T = tree F = forward B = back C = cross

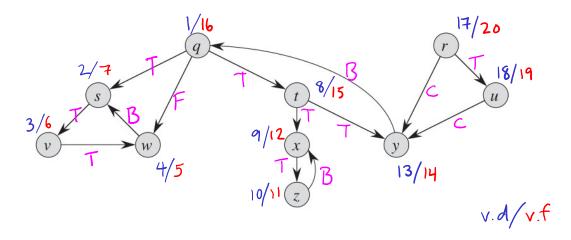


Figure 22.6 A directed graph for use in Exercises 22.3-2 and 22.5-2.

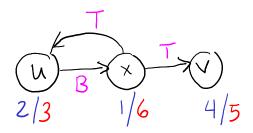
Complete the following exercises on a separate sheet of paper. Refer to the next page for DFS code.

22.3-2

Show how depth-first search works on the graph of Figure 22.6. Assume that the **for** loop of lines 5–7 of the DFS procedure considers the vertices in alphabetical order, and assume that each adjacency list is ordered alphabetically. Show the discovery and finishing times for each vertex, and show the classification of each edge.

22.3-9

Give a counterexample to the conjecture that if a directed graph G contains a path from u to v, then any depth-first search must result in $v \cdot d \leq u \cdot f$.



```
DFS(G)
   for each vertex u \in G. V
2
        u.color = WHITE
3
       u.\pi = NIL
  time = 0
   for each vertex u \in G.V
5
6
       if u.color == WHITE
7
            DFS-VISIT(G, u)
DFS-VISIT(G, u)
 1 \quad time = time + 1
                                   // white vertex u has just been discovered
 2 \quad u.d = time
 3 u.color = GRAY
 4 for each v \in G.Adj[u]
                                   /\!\!/ explore edge (u, v)
 5
         if v.color == WHITE
 6
             \nu.\pi = u
 7
             DFS-VISIT(G, \nu)
 8 u.color = BLACK
                                   // blacken u; it is finished
 9 time = time + 1
10 u.f = time
```

Definitions of edge types:

- 1. **Tree edges** are edges in the depth-first forest G_{π} . Edge (u, v) is a tree edge if v was first discovered by exploring edge (u, v).
- 2. **Back edges** are those edges (u, v) connecting a vertex u to an ancestor v in a depth-first tree. We consider self-loops, which may occur in directed graphs, to be back edges.
- 3. Forward edges are those nontree edges (u, v) connecting a vertex u to a descendant v in a depth-first tree.
- 4. *Cross edges* are all other edges. They can go between vertices in the same depth-first tree, as long as one vertex is not an ancestor of the other, or they can go between vertices in different depth-first trees.