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Grade received **100%** To pass 80% or higher

1. It's more useful to visualize the manipulability ellipsoid using the body Jacobian than the space Jacobian, since the body Jacobian measures linear velocities at the origin of the end-effector frame, which has a more intuitive meaning than the linear velocity at the origin of the space frame. If the robot has n joints, then the body Jacobian J_b is $6 \times n$. We can break J_b into two sub-Jacobians, the angular and linear Jacobians:

1 / 1 point

$$J_b = \begin{bmatrix} J_{b\omega} \\ J_{bv} \end{bmatrix}.$$

What is the dimension of $J_{bv}J_{bv}^T$, which is used to generate the linear component of the manipulability ellipsoid?

- ☒ 3×3
☐ 6×6
☐ $n \times n$

 Correct

The linear component of a twist is 3-dimensional.

2. Consider a robot with a full rank Jacobian as it approaches a singular configuration. As it approaches a singular configuration, what happens to the manipulability ellipsoid? Select all that apply.

1 / 1 point

- ☒ The length of one principal axis approaches zero.

 Correct

- ☐ The length of one principal axis approaches infinity.
☒ The interior "volume" of the ellipsoid approaches zero.

 Correct

- ☐ The interior "volume" of the ellipsoid approaches infinity.

3. Consider a robot with a full rank Jacobian as it approaches a singular configuration. As it approaches the singular configuration, what happens to the force ellipsoid? Select all that apply.

1 / 1 point

- ☐ The length of one principal axis approaches zero.
☒ The length of one principal axis approaches infinity.

 Correct

At a singularity, the robot can resist wrenches in some direction with zero joint forces and torques.

- ☐ The interior "volume" of the ellipsoid approaches zero.
☒ The interior "volume" of the ellipsoid approaches infinity.

 Correct

At least one principal axis approaches infinity while the others are nonzero, so the volume approaches infinity.