Problem 1. [20 points] Consider the AdaBoost algorithm we discussed in the class. AdaBoost is an example of ensemble classifiers where the weights in next round are decided based on the training error of the weak classifier learned on the current weighted training set. We wish to run the AdaBoost on the dataset provided in Table 1.

1. Assume we choose the following decision stump f_1 (a shallow tree with a single decision node), as the first predictor (i.e., when training instances are weighted uniformly):

if(Color is Yellow): $predict\ Edible = Yes$ predict Edible = No

What would be the weight of f_1 in final ensemble classifier (i.e., α_1 in $f(x) = \sum_{i=1}^{K} \alpha_i f_i(x)$)?

- 2. After computing f_1 , we proceed to next round of AdaBoost. We begin by recomputing data weights
- depending on the error of f_1 and whether a point was (mis)classified by f_1 . What is the weight of each instance in second boosting iteration, i.e., after the points have been re-weighted? Please note that the weights across the training set are to be uniformly initialized.
- 3. In AdaBoost, would you stop the iteration if the error rate of the current weak classifier on the

Table 1: Mushroom data with 16 instances, three categorical features, and binary labels

1 is just a normalizing

WEIGHT

1) W = [16 , ... , 16]

$$E_{1} = g_{i=1}^{16} \omega_{i}^{0} \mathbb{I} \left[w_{i} \neq f_{k}(x_{i}) \right]$$

$$= \left(\frac{1}{16} \right) \left(0 \right) + \left(\frac{1}{16} \right) \left(1 \right) + \dots + \left(\frac{1}{16} \right) \left(0 \right)$$

$$= \left(\frac{1}{16}\right)(6) = \frac{6}{16}$$

$$\alpha_{1} = \frac{1}{2} \log \left(\frac{1 - \frac{6}{16}}{\frac{6}{16}} \right) = \frac{1}{2} \log \left(\frac{10/16}{6/16} \right) = \frac{1}{2} \log \left(\frac{5}{3} \right)$$

$$W_{i}^{(K)} = \frac{1}{Z} W_{i}^{(K-1)} e^{-A_{K} W_{i}^{*} f_{K}(x_{i})}$$

Right =>
$$W_1(2) = \frac{1}{2} W_4(0) = -\left(\frac{\frac{1}{2}\log_2(\frac{5}{3})}{2}\right)(2)(2)$$

$$= \frac{1}{16} \left(\frac{1}{16} \right) e^{-\frac{1}{2} \cdot 10} \left(\frac{5}{3} \right)$$

$$= \frac{1}{16} e^{-0.255} = 0.04843$$

Wrong =>
$$W_{1}^{(2)} = \frac{1}{2} \left(\frac{1}{16} \right) e^{-\left(\frac{1}{2} \log \left(\frac{C}{2}\right)\right)} \left(-2\right) (2)$$

$$= \frac{1}{2} \left(\frac{1}{16} \right) e^{\left(\frac{1}{2} \log \left(\frac{C}{2}\right)\right)}$$

NEW Weight for D1, D4, D5, D6, D7, D8, D4, D11, D15, D16

15 0.04843

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