HW05WP ML

July 29, 2023

1 Logistic Regression: HW #5

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1.1 Preliminaries

Date of analysis:

```
[]: from datetime import datetime as dt
now = dt.now()
print("Analysis on ", now.strftime("%Y-%m-%d"), "at", now.strftime("%H:%M %p"))
```

Analysis on 2023-07-29 at 23:00 PM

Establish current working directory:

```
[]: import os os.getcwd()
```

[]: '/Users/chasecarlson/Documents/GSCM Course Materials/GSCM 575 Machine Learning in Business/Python Pjojects/GSCM-575-ML/code'

Import standard libraries

```
[]: import pandas as pd
import numpy as np
import seaborn as sns
import matplotlib.pyplot as plt
```

1.2 Read and Prepare data

A classic application of supervised machine learning classification is customer churn. The ability to successfully forecast a customer of a company's services and products about to no longer be a customer allows the company to commit resources to attempt to salvage the relationship.

The following data file contains information on over 7000 customers of a telecom service, including former customers who left the service plan within the last 30 days the data was collected. Build a model to predict customer churn (customer exits the service plan), one of the variables in the data set.

Data: http://web.pdx.edu/~gerbing/data/CustomerChurn.csv

1.2.1 Read and Verify Data

No

a. - Read the data into a data frame. - Display the number of rows and columns in the data file, and the first five lines of the data file, including the variable names. - Display all variable names and corresponding data values by transposing the output table. - Display the data type for each variable.

Read-in data and display first 5 rows. Number of rows and columns is displayed at the bottom.

```
[]: df = pd.read_csv("http://web.pdx.edu/~gerbing/data/CustomerChurn.csv")
    df.head()
```

[]	:	customerID	gender	SeniorCitizen	Partner	Dependen	ts tenure	PhoneService	\
	0	7590-VHVEG	Female	0	Yes		No 1	. No	
	1	5575-GNVDE	Male	0	No		No 34	Yes	
	2	3668-QPYBK	Male	0	No		No 2	Yes	
	3	7795-CFOCW	Male	0	No		No 45	No No	
	4	9237-HQITU	Female	0	No		No 2	Yes	
		Multiple	Lines Ir	nternetService (OnlineSed	curity	DevicePro	tection \	
	0	No phone se	ervice	DSL		No		No	
	1		No	DSL		Yes		Yes	
	2		No	DSL		Yes		No	
	3	No phone se	rvice	DSL		Yes		Yes	

Fiber optic

No

No

	TechSupport	Streaming	TV St	reamingMovies	Contract	Paperle	essBilling	\
0	No		No	No	${\tt Month-to-month}$		Yes	
1	No		No	No	One year		No	
2	No		No	No	${\tt Month-to-month}$		Yes	
3	Yes		No	No	One year		No	
4	No		No	No	${\tt Month-to-month}$		Yes	
		PaymentM	ethod	MonthlyCharge	s TotalCharges	Churn		
0	E.	lectronic	check	29.8	5 29.85	No		
1		Mailed	check	56.9	5 1889.5	No		
2		Mailed	check	53.8	5 108.15	Yes		
3	Bank trans	fer (autom	atic)	42.3	1840.75	No		
4	E.	lectronic	check	70.7	151.65	Yes		

[5 rows x 21 columns]

Display the variable names and values using transpose () $\,$

[]: df.head().transpose()

[]:		0	1	2	\
	customerID	7590-VHVEG	5575-GNVDE	3668-QPYBK	•
	gender	Female	Male	Male	
	SeniorCitizen	0	0	0	
	Partner	Yes	No	No	
	Dependents	No	No	No	
	tenure	1	34	2	
	PhoneService	No	Yes	Yes	
	MultipleLines	No phone service	No	No	
	InternetService	DSL	DSL	DSL	
	OnlineSecurity	No	Yes	Yes	
	OnlineBackup	Yes	No	Yes	
	${\tt DeviceProtection}$	No	Yes	No	
	TechSupport	No	No	No	
	StreamingTV	No	No	No	
	${\tt StreamingMovies}$	No	No	No	
	Contract	Month-to-month	One year	Month-to-month	
	PaperlessBilling	Yes	No	Yes	
	${\tt PaymentMethod}$	Electronic check	Mailed check	Mailed check	
	MonthlyCharges	29.85	56.95	53.85	
	TotalCharges	29.85	1889.5	108.15	
	Churn	No	No	Yes	
			3	4	
	customerID	77	95-CFOCW	9237-HQITU	
	gender		Male	Female	
	SeniorCitizen		0	0	

Partner	No	No
Dependents	No	No
tenure	45	2
PhoneService	No	Yes
MultipleLines	No phone service	No
InternetService	DSL	Fiber optic
OnlineSecurity	Yes	No
OnlineBackup	No	No
${\tt DeviceProtection}$	Yes	No
TechSupport	Yes	No
StreamingTV	No	No
${\tt StreamingMovies}$	No	No
Contract	One year	Month-to-month
PaperlessBilling	No	Yes
PaymentMethod	Bank transfer (automatic)	Electronic check
MonthlyCharges	42.3	70.7
TotalCharges	1840.75	151.65
Churn	No	Yes

Display the data types for each variable:

[]: df.dtypes

[]:	customerID	object
	gender	object
	SeniorCitizen	int64
	Partner	object
	Dependents	object
	tenure	int64
	PhoneService	object
	MultipleLines	object
	InternetService	object
	OnlineSecurity	object
	OnlineBackup	object
	DeviceProtection	object
	TechSupport	object
	StreamingTV	object
	StreamingMovies	object
	Contract	object
	PaperlessBilling	object
	PaymentMethod	object
	MonthlyCharges	float64
	TotalCharges	object
	Churn	object
	dtype: object	

b. The variable TotalCharges is conceptually a numeric variable but is read into the data frame as an object variable, i.e., non-numeric. Convert to numeric. As always, audit (verify) any change to

the data table.

Use the following code for the $to_numeric$ function to convert (where d is the data frame name, but could be any valid Python name).

```
d['TotalCharges'] = pd.to_numeric(d['TotalCharges'], errors='coerce')
```

The errors parameter set to 'coerce' instructs to covert to a NaN any data value that cannot be converted to a legitimate number.

```
[]: df['TotalCharges'] = pd.to_numeric(df['TotalCharges'], errors='coerce')
```

View total missing data:

[]: df.isna().sum()

[]:	customerID	0
	gender	0
	SeniorCitizen	0
	Partner	0
	Dependents	0
	tenure	0
	PhoneService	0
	MultipleLines	0
	InternetService	0
	OnlineSecurity	0
	OnlineBackup	0
	DeviceProtection	0
	TechSupport	0
	StreamingTV	0
	StreamingMovies	0
	Contract	0
	PaperlessBilling	0
	PaymentMethod	0
	MonthlyCharges	0
	TotalCharges	11
	Churn	0
	dtype: int64	

1.2.2 Pre-Process Data

c. Drop the customerID variable.

Hint: Illustrated in several previous notebooks, including 02Wrangle.

Verify customerID was dropped by displaying the first few rows agian:

```
[]: df = df.drop(axis=1, columns=['customerID'])
    df.head().transpose()
```

]:		0		1	2
	gender	Female	M	Male	Male
	SeniorCitizen	0		0	0
	Partner	Yes		No	No
	Dependents	No		No	No
	tenure	1		34	2
	PhoneService	No		Yes	Yes
	MultipleLines	No phone service		No	No
	InternetService	DSL		DSL	DSL
	OnlineSecurity	No		Yes	Yes
	OnlineBackup	Yes		No	Yes
	${\tt DeviceProtection}$	No		Yes	No
	TechSupport	No		No	No
	StreamingTV	No		No	No
	StreamingMovies	No		No	No
	Contract	Month-to-month	One y	ear Mont	th-to-month
	PaperlessBilling	Yes		No	Yes
	PaymentMethod	Electronic check	Mailed ch	neck Ma	ailed check
	MonthlyCharges	29.85	56	5.95	53.85
	TotalCharges	29.85	188	39.5	108.15
	Churn	No		No	Yes
	_		3		4
	gender		Male		Female
	SeniorCitizen		0		0
	Partner		No		No
	Dependents		No		No
	tenure		45		2
	PhoneService		No		Yes
	MultipleLines	No phone	service		No
	InternetService		DSL	Fibe	er optic
	OnlineSecurity		Yes		No
	OnlineBackup		No		No
	DeviceProtection		Yes		No
	TechSupport		Yes		No
	StreamingTV		No		No
	StreamingMovies		No		No
	Contract		One year	Month-	to-month
	PaperlessBilling		No		Yes
	PaymentMethod	Bank transfer (au		Electron	
	MonthlyCharges		42.3		70.7
	• •				
	TotalCharges Churn		1840.75 No		151.65 Yes

\

d. Most of the variables are categorical. Pre-process each categorical variable to become a dummy variable, a type of indicator variable. Retain all k dummy variables for each categorical variable with k levels (to be able to pick and choose the dummy variables to analyze.

Hint: You do not need to list each variable, though could, just the data frame name.

Use get_dummies() to transform all categorical variables in the data frame to dummy variables:

```
[]: df = pd.get_dummies(df)
```

e. To keep the analysis simpler, and to drop excess dummy variables retain just the following (mostly indicator) variables for analysis.

'MonthlyCharges', 'TotalCharges', 'PaperlessBilling_Yes', 'PaymentMethod_Mailed check', 'PhoneService_Yes', 'tenure', 'Dependents_Yes', 'InternetService_No', 'Churn_Yes'

Hint: See subsetting in 02Wrangling.

[]:		0	1	2	3	4
	MonthlyCharges	29.85	56.95	53.85	42.3	70.7
	PaperlessBilling_Yes	1.00	0.00	1.00	0.0	1.0
	PaymentMethod_Mailed check	0.00	1.00	1.00	0.0	0.0
	PhoneService_Yes	0.00	1.00	1.00	0.0	1.0
	tenure	1.00	34.00	2.00	45.0	2.0
	Dependents_Yes	0.00	0.00	0.00	0.0	0.0
	<pre>InternetService_No</pre>	0.00	0.00	0.00	0.0	0.0
	Churn_Yes	0.00	0.00	1.00	0.0	1.0

In the correlation matrix later in the analysis "TotalCharges" was found to be highly correlated with MonthlyCharges. Since TotalCharges contained missing data, I dropped it from this analysis and retained MonthlyCharges instead.

f. Simplify the variable names. Rename as follows. Audit.

- MonthlyCharges -> Charges,
- PaperlessBilling Yes -> Paperless,
- PaymentMethod Mailed check -> Check,
- PhoneService Yes -> Phone,
- tenure -> Tenure,
- Dependents Yes -> Dependents,
- $\bullet \ \ InternetService_No -> Internet,$
- Churn_Yes -> Churn

Hint: Several previous examples, including 02Wrangle.

```
[]: df2.rename(columns={'MonthlyCharges': 'Charges', 'PaperlessBilling_Yes':⊔

→'Paperless',
```

```
'PaymentMethod_Mailed check': 'Check', 'PhoneService_Yes': 

'tenure': 'Tenure', 'Dependents_Yes': 'Dependents',

'InternetService_No': 'Internet', 'Churn_Yes': 'Churn'},

inplace=True)

df2.head()
```

[]:	Charges	Paperless	Check	Phone	Tenure	Dependents	Internet	Churn
0	29.85	1	0	0	1	0	0	0
1	56.95	0	1	1	34	0	0	0
2	53.85	1	1	1	2	0	0	1
3	42.30	0	0	0	45	0	0	0
4	70.70	1	0	1	2	0	0	1

To review the syntax, everything inside { } is called a Python dictionary, a core Python data structure. The dictionary lists keyword-value pairs.

g. Check for missing data. If not too much, delete the offenders. If severe, impute the missing values. Audit.

Hint: Done in 02PreProcess.

```
[]: print(df2.isna().sum())
print("Total Missing: ", df2.isna().sum().sum())
```

Charges Paperless 0 Check 0 Phone 0 Tenure 0 Dependents 0 Internet 0 Churn 0 dtype: int64 Total Missing: 0

No missing data after dropping the TotalCharges column, which had 11 missing.

1.2.3 Pre-Analysis Understanding and Feature Selection

1.2.4 Target Distribution

h. Check out the distribution of the target, with a frequency distribution and then the corresponding bar chart.

```
[]: df2['Churn'].value_counts()
```

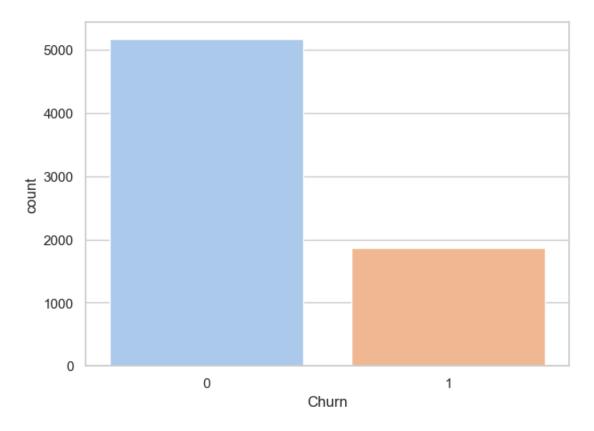
[]: 0 5174 1 1869

Name: Churn, dtype: int64

1,869 customers have left the service, and 5,174 have not left the service. See the bar chart below for visual representation:

```
[]: sns.countplot(df2, x='Churn', palette='pastel')
```

[]: <Axes: xlabel='Churn', ylabel='count'>



1.2.5 Feature Relevance

i. Are all the features relevant? Examine the difference in means of Churn across the features.

Examining the difference in means of Churn across the features, the majority of them have fairly recognizable differences except for Phone, which is 0.901 for existing customers and 0.909 for former customers.

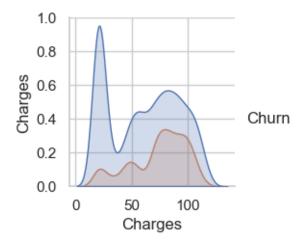
]: df2.gr	df2.groupby('Churn').mean()								
]:	Charges	Paperless	Check	Phone	Tenure	Dependents	\		
Churn									
0	61.265124	0.535562	0.252029	0.901044	37.569965	0.344801			
1	74.441332	0.749064	0.164794	0.909042	17.979133	0.174425			
	Internet								

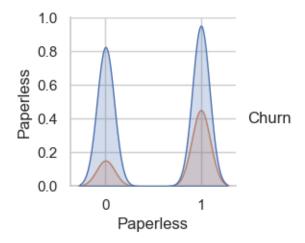
Churn

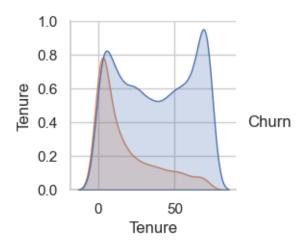
0 0.273096 1 0.060460

j. Examine the overlap in the distributions of Churn for numerical features TotalCharges, Paperless, and tenure. Which variable is likely the best predictor of churn?

```
[]: pred_vars = ['Charges', 'Paperless', 'Tenure']
for column in df2[pred_vars]:
    sns.pairplot(df2, vars=[column], hue='Churn')
```







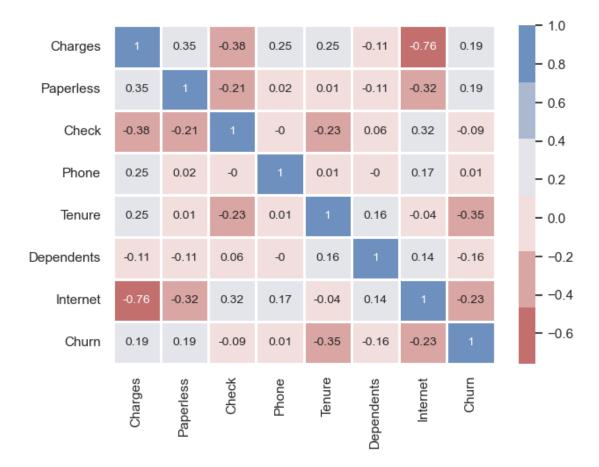
Based on the distributions of the selected predictor variables, it appears that tenure will have the most impact on Churn rate due to having a significantly different pattern with less overlap.

1.2.6 Feature Redundancy

k. Check for collinearity. Comment.

Because correlations span from negative to positive, use a diverging color palette, with blue indicating positive correlations and red indicating very small positive to negative correlations.

[]: <Axes: >



Based on the correlation matrix, we can identify the significant collinearity between the following variables, some of which may be dropped from the analysis: - Internet -> Charges: -0.76 - Total Charges -> Tenure: 0.83 TotalCharges was dropped from the analysis due to changes in the HW template - Contract -> Tenure: -0.65 Contract was dropped from the analysis due to changes in the HW template - Charges -> Total_Charges: 0.65

Instead of going back to the beginning of the script to drop the columns, I could have filtered them out at this point to reduce the collinearity by manual selection.

1.2.7 Create Feature and Target Data Structures

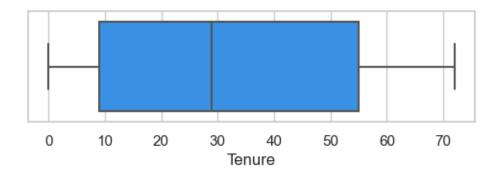
l. Define all feature variables in a data structure X. Define the target variable as a data structure y, a column of 0's and 1's.

[]: (7043, 7)

m. All dummy variables consist of values of only 0 or 1. The numerical variables Charges and Tenure range much more than 0 to 1. Generate a box plot for these variables to examine their range and check for outliers. Discuss.

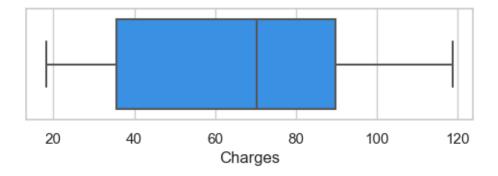
```
[]: plt.figure(figsize=(6,1.5))
    sns.set_theme(style='whitegrid')
    sns.boxplot(df2, x='Tenure', color='dodgerblue')
```

[]: <Axes: xlabel='Tenure'>



```
[]: plt.figure(figsize=(6,1.5))
sns.set_theme(style='whitegrid')
sns.boxplot(df2, x='Charges', color='dodgerblue')
```

[]: <Axes: xlabel='Charges'>



The innerquartile range of the Tenure column is about 9-55, with a median of just under 30. I do not see any outliers in either direction. The IQR of the Charges column is about 35-90, with a median value of about 70. Again, I do not see any outliers indicated outside of the whiskers in either direction.

n. Convert Charges and Tenure variables to a 0 to 1 range so that all feature variables are on the same scale. As always, verify any change in the data.

Hint: Re-scaling done in 02PreProcess.

Import the necessary package from sklearn:

```
[]: from sklearn import preprocessing
```

Check data types to convert if necessary:

```
[]: df2[['Charges', 'Tenure']].dtypes
```

[]: Charges float64
Tenure int64
dtype: object

Convert Tenure to float64 and verify change:

```
[]: df2.loc[:, 'Tenure'] = df2.loc[:, 'Tenure'].astype('float64')
df2[['Charges', 'Tenure']].dtypes
```

/var/folders/0r/8gtkp8rd5lx4q_4w2fvszkz80000gn/T/ipykernel_30884/3854154697.py:1 : DeprecationWarning: In a future version, `df.iloc[:, i] = newvals` will attempt to set the values inplace instead of always setting a new array. To retain the old behavior, use either `df[df.columns[i]] = newvals` or, if columns are non-unique, `df.isetitem(i, newvals)`

```
df2.loc[:, 'Tenure'] = df2.loc[:, 'Tenure'].astype('float64')
```

[]: Charges float64
Tenure float64
dtype: object

Scale using min/max scaler

Import MinMaxScaler from sklearn and instantiate:

```
[]: from sklearn.preprocessing import MinMaxScaler mm_scaler = preprocessing.MinMaxScaler()
```

Use fit_transform() to transform Charges and Tenure columns in the df2 data frame and preview the result:

```
[]:
        Charges Paperless Check Phone
                                            Tenure
                                                   Dependents Internet Churn
    0 0.115423
                       1.0
                              0.0
                                          0.013889
                                                           0.0
                                     0.0
                                                                     0.0
                                                                             0
    1 0.385075
                       0.0
                              1.0
                                     1.0
                                          0.472222
                                                           0.0
                                                                     0.0
                                                                             0
    2 0.354229
                       1.0
                              1.0
                                     1.0 0.027778
                                                           0.0
                                                                     0.0
                                                                              1
```

```
0.239303
                     0.0
                             0.0
                                    0.0
                                          0.625000
                                                             0.0
                                                                        0.0
                                                                                  0
3
   0.521891
                     1.0
                                          0.027778
                                                             0.0
                                                                        0.0
                                                                                   1
                             0.0
                                     1.0
```

Check the min & max values:

```
[]: print("Min Values:")
   print(df2[['Charges', 'Tenure']].min(), "\n")
   print("Max Values:")
   print(df2[['Charges', 'Tenure']].max())
```

Charges 0.0 Tenure 0.0

Min Values:

dtype: float64

Max Values: Charges 1.0 Tenure 1.0 dtype: float64

Data Leak Warning: Better to do this analysis with the re-scaling only done on test data, then done again, anew, on the testing data separately. Otherwise, there is *data leakage*, where the testing data is confounded with the training data because at this point in the analysis, the training and testing data are together. Characteristics of the training data will impact the way that later test data is tested.

If doing just one train/test split, separate re-scaling of training and testing data can easily be accomplished with what we know. Just rescale separately the two data sets after forming the split. For the preferred k-fold cross-validation, however, the testing data in each fold needs to be re-scaled separately. To do so we need to introduce the concept of a pipeline, which starts to be too much after introducing everything else. To be pure, if on the job for example, should do the separate re-scaling after the train/test split and not do k-fold. Or, even better, learn about constructing a pipeline, such as here and here. Another straightforward step, not that hard, but enough for now and not included in this course.

Preferably, we would estimate the re-scaling parameters and then the model itself on all of the data only after successful model validation. This version of the model would then be used to forecast from new data.

Fortunately, with such a large data set, the re-scaling parameters should be reasonably robust. If not constructing a pipeline, this step of doing one data rescaling before validation is better than not doing any rescaling at all given the large discrepancies of scales for *TotalCharges* and *Tenure*.

1.3 Fit Model and Evaluate with *One* Hold-Out Sample

o. Do a 70% training data and 30% testing data split of X and y data structures. Show the dimensions of the output data structures.

Restablish X and y data structures due to scaling earlier:

[]: (7043, 7)

Split the dataset and set:

Show dimensions of output data structures:

```
[]: print("Shape of X data structures: ", X_train.shape, X_test.shape) print("Shape of y data structures: ", y_train.shape, y_test.shape)
```

```
Shape of X data structures: (4930, 7) (2113, 7)
Shape of y data structures: (4930,) (2113,)
```

Seven features are included in the X data structure.

p. Fit the model to the training data.

Access the solution algorithm and instantiate:

```
[]: from sklearn.linear_model import LogisticRegression logistic_model = LogisticRegression(solver='lbfgs', max_iter=500)
```

```
[]: logistic_model.fit(X_train, y_train)
```

[]: LogisticRegression(max_iter=500)

Evaluate fit:

```
[]: y_fit = logistic_model.predict(X_train)
y_pred = logistic_model.predict(X_test)
```

q. Calculate the baseline probability for prediction in the absence of all information regarding X, the null model, the group with the largest proportion.

```
[]: my = y.mean()
max_my = np.max([y.mean(), 1-y.mean()])
print('Proportion of 0\'s (no-churn): %.3f' % (1-my))
print('Proportion of 1\'s (churn): %.3f' % my)
print('Null model accuracy: %.3f' % max_my)
```

```
Proportion of 0's (no-churn): 0.735
Proportion of 1's (churn): 0.265
Null model accuracy: 0.735
```

r. As a basis for evaluating forecasting accuracy, get the values fit by the model from the corresponding X values, for training and testing data.

```
[]: from sklearn.metrics import accuracy_score
print('Accuracy for training data: %.3f' % accuracy_score(y_train, y_fit))
print('Accuracy for testing data: %.3f' % accuracy_score(y_test, y_pred))
```

```
Accuracy for training data: 0.786 Accuracy for testing data: 0.794
```

s. For the testing data, calculate the probability of Churning for all the rows of testing data from the values of the features, the predictor variables.

```
[]: probability = logistic_model.predict_proba(X_test)
   probability = pd.DataFrame(probability)
   probability.head().transpose()
```

```
[]: 0 1 2 3 4
0 0.585594 0.45607 0.933973 0.770412 0.558314
1 0.414406 0.54393 0.066027 0.229588 0.441686
```

t. To understand more of what is happening here (for pedagogy), view the true values, forecasted values, and the estimated probability of Churning for about 10 or so rows of data. Best display is as a data frame.

```
[]: probs = [i[0] for i in logistic_model.predict_proba(X_test)]
    pred_df = pd.DataFrame({'true_values': y_test,
    'pred_values': y_pred,
    'pred_probs':probs})
    pred_df.head(10).transpose().style.format("{:.3}")
```

[]: <pandas.io.formats.style.Styler at 0x2931d7d30>

u. Assess the accuracy of the model on training and testing data. Any overfitting?

Null model accuracy: 0.735 Accuracy for testing data: 0.794 The testing performance improved 5.9% from 73.5% to 79.4%. However, at just 79.4% testing accuracy, there is significant room for improvement in forecasting accuracy. At 79.4% testing accuracy, the model is only slightly more accurate than the null model (73.5%).

v. Show the confusion matrix and explicitly identify the True Negatives, True Positives, False Negatives, and False Positives.

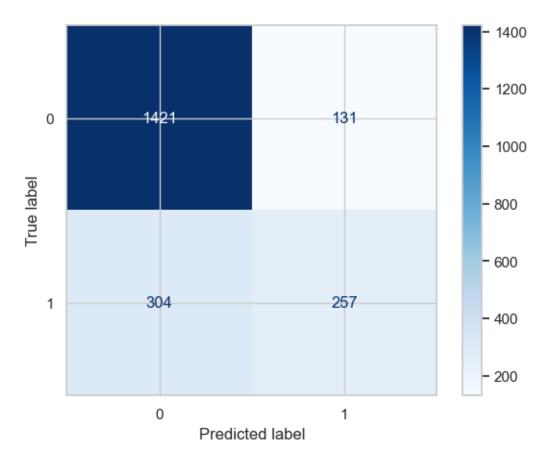
```
[]: from sklearn.metrics import confusion_matrix
dc = pd.DataFrame(confusion_matrix(y_test, y_pred))
dc
```

[]: 0 1 0 1421 131 1 304 257

True Negatives: 1,421True Positives: 257False Negatives: 304False Positives: 131

```
[]: from sklearn.metrics import ConfusionMatrixDisplay ConfusionMatrixDisplay.from_predictions(y_test, y_pred, cmap="Blues")
```

[]: <sklearn.metrics._plot.confusion_matrix.ConfusionMatrixDisplay at 0x2930a8a90>



```
[]: print("True Negatives: ", dc.iloc[0,0])
    print("True Positives: ", dc.iloc[1,1])
    print("False Negatives: ", dc.iloc[1,0])
    print("False Positives: ", dc.iloc[0,1])
```

True Negatives: 1421
True Positives: 257

False Negatives: 304 False Positives: 131

w. Calculate the recall, precision, and, F1 metrics. Comment on the meaning of each from the perspective of management.

```
[]: from sklearn.metrics import recall_score, precision_score, f1_score print ('Recall for testing data: %.3f' % recall_score(y_test, y_pred)) print ('Precision for testing data: %.3f' % precision_score(y_test, y_pred)) print ('F1 for testing data: %.3f' % f1_score(y_test, y_pred))
```

Recall for testing data: 0.458 Precision for testing data: 0.662 F1 for testing data: 0.542

- Recall is a measure of the proportion of actual positive instances correctly detected as positive. A recall of .460 indicates that only 46% of the positive predictions will be correctly labeled as positive, leaving a 54% chance of misclassifying a 1 as a 0 (customer churn as a customer retained). There were 303 false negatives in the confusion matrix.
- Precision is a measure of the proportion of correctly labeled positive outcomes. A precision score of 0.662 indicates that of those that the model forecasted as churn, 66.2% are actually churn, and 33.8% are not churn (132 false positives).
- The F1 score is the balance betwee Recall and Precision, and provides the harmonic mean.

1.4 Fit Model, then Predict, Evaluate with Multiple Hold-Out Samples

x. Do a 5-fold cross-validation an report individual fold and average values of accuracy, recall, and precision.

Access the StratifiedKFold algorithm and instantiate with 5 splits:

```
[]: from sklearn.model_selection import StratifiedKFold skf = StratifiedKFold(n_splits=5, shuffle=True, random_state=1)
```

Use cross_validate() to generate the scores:

```
[]: from sklearn.model_selection import cross_validate
   scores = cross_validate(logistic_model, X, y, cv=skf,
   scoring=('accuracy', 'recall', 'precision'),
   return_train_score=True)
```

Display the scores as a data frame:

```
[ ]: ds = pd.DataFrame(scores).round(3)
  ds.head()
```

```
[]:
        fit_time
                  score_time test_accuracy train_accuracy test_recall \
     0
           0.142
                       0.002
                                       0.793
                                                        0.789
                                                                     0.492
     1
           0.016
                       0.002
                                       0.783
                                                        0.791
                                                                      0.414
     2
           0.011
                                                                     0.495
                       0.011
                                       0.791
                                                        0.787
     3
           0.046
                       0.018
                                       0.798
                                                                     0.509
                                                        0.787
```

4	0.021	0.015	0.777	0.793	0.457
	train_recall	test_precision	train_precision		
0	0.471	0.646	0.638		
1	0.476	0.640	0.642		
2	0.470	0.638	0.634		
3	0.467	0.651	0.635		
4	0.487	0.606	0.647		

Average values for fit metrics:

```
[]: print('Mean of test accuracy: %.3f' % ds['test_accuracy'].mean())
print('Mean of test recall: %.3f' % ds['test_recall'].mean())
print('Mean of test precision: %.3f' % ds['test_precision'].mean())
```

```
Mean of test accuracy: 0.788
Mean of test recall: 0.473
Mean of test precision: 0.636
```

y. Comment on the worth of the model.

The results from the K-fold analysis are split. Accuracy dropped slightly from 0.794 to 0.788, recall improved slightly from 0.460 to 0.478, and precision dropped slightly from 0.662 to 0.635. Overall, I would suggest that this model is not highly effective at predicting customer churn due to the high probability of predicing false positives and false negatives.

1.5 Automated Feature Selection

1.5.1 Univariate Selection

z. Do a univariate feature selection of the top 4 features. Identify these features.

```
[]: from sklearn.feature_selection import SelectKBest, f_classif
selector = SelectKBest(k=4).fit(X,y)
selected = selector.get_support()
selected
```

[]: array([True, True, False, False, True, False, True])

Reduce the X data structure to include only the top 4 features selected into a new data structure, X2:

```
[]: X2 = X.iloc[:, selected]
X2.head()
```

```
[]:
        Charges Paperless
                              Tenure
                                      Internet
    0 0.115423
                                           0.0
                       1.0
                           0.013889
    1 0.385075
                       0.0 0.472222
                                           0.0
                       1.0 0.027778
    2 0.354229
                                           0.0
    3 0.239303
                       0.0
                           0.625000
                                           0.0
    4 0.521891
                       1.0 0.027778
                                           0.0
```

The top 4 features using the univariate selection process include: Charges, Paperless, Tenure, and Internet.

1.5.2 Multivariate Selection

aa. Do a multivariate feature selection. Identify the selected features.

```
[]: from sklearn.feature_selection import SelectKBest from sklearn.feature_selection import RFE selector = RFE(logistic_model, n_features_to_select=4, step=1).fit(X,y)
```

```
[]: print(selector.support_)
```

[True True False True True False False]

Reduce the X data structure to include only the top 4 features selected into a new data structure, X3:

```
[]: X3 = X.iloc[:, selector.support_]
X3.head()
```

```
[]:
        Charges Paperless Phone
                                     Tenure
    0 0.115423
                       1.0
                              0.0 0.013889
    1 0.385075
                       0.0
                              1.0 0.472222
    2 0.354229
                       1.0
                              1.0 0.027778
                       0.0
    3 0.239303
                              0.0 0.625000
       0.521891
                       1.0
                              1.0 0.027778
```

The top 4 features using the multivariate selection process include: Charges, Paperless, Phone, & Tenure

ab. Rank the features in importance.

```
[]: rnk = pd.DataFrame()
    rnk['Feature'] = X.columns
    rnk['Rank']= selector.ranking_
    rnk.sort_values('Rank').transpose()
```

```
[]:
                                         3
                                                  4
                                                               5
                                                                      2
                                                                                 6
     Feature
              Charges
                        Paperless
                                    Phone
                                            Tenure
                                                     Dependents
                                                                  Check
                                                                         Internet
     Rank
                                         1
                                                                      3
                                                  1
```

No validation of the reduced model as the full model did not validate. Knowing the most important features serves as a building block to future models, not to serve as model on its own.

```
[]: scores = cross_validate(logistic_model, X3, y, cv=skf,
    scoring=('accuracy', 'recall', 'precision'),
    return_train_score=True)
    ds = pd.DataFrame(scores).round(3)
    print(ds)
    print('\n')
```

```
print('Mean of test accuracy: %.3f' % ds['test_accuracy'].mean())
21
print('Mean of test recall: %.3f' % ds['test_recall'].mean())
print('Mean of test precision: %.3f' % ds['test_precision'].mean())
```

	${ t fit_time}$	score_time	test_accuracy	train_accuracy	test_recall	\
0	0.038	0.002	0.791	0.785	0.468	
1	0.006	0.002	0.779	0.789	0.414	
2	0.004	0.002	0.785	0.788	0.449	
3	0.016	0.002	0.796	0.785	0.488	
4	0.010	0.002	0.781	0.789	0.452	

	train_recall	test_precision	train_precision
0	0.454	0.646	0.632
1	0.460	0.625	0.642
2	0.453	0.634	0.642
3	0.454	0.655	0.634
4	0.466	0.619	0.641

Mean of test accuracy: 0.786 Mean of test recall: 0.454 Mean of test precision: 0.636

1.5.3 Estimate Validated Model on All Data

Not going to be using this model in the future in its current form, but for completeness, provide the best estimate of the model from all of the data.

```
[]: logistic_model.fit(X3, y)
```

[]: LogisticRegression(max_iter=500)

1.6 Apply the Model

ac. Forecast if the customer churns from new data.

Customer data:

Charges: 200Paperless: 1Check: 1Phone: 1Tenure: 12Dependents: 0

• Internet: 0

Create a list of these data values, making sure to enter in the same order that the variables appear in the X data frame.

Also, because the data was re-scaled, any new data from which to make a prediction also needs to be re-scaled. I do not believe there was an example of this, so the re-scaling transformation is provided here. Basically, take the mm_scaler construct previously defined from the original transformation, and then apply the transform() function by itself, without the fit() function.

```
[]: X_new = [[200, 1, 1, 1, 12, 0, 0]]

X_new = mm_scaler.transform(X_new)

X_new
```

/Users/chasecarlson/anaconda3/envs/GSCM575-env/lib/python3.10/site-packages/sklearn/base.py:439: UserWarning: X does not have valid feature names, but MinMaxScaler was fitted with feature names warnings.warn(

```
[]: array([[1.80845771, 1. , 1. , 1. , 0.16666667, 0. , 0. ]])
```

Now from this re-scaled list, create the forecast, Group 0 (not-churn) or Group 1 (churn) and the associated probability.

Reestablish the regression model with the full data set and all predictor variables:

```
[]: logistic_model.fit(X, y)
```

[]: LogisticRegression(max iter=500)

Run the model with the new variables:

```
[]: y_new = logistic_model.predict(X_new)
print("Predicted group membership:", y_new)
y_prob = logistic_model.predict_proba(X_new)
print(round(y_prob[0,1], 3))
```

Predicted group membership: [1] 0.97

/Users/chasecarlson/anaconda3/envs/GSCM575-env/lib/python3.10/site-packages/sklearn/base.py:439: UserWarning: X does not have valid feature names, but LogisticRegression was fitted with feature names warnings.warn(

/Users/chasecarlson/anaconda3/envs/GSCM575-env/lib/python3.10/site-packages/sklearn/base.py:439: UserWarning: X does not have valid feature names, but LogisticRegression was fitted with feature names warnings.warn(

The probability of this person being a member of group 1 is 97%, so label as Churn.