

$$\underline{Q2} \quad k\text{-form } \lambda = \sum_i f_i dx_{i_1} \wedge \dots \wedge dx_{i_k}$$

$$l\text{-form } \eta = \sum_j g_j dx_{j_1} \wedge \dots \wedge dx_{j_l}$$

$$d(\lambda \wedge \eta) = \sum_i \sum_j d(f_i g_j) \wedge dx_{i_1} \wedge \dots \wedge dx_{i_k} \wedge dx_{j_1} \wedge \dots \wedge dx_{j_l}$$

$$= \sum_i \sum_j (g_j df_i + f_i dg_j) \wedge dx_{i_1} \wedge \dots \wedge dx_{i_k} \wedge dx_{j_1} \wedge \dots \wedge dx_{j_l}$$

$$= \sum_i \sum_j \left( (df_i \wedge dx_{i_1} \wedge \dots \wedge dx_{i_k}) \wedge (g_j dx_{j_1} \wedge \dots \wedge dx_{j_l}) \right. \\ \left. + f_i dg_j \wedge \underbrace{dx_{i_1} \wedge \dots \wedge dx_{i_k}} \wedge dx_{j_1} \wedge \dots \wedge dx_{j_l} \right)$$

$$= \sum_i \sum_j (df_i \wedge dx_{i_1} \wedge \dots \wedge dx_{i_k}) \wedge (g_j dx_{j_1} \wedge \dots \wedge dx_{j_l}) \\ + \sum_i \sum_j (-1)^k (f_i \underbrace{dx_{i_1} \wedge \dots \wedge dx_{i_k}}) \wedge (dg_j \wedge dx_{j_1} \wedge \dots \wedge dx_{j_l})$$

$$= (d\lambda) \wedge \eta + (-1)^k \lambda \wedge d\eta$$