

## Congratulations! You passed!

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Grade received **100%** To pass 80% or higher

1. The solution to the differential equation  $\dot{p}(t) = \hat{\omega} \times p(t) = [\hat{\omega}]p(t)$  is  $p(t) = e^{[\hat{\omega}t]}p(0)$ , where  $p(0)$  is the initial vector and  $p(t)$  is the vector after it has been rotated at the angular velocity  $\hat{\omega}$  for time  $t = \theta$  (where  $\hat{\omega}\theta$  are the exponential coordinates). You can think of  $R = e^{[\hat{\omega}\theta]}$  as the rotation operation that moves  $p(0)$  to  $p(t) = p(\theta)$ .

1 / 1 point

Which of the following statements is correct? Select all that apply.

- ☒  $R_{sb'} = R_{sb}e^{[\hat{\omega}\theta]}$  represents the orientation of a new frame {b'} relative to {s} after the frame {b} has been rotated by  $\theta$  about an axis  $w$  represented in the {b} frame as  $\hat{\omega}$ .

 **Correct**

Multiplication of the rotation operation on the right corresponds to  $\omega$  being interpreted in the frame of the second subscript, {b}.

- ☐  $R_{sb'} = R_{sb}e^{[\hat{\omega}\theta]}$  represents the orientation of a new frame {b'} relative to {s} after the frame {b} has been rotated by  $\theta$  about an axis  $w$  represented in the {s} frame as  $\hat{\omega}$ .
- ☐  $R_{sb'} = e^{[\hat{\omega}\theta]}R_{sb}$  represents the orientation of a new frame {b'} relative to {s} after the frame {b} has been rotated by  $\theta$  about an axis  $w$  represented in the {b} frame as  $\hat{\omega}$ .
- ☒  $R_{sb'} = e^{[\hat{\omega}\theta]}R_{sb}$  represents the orientation of a new frame {b'} relative to {s} after the frame {b} has been rotated by  $\theta$  about an axis  $w$  represented in the {s} frame as  $\hat{\omega}$ .

 **Correct**

Multiplication of the rotation operation on the left corresponds to  $\omega$  being interpreted in the frame of the first subscript, {s}.

2. The simple closed-form solution to the infinite series for the matrix exponential when the matrix is an element of  $so(3)$  (a skew-symmetric 3x3 matrix) is called what?

1 / 1 point

- ☐ Ramirez's formula.
- ☒ Rodrigues' formula.
- ☐ Robertson's formula.

 **Correct**

3. The matrix exponential and the matrix log relate a rotation matrix (an element of  $SO(3)$ ) and the skew-symmetric representation of the exponential coordinates (elements of  $so(3)$ ), which can also be thought of as the  $so(3)$  representation of the angular velocity followed for unit time. Which of the following statements is correct? Select all that apply.

1 / 1 point

- ☒  $\exp: so(3) \rightarrow SO(3)$

 **Correct**

The matrix exponential "integrates" the skew-symmetric  $so(3)$  representation of an angular velocity for unit time to yield the rotation matrix describing the orientation achieved after rotating from an initial orientation described by the identity matrix.

- ☐  $\exp: SO(3) \rightarrow so(3)$
- ☐  $\log: so(3) \rightarrow SO(3)$
- ☒  $\log: SO(3) \rightarrow so(3)$

 **Correct**

The matrix logarithm of a rotation matrix  $R$  gives the angular velocity that must be followed for unit time, starting from a frame represented as the identity matrix, to rotate to  $R$ . It "differentiates" the net rotational displacement to find the angular velocity that must be followed for unit time.