

1. Thinning operator

Algorithm:

step1: mark-interior/border-pixel operator

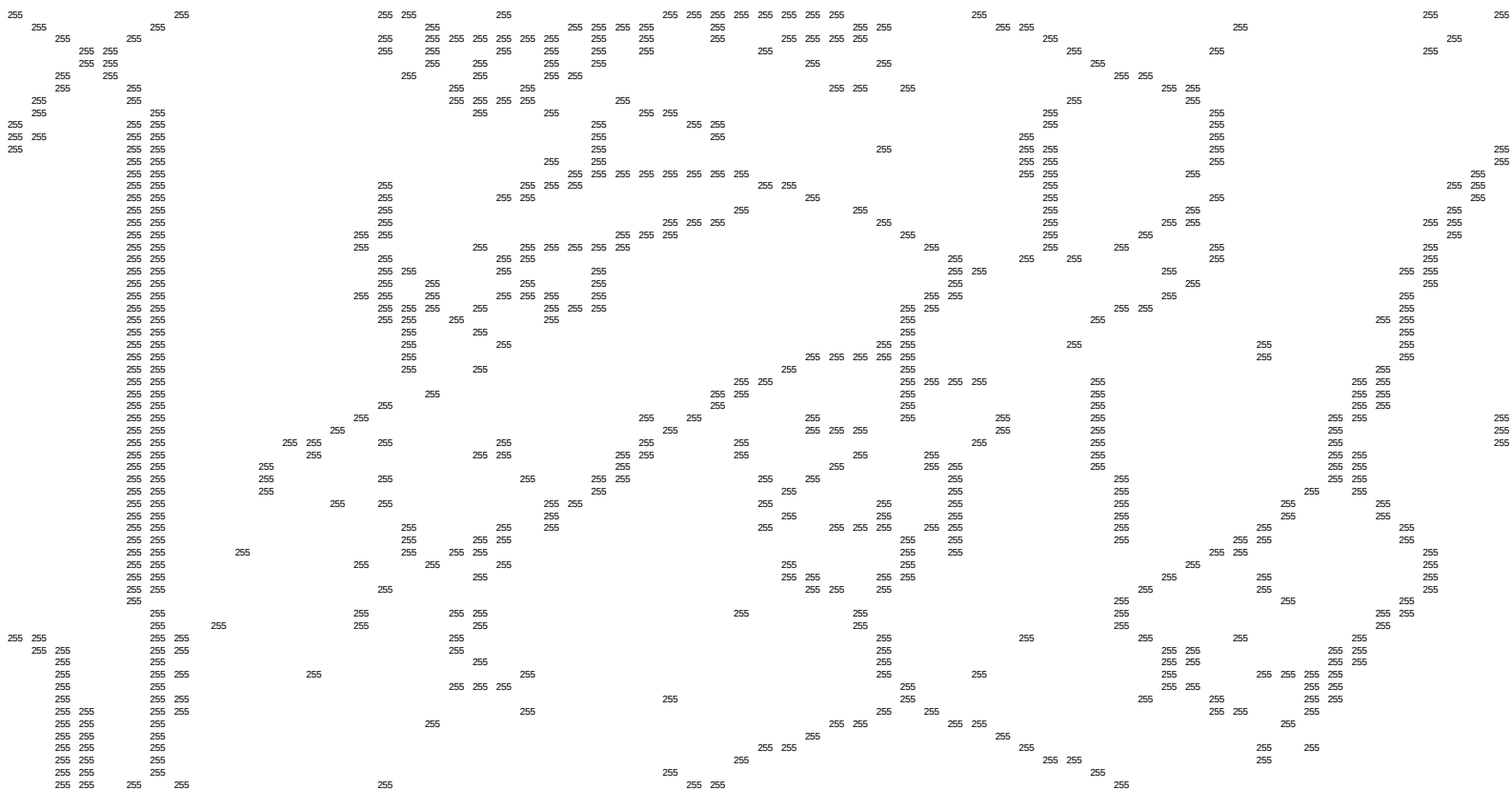
step2: pair relationship operator

step3: marked-pixel connected shrink operator

Repeat step 1, 2, 3 until the output never change.

The input image is gray scale Lena.jpg downside from 512*512 to 64*64 and binary at 128.

Result:



Code:

Follow the slide to implement h, I, f, function for interior/border operator

```
def h(c,d):  
    if c==d:  
        return 255  
    elif c!=d:  
        return 0  
def I(a,i):  
    if a=="i":  
        return 1  
    else:  
        return 0  
def f(c):  
    if c==0:  
        return "b"  
    elif c!=0:  
        return "i"
```

Interior/border operator work as IB function

```
def IB(img):#thinning  
    #row,col=img.shape  
    row=len(img)  
    col=len(img)  
    new=[[" "for i in range(row+2)] for i in range(col+2)]  
    res=[[" "for i in range(row+2)] for i in range(col+2)]  
    fres=[[" "for i in range(row)] for i in range(col)]  
    for i in range(row):  
        for j in range(col):  
            if img[i][j]==255:  
                new[i+1][j+1]=img[i][j]  
    for i in range(1,row+1):  
        for j in range(1,col+1):  
            if new[i][j]==255:  
                a0=new[i][j]  
                a1=h(a0,new[i][j+1])  
                a2=h(a1,new[i-1][j])  
                a3=h(a2,new[i][j-1])  
                a4=h(a3,new[i+1][j])  
  
                res[i][j]=f(a4)  
  
    for i in range(row):  
        for j in range(col):  
            fres[i][j]=res[i+1][j+1]
```

After define border and interior point, we should do the pair relation operator

```
def PairRelation(i,j,img):
    if I(img[i][j+1],"i")+I(img[i-1][j],"i")+I(img[i][j-1],"i")+I(img[i+1][j],"i")<1 or img[i][j]!="b":
        #print(I(img[i][j+1],"i")+I(img[i-1][j],"i")+I(img[i][j-1],"i")+I(img[i+1][j],"i"))
        return "q"
    elif I(img[i][j+1],"i")+I(img[i-1][j],"i")+I(img[i][j-1],"i")+I(img[i+1][j],"i")>=1 and img[i][j]=="b":
        return "p"
def PR(img):
    row=len(img)
    col=len(img)
    #print(row,col)
    new=[[" " for i in range(row+2)] for i in range(col+2)]
    res=[[" " for i in range(row+2)] for i in range(col+2)]
    fres=[[" " for i in range(row)] for i in range(col)]
    for i in range(row):
        for j in range(col):
            if img[i][j]=="b" or img[i][j]=="i":
                new[i+1][j+1]=img[i][j]
    for i in range(1,row+1):
        for j in range(1,col+1):
            if new[i][j]=="b" or new[i][j]=="i":
                #print(i,j)
                res[i][j]=PairRelation(i,j,new)
    for i in range(row):
        for j in range(col):
            fres[i][j]=res[i+1][j+1]
    return fres
```

the pixel is removable if the pixel is marked as “p” and the value of f function return is exactly 1

```
def removeable(i,j,new):
    def h(b,c,d,e):
        if b==c and ((d != b) or (e != b)):
            return "q"
        elif b==c and ((d==b) and (e==b)):
            return "r"
        elif b != c:
            return "s"
    def f(a1,a2,a3,a4):
        if a1==a2 and a1==a3 and a1==a4 and a1=="r":
            return 5
        else:
            l=[a1,a2,a3,a4]
            #print(l)
            count=l.count("q")
            return count
    l=[]
    l.append(h(new[i][j],new[i][j+1],new[i-1][j+1],new[i-1][j]))
    l.append(h(new[i][j],new[i-1][j],new[i-1][j-1],new[i][j-1]))
    l.append(h(new[i][j],new[i][j-1],new[i+1][j-1],new[i+1][j]))
    l.append(h(new[i][j],new[i+1][j],new[i+1][j+1],new[i][j+1]))
    res=f(l[0],l[1],l[2],l[3])
    if res==1:
        return True
```

The thinning operator

```

def thinning(img):
    row=len(img)
    col=len(img)
    #print(row,col,"fuck")
    new=[[" " for i in range(row+2)] for i in range(col+2)]
    res=[[" " for i in range(row+2)] for i in range(col+2)]
    fres=[[" " for i in range(row)] for i in range(col)]

    ib=IB(img)
    pr=PR(ib)
    for i in range(row):
        for j in range(col):
            if img[i][j]==255:
                new[i+1][j+1]=img[i][j]
                res[i+1][j+1]=img[i][j]
    for i in range(1,row+1):
        for j in range(1,col+1):
            if removeable(i,j,new) and pr[i-1][j-1]=="p":
                #print(new[i][j],removeable(i,j,new),pr[i-1][j-1])
                res[i][j]=0
    for i in range(row):
        for j in range(col):
            fres[i][j]=res[i+1][j+1]
    return fres

```

Use main function to repeat step 1,2,3 until the output never change

```

def main():
    bi=bin(img)
    ds=downside(bi)#255
    yk=IB(ds)#interior border
    pr=PR(yk)#qp

    check=True
    while(check):
        th=thinning(ds)
        if th==ds:
            check=False
        else:
            ds=th
    new=np.zeros((64,64),dtype=np.int)
    for i in range(64):
        for j in range(64):
            if th[i][j]==255:
                new[i][j]=255

    # np.asarray(th)
    cv2.imwrite("thinning.jpg",new)
    df1=pd.DataFrame(th)
    df1.to_csv("hw7.csv")

```

Discussion:

we can find that there is a line with two pixel width. I first regard it as not reasonable, but after I check the algorithm in slides, this is the correct result. It is because when the line is shrunk to two parallel pixel, they are both border which are marked q (no interior point), so the pixel will not be canceled.