        | 0.7866        | 0.2599        | 0.1317        | 0.1085        |
| LSTM-TR-AO (Categories)   | 0.8439        | 0.7860        | 0.2774        | 0.1330        | 0.1138        |
| LSTM Models with Dropout (probability 0.5) and two 128-cell hidden layers |               |               |               |               |               |
| LSTM-DO   | 0.8377        | 0.7741        | 0.2748        | 0.1371        | 0.1110        |
| LSTM-DO-AO (Diagnoses)  | 0.8365        | 0.7785        | 0.2581        | 0.1366        | 0.1104        |
| LSTM-DO-AO (Categories)   | 0.8399        | 0.7783        | 0.2804        | 0.1361        | 0.1123        |
| LSTM-DO-TR  | <b>0.8560</b> | <b>0.8075</b> | <b>0.2938</b> | 0.1485        | <b>0.1172</b> |
| LSTM-DO-TR-AO (Diagnoses)   | 0.8470        | 0.7929        | 0.2735        | 0.1488        | 0.1149        |
| LSTM-DO-TR-AO (Categories)  | 0.8543        | 0.8015        | 0.2887        | 0.1446        | 0.1161        |
| LSTM-DO-TR (Linear Gain)  | 0.8480        | 0.7986        | 0.2896        | <b>0.1530</b> | 0.1160        |
| Ensembles of Best MLP and Best LSTM                                       |               |               |               |               |               |
| Mean of LSTM-DO-TR & MLP  | 0.8611        | 0.8143        | 0.2981        | 0.1553        | 0.1201        |
| Max of LSTM-DO-TR & MLP   | <b>0.8643</b> | <b>0.8194</b> | <b>0.3035</b> | <b>0.1571</b> | <b>0.1218</b> |



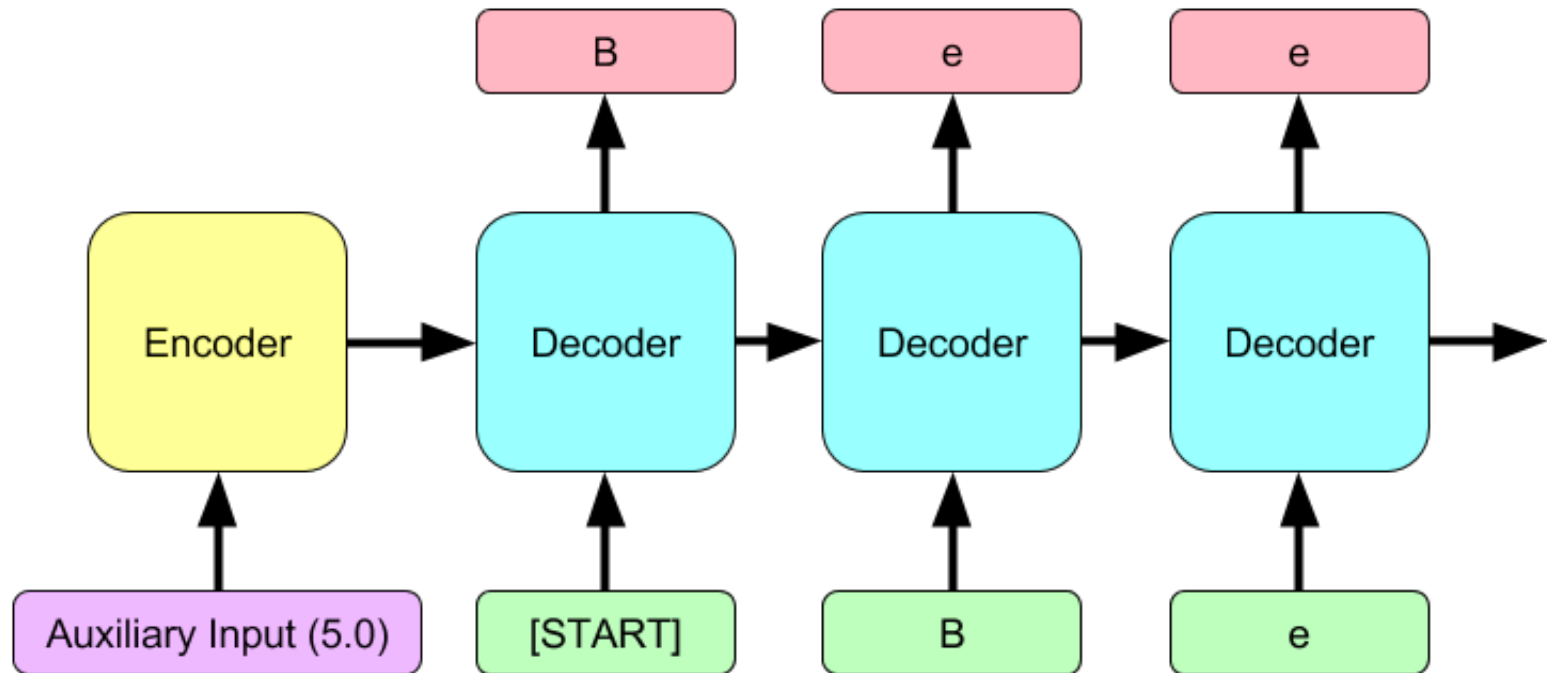
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- Jointly Learning to Generate and Classify Beer Reviews

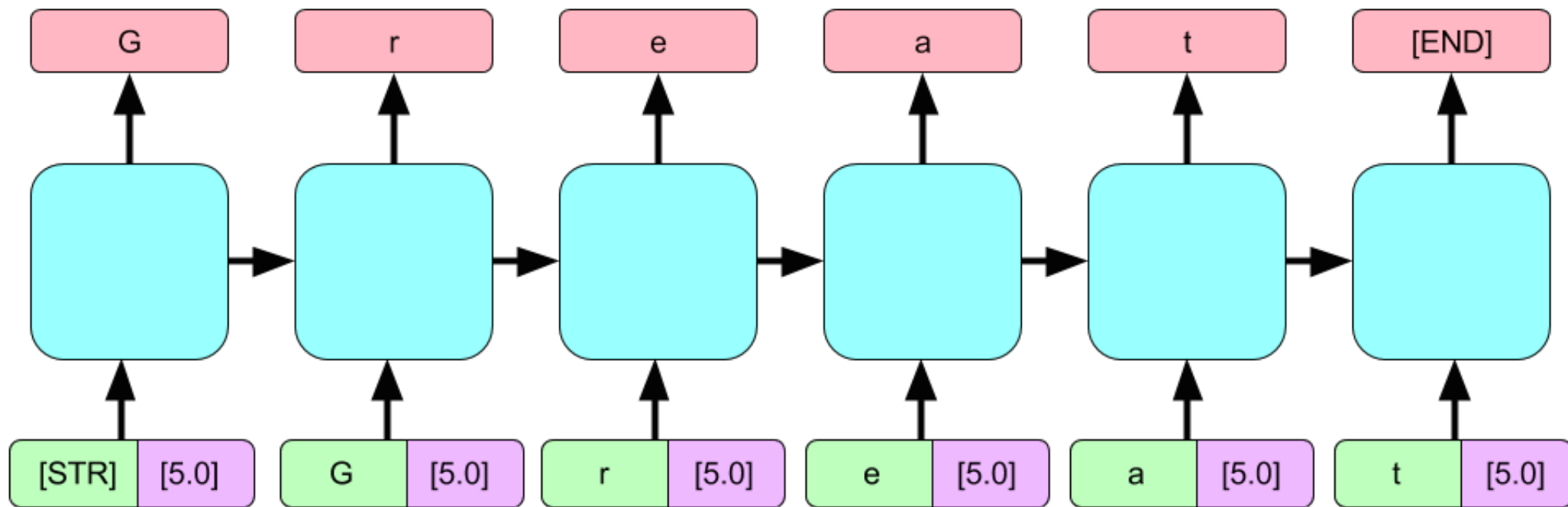
# RNN Language Model



# Past Supervised Approaches relied upon Encoder-Decoder Model



# Bridging Long Time Intervals with Concatenated Inputs

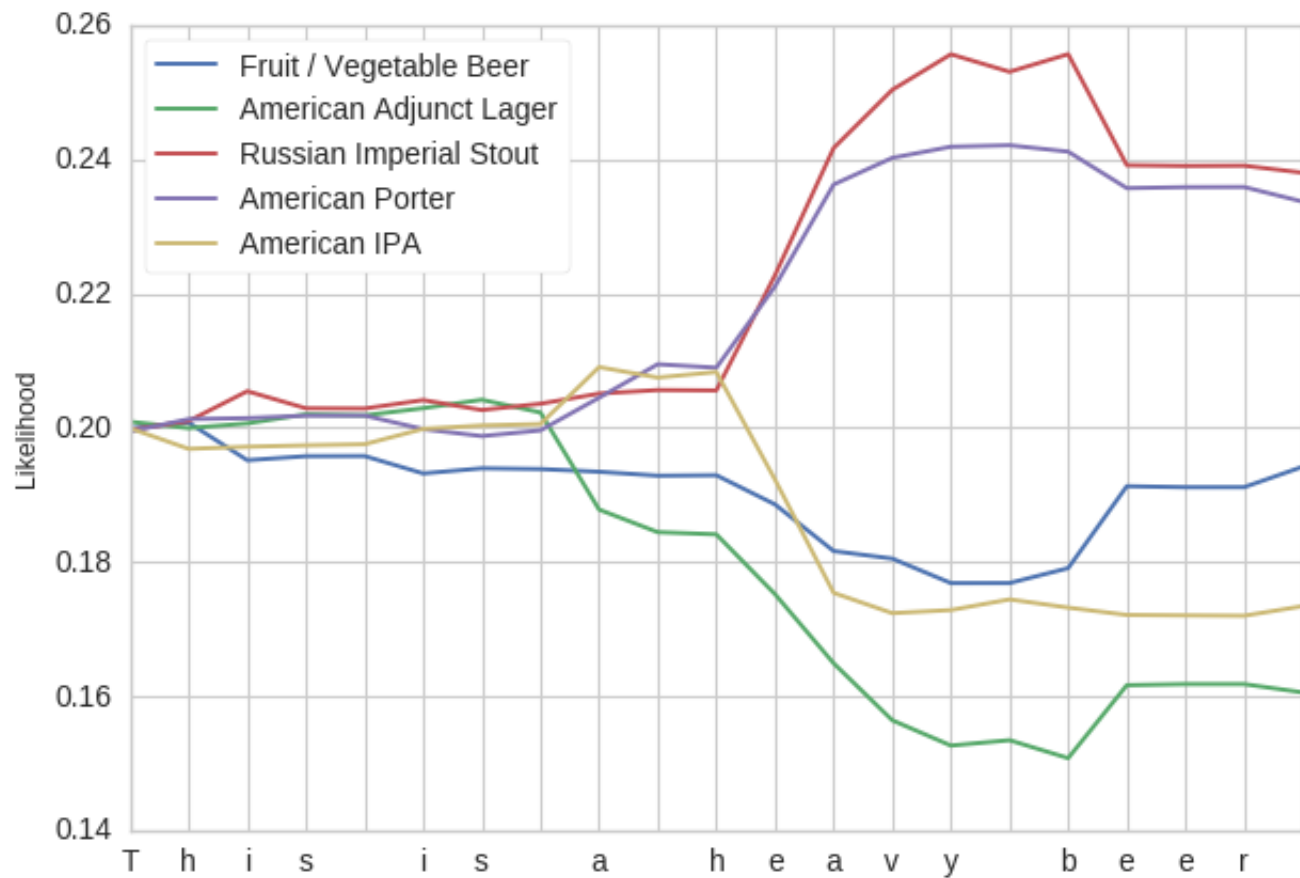


# Example

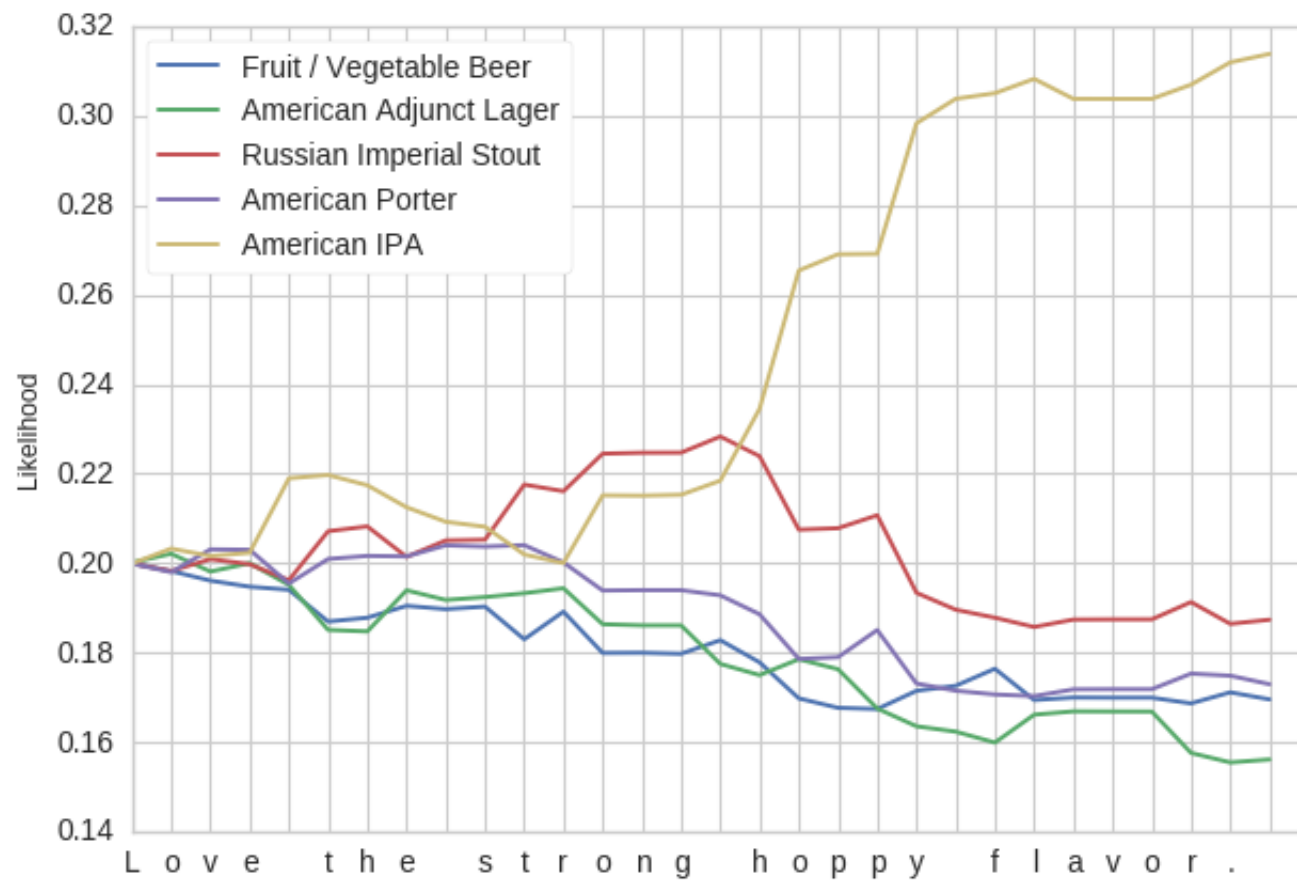
## A.5 FRUIT/VEGETABLE BEER

<STR>On tap at the brewpub. A nice dark red color with a nice head that left a lot of lace on the glass. Aroma is of raspberries and chocolate. Not much depth to speak of despite consisting of raspberries. The bourbon is pretty subtle as well. I really don't know that I find a flavor this beer tastes like. I would prefer a little more carbonization to come through. It's pretty drinkable, but I wouldn't mind if this beer was available. <EOS>

# Character-based Classification



# “Love the Strong Hoppy Flavor”



# Thanks!

**Contact:**

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[zacklipton.com](http://zacklipton.com)

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