

Problem 1)

1	{ int x;	[x:?]
2	int y;	[y:?, x:?]
3	y := 1;	[y:1, x:?]
4	{ int f(int x) {	[f{}, y:1, x:?]
...		
10	};	
first f call		
11	x := f(2);	[f{}, y:1, x:?]
4	{ int f(int x) {	
x is not 0, so		
7	else {	[[x:2, f{}, y:1],[f{}, y:1, x:?]]
8	y := f(x-1)*y+1 };	
x still not 0, so 2nd call for f		
11	x := f(2);) {	[[x:1, f{}, y:1], [x:2, f{}, y:1], [f{}, y:1, x:?]]
7	else {	
8	y := f(x-1)*y+1 };	[[x:0, f{}, y:1], [x:1, f{}, y:1], [x:2, f{}, y:1], [f{}, y:1, x:?],]
x == 0 here 3rd call for f		
4	{ int f(int x) {	[[y:1, x:1, f{}, y:1], f(x-1)*y+1 = 2 [x:2, f{}, y:1], [f{}, y:1, x:?]
5	if x=0 then {	
6	y := 1 }	[[y:2, x:2, f{}, y:1], [f{}, y:1, x:?]] f(...) = 4
back to 2nd call		
8	y := f(x-1)*y+1 };	[[x:4]
9	return y; 2	
back at first call of f		
8	y := f(x-1)*y+1 };	[x:4]
9	return y; 4	
11	x := f(2);	

Problem 2)

In static scoping, z would be assigned 21. ($x*y, 3*7$)

The earliest x, 3, would be referred to, as well as the earliest y.

In dynamic scoping, z would be assigned 26. ($2*13$)

The latest definition of x would be in function g(int x), which a 2 was passed into.

Latest definition of y would be the 13 in where the block of the function g exists.

Problem 3)

Call by value:

[x:14, g{}, f{}, z:?, y:7]

[y:16, a:15, x:14, g{}, f{}, z:?, y:7] at first f

[y:32, x:14, g{}, f{}, z:?, y:7] after first function call

[a:-15, y:32, x:14, g{}, f{}, z:?, y:7] in second f

[z:-29, y:32, x:14, g{}, f{}, z:?, y:7] after second f

[z:-28, y:7] returned to the first call of z

Call By Name:

[g{}, f{}, z:?, y:7], before first function call

[x:(y*2), g{}, f{}, z:g(y*2), y:7], at g

[a:(x+1), x:y*2, g{}, f{}, z:g(y*2), y:7] in first f call

[y:(a+1), a:(x+1), x:y*2, g{}, f{}, z:g(y*2), y:7] in first f call

y =
(a+1)
((x+1)+1)
(((y*2)+1)+1)
(((14)+1)+1) = 16

return =
16+a
16 + x+1
16 + ((y*2) + 1)
16 + (14 + 1) = 31

[y:32, a:(x+1), x:y*2, g{}, f{}, z:g(y*2), y:7] After first f call
[a:(x-y+3), y:32, x:y*2, g{}, f{}, z:g(y*2), y:7] in second f call
[y:(a+1), a:(x-y+3), x:y*2, g{}, f{}, z:g(y*2), y:7]

y = (a+1) = (x-y+3)+1 = (y*2 - 32 + 3) + 1 = (64 - 32 + 3) + 1
= 36

return = (36+(x-y+3)) = (36+(64-32+3)) = 71

[z:71, y:32, x:y*2, g{}, f{}, z:g(y*2), y:7], return z + 1

[z: 72, y:32, y:7]

Z = 72, newer y = 32, original y = 7

Call by Need:

[g{}, f{}, z:?, y:7], before first function call

[x:y*2, g{}, f{}, z:?, y:7]

[a:x+1, x:y*2, g{}, f{}, z:?, y:7]

[y:(a+1), a:x+1, x:y*2, g{}, f{}, z:?, y:7]

[y:16, a:15, x:14, g{}, f{}, z:?, y:7] evaluated according to call by need

return y+a from first call of f

[y:32, x:14, g{}, f{}, z:?, y:7]

[a:(x-y+3), y:32, x:14, g{}, f{}, z:?, y:7]

[y:(a+1), a:(x-y+3), y:32, x:14, g{}, f{}, z:?, y:7]

[y:-14, a:-15, y:32, x:14, g{}, f{}, z:?, y:7] evaluated according to call by need

$y = (x - y + 3 + 1) = (14 - 32 + 4) = -14$

[z:-29, y:32, x:14, g{}, f{}, z:?, y:7]

z = -28, local y in g = 32, global y = 7