Team notebook

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16 edmond $_k arp$	10	a.push_back(0); for (int i = 0; i < a.size() - 1; i++) {	

```
a[i + 1] += a[i] / BASE;
               a[i] %= BASE;
               if (a[i] < 0) a[i] += BASE, a[i + 1]--;</pre>
       while (a.size() >= 2 && a.back() == 0) a.pop_back();
}
big operator + (big a, const big& b) {
       a.resize(max(a.size(), b.size()));
       for (int i = 0; i < b.size(); i++) a[i] += b[i];</pre>
       fix(a); return a;
}
big operator - (big a, const big& b) {
       for (int i = 0; i < b.size(); i++) a[i] -= b[i];</pre>
       fix(a); return a;
big operator * (const big& a, const big& b) {
       big c(a.size() + b.size());
       for (int i = 0; i < a.size(); i++)</pre>
       for (int j = 0; j < b.size(); j++) c[i + j] += a[i] * b[j];</pre>
       fix(c); return c;
}
big operator / (const big& a, int x) {
       big res;
       int r = 0:
       for (int i = a.size() - 1; i >= 0; i--) {
               r = r * BASE + a[i]:
               res.push_back(r / x);
               r %= x;
       reverse(res.begin(), res.end());
       fix(res); return res;
}
int operator % (const big& a, int x) {
       int r = 0:
       for (int i = a.size() - 1; i >= 0; i--) {
              r = r * BASE + a[i];
              r %= x;
       return r;
}
bool operator < (const big& a, const big& b) {</pre>
       if (a.size() != b.size()) return a.size() < b.size();</pre>
       for (int i = a.size() - 1; i >= 0; i--)
       if (a[i] != b[i]) return a[i] < b[i];</pre>
       return 0;
```

```
big stringToBig(const string& s) {
    big a(s.size() / LBASE + 1);
    for (int i = 0; i < s.size(); i++) {
        int x = (s.size() - i - 1) / LBASE;
        a[x] = a[x] * 10 + s[i] - '0';
    }
    fix(a); return a;
}

void Print(const big& a) {
    cout << a.back();
    for (int i = (int) a.size() - 2; i >= 0; i--)
        cout << setw(LBASE) << setfill('0') << a[i];
}</pre>
```

2 Bridge+Articuno

```
void dfs(int u, int p) {
       tin[u] = low[u] = ++now;
       if (u != p) parts[u]++;
       for (int v : a[u]) {
              if (v == p) continue;
              if (tin[v]) low[u] = min(low[u], tin[v]);
              else {
                      dfs(v, u);
                     low[u] = min(low[u], low[v]);
                      if (low[v] > tin[u]) bridge++;
                     if (low[v] >= tin[u]) parts[u]++; // part >= 2 ->
                          articuno++
              }
       }
void dfs(int u,int p){
       check[u]=root.size();
       if(u!=p)h[u]=h[p]+1;
       sz[u]=1;
       for(int v:a[u]){
              if(v==p)continue;
              if(!check[v]){
                      dfs(v.u):
                      sz[u]+=sz[v]:
                      dp[u] += dp[v];
```

```
}
else{
    if(h[u]<h[v])dp[u]--;
    else dp[u]++;
}
if(u!=p&&dp[u]==0)bridge.push_back(u);
}
```

3 ConvexHullTrick

```
struct Line {
       mutable int k, m, p;
       bool operator < (const Line& oth) const {</pre>
               if (oth.k == INF && oth.m == INF) return p < oth.p;</pre>
               return k < oth.k;</pre>
       }
};
struct ConvexHull : multiset<Line> {
       int divi(int x, int y) {
               return x / y - ((x ^y) < 0 & x % y);
       bool isect(iterator x, iterator y) {
               if (y == end()) return x \rightarrow p = INF, 0;
               if (x->k == y->k) x->p = x->m > y->m ? INF : -INF;
               else x->p = divi(y->m - x->m, x->k - y->k);
               return x->p >= y->p;
       }
       void add(int k, int m) {
               auto z = insert(\{k, m, 0\}), y = z++, x = y;
               while (isect(y, z)) z = erase(z);
               if (x != begin() && isect(--x, y)) isect(x, erase(y));
               while ((y = x) != begin() && (--x)->p >= y->p)
                      isect(x, erase(y));
       int query(int x) {
               assert(!empty());
               auto 1 = *lower_bound({INF, INF, x});
               return 1.k * x + 1.m:
       }
};
```

4 DSUrollback

```
int par[maxN];
int up[maxN];
int dist[maxN];
int cnt;
vector<pair<int*, int>> changes;
void rickroll(int id) {
       while (id < changes.size()) {</pre>
              *changes.back().first = changes.back().second;
              changes.pop_back();
       }
int Find(int u) {
       int res = par[u] >= 0 ? Find(par[u]) : u;
       if (res == u) up[u] = dist[u] = 0;
       else dist[u] = up[u] ^ dist[par[u]];
       return res;
}
void Unite(int u, int v) {
       int x = Find(u), y = Find(v);
       if (x == y) {
              if (dist[u] == dist[v]) {
                      changes.push_back({&cnt, cnt});
                      cnt++;
              return;
       if (par[x] > par[y]) swap(x, y);
       changes.push_back({&par[x], par[x]});
       changes.push_back({&par[y], par[y]});
       par[x] += par[y];
       par[y] = x;
       up[y] = dist[u] ^ dist[v] ^ 1;
```

5 DinicLowerbound

```
struct Dinic_lowerbound {
    struct edge {
        int v, rev;
}
```

```
int cap, flow;
       int dem;
};
int S, T;
vector<int> depth, ptr;
vector<vector<edge>> adj;
Dinic_lowerbound(int n) : S(n + 1), T(n + 2), depth(n + 5), ptr(n + 1)
    + 5), adj(n + 5) {}
Dinic_lowerbound() {}
void addEdge(int u, int v, int cap, int dem) {
       adj[u].push_back({v, (int)adj[v].size(), cap, 0, dem});
       adj[v].push_back({u, (int)adj[u].size() - 1, 0, 0, 0});
}
bool bfs() {
       fill(depth.begin(), depth.end(), 0);
       queue<int> q;
       depth[S] = 1;
       q.push(S);
       while (!q.empty() && !depth[T]) {
              int u = q.front(); q.pop();
              for (edge& e : adj[u]) {
                      if (depth[e.v] || e.cap - e.flow < 1)</pre>
                          continue;
                      depth[e.v] = depth[u] + 1;
                      q.push(e.v);
              }
       }
       return depth[T];
int dfs(int u, int flowIn) {
       if (u == T) return flowIn;
       int flowOut = 0;
       for (; ptr[u] < adj[u].size(); ptr[u]++) {</pre>
              edge& e = adj[u][ptr[u]];
              if (depth[u] + 1 != depth[e.v] || e.cap - e.flow ==
                   0) continue;
              int q = dfs(e.v, min(flowIn, e.cap - e.flow));
              flowOut += q;
              flowIn -= q;
              e.flow += q;
              adj[e.v][e.rev].flow -= q;
              if (flowIn == 0) break;
       }
       return flowOut;
}
```

```
int calc() {
               int maxFlow = 0;
               while (bfs()) {
                      fill(ptr.begin(), ptr.end(), 0);
                      maxFlow += dfs(S, INF);
               }
               return maxFlow;
       }
       int calc_with_lowerbound() {
               int n = S - 1;
               int s = n + 3:
               int t = n + 4;
               int sumDem = 0;
               vector\langle int \rangle in(n + 3), out(n + 3);
               for (int u = 1; u <= n + 2; u++)
               for (edge& e : adj[u]) {
                      sumDem += e.dem;
                      out[u] += e.dem;
                      in[e.v] += e.dem;
                      e.cap -= e.dem;
              }
               for (int u = 1; u <= n; u++) {</pre>
                      addEdge(s, u, in[u], 0);
                      addEdge(u, t, out[u], 0);
               addEdge(T, S, INF, 0);
               swap(s, S); swap(t, T);
               if (calc() != sumDem) return -1;
               swap(s, S); swap(t, T);
               for (int u = 1; u \le n + 2; u++)
               for (edge& e : adj[u]) {
                      e.cap += e.dem;
                      e.flow += e.dem;
               }
               for (int u = 1; u <= n; u++) {</pre>
                      adj[u].pop_back();
                      adj[u].pop_back();
               adj[S].pop_back(); adj[T].pop_back();
               return calc() + sumDem;
       }
};
```

6 Euclid*Diophante*

```
struct vl{
       long x,y;
};
long t;
long a,b,c,d;
long gcd(long a,long b){
       return b?gcd(b,a%b):a;
vl extended_euclid(long a,long b){
       long m=a,xm=1;
       long n=b, xn=0;
       while(n){
               long q=m/n;
               long r=m-q*n,xr=xm-q*xn;
               m=n, xm=xn;
               n=r,xn=xr;
       // \text{ if m < 0 } ?? (d = -1)
       return {xm,(m-a*xm)/b};
```

7 EulerCircle

8 Geometry

```
const double EPS = 1e-7;
const double DFT = 6969.69;
bool equal(const double& a, const double& b) {
       return abs(a - b) < EPS;</pre>
struct point {
       int x, y;
       point operator + (const point& oth) const {
              return {x + oth.x, y + oth.y};
       point operator - (const point& oth) const {
              return {x - oth.x, y - oth.y};
       }
       // Dot product
       int operator % (const point& oth) const {
              return x * oth.x + y * oth.y;
       }
       // Cross product
       int operator * (const point& oth) const {
              // Equal to 2 * area(a0b)
              // Postive if slope(a) < slope(b)</pre>
              // Negative if slope(a) > slope(b)
              // |x1 y1|
              // |x2 y2|
              return x * oth.y - oth.x * y;
       }
       int sqrlen() const {
              return x * x + y * y;
       double len() const {
              return sqrt(sqrlen());
       }
};
using Polygon = vector<point>;
point vect(const point& a, const point& b) {
       return b - a;
double turn(const point& a, const point& b) {
       // angle aOb in radian
       return atan2(a * b, a % b);
bool collinear(const point& a, const point& b, const point& c) {
```

```
return vect(a, b) * vect(b, c) == 0;
}
bool between(const point& a, const point& b, const point& c) {
       return collinear(a, b, c) && vect(a, b) % vect(b, c) >= 0;
}
// a -> b -> c = left turn?
bool leftTurn(const point& a, const point& b, const point& c) {
       return vect(a, b) * vect(b, c) > 0;
}
int polygonArea2(const vector<point>& p) {
       // Two times the area of a polygon with integral vertices
       // Positive if counterclockwise
       // Negative if clockwise
       int area2 = 0;
       for(int i = 0; i < p.size(); i++) {</pre>
              int j = (i + 1) % p.size();
              area2 += p[i] * p[j];
       }
       return area2:
}
bool inside_polygon(const point& a, const Polygon& p) {
       double angle = 0;
       for (int i = 0; i < p.size(); i++) {</pre>
              int j = (i + 1) % p.size();
              if (between(p[i], a, p[j])) return 1;
              angle += turn(vect(a, p[i]), vect(a, p[j]));
       }
       return equal(abs(angle), 2 * PI);
}
struct segment {
       point a, b;
}:
struct line {
       int a, b, c;
       line(const segment& 1) {
              point n = vect(1.a, 1.b);
              n = \{n.y, -n.x\};
              a = n.x;
              b = n.y;
              c = -(a * 1.a.x + b * 1.a.y);
       }
};
point line_intersection(const line& 11, const line& 12) {
       // la1 b1|
       // la2 b2l
```

```
double d = 11.a * 12.b - 12.a * 11.b;
       // |b1 c1|
       // lb2 c2l
       double dx = 11.b * 12.c - 12.b * 11.c;
       // |c1 a1|
       // lc2 a2l
       double dy = 11.c * 12.a - 12.c * 11.a;
       if (equal(d, 0)) {
              // Coincide
              if (equal(dx + dy, 0)) return {DFT, 1};
              // Nope
              return {DFT, 0};
       }
       return {dx / d, dy / d};
}
point intersection(const segment& 11, const segment& 12) {
       point p = line_intersection(line(l1), line(l2));
       if (p.x == DFT || !between(11.a, p, 11.b) || !between(12.a, p,
           12.b))
              return {DFT};
       return p;
}
void convex_hull {
       cin >> n; point p0 = {INF, INF};
       for (int i = 0; i < n; i++) {</pre>
              cin >> p[i].x >> p[i].y;
              if (p[i].y < p0.y \mid | (p[i].y == p0.y \&\& p[i].x < p0.x))
                      id = i, p0 = p[i];
       // Lowest + Leftmost point
       swap(p[id], p[0]);
       // Graham Scan
       sort(p + 1, p + n, [](const point& a, const point& b) {
              // Sort by slope
              // Same slope -> sort by len
              point u = a - p0;
              point v = b - p0;
              int t = u * v;
              return t > 0 || (t == 0 && u.sqrlen() < v.sqrlen());</pre>
       });
       // Find convex hull
       vector<point> q;
       for (int i = 0; i < n; i++) {</pre>
              // If right turn -> goodbye fellow
```

9 HLD

```
void pre_dfs(int u, int p) {
       par[u] = p;
       if (u != p) depth[u] = depth[p] + 1;
       sz[u] = 1;
       for (int& i : adj[u]) {
              int v = e[i].u ^ e[i].v ^ u;
              if (v == p) continue;
              pre_dfs(v, u);
              sz[u] += sz[v];
       }
}
void hld(int u, int p, int is_heavy, int lastEdge) {
       if (!is_heavy) head[u] = u;
       else head[u] = head[p];
       treePos[u] = ++ti;
       edgePos[lastEdge] = ti;
       int maxsz = 0, heavy = -1, heavyEdge;
       for (int& i : adj[u]) {
              int v = e[i].u ^ e[i].v ^ u;
              if (v == p || sz[v] <= maxsz) continue;</pre>
              maxsz = sz[v], heavy = v, heavyEdge = i;
       }
       if (heavy != -1) hld(heavy, u, 1, heavyEdge);
       for (int& i : adj[u]) {
              int v = e[i].u ^ e[i].v ^ u;
              if (v == p || v == heavy) continue;
              hld(v, u, 0, i);
       }
}
int query(int u, int v) {
       int res = 0:
       for (; head[u] != head[v]; v = par[head[v]]) {
              if (depth[head[u]] > depth[head[v]]) swap(u, v);
```

```
res = max(res, st.get(treePos[head[v]], treePos[v]));
}
if (depth[u] > depth[v]) swap(u, v);
res = max(res, st.get(treePos[u] + 1, treePos[v]));
return res;
}
```

10 PersitentSegtri

```
struct segment {
       int 1, r, p;
       bool operator < (const segment& oth) const {</pre>
               return 1 < oth.1;</pre>
}:
int n, m, k;
vector<segment> vec;
struct PersistentSegmentTree {
       static const int maxNodes = maxN * 19;
       struct Node {
               int v, lc, rc;
       };
       int n;
       vector<Node> st;
       vector<int> ver;
       PersistentSegmentTree(int n) {
               this \rightarrow n = n;
               st.reserve(maxNodes);
       PersistentSegmentTree() {}
       int create(Node a) {
               st.push_back(a);
               return st.size() - 1;
       int build(int 1, int r) {
               if (1 == r) {
                      return create({INF});
               int mid = (1 + r) / 2;
               int id = create({INF, build(1, mid), build(mid + 1, r)});
               return id:
       }
```

```
int update(int i, int v, int oldId, int l, int r) {
              if (1 == r) {
                      return create({min(v, st[oldId].v)});
              }
              int mid = (1 + r) / 2;
              int id = create(st[oldId]);
              if (i <= mid)</pre>
                      st[id].lc = update(i, v, st[oldId].lc, l, mid);
              else
                      st[id].rc = update(i, v, st[oldId].rc, mid + 1, r);
              st[id].v = max(st[st[id].lc].v, st[st[id].rc].v);
              return id;
       }
       int get(int L, int R, int id, int 1, int r) {
              if (R < 1 || r < L) return -1;
              if (L <= 1 && r <= R) return st[id].v;</pre>
              int mid = (1 + r) / 2;
              int lv = get(L, R, st[id].lc, l, mid);
              int rv = get(L, R, st[id].rc, mid + 1, r);
              return max(lv, rv);
       }
       void build() {
              ver.push_back(0);
              build(1, n);
       void update(int i, int v) {
              ver.push_back(update(i, v, ver.back(), 1, n));
       }
       int get(int L, int R, int k) {
              return get(L, R, ver[k], 1, n);
       }
} pst;
```

11 $\mathbf{Z}_a lgo$

```
r = i + z[i] - 1;
}
}
```

12 ahocorasick

```
struct Trie {
       struct Node {
              int child[C];
              int par;
              int val;
              int link = 0;
              int nex[C];
              int ends = 0:
              int cnt = 0;
              Node(int par = -1, int val = -1) : par(par), val(val) {
                     fill(child, child + C, 0);
                     fill(nex, nex + C, 0);
              }
       };
       vector<Node> trie;
       Trie() {
              trie.reserve(maxLen);
              trie.push_back(Node());
       }
       void add(const string& s) {
              int v = 0;
              for (char c : s) {
                     c = 'A';
                     if (!trie[v].child[c]) {
                             trie[v].child[c] = trie.size();
                             trie.push_back(Node(v, c));
                     v = trie[v].child[c];
              trie[v].ends++;
       }
       void Ahchoo() {
              queue<int> q;
              q.push(0);
              while (!q.empty()) {
```

```
int u = q.front(); q.pop();
                      int p = trie[u].link;
                      trie[u].cnt = trie[p].cnt + trie[u].ends;
                      for (int c = 0; c < C; c++) {</pre>
                             if (trie[u].child[c]) {
                                     trie[trie[u].child[c]].link =
                                         trie[p].nex[c];
                  trie[u].nex[c] = trie[u].child[c];
                                     q.push(trie[u].child[c]);
                             }
                             else {
                                     trie[u].nex[c] = trie[p].nex[c];
                             }
                      }
              }
       }
} trie;
```

13 bit2d

```
int BIT[N][M];
void add(int u, int v, int x){
   for(int i = u; i <= n; i += i&(-i)){
       for(int j = v; j <= m; j += j&(-j))BIT[i][j]+=x;
   }
}
int query(int u, int v){
   int sum = 0;
   for(int i = u; i > 0; i -= i\&(-i)){
       for(int j = v; j > 0; j -= j\&(-j))sum += BIT[i][j];
   }
   return sum;
}
void rectAdd(int a, int b, int u, int v, int x){
   add(a, b, x);
   add(u+1, v+1, x);
   add(u+1, b, -x);
   add(a, v+1, -x);
}
int BIT[4][N][M]; // {D[i][j]; i*D[i][j]; j*D[i][j]; i*j*D[i][j]}
```

```
void add(int u, int v, int x){
   for(int i = u; i <= n; i += i&(-i)){
       for(int j = v; j <= m; j += j&(-j)){
           BIT[0][i][j] += x;
           BIT[1][i][j] += u * x;
           BIT[2][i][j] += v * x;
           BIT[3][i][j] += u * v * x;
       }
   }
}
void rectAdd(int a, int b, int u, int v, int x){
   add(a, b, x);
   add(a, v + 1, -x);
   add(u + 1, b, -x);
   add(u + 1, v + 1, x);
// ben bit 2d
vector<int> pos[N];
vector<int> BIT[N];
void fakeAdd(int u, int v, int x){
   for(u; u <= n; u += u&(-u)){</pre>
       pos[u].push_back(v);
}
void fakeQuery(int u, int v){
   for(u; u <= n; u += u&(-u)){</pre>
       pos[u].push_back(v);
   }
}
void compress(){
   for(int i = 1; i <= n; i++){</pre>
       pos[i].push_back(0);
       sort(pos[i].begin(), pos[i].end());
       pos[i].erase(unique(pos[i].begin(), pos[i].end()), pos[i].end());
       BIT[i].assign(pos[i].size(), 0);
   }
}
void add(int u, int v, int x){
   for(int i = u; i <= n; i += i&(-i)){
       for(int j = lower_bound(pos[i].begin(), pos[i].end(), v) -
           pos[i].begin(); j < BIT[i].size(); j += j&(-j)){
           BIT[i][j] += x;
```

```
}
}

void query(int u, int v){
   int sum = 0;
   for(int i = u; i > 0; i -= i&(-i)){
      for(int j = lower_bound(pos[i].begin(), pos[i].end(), v) -
            pos[i].begin(); j > 0; j -= j&(-j)){
        sum += BIT[i][j];
      }
}
return sum;
}
```

14 centroid

```
void pre_dfs(int u, int p) {
       sz[u] = 1;
       for (int& v : adj[u]) {
              if (v == p || ban[v]) continue;
              pre_dfs(v, u);
              sz[u] += sz[v];
       }
}
int centos(int u, int p, int root) {
       for (int& v : adj[u]) {
              if (v == p || ban[v]) continue;
              if (sz[v] * 2 > sz[root])
                      return centos(v, u, root);
       }
       return u;
}
void decompose(int u) {
       pre_dfs(u, u);
       ban[u = centos(u, u, u)] = 1;
       for (int& v : adj[u])
       if (!ban[v]) decompose(v);
```

15 dinic

```
struct Dinic {
       static const bool SCALING = false;
       int lim;
       struct edge {
              int v, rev;
              int cap, flow;
       };
       int S, T;
       vector<int> depth, ptr;
       vector<vector<edge>> adj;
       Dinic(int n): S(n + 1), T(n + 2), depth(n + 3), ptr(n + 3), adj(n + 3)
           + 3) {}
       Dinic() {}
       void addEdge(int u, int v, int cap, int undirected = 0) {
              adj[u].push_back({v, (int)adj[v].size(), cap, 0});
              adj[v].push_back({u, (int)adj[u].size() - 1, cap *
                   undirected, 0});
       }
       bool bfs() {
              fill(depth.begin(), depth.end(), 0);
              queue<int> q;
              depth[S] = 1;
              q.push(S);
              while (!q.empty() && !depth[T]) {
                      int u = q.front(); q.pop();
                      for (edge& e : adj[u]) {
                             if (depth[e.v] || e.cap - e.flow < lim)</pre>
                                 continue;
                             depth[e.v] = depth[u] + 1;
                             q.push(e.v);
                      }
              return depth[T];
       }
       int dfs(int u, int flowIn) {
              if (u == T) return flowIn;
              int flowOut = 0;
              for (; ptr[u] < adj[u].size(); ptr[u]++) {</pre>
                      edge& e = adj[u][ptr[u]];
                      if (depth[u] + 1 != depth[e.v] || e.cap - e.flow ==
                          0) continue;
                      int q = dfs(e.v, min(flowIn, e.cap - e.flow));
```

```
flowIn -= q;
                      flowOut += q;
                      e.flow += q;
                      adj[e.v][e.rev].flow -= q;
                     if (flowIn == 0) break;
              }
              return flowOut;
       }
       int calc() {
              int maxFlow = 0;
              for (lim = SCALING ? (1 << 12) : 1; lim; lim >>= 3) {
                      while (bfs()) {
                             fill(ptr.begin(), ptr.end(), 0);
                             maxFlow += dfs(S, INF);
                     }
              }
              return maxFlow;
       }
};
```

16 $edmond_k arp$

```
void add_edge(int u, int v, int c) {
       a[u].push_back(v);
       a[v].push_back(u);
       cap[u][v] = c;
void inc_flow(int u, int v, int f) {
       flow[u][v] += f;
       flow[v][u] -= f;
       if (u == s) max_flow += f;
}
int residual(int u, int v) {
       return cap[u][v] - flow[u][v];
}
void bfs(int s, int t) {
       fill(par + 1, par + 1 + n, 0);
       queue<int> q;
       par[s] = s;
       q.push(s);
       while (!q.empty() && par[t] == 0) {
              int u = q.front(); q.pop();
```

```
for (int& v : a[u]) {
                      if (par[v] != 0 || residual(u, v) == 0) continue;
                      par[v] = u;
                      q.push(v);
              }
       }
bool find_augmenting_path() {
       bfs(s, t);
       return par[t] != 0;
}
void augment() {
       int minn = INF;
       for (int v = t; v != s; v = par[v])
              minimize(minn, residual(par[v], v));
       for (int v = t; v != s; v = par[v])
              inc_flow(par[v], v, minn);
signed main() {
       while (find_augmenting_path())
              augment();
       cout << max_flow;</pre>
}
```

17 fft

```
using namespace std;

#define pb push_back
#define mp make_pair
#define sz(a) (int)(a).size()
#define all(a) (a).begin(), (a).end()

#define forn(i,n) for (int i=0; i<int(n); ++i)
#define fornd(i,n) for (int i=int(n)-1; i>=0; --i)
#define xrange(i,a,b) for (int i=int(a); i<int(b); ++i)

typedef long long ll;
typedef long double ld;
typedef unsigned long long ull;</pre>
```

```
const int INF = (int) 1e9;
const long long INF64 = (long long) 1e18;
const long double eps = 1e-9;
const long double pi = 3.14159265358979323846;
const int mod = 7340033;
const 11 root = 5:
const 11 root_1 = 4404020;
const ll root_pw = 1<<20;</pre>
int rev_element[7340033];
11 getmod(ll a, ll tmod){
    return ((a%tmod)+tmod)%tmod;
}
void fft (vector<ll> & a, bool invert) {
    int n = (int) a.size():
   for (int i=1, j=0; i<n; ++i) {</pre>
       int bit = n >> 1;
       for (; j>=bit; bit>>=1)
           j -= bit;
       j += bit;
       if (i < j)
           swap (a[i], a[j]);
    }
    for (int len=2; len<=n; len<<=1) {</pre>
       11 wlen = invert ? root_1 : root;
       for (int i=len; i<root_pw; i<<=1)</pre>
           wlen = ll (wlen * 1ll * wlen % mod);
       for (int i=0; i<n; i+=len) {</pre>
           11 w = 1;
           for (int j=0; j<len/2; ++j) {</pre>
               ll u = a[i+j], v = ll (a[i+j+len/2] * 1ll * w % mod);
               a[i+j] = getmod(u+v,mod);
               a[i+j+len/2] = getmod(u-v,mod);
               w = 11 (w * 111 * wlen % mod);
           }
       }
    }
    if (invert) {
       11 nrev = rev_element[n];
```

```
for (int i=0; i<n; ++i)</pre>
           a[i] = int (a[i] * 111 * nrev % mod);
   }
}
void precalc(){
    rev_element[1] = 1;
    for (int i=2; i<mod; i++)</pre>
       rev_element[i] = (mod - (mod/i) * rev_element[mod%i] % mod) % mod;
}
void multiply (const vector<11> & a, const vector<11> & b, vector<11> &
    vector <11> fa (a.begin(), a.end()), fb (b.begin(), b.end());
    size_t n = 1;
   while (n < max (a.size(), b.size())) n <<= 1;</pre>
    n <<= 1:
    fa.resize (n), fb.resize (n);
    fft (fa, false), fft (fb, false);
    forn(i,n)
       fa[i] *= fb[i];
    fft (fa, true);
    res.resize (n):
    forn(i,n)
       res[i] = fa[i] % mod:
}
int MN = 29;
int MK = 1001;
vector <vector <11> > dp(MN+2,vector <11> (MK,0));
vector <11> d:
void init(){
    int m;
    for (int i=0; i<=MN; i++){</pre>
       dp[i][0] = 1;
       multiply(dp[i],dp[i],d);
       d.resize(MK);
       multiply(d,d,dp[i+1]);
       dp[i+1].insert(dp[i+1].begin(),0);
       dp[i+1].resize(MK);
   }
```

18 gauss

```
void Gauss(int n) {
       for(int i = 0; i < n; i++) {</pre>
               for(int j = i; j < n; j++) {
                       if(P[j][i] != 0) {
                               for(int k = 0; k <= n; k++) {</pre>
                                       swap(P[j][k], P[i][k]);
                               break;
                       }
               }
               if(P[i][i] == 0) continue;
               for(int j = 0; j < n; j++) {</pre>
                       if(i == j) continue;
                       num coef = P[j][i] / P[i][i];
                       for(int k = 0; k <= n; k++) P[j][k] -= P[i][k] *</pre>
               }
       }
       for(int i = 0; i < n; i++) C[i] = P[i][n] / P[i][i];</pre>
       degree = n - 1;
```

19 $\mathbf{hash}_N ewSA_w ip$

```
const int K = 269;
const int MOD1 = 1e9 + 7, MOD2 = 998244353;
int pw1[maxLen], pw2[maxLen];
void init_pw() {
        for (int i = 0; i < maxLen; i++) {
            pw1[i] = i ? pw1[i - 1] * K % MOD1 : 1;
            pw2[i] = i ? pw2[i - 1] * K % MOD2 : 1;
        }
}
struct Hash {
    int x, y;
    bool operator == (const Hash& oth) const {
        return x == oth.x && y == oth.y;
}</pre>
```

```
};
struct Roll : vector<Hash> {
       string s;
       Roll(const string& s) : s(s) {
              assign(s.size(), {0, 0});
              for (int i = 1; i < s.size(); i++) {</pre>
                      at(i).x = (at(i - 1).x * K + s[i]) % MOD1;
                      at(i).y = (at(i - 1).y * K + s[i]) % MOD2;
              }
       }
       Roll() {}
       Hash get(int 1, int r) {
              Hash res;
              res.x = (at(r).x - at(1 - 1).x * pw1[r - 1 + 1] + MOD1 *
                   MOD1) % MOD1;
              res.y = (at(r).y - at(1 - 1).y * pw2[r - 1 + 1] + MOD2 *
                   MOD2) % MOD2;
              return res;
       }
       int lcp(int i, int j) {
              int l = 0, r = size() - max(i, j);
              while (1 < r) {
                     int mid = (r - 1) / 2 + 1 + 1;
                      if (get(i, i + mid - 1) == get(j, j + mid - 1)) l =
                          mid;
                     else r = mid - 1;
              }
              return 1;
       bool cmp(int i, int j) {
              int 1 = lcp(i, j);
              if (i + 1 - 1 == size() - 1) return 1;
              if (j + 1 - 1 == size() - 1) return 0;
              return s[i + 1] < s[j + 1];
       }
};const int K = 269;
const int MOD1 = 1e9 + 7, MOD2 = 998244353;
int pw1[maxLen], pw2[maxLen];
void init_pw() {
       for (int i = 0; i < maxLen; i++) {</pre>
              pw1[i] = i ? pw1[i - 1] * K % MOD1 : 1;
              pw2[i] = i ? pw2[i - 1] * K % MOD2 : 1;
       }
struct Hash {
```

```
int x, y;
       bool operator == (const Hash& oth) const {
              return x == oth.x && y == oth.y;
};
struct Roll : vector<Hash> {
       string s;
       Roll(const string& s) : s(s) {
              assign(s.size(), {0, 0});
              for (int i = 1; i < s.size(); i++) {</pre>
                      at(i).x = (at(i - 1).x * K + s[i]) % MOD1;
                      at(i).y = (at(i - 1).y * K + s[i]) % MOD2;
              }
       }
       Roll() {}
       Hash get(int 1, int r) {
              Hash res;
              res.x = (at(r).x - at(1 - 1).x * pw1[r - 1 + 1] + MOD1 *
                   MOD1) % MOD1;
              res.y = (at(r).y - at(1 - 1).y * pw2[r - 1 + 1] + MOD2 *
                   MOD2) % MOD2;
              return res;
       }
       int lcp(int i, int j) {
              int l = 0, r = size() - max(i, j);
              while (1 < r) {
                      int mid = (r - 1) / 2 + 1 + 1;
                      if (get(i, i + mid - 1) == get(j, j + mid - 1)) l =
                          mid:
                      else r = mid - 1;
              }
              return 1;
       bool cmp(int i, int j) {
              int l = lcp(i, j);
              if (i + 1 - 1 == size() - 1) return 1;
              if (j + 1 - 1 == size() - 1) return 0;
              return s[i + 1] < s[j + 1];
       }
};
```

20 kmp

```
void kmp (string &s) {
       // KMP
       s = " " + s;
   for (int i = 2; i <= n; i++) {
       int j = p[i - 1];
       while (j > 0 \&\& s[j + 1] != s[i])
           j = p[j];
       if (s[j + 1] == s[i]) p[i] = j + 1;
    // Automation
   for (int i = 0; i <= n; i++) {</pre>
       for (int j = 0; j < C; j++) {</pre>
           int t = i;
           while (t > 0 \&\& s[t + 1] != 'a' + j)
               t = p[t];
           if(s[t + 1] == 'a' + j) f[i][j] = t + 1;
       }
}
```

21 lagrange interpolation

```
void add_poly (vector<ll> &a, vector<ll> &b) {
       for (int i = 0; i < (int) a.size(); i++) {</pre>
               a[i] = add (a[i], b[i]);
       }
void nhan (vector<ll> &a , ll chim) {
       vector<11> tmp (k + 2, 0);
       for (int i=0;i<=k;i++) {</pre>
               tmp[i + 1] = a[i];
       }
       for (int i=0;i<=k + 1;i++) {</pre>
               tmp[i] = sub (tmp[i], 1ll * chim * a[i] % mod);
       }
       a = tmp;
void init () {
       dt.resize (k + 2);
       for (int i=1;i<=k + 1;i++) {</pre>
               p[i] = add (p[i - 1], cdt (i, k));
       }
```

```
for (int i=0;i<=k + 1;i++) {
    vector<ll> tmp (k + 2, 0);
    tmp[0] = p[i];
    ll dak = 1;
    for (int j=0;j<=k + 1;j++) {
        if (j==i) continue;
        nhan (tmp, j);
        dak = 1ll * dak * cdt ( sub (i, j), mod - 2) % mod;
    }
    for (ll &j : tmp) {
        j = 1ll * j * dak % mod;
    }
    add_poly (dt, tmp);
}</pre>
```

$22 \quad \mathbf{max}_m atch$

```
bool dfs (int u) {
       if (vis[u]) return 0;
       vis[u] = 1;
       for (int v : adj[u]) {
               if (ass[v] == 0 || dfs (ass[v])) {
                       ass[v] = u;
                       return 1;
               }
       return 0;
}
signed main () {
       random_shuffle (p + 1, p + 1 + n);
       for (int i=1;i<=n;i++) {</pre>
               memset (vis , 0 , sizeof (vis));
               match += dfs (p[i]);
       }
       cout<<match<<'\n';</pre>
       for (int i=1;i<=m;i++) {</pre>
               cout<<ass[i]<<" ":
       }
```

23 mincostflow

```
struct MinCostFlow {
       struct edge {
              int u, v, rev;
              int cap, flow;
              int cost;
       };
       int S, T;
       vector<int> dist, inq;
      vector<edge*> par;
      vector<vector<edge>> adj;
       MinCostFlow(int n) : S(n + 1), T(n + 2), dist(n + 3), inq(n + 3),
           par(n + 3), adj(n + 3) {}
      MinCostFlow() {}
       void addEdge(int u, int v, int cap, int cost) {
              adj[u].push_back({u, v, (int)adj[v].size(), cap, 0, cost});
              adj[v].push_back({v, u, (int)adj[u].size() - 1, 0, 0,
                  -cost});
       }
       bool spfa() {
              fill(dist.begin(), dist.end(), INF);
              queue<int> q;
              dist[S] = 0;
              q.push(S);
              inq[S] = 1;
              while (!q.empty()) {
                     int u = q.front(); q.pop();
                     inq[u] = 0;
                     for (edge& e : adj[u]) {
                             if (dist[u] + e.cost >= dist[e.v] || e.cap -
                                 e.flow == 0) continue;
                             dist[e.v] = dist[u] + e.cost;
                             par[e.v] = &e;
                             if (!inq[e.v]) {
                                    q.push(e.v);
                                    inq[e.v] = 1;
                             }
                     }
```

```
return dist[T] != INF;
       }
       pair<int, int> calc() {
               int flow = 0, cost = 0;
               while (spfa()) {
                      int f = INF;
                      for (int u = T; u != S; u = par[u] \rightarrow u)
                              f = min(f, par[u]->cap - par[u]->flow);
                       for (int u = T; u != S; u = par[u] -> u) {
                              par[u]->flow += f;
                              adj[u][par[u]->rev].flow -= f;
                      flow += f;
                       cost += f * dist[T];
               }
               return {flow, cost};
       }
};
```

24 \mathbf{pst}_lazy

```
struct PersistentSegmentTree {
       static const int maxNodes = maxN * (logN + 4) * 3;
       int n, p = 0;
       vector<int> lc, rc;
       vector<int> st;
       vector<int> lazy1, lazy2;
       vector<int> ver;
       PersistentSegmentTree(int n) : n(n), lc(maxNodes), rc(maxNodes),
           st(maxNodes), lazy1(maxNodes), lazy2(maxNodes) {}
       PersistentSegmentTree() {}
       int leaf(int v) {
              st[++p] = v;
              return p;
       }
       int parent(int 1, int r) {
              p++;
              if (p >= maxNodes) {cout << "br0"; exit(0);}</pre>
              lc[p] = 1;
              rc[p] = r;
              st[p] = st[1] + st[r];
              return p;
```

```
}
void change(int v1, int v2, int id, int 1, int r) {
       st[id] += v1 * (r - 1 + 1);
       lazv1[id] += v1;
       st[id] += v2 * (1 + r) * (r - 1 + 1) / 2;
       lazy2[id] += v2;
}
int lazykid(int v1, int v2, int id, int l, int r) {
       p++;
       if (p >= maxNodes) {cout << "br0"; exit(0);}</pre>
       lc[p] = lc[id]:
       rc[p] = rc[id];
       st[p] = st[id];
       lazy1[p] = lazy1[id];
       lazy2[p] = lazy2[id];
       change(v1, v2, p, 1, r);
       return p;
}
void down(int id, int 1, int r) {
       if (lazy1[id] == 0 && lazy2[id] == 0) return;
       int mid = (1 + r) / 2;
       lc[id] = lazykid(lazy1[id], lazy2[id], lc[id], l, mid);
       rc[id] = lazykid(lazy1[id], lazy2[id], rc[id], mid + 1, r);
       lazy1[id] = 0;
       lazy2[id] = 0;
}
int build(int 1, int r) {
       if (1 == r) return leaf(0);
       int mid = (1 + r) / 2;
       return parent(build(1, mid), build(mid + 1, r));
}
int update(int L, int R, int v1, int v2, int id, int 1, int r) {
       if (R < 1 \mid | r < L) return id;
       if (L <= 1 && r <= R) return lazykid(v1, v2, id, 1, r);</pre>
       down(id, 1, r);
       int mid = (1 + r) / 2;
       return parent(update(L, R, v1, v2, lc[id], 1, mid),
           update(L, R, v1, v2, rc[id], mid + 1, r));
}
int get(int L, int R, int id, int l, int r) {
       if (R < 1 || r < L) return 0;
       if (L <= 1 && r <= R) return st[id];</pre>
       down(id, 1, r);
       int mid = (1 + r) / 2;
       int lv = get(L, R, lc[id], 1, mid);
```

25 pst_new

```
struct v1 {
       int x, y;
       bool operator < (const vl& oth) const {</pre>
               if (x != oth.x) return x > oth.x;
              return y < oth.y;</pre>
       }
};
int n, q;
int a[maxN];
vl b[maxN];
struct PersistentSegmentTree {
       static const int maxNodes = maxN * (logN + 4);
       int n, p = 0;
       vector<int> lc, rc;
       vector<int> st;
       vector<int> ver;
       PersistentSegmentTree(int n) : n(n), lc(maxNodes), rc(maxNodes),
            st(maxNodes) {}
       PersistentSegmentTree() {}
       int leaf(int v) {
               st[++p] = v;
               return p;
       int parent(int 1, int r) {
               p++;
              lc[p] = 1;
```

```
rc[p] = r;
              st[p] = st[1] + st[r];
              return p;
       }
       int build(int 1, int r) {
              if (1 == r) return leaf(0);
              int mid = (1 + r) / 2;
              return parent(build(1, mid), build(mid + 1, r));
       }
       int update(int i, int v, int id, int l, int r) {
              if (i < 1 | | r < i) return id:
              if (1 == r) return leaf(st[id] + v);
              int mid = (1 + r) / 2;
              return parent(update(i, v, lc[id], l, mid), update(i, v,
                   rc[id], mid + 1, r));
       }
       int get(int L, int R, int id, int 1, int r) {
              if (R < 1 || r < L) return 0;</pre>
              if (L <= 1 && r <= R) return st[id];</pre>
              int mid = (1 + r) / 2;
              int lv = get(L, R, lc[id], 1, mid);
              int rv = get(L, R, rc[id], mid + 1, r);
              return lv + rv;
       }
       void build() {
              ver.push_back(build(1, n));
       }
       void update(int i, int v) {
              ver.push_back(update(i, v, ver.back(), 1, n));
       }
       int get(int L, int R, int k) {
              return get(L, R, ver[k], 1, n);
       }
} pst;
```

$26 \quad \mathbf{rabin}_m iller r$

```
bool isPrime(ull n) {
    if (n < 2 || n % 6 % 4 != 1) return (n | 1) == 3;
    ull A[] = {2, 325, 9375, 28178, 450775, 9780504, 1795265022},
        s = __builtin_ctzll(n-1), d = n >> s;
    for (ull a : A) { // ^ count trailing zeroes
```

$27 ext{ segtri2D}$

```
struct io {
     template
                   <class T> inline static T next() {
           Т
                        n; std::cin >> n;
           return
                             n;
           }
};
struct node {
               () : max(INT_MIN), min(INT_MAX) {}
     node
               begin, end, mid, min, max;
     int
};
template<int size> struct segment_tree {
     node
                tree[size << 2];</pre>
     void
                init_tree(int index, int left, int right, int values[]) {
                          & now = tree[index];
           node
                         .begin = left, now.end = right;
           now
                         .mid = (now.begin + now.end) >> 1;
           now
           if
                         (now.begin != now.end) {
                init_tree
                                          (L(index), now.begin, now.mid,
    values);
                                          (R(index), now.mid + 1, now.end,
                init tree
    values);
                                    .max = max(now.max,
                now
    max(tree[L(index)].max, tree[R(index)].max));
                                    .min = min(now.min,
    min(tree[L(index)].min, tree[R(index)].min));
                      } else
                                    .min = now.max = values[now.begin]:
                now
           }
```

```
state
                 update(int index, int at, int value, int values[]) {
           node
                          & now = tree[index];
                          (now.begin == at && now.end == at) {
           if
                                     .max = now.min = value;
                 now
                 values
                                        [at] = value;
                 return
                                        state(value, value);
           if
                          (now.begin > at || now.end < at)</pre>
                                        state(now.max, now.min);
                 return
                            s1 = update(L(index), at, value, values);
           state
                            s2 = update(R(index), at, value, values);
           state
                          .max = max(s1.first, s2.first);
           now
                          .min = min(s1.second, s2.second);
           now
                             state(now.max, now.min);
           return
           }
     state
                 query(int index, int left, int right) {
           node
                          & now = tree[index];
           if
                          (now.begin >= left && now.end <= right)</pre>
                 return
                                        state(now.max, now.min);
                          (now.begin > right || now.end < left)</pre>
           if
                 return
                                        state(INT_MIN, INT_MAX);
                            result(INT_MIN, INT_MAX);
           state
                            s1 = query(L(index), left, right);
           state
           state
                            s2 = query(R(index), left, right);
                            .first = max(result.first, max(s1.first,
           result
    s2.first)):
                            .second = min(result.second, min(s1.second,
           result
    s2.second)):
           return
                             result;
           }
};
segment_tree<MAXN> tree[MAXN];
int values[MAXN][MAXN];
```

28 $suffix_a rray$

```
#include<bits/stdc++.h>
using namespace std;
using 11 = long long;
mt19937 rng(time(NULL));
```

```
int ran(int 1, int r) {
       return rng() % (r - 1 + 1) + 1;
bool is_prime(int x) {
       for (int i = 2; i * i <= x; i++)
       if (x % i == 0) return 0;
       return 1;
}
const int maxLen = 2e5 + 69;
const int K = 317;
const int MS = 1:
int MODS[MS];
11 MM[MS];
using hsh = array<int, MS>;
hsh powK[maxLen];
hsh operator + (hsh h, int c) {
       for (int i = 0; i < MS; i++)</pre>
              h[i] = (111 * h[i] * K + c) % MODS[i];
       return h:
}
void init_hsh() {
       const int MINN = 8e8, MAXX = 1e9;
       for (int i = 0; i < MS; i++) {</pre>
              MODS[i] = ran(MINN, MAXX);
               while (!is_prime(MODS[i])) MODS[i]++;
              MM[i] = 111 * MODS[i] * MODS[i];
              powK[0][i] = 1:
       for (int i = 1; i < maxLen; i++) powK[i] = powK[i - 1] + 0;</pre>
}
struct Hash {
       string s;
       vector<hsh> h;
       Hash(const string& s) {
              this->s = s;
              h.resize(s.size());
              for (int i = 1; i < s.size(); i++) h[i] = h[i - 1] + s[i];</pre>
       Hash() {}
       hsh get(int 1, int r) {
              hsh res;
              for (int i = 0; i < MS; i++)</pre>
              res[i] = (h[r][i] - 111 * h[1 - 1][i] * powK[r - 1 + 1][i]
                   + MM[i]) % MODS[i];
               return res;
```

```
}
       int lcp(int i, int j) {
               int l = 0, r = s.size() - max(i, j);
               while (1 < r) {
                      int mid = (r - 1) / 2 + 1 + 1;
                      if (get(i, i + mid - 1) == get(j, j + mid - 1)) l =
                          mid;
                      else r = mid - 1:
              }
               return 1;
       }
       bool cmp(int i, int j) {
               int 1 = lcp(i, j);
               if (i + 1 - 1 == s.size() - 1) return 1;
               if (j + 1 - 1 == s.size() - 1) return 0;
              return s[i + 1] < s[j + 1];
       }
};
bool minimize(int& a, int b) {
       return a > b? a = b, 1 : 0;
}
const int maxN = 2e5 + 69;
const int logN = 19;
struct vl {
       int x, y;
       bool operator < (const vl& oth) const {</pre>
               if (x != oth.x) return x < oth.x;</pre>
               return y < oth.y;</pre>
       }
};
int n;
string s;
Hash h;
int sa[maxN];
int lcp[maxN];
vl minn[maxN][logN];
set<int> se[maxN];
int x = 0, y = 1;
void Try(int a, int b) {
       // x / y vs a / b
       if (111 * x * b < 111 * a * y) x = a, y = b;
```

```
}
void build() {
       for (int i = 1; i < n; i++) minn[i][0] = {lcp[i], i};</pre>
       for (int j = 1; j < logN; j++)
       for (int i = 1; i + (1 << j) - 1 < n; i++)
              minn[i][j] = min(minn[i][j - 1], minn[i + (1 << (j -
                  1))][j - 1]);
}
vl get(int 1, int r) {
       int j = 31 - \_builtin\_clz(r - 1 + 1);
       return min(minn[1][j], minn[r - (1 << j) + 1][j]);</pre>
}
int solve(int 1, int r) {
       if (1 == r) {
              se[1].insert(sa[1]);
              return 1:
       }
       vl mid = get(1, r - 1);
       int left = solve(1, mid.y);
       int right = solve(mid.y + 1, r);
       if (se[left].size() > se[right].size()) swap(left, right);
       for (auto& u : se[left]) {
              auto it = se[right].lower_bound(u);
              if (it != se[right].end()) Try(mid.x, abs(u - *it));
              if (it != se[right].begin()) {
                     it--;
                      Try(mid.x, abs(u - *it));
              }
       }
       for (auto& u : se[left]) se[right].insert(u);
       return right;
}
signed main() {
       ios::sync_with_stdio(0);
       cin.tie(0); cout.tie(0);
       init_hsh();
       cin >> s;
       n = s.size();
       s = ' + s;
       h = Hash(s);
```

```
for (int i = 1; i <= n; i++) sa[i] = i;
stable_sort(sa + 1, sa + 1 + n, [&] (int i, int j) {
          return h.cmp(i, j);
});

for (int i = 1; i < n; i++) lcp[i] = h.lcp(sa[i], sa[i + 1]);
build();

solve(1, n);

int d = __gcd(x, y);
x /= d;
y /= d;
x += y;
cout << x << '/' << y;
}</pre>
```

29 tarjanSCC

```
void dfs(int u) {
       tin[u] = low[u] = ++cnt;
       st.push_back(u);
       for (int v : a[u]) {
              if (tin[v]) low[u] = min(low[u], tin[v]);
              else {
                     dfs(v):
                     low[u] = min(low[u], low[v]);
              }
       }
       if (tin[u] == low[u]) {
              scc++;
              while (1) {
                     int v = st.back();
                     st.pop_back();
                     tin[v] = low[v] = INF;
                     root[v] = scc;
                     sz[scc]++;
                     if (v == u) break;
              }
      }
```