## ADVANCE ALGORITHM

Tree data structure



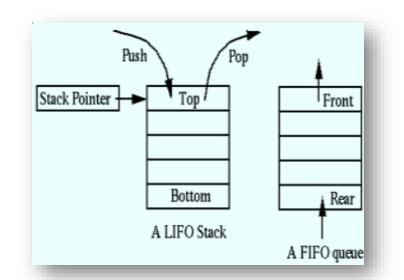
#### Outline

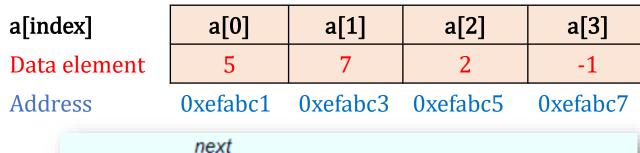
- Data structure
  - Linear Vs. Non linear
- What is Tree? Binary tree? Binary search tree (BST)?
- What are Tree operations?
- Traversal of Tree
- How to implement Tree in C++
- Examples

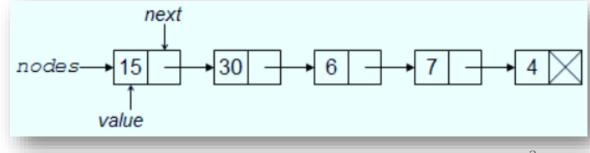
#### Data structure

#### ☐ Linear Data Structure

- Data structure helps to store and organize data in computer
- Linear data structure stores data in such a way that the data can be accessed sequentially (continuous)
  - Array, linked list, stack queue







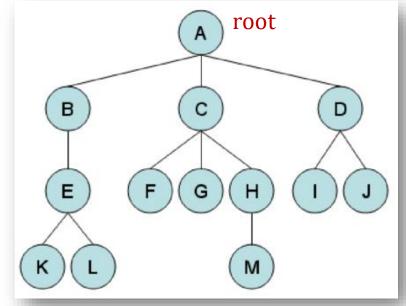
## Linear Vs. Non-linear data structure

## ☐ Comparison

Factor	Linear data structure	Non-linear data structure
How data is stored	Data elements construct a sequence of a linear list.	Does not arrange data consecutively but arrange in sorted order.
Traversal of data	<ul> <li>Data elements are visited sequentially</li> <li>Traversal of element is easy</li> </ul>	<ul> <li>Traversal of data elements and insertion/deletion are not done sequentially</li> <li>Traversal of element is difficult</li> </ul>
Implementation	Simple	Complex
Levels	Single level of elements	Multiple levels of elements (hierarchical)
Memory utilization	Ineffective	Effective
Example	Array, linked list, stack, queue	Tree, graph

#### Tree

- A tree is a hierarchical (non-linear) data structure defined on a set of elements called nodes
- A tree can be empty or composed of nodes
  - The top-level node is called *root*,
     while other nodes are sub-tree



An example of a tree

#### Tree

#### ☐ Relation of Tree

■ **Root** : top element

• **Children** : have same parents,

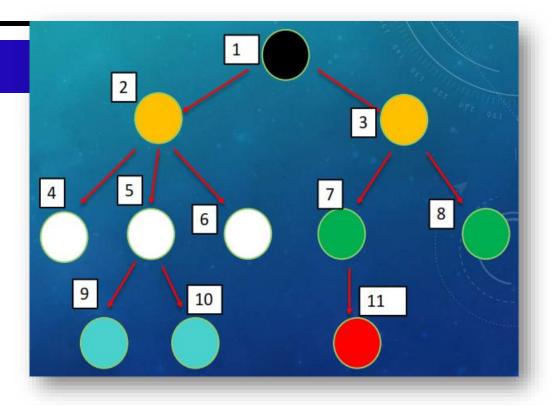
grant parents, great grant parents, ...

**Parents**: have children

• **Siblings** : have same parent

• **Leaf** : is element that has no children

• Remark: In particular, leaf element has pointer points to NULL



How many leaves are there?

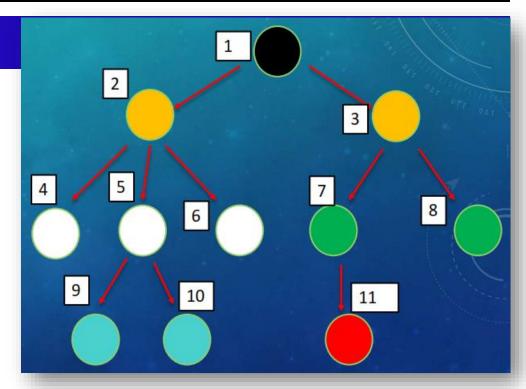
$$=>6$$

What are they?

#### Relation of Tree

## ☐ Edge Vs. Depth Vs. Height

- Edge (path)
  - An edge is a line connected two nodes together
  - If a tree have N nodes, then it has (N-1) edges
- Depth of node x
  - Depth of node x is number of edges from x to root
  - <u>Note</u>: Depth of root is 0
- Height of node x
  - Height of node x is number of edges on longest path from x to a leaf
- Remark:
  - Height of a tree = depth of a tree = longest path of the tree
  - Size of a tree is the number of elements (nodes)
  - Branch is any path from the root to a leaf



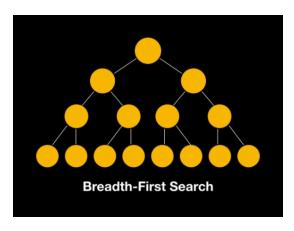
How many edges? => 10 edges
What is the depth of node 7? => 2
What is the height of node 1? => 3

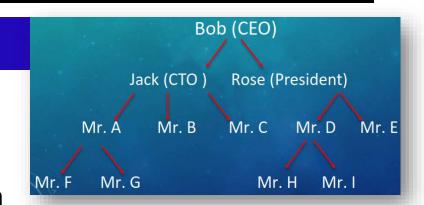
## Tree applications

### ☐ Some examples

1. Store hierarchical data

- (file system)
- 2. Organize data for quick search, insertion, deletion
  - Binary search tree (BST)
- 3. Dictionary
- 4. Network routing algorithm





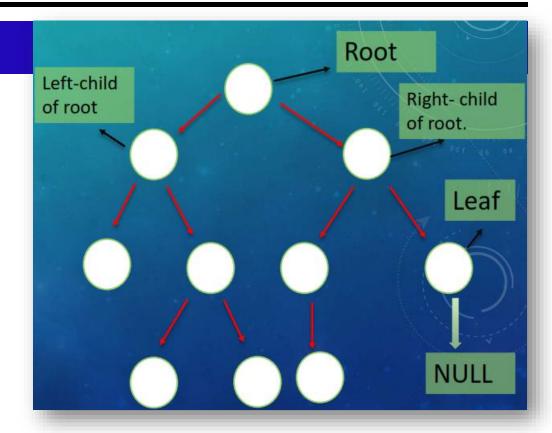
## **Binary Tree**

#### Definition

- Each node can have at most 2 children
- A node has left and/or right child
- A leaf node has no left or right child.
  - It has only NULL

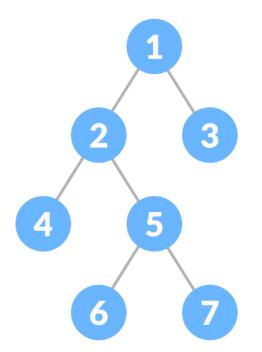
#### **Types of Binary Tree**

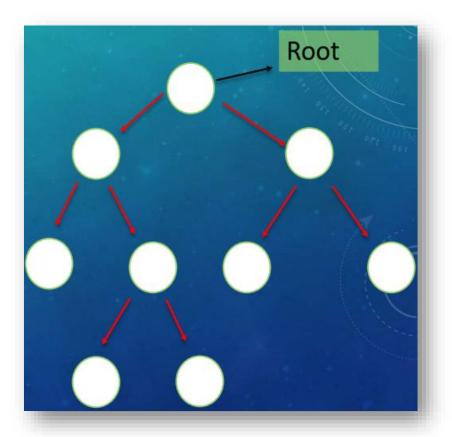
- 1. Strict/proper/full binary tree
- 2. Complete binary tree
- 3. Perfect binary tree



## Strict/proper/full Binary Tree

- Each node can have either 2 or 0 child
- It can not have only one left or right child

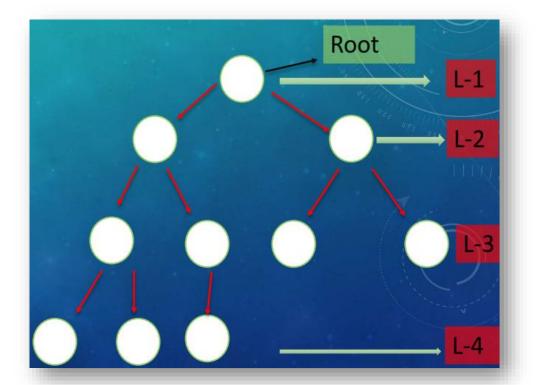


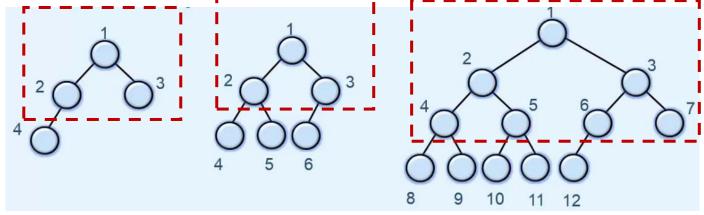


## **Complete Binary Tree**

#### Definition

 A complete binary tree is a binary tree in which every level, except possibly the last level, is completely filled and all nodes are as far left as possible.

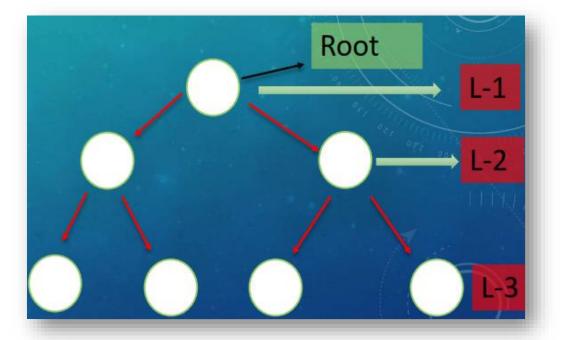




## **Perfect Binary Tree**

## Definition

• All levels are completed filled and balanced

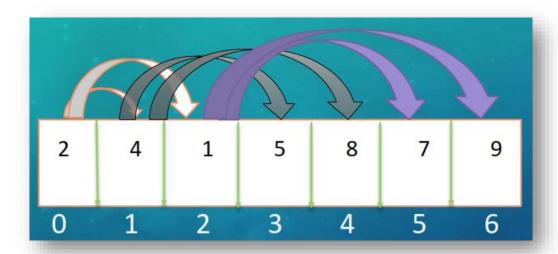


## Tree Implementation

## Tree implementation

- ☐ There are 2 types of implementation
- Dynamically created nodes
- 2. Array

- int data; struct Node \*left;
- struct Node{ struct node \*right;
- It work only for Perfect Binary Tree
  - For node at index i
    - Left child's index = 2i + 1
    - Right child's index = 2i + 2

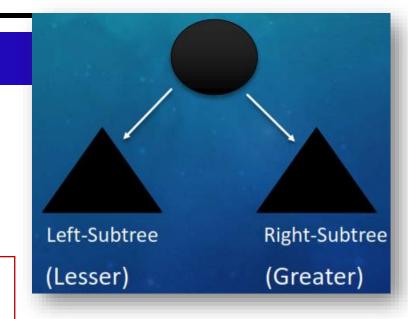


4

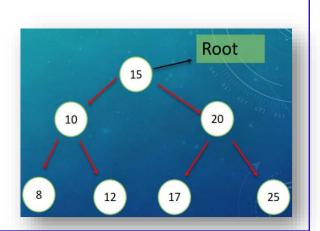
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## **Binary Search Tree (BST)**

- A BST is a binary tree that is constructed in such a way that it is easy to search for the values it contains
- Rules in BST
  - ❖ All values less than (or equal) to root value are stored in the left subtree
  - ❖ All values greater than the root are stored in the right subtree



- **Example**: Suppose we have number 15 as root. We want to add **10, 20, 8, 12, 17, 25** to the tree.
  - 10 < 15 => 10 is inserted to left of the root
  - 20>15 => 20 is inserted to right of the root
  - 8<15 => 8 goes left
    - 8<10 => 8 goes left
  - ... etc.



#### Insert a node in BST

#### Definition

- To insert a new item in a tree, we should check that there is no duplication
  - If a new value is less than the current node's value
    - Go to the left subtree
  - Else,
    - Go to the right subtree

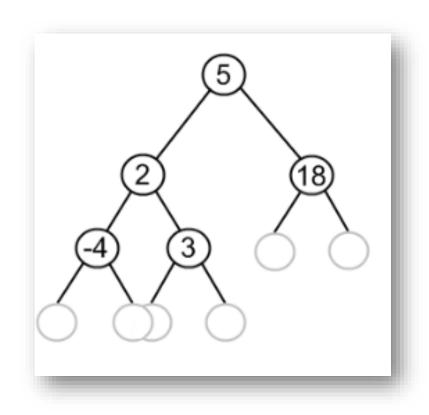
#### Remark:

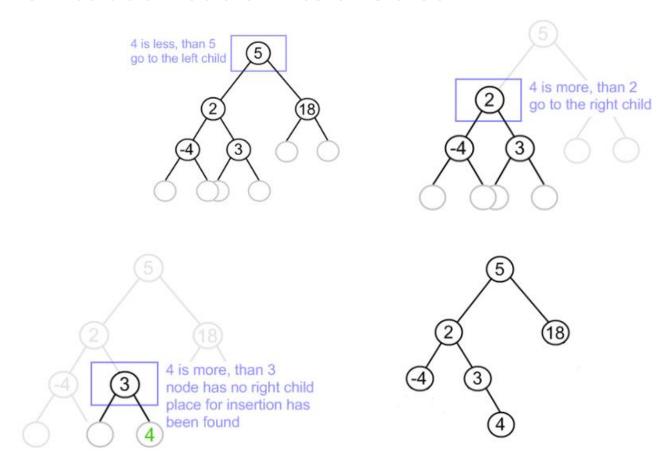
- With this simple rule, the algorithm reaches a node (leaf) which has no left/right subtree
- By the moment a place for insertion is found, we can say that a new value has no duplicate in the tree

#### Insert a node in BST

## ☐ Example

• Given a tree below on the left. How to add node of 4 to this tree?



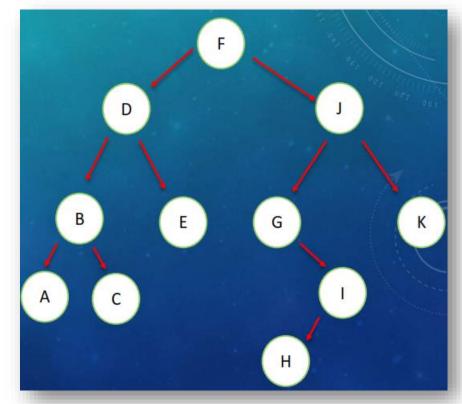


## Insert data to a tree by knowing the tree's root

```
Node *insert(Node *root, int data){
           if(root==NULL){
                root=new Node;
3
                                              Insert data
4
                root->left=NULL;
                root->right=NULL;
5
                root->data=data;
6
           }else if(data < root->data){
                                                                    Go left
                root->left = insert(root->left, data);
8
           }else if(data > root->data){
9
                                                                    Go right
               root->right = insert(root->right, data);
10
11
12
           return root;
13
```

## **Traversal of Binary Tree**

- Traversal of a tree is a way that is used to visit each node in the tree
- 2 main types of tree traversal
  - 1. Breadth-first (level-order) traversal
    - FDJBEGKACIH
  - 2. Depth-first traversal
    - Pre-order
    - In-order
    - Post-order



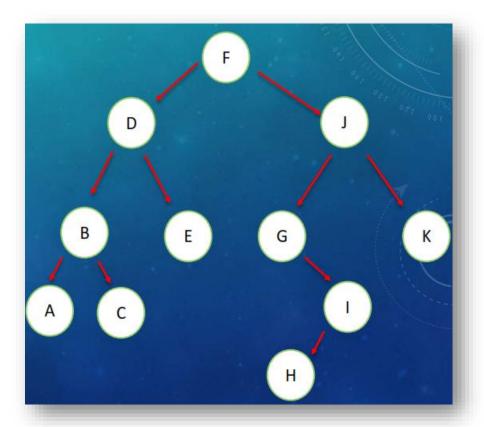
## Depth-first Traversal

- 1. Pre-order
- 2. In-order
- 3. Post-order

#### **Pre-order Traversal**

- It follows data-left-right order (DLR)
- <root's data><left><right>
  - FDBACEJGIHK

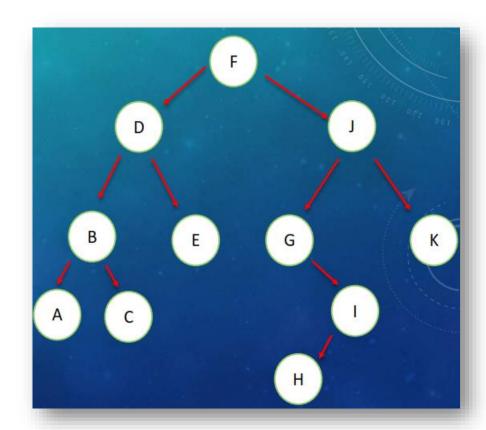
```
void preorder(Node *root){
    if(root!=NULL){
        cout<<root->data;
        preorder(root->left);
        preorder(root->right);
    }
}
```



## **In-order Traversal**

- It follows left-data-right order (LDR)
- <left>< root's data ><right>
  - ABCDEFGHIJK

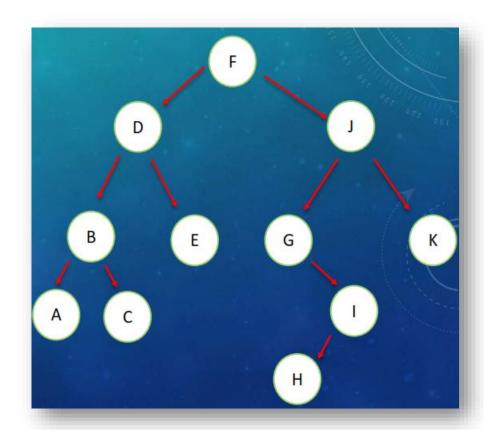
```
void inorder(Node *root){
    if(root!=NULL){
        inorder(root->left);
        cout<<root->data;
        inorder(root->right);
    }
}
```



#### **Post-order Traversal**

- It follows left-right-data order (LRD)
- <left><right><root's data>
  - ACBEDHIGKJF

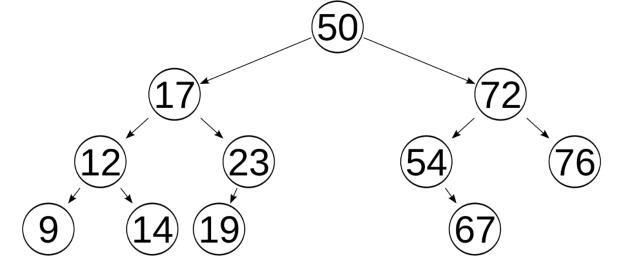
```
void postorder(Node *root){
    if(root!=NULL){
        postorder(root->left);
        postorder(root->right);
        cout<<root->data;
    }
}
```



## Example practice: Tree traversal

## What are the outputs?

- a. Pre-order traversal
- b. In-order traversal
- c. Post-order traversal



Pre-order traversal: 50 17 12 9 14 23 19 72 54 67 76 In-order traversal: 9 12 14 17 19 23 50 54 67 72 76 Post-order traversal: 9 14 12 19 23 17 67 54 76 72 50

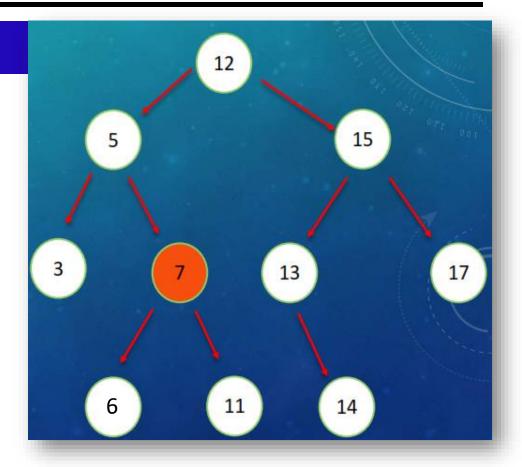
#### Outputs:

#### Search for an Element in BST

#### Definition

Loop to each node and compare the data

```
bool search(Node *root, int data){
     if(root == NULL){
          return false;
     }else if(data == root->data){
          return true;
     }else if(data > root->data){
          return search(root->right, data);
     }else if(data < root->data){
          return search(root->left, data);
```



# Q and A

## **Assignment 7**

#### Exercise

Given a binary search tree (BST) below.

## What are the output of the following tree traversal?

- a. Pre-order traversal
- b. In-order traversal
- c. Post-order traversal

