



Data Structure & Algorithm II

Lecture 5 **Binary Tree**

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Content

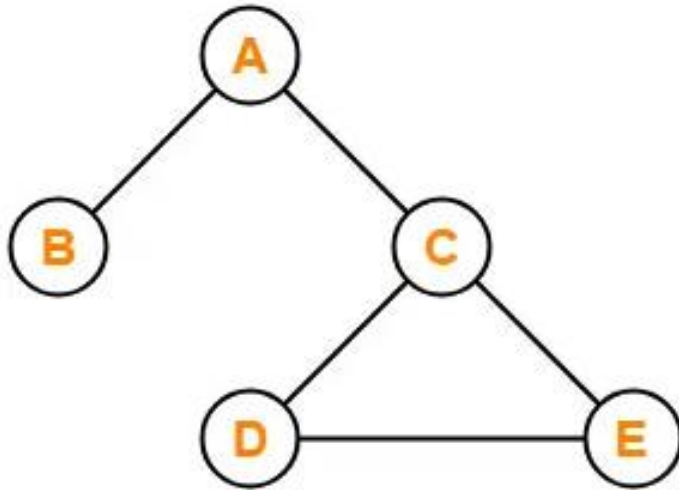
- Tree
- Terminology
- Traversal

Tree Definition

- Tree is a non-linear data structure which organizes data in a hierarchical structure and this is a recursive definition.
- If in a graph, there is one and only one path between every pair of vertices, then the graph is called a tree.

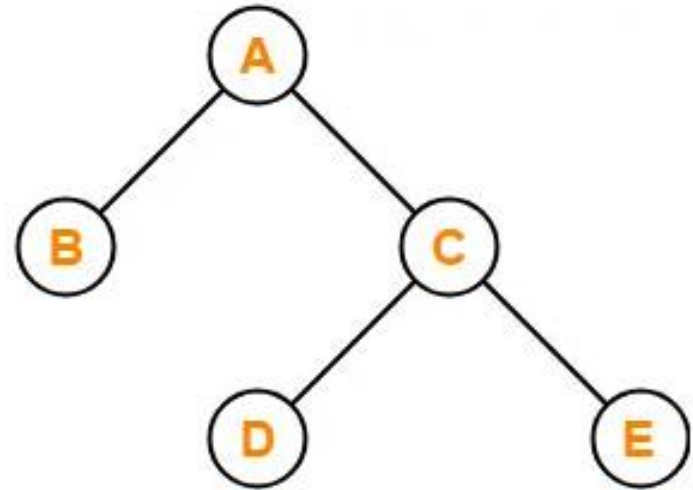
Tree Definition

Example



X

This graph is not a Tree



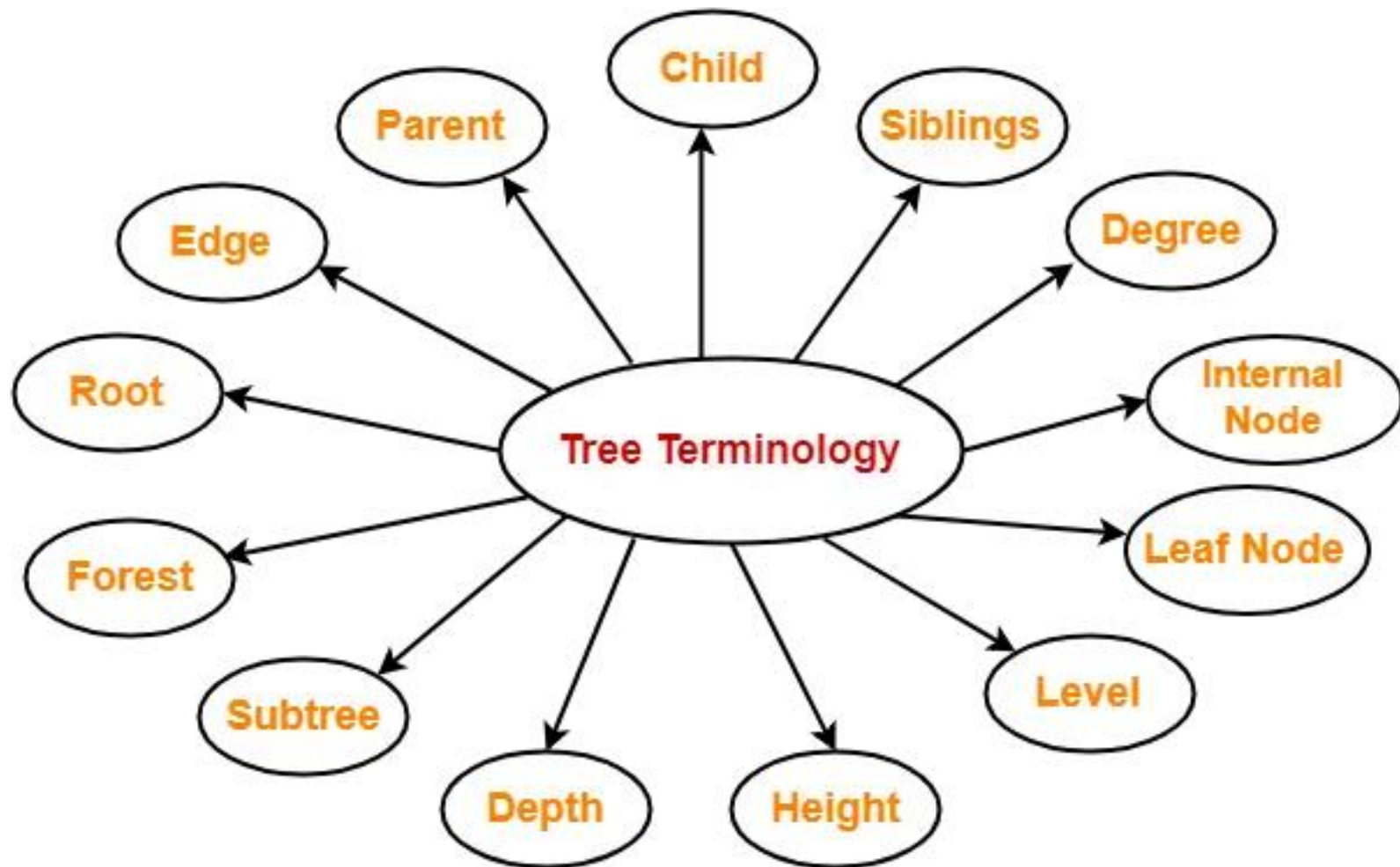
✓

This graph is a Tree

Tree Definition - Properties-

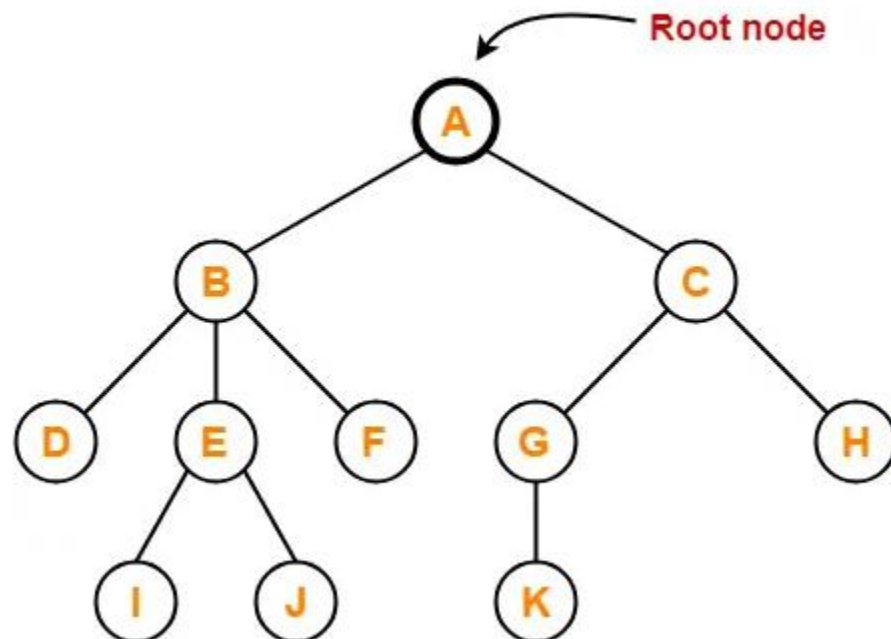
- There is one and only one path between every pair of vertices in a tree.
- A tree with n vertices has exactly $(n-1)$ edges.

Tree Terminology



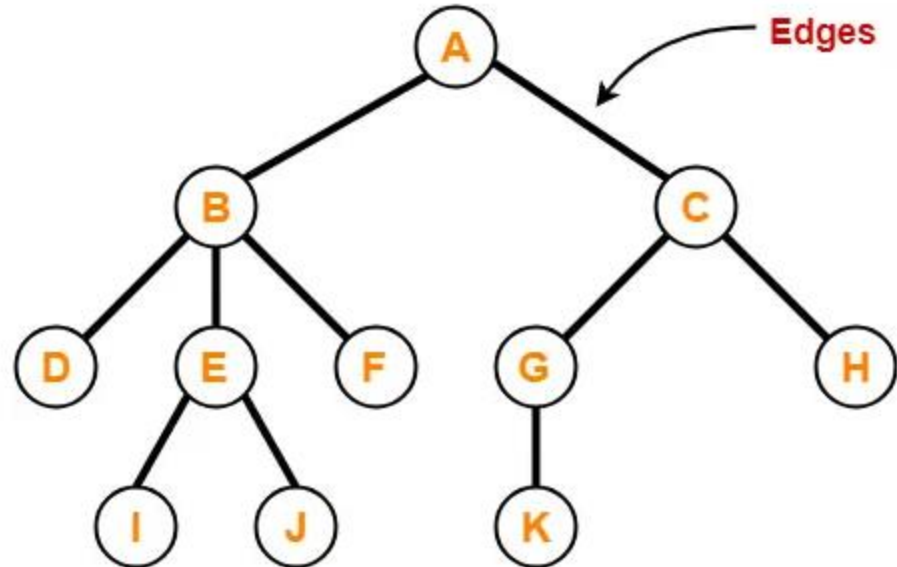
Tree Terminology-Root

- The **first node** from where the tree originates is called as a root node.
- In any tree, there must be **only one root** node.
- We can **never have multiple root** nodes in a tree data structure.



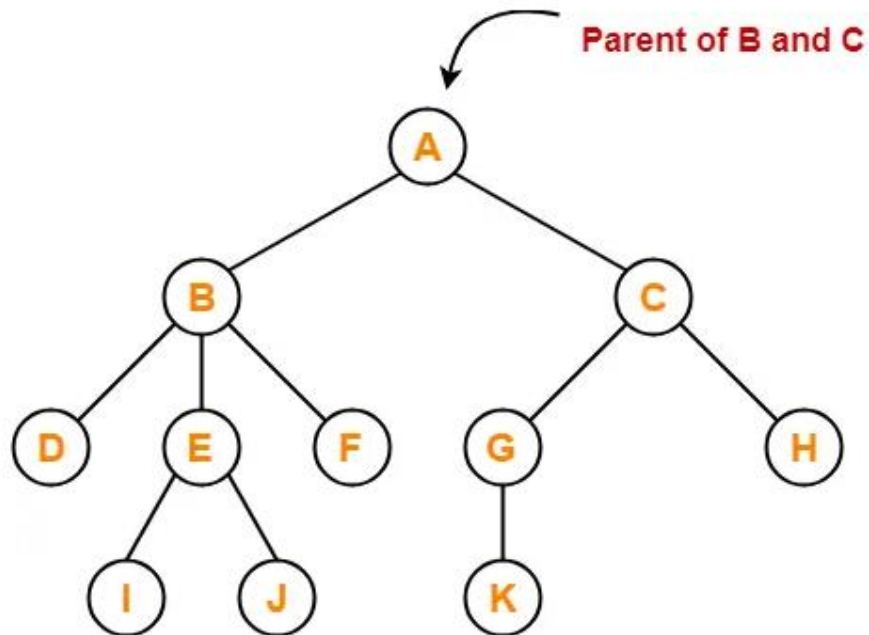
Tree Terminology-Edge

- The connecting link between any two nodes
- In a tree with **n** number of nodes, there are exactly **(n-1)** number of edges.



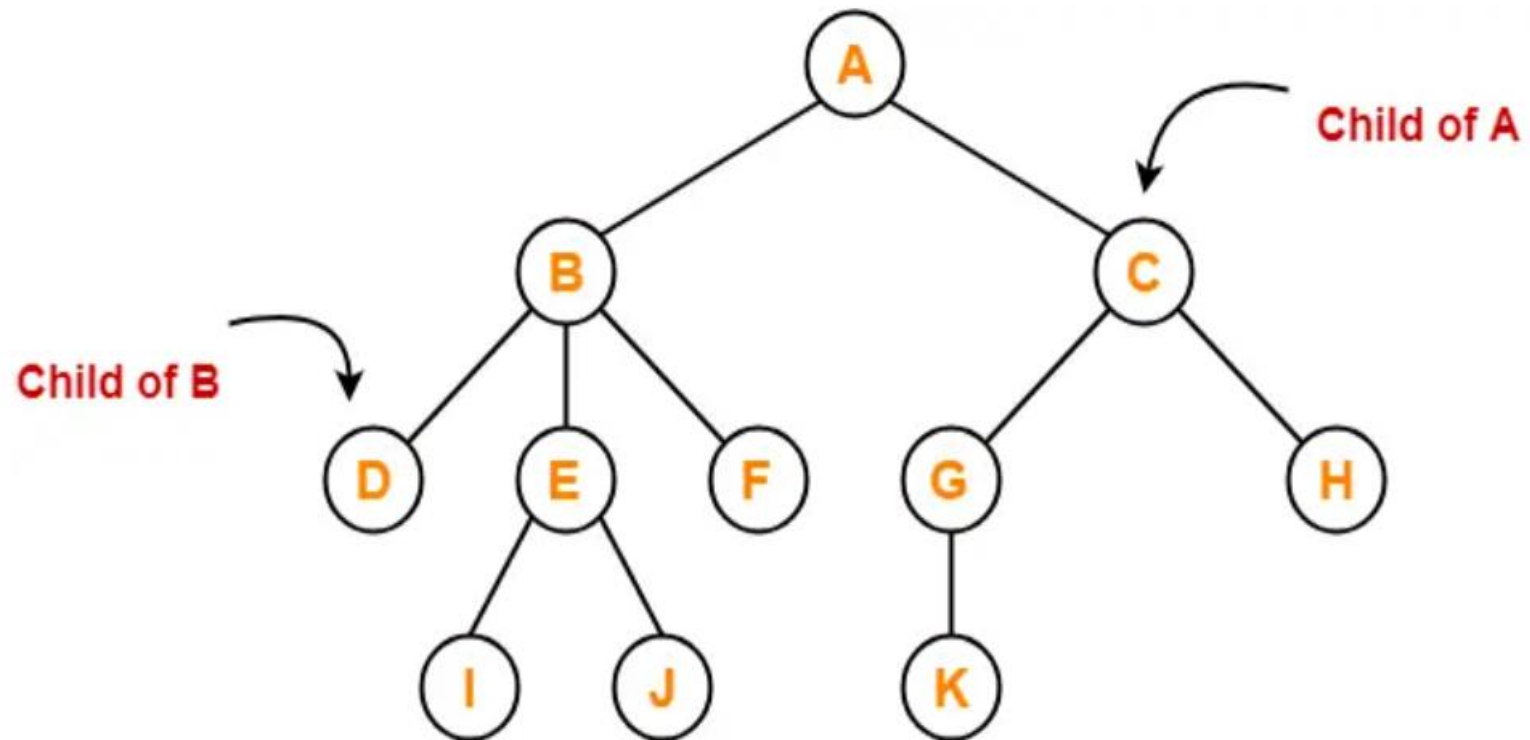
Tree Terminology-Parent

- The node which has a branch from it to any other node
- the node which has one or more children
- In a tree, a parent node can have any number of child nodes.



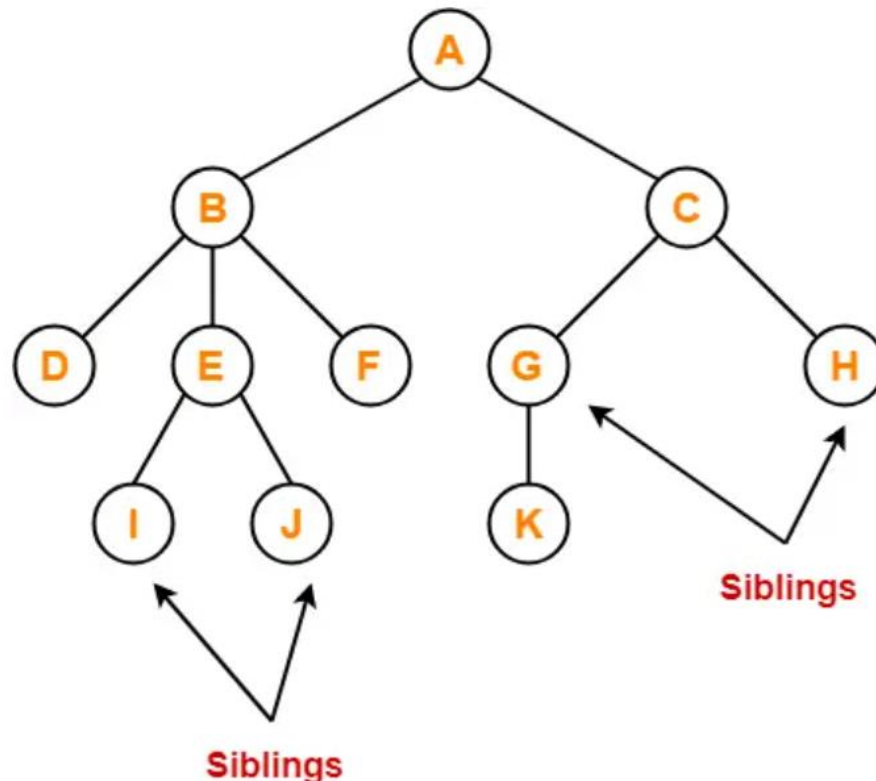
Tree Terminology-Child

- The node which is a descendant of some node
- All the nodes except root node are child nodes.



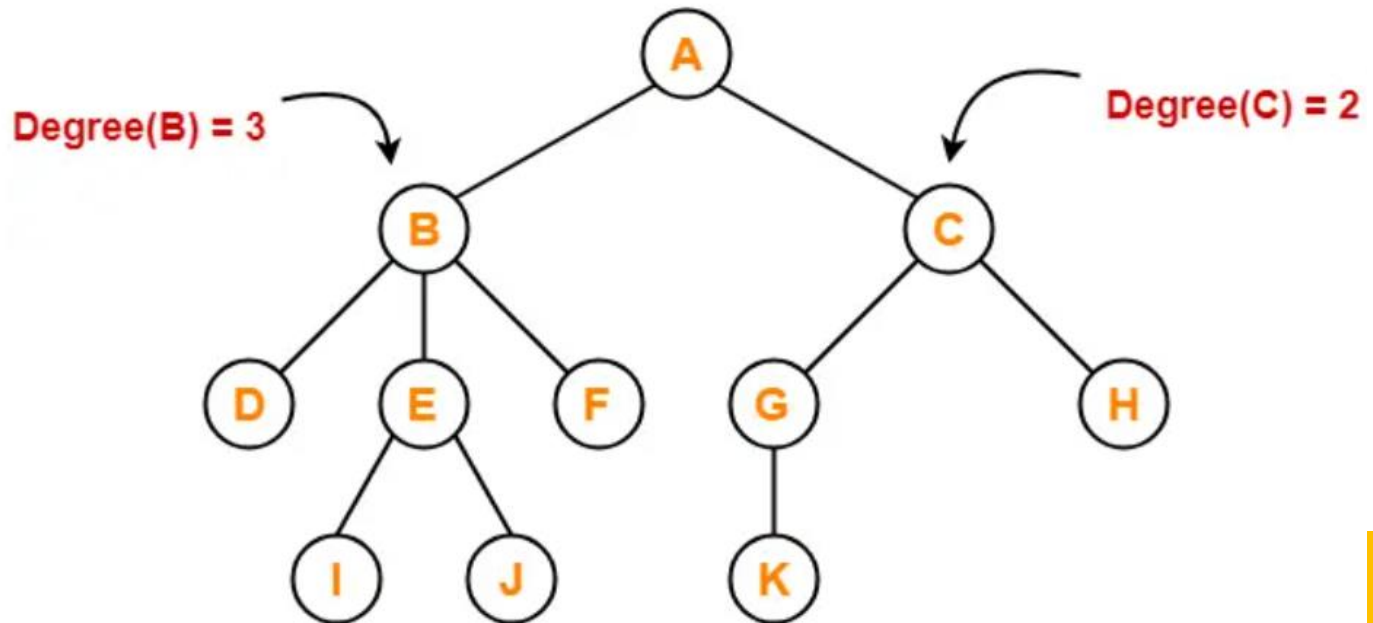
Tree Terminology - Siblings

- Nodes which belong to the same parent
- nodes with the same parent are sibling nodes.



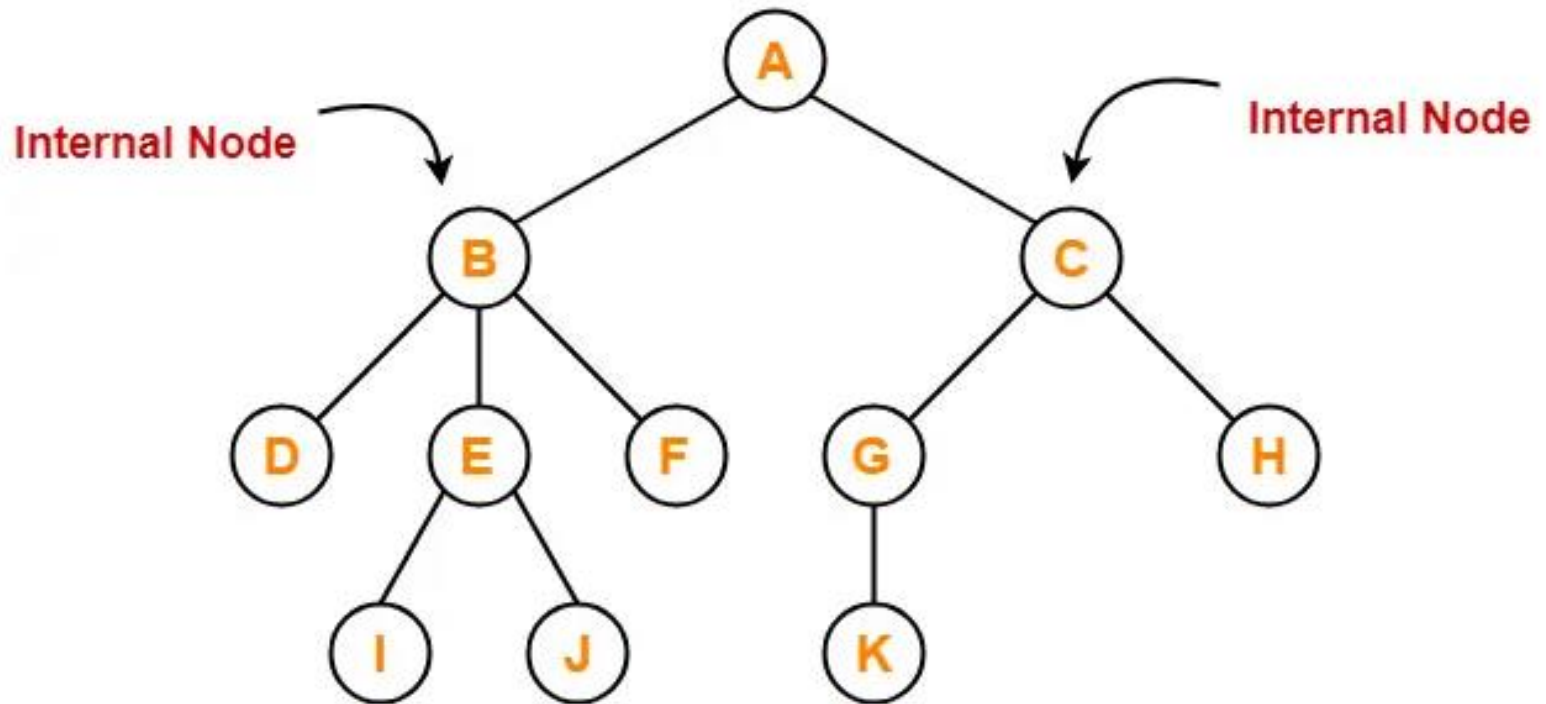
Tree Terminology- Degree

- Degree of a node is the total number of children of that node.
- Degree of a tree is the highest degree of a node among all the nodes in the tree.



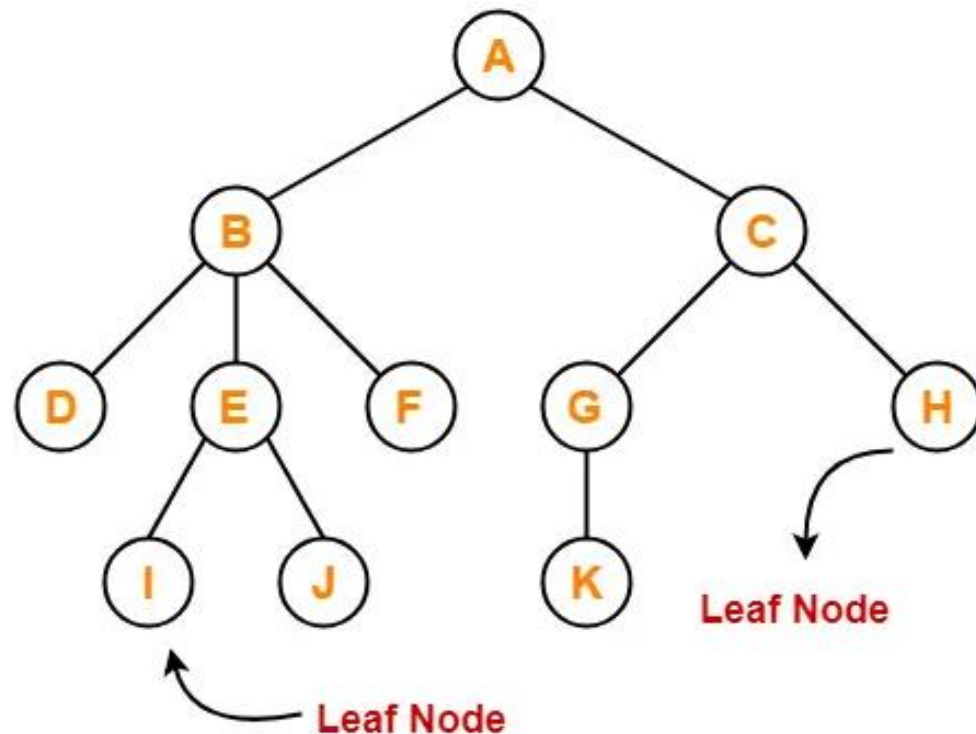
Tree Terminology - Internal Node

- The node which has at least one child



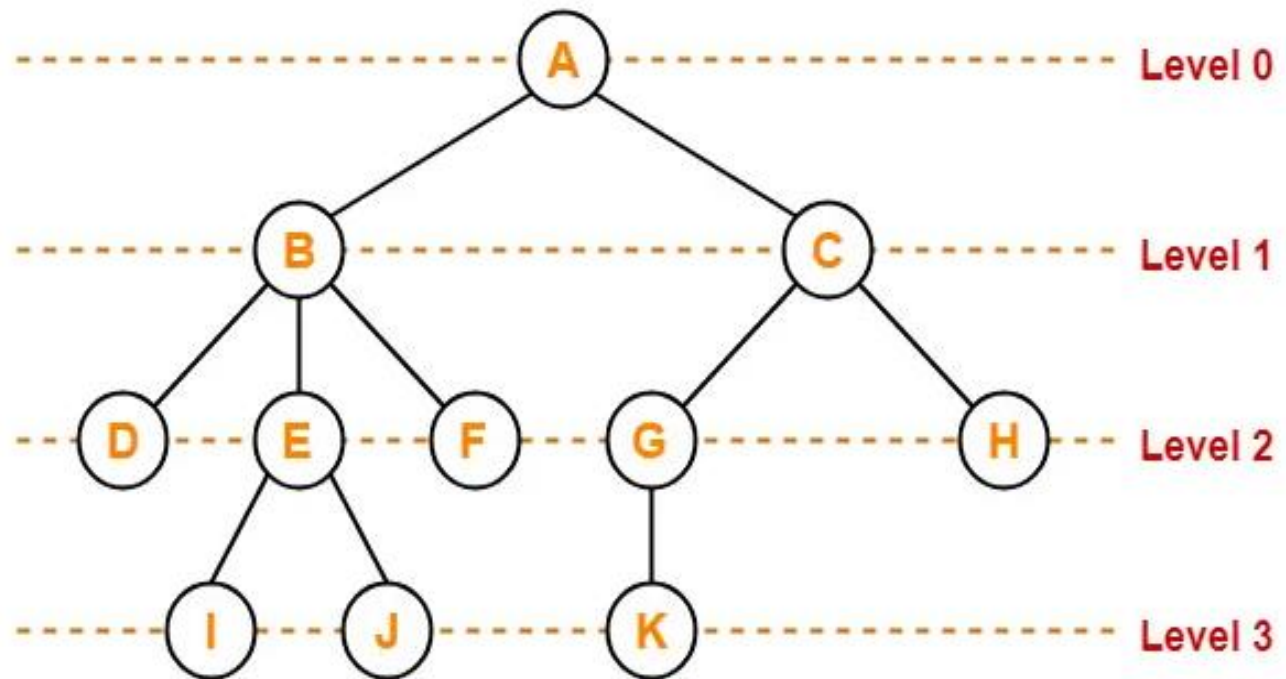
Tree Terminology - Leaf Node

- The node which does not have any child
- Leaf nodes are also called as external nodes or terminal nodes.



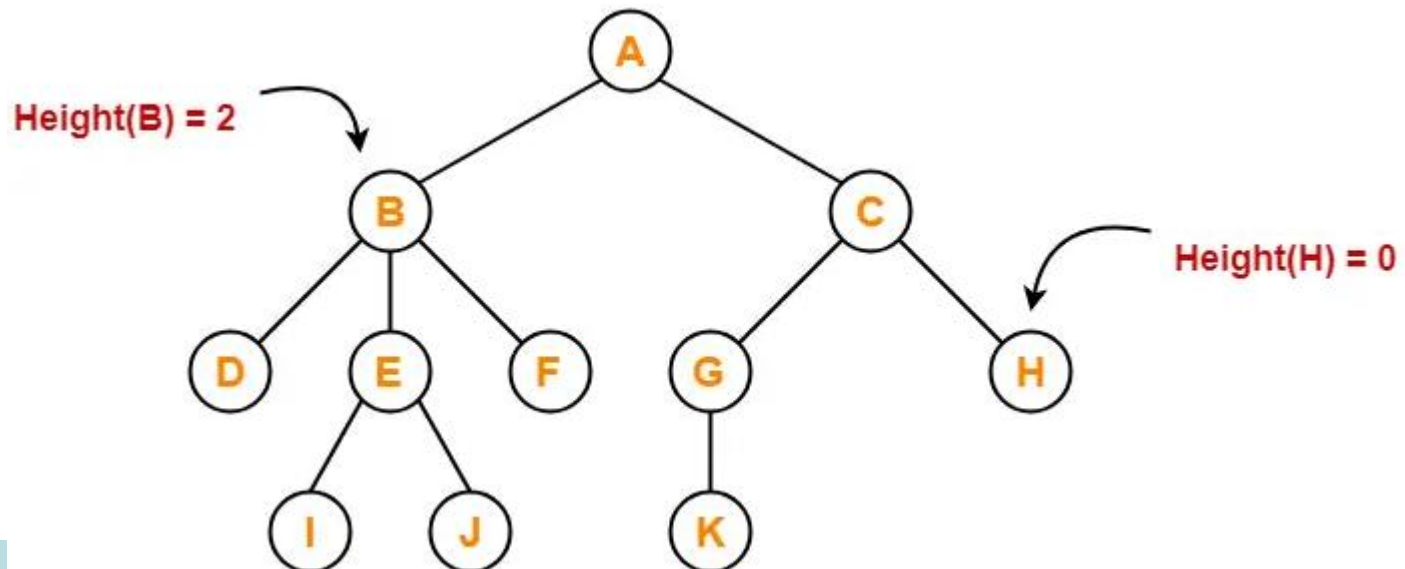
Tree Terminology - Level

- In a tree, each step from top to bottom
- The level count starts with 0 and increments by 1 at each level or step.



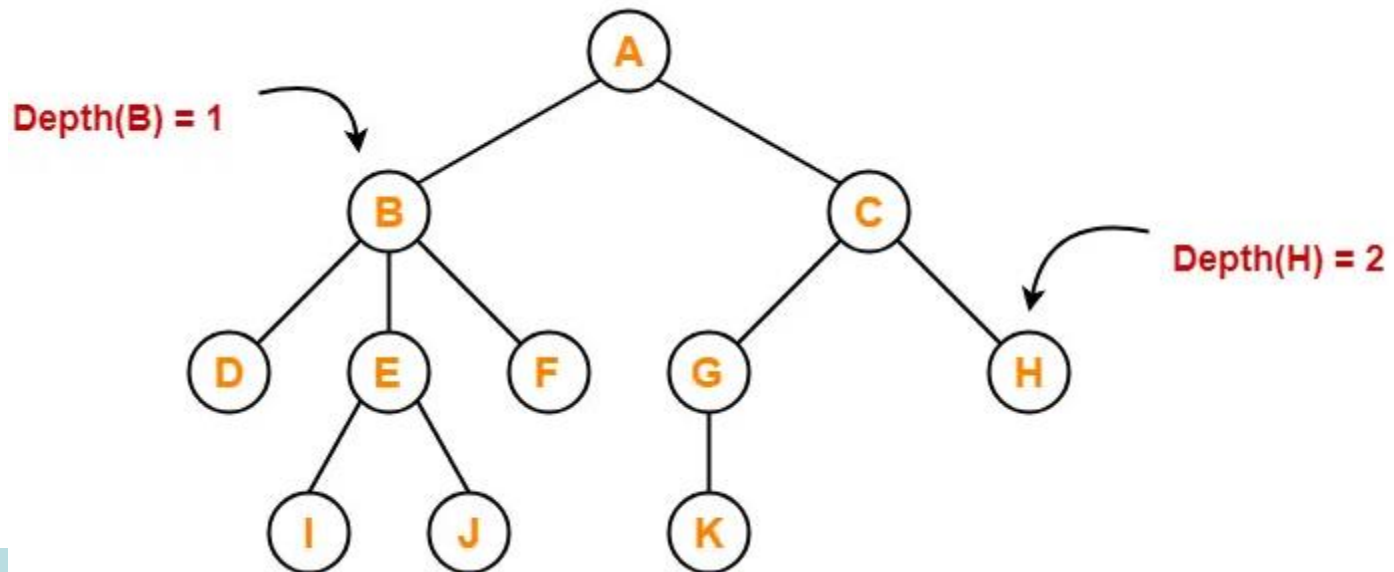
Tree Terminology - Height

- Total number of edges that lies on the longest path from any leaf node to a particular node is called as height of that node.
- Height of a tree is the height of root node.
- Height of all leaf nodes = 0



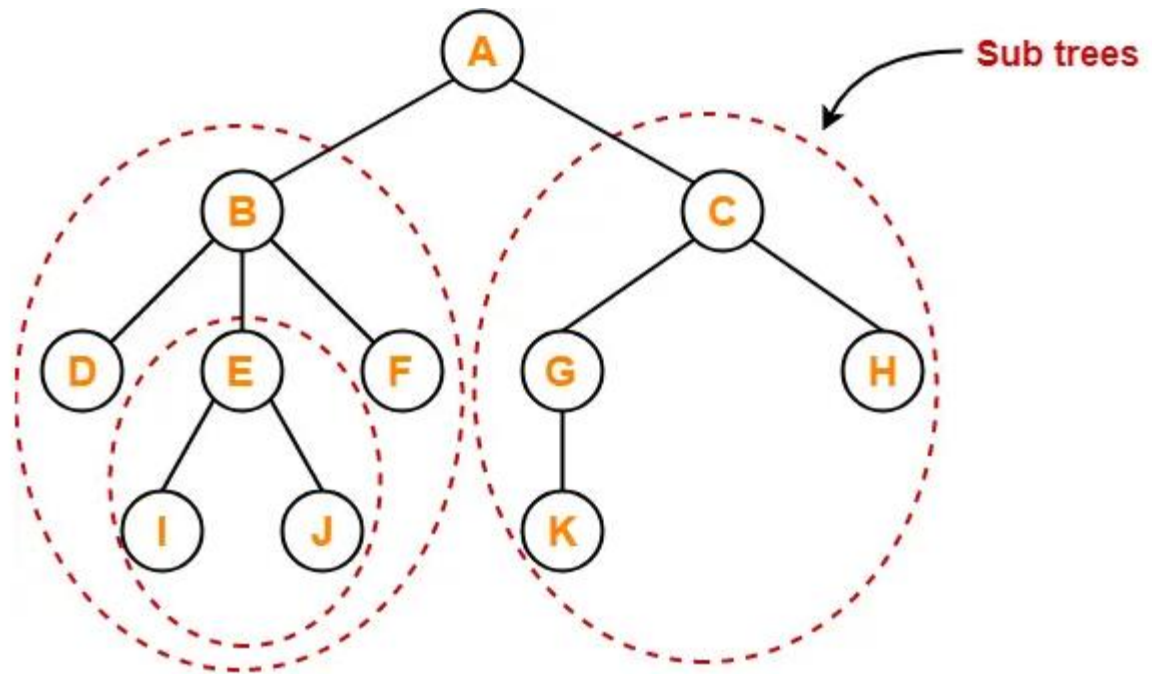
Tree Terminology - Depth

- Total number of edges from root node to a particular node is called as depth of that node.
- Depth of a tree is the total number of edges from root node to a leaf node in the longest path.
- Depth of the root node = 0



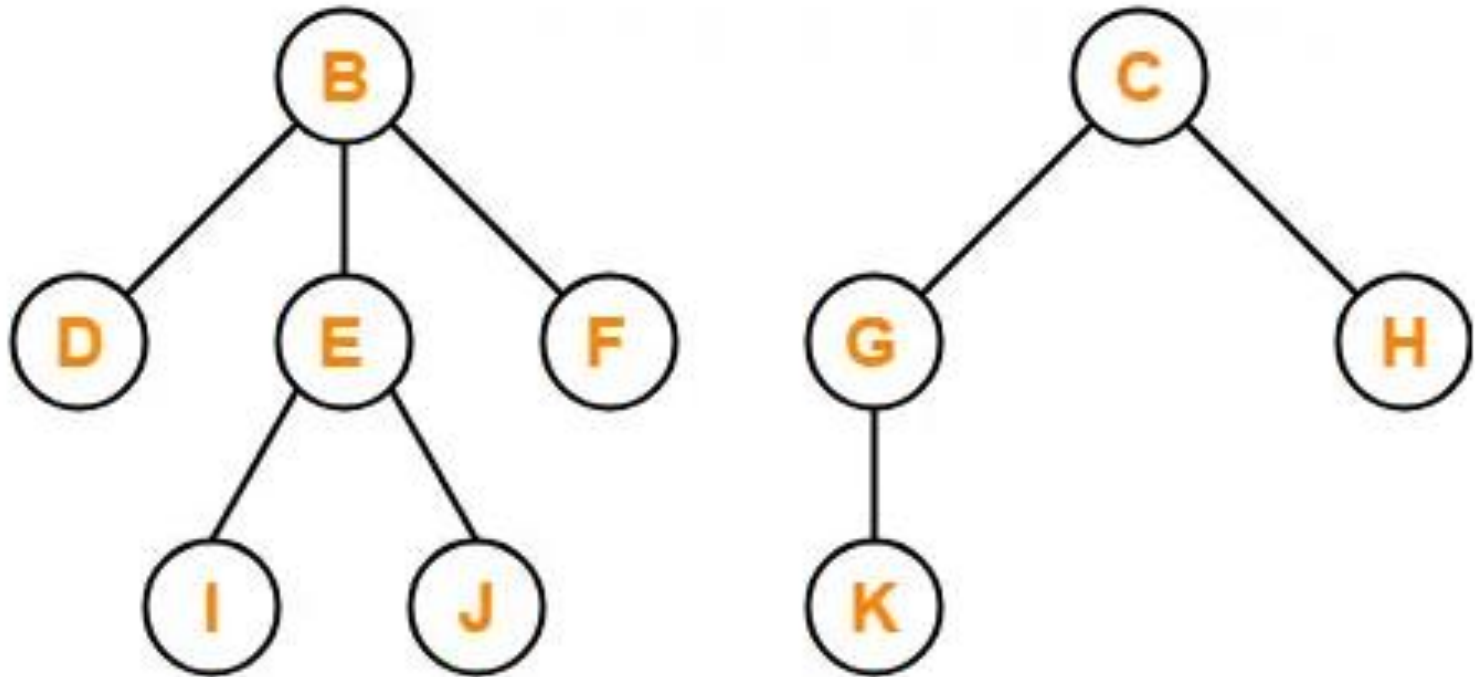
Tree Terminology - Subtree

- In a tree, each child from a node forms a subtree recursively.
- Every child node forms a subtree on its parent node.



Tree Terminology - Forest

- A forest is a set of disjoint trees.

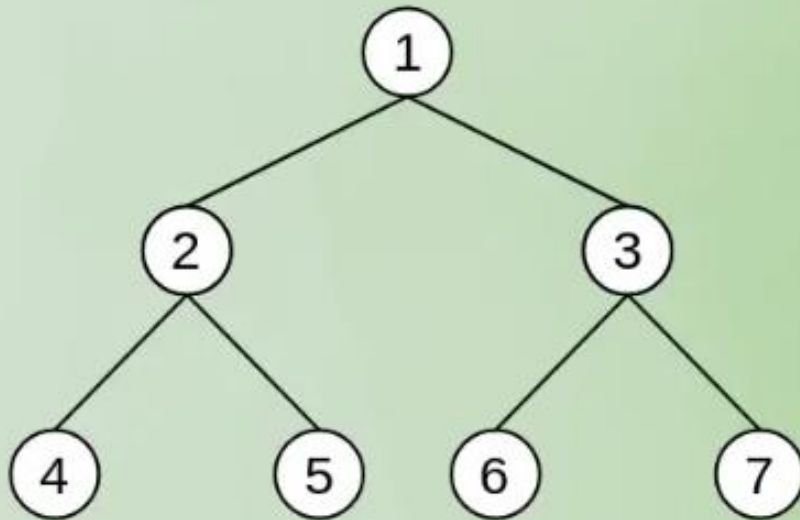


Tree Traversal

- Depth First Search (DFS)
 - Inorder Traversal
 - Preorder Traversal
 - Postorder Traversal
- Level Order Traversal or Breadth First Search or BFS
- Boundary Traversal
- Diagonal Traversal

Tree Traversal -

Tree Traversal Techniques



Inorder Traversal

4	2	5	1	6	3	7
---	---	---	---	---	---	---

Preorder Traversal

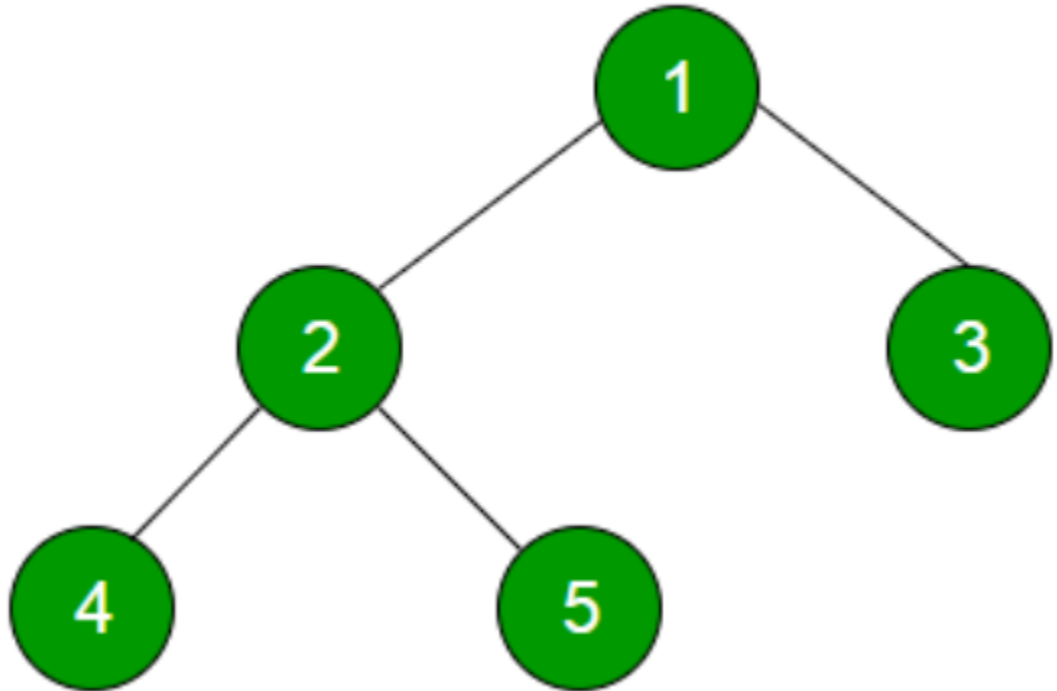
1	2	4	5	3	6	7
---	---	---	---	---	---	---

Postorder Traversal

7	6	3	5	4	2	1
---	---	---	---	---	---	---

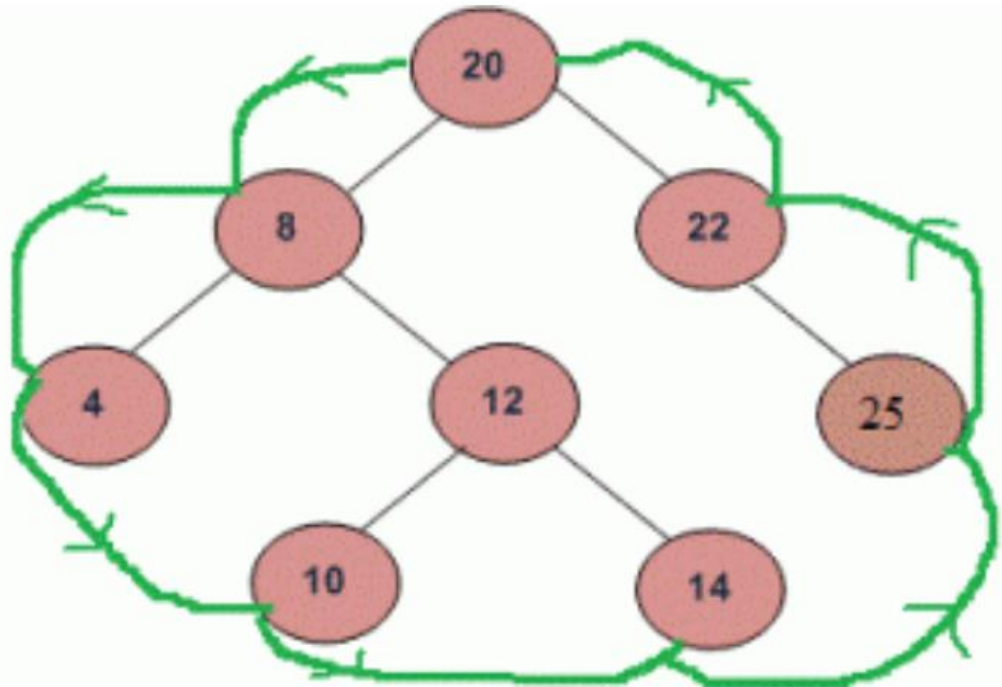
Tree Traversal - Level Order Traversal

- 1
- 2 3
- 4 5



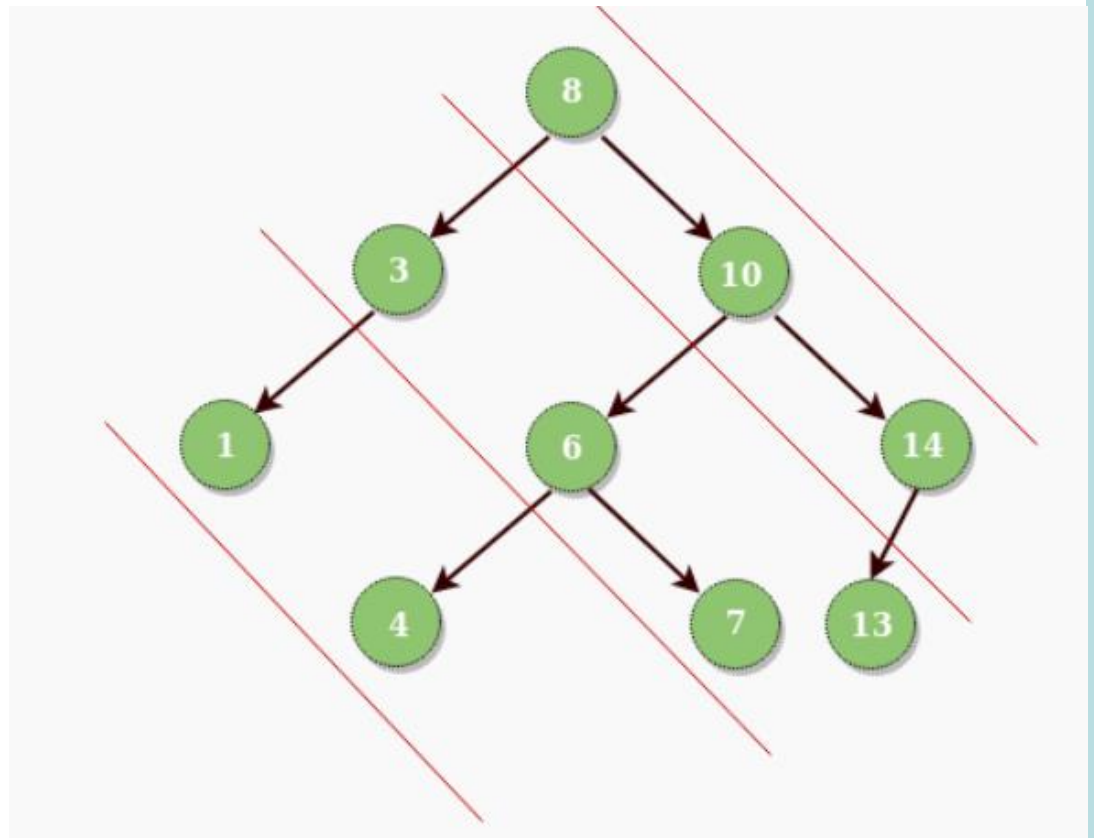
Tree Traversal - Boundary Traversal

- left boundary (nodes on left excluding leaf nodes)
- leaves (consist of only the leaf nodes)
- right boundary (nodes on right excluding leaf nodes)



Tree Traversal - Diagonal Traversal

- all the nodes in a single diagonal will be printed one by one.
 - 8 10 14
 - 3 6 7 13
 - 1 4



W5 – Lab

Struct node of Tree

```
1  // Binary Tree in C++
2  ✓ #include <stdlib.h>
3  #include <iostream>
4  using namespace std;
5  ✓ struct node
6  {
7      int data;
8      struct node *left;
9      struct node *right;
10 };
```

Struct node of Tree

```
11 // New node creation
12 ✓ struct node *newNode(int data)
13 {
14     struct node *node = (struct node *)malloc(sizeof(struct node));
15     node->data = data;
16     node->left = NULL;
17     node->right = NULL;
18     return (node);
19 }
```

Struct node of Tree

```
20  // Traverse Inorder
21  void traverseInOrder(struct node *temp)
22  {
23      if (temp != NULL)
24      {
25          traverseInOrder(temp->left);
26          cout << " " << temp->data;
27          traverseInOrder(temp->right);
28      }
29  }
```

Struct node of Tree

```
30 // Traverse Preorder
31 void traversePreOrder(struct node *temp)
32 {
33     if (temp != NULL)
34     {
35         cout << " " << temp->data;
36         traversePreOrder(temp->left);
37         traversePreOrder(temp->right);
38     }
39 }
```

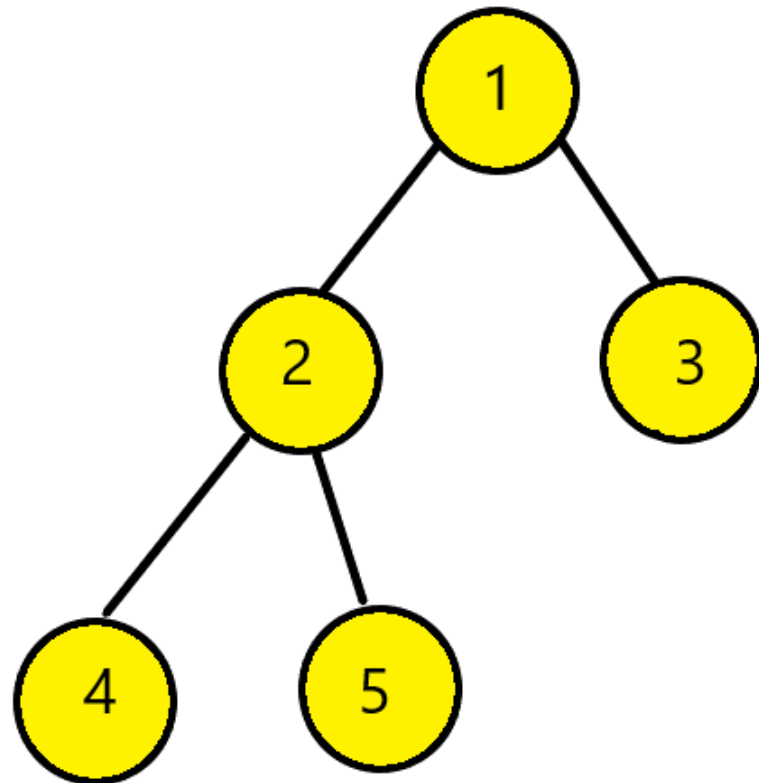
Struct node of Tree

```
40  // Traverse Postorder
41  void traversePostOrder(struct node *temp)
42  {
43      if (temp != NULL)
44      {
45          traversePostOrder(temp->left);
46          traversePostOrder(temp->right);
47          cout << " " << temp->data;
48      }
49  }
```

Ex. 1 – Tree 1

Execute in Main() trees in the figure below and access the tree with three traversal algorithms

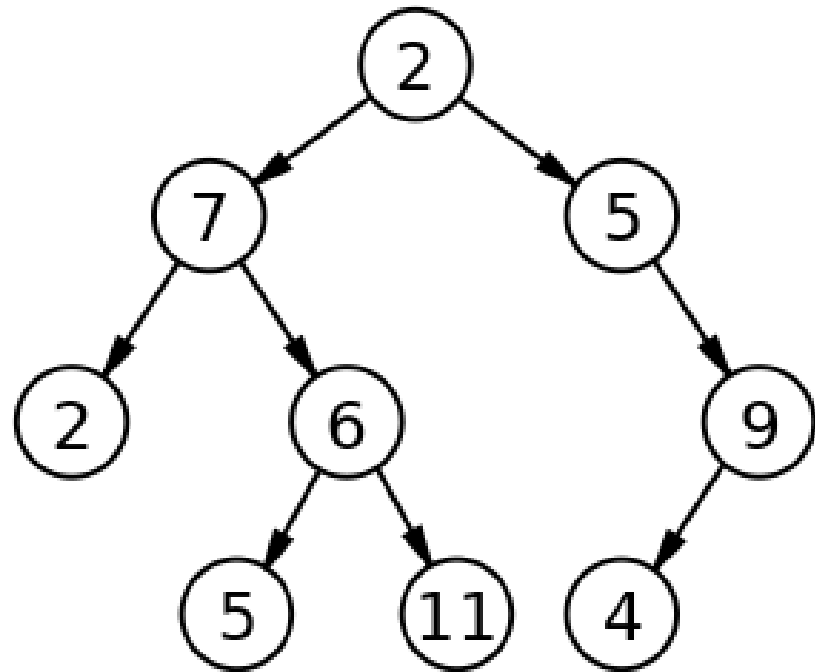
- Inorder Traversal
- Preorder Traversal
- Postorder Traversal



Ex. 2 – Tree 2

Execute in Main() trees in the figure below and access the tree with three traversal algorithms

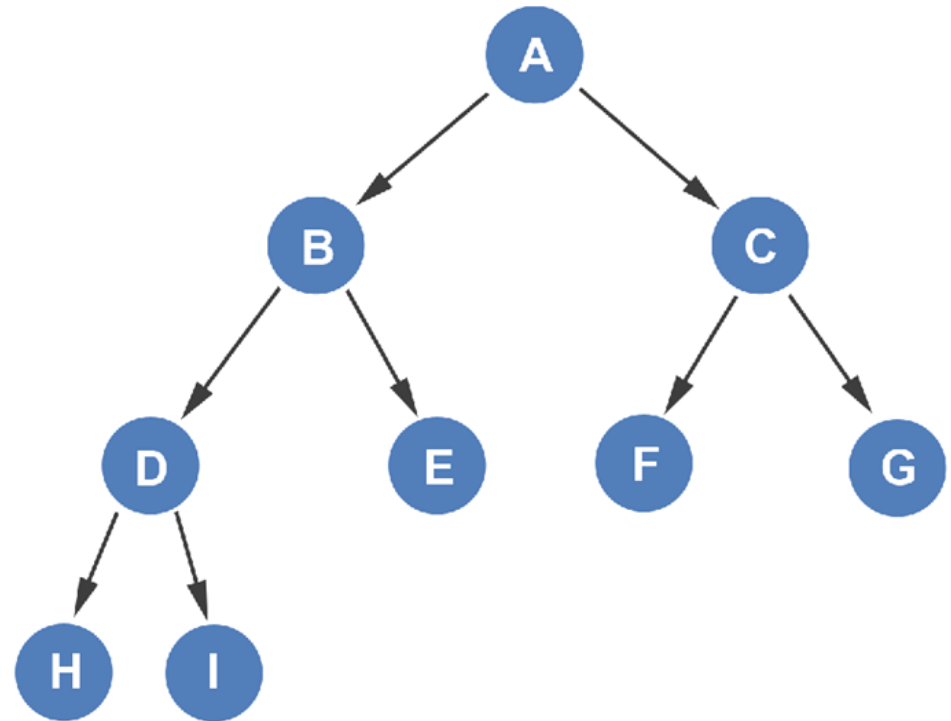
- Inorder Traversal
- Preorder Traversal
- Postorder Traversal



Ex. 3 – Tree 3

Execute in Main() trees in the figure below and access the tree with three traversal algorithms

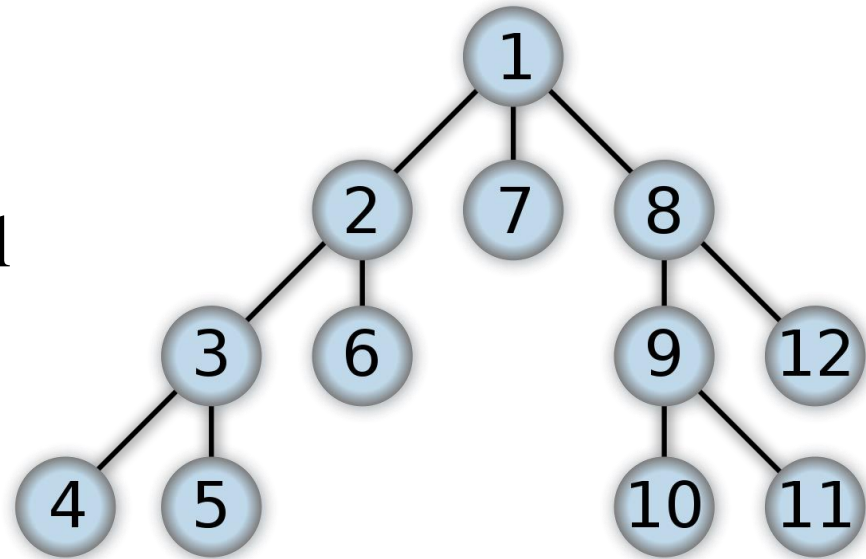
- Inorder Traversal
- Preorder Traversal
- Postorder Traversal



Ex. 4 – Teamwork

1. Execute in Main() trees in the figure below and access the tree with three traversal algorithms

- Inorder Traversal
- Preorder Traversal
- Postorder Traversal



2. Analysis of tree step of each function in tree

Thanks!