

1.Laplace mask1

[[0,1,0],
[1,-4,1],
[0,1,0]]

threshold at 15



threshold at 18



threshold at 20



2.Laplace mask 2

mask=[[1.0/3,1.0/3,1.0/3],[1.0/3,-8.0/3,1.0/3],[1.0/3,1.0/3,1.0/3]]

threshold at 15



threshold at 18
good for noise removed and clear contour



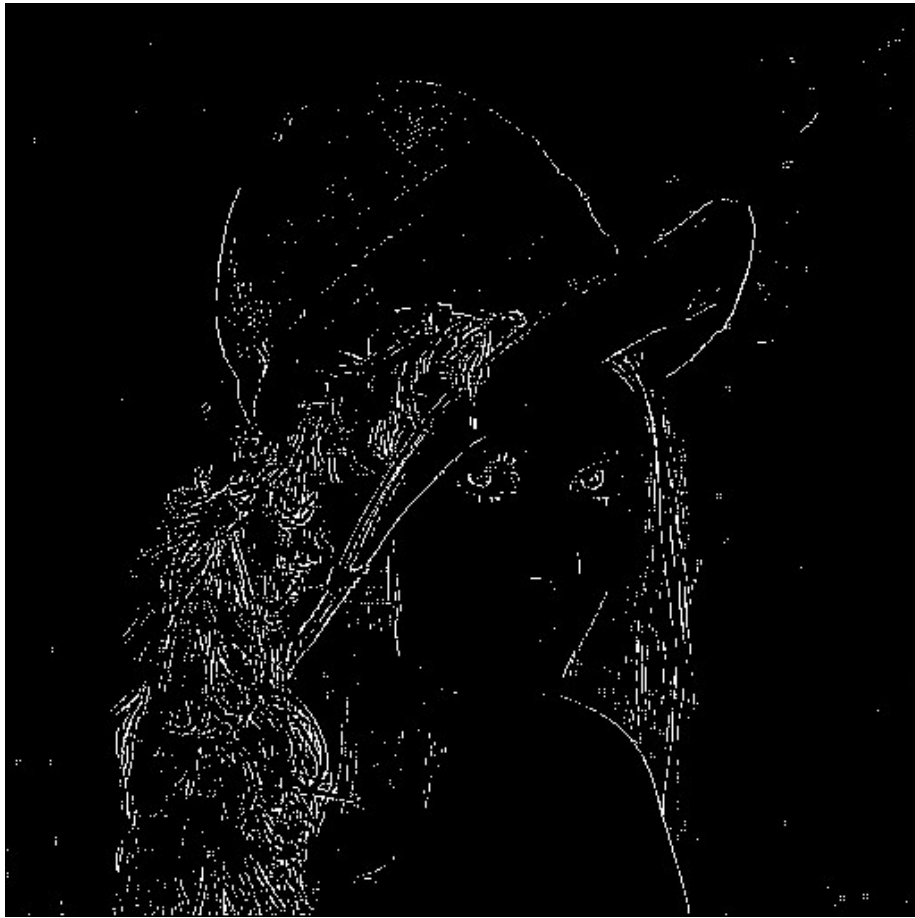
3.mini variance
mask=[[2.0/3,-1.0/3,2.0/3],[-1.0/3,-4.0/3,-1.0/3],[2.0/3,-1.0/3,2.0/3]]
threshold at 12



threshold at 15



threshold at 20



4. Laplace of Gaussian

```
mask=[[0,0,0,-1,-1,-2,-1,-1,0,0,0],  
      [0,0,-2,-4,-8,-9,-8,-4,-2,0,0],  
      [0,-2,-7,-15,-22,-23,-22,-15,-7,-2,0],  
      [-1,-4,-15,-24,-14,-1,-14,-24,-15,-4,-1],  
      [-1,-8,-22,-14,52,103,52,-14,-22,-8,-1],  
      [-2,-9,-23,-1,103,178,103,-1,-23,-9,-2],  
      [-1,-8,-22,-14,52,103,52,-14,-22,-8,-1],  
      [-1,-4,-15,-24,-14,-1,-14,-24,-15,-4,-1],  
      [0,-2,-7,-15,-22,-23,-22,-15,-7,-2,0],  
      [0,0,-2,-4,-8,-9,-8,-4,-2,0,0],  
      [0,0,0,-1,-1,-2,-1,-1,0,0,0]]
```

threshold at 1200



threshold at 1300

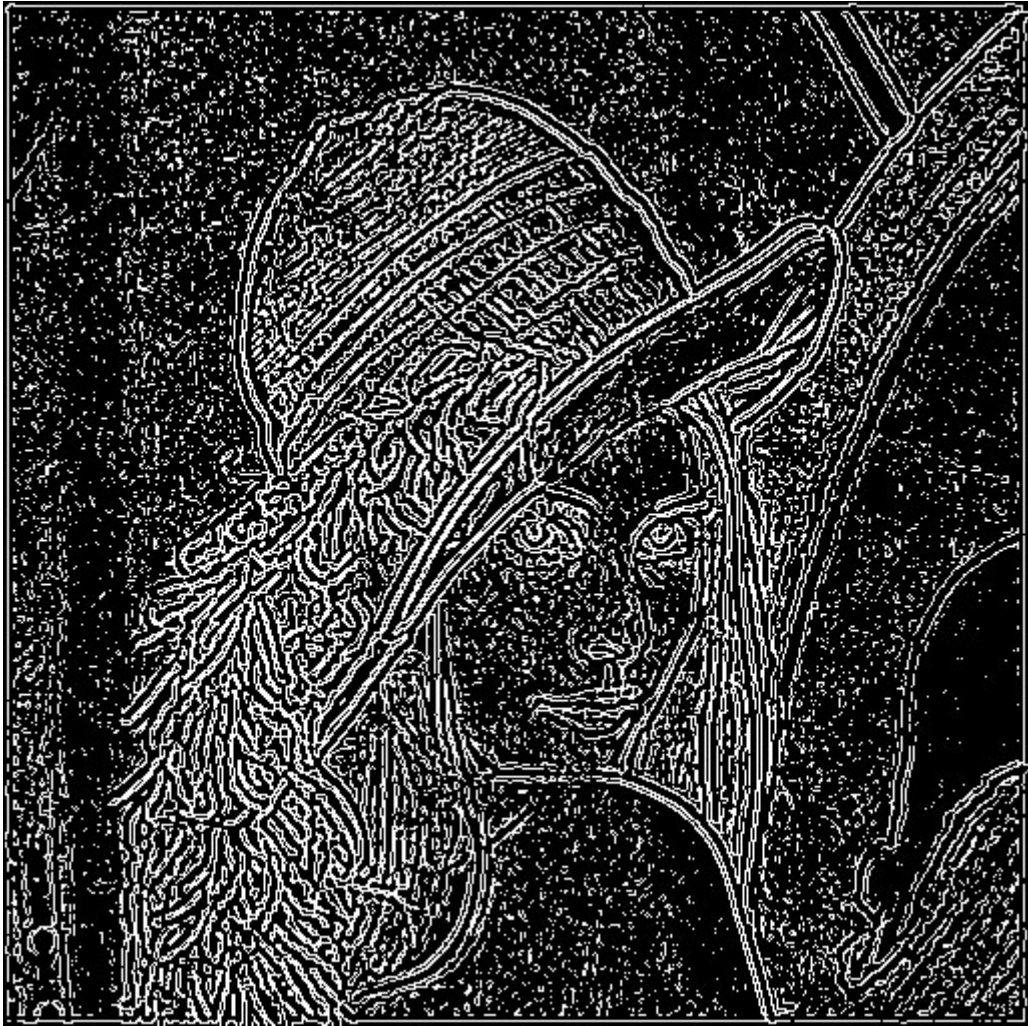


5. Difference Gaussian

I generate difference Gaussian mask by $G(0,1)-G(0,3)$ in $11*11$ mask code:

```
mask=np.zeros(shape=(11,11))
sigma1=1
sigma2=3
mean=0
for i in range(-5,6):
    for j in range(-5,6):
        a=math.exp(-(i**2+j**2)/(2.0*sigma1*sigma1))/(math.sqrt(2*math.pi)*sigma1)
        b=math.exp(-(i**2+j**2)/(2.0*sigma2*sigma2))/(math.sqrt(2*math.pi)*sigma2)
        mask[i+5][j+5]=a-b
        mean+=a-b
mean/=11*11
for i in range(11):
    for j in range(11):
        mask[i][j]-=mean
```


threshold at 1



threshold at 2



threshold at 3



threshold at 4




```

def Difference_Gaussian(img, threshold):
    row, col = img.shape
    new = np.zeros(shape=(row, col))
    res = np.zeros(shape=(row, col))
    mask = np.zeros(shape=(11, 11))
    sigma1 = 1
    sigma2 = 3
    mean = 0
    for i in range(-5, 6):
        for j in range(-5, 6):
            a = math.exp(-(i**2 + j**2) / (2.0 * sigma1 * sigma1)) / (math.sqrt(2 * math.pi) * sigma1)
            b = math.exp(-(i**2 + j**2) / (2.0 * sigma2 * sigma2)) / (math.sqrt(2 * math.pi) * sigma2)
            mask[i+5][j+5] = a - b
            mean += a - b
    mean /= 11 * 11
    for i in range(11):
        for j in range(11):
            mask[i][j] -= mean

    for i in range(row):
        for j in range(col):
            s1 = 0.0
            for X in range(-5, 6):
                for Y in range(-5, 6):
                    if X+i >= 0 and X+i < row and j+Y >= 0 and j+Y < col:
                        s1 += mask[X+5][Y+5] * img[i+X][j+Y]
                        #print(X, Y, i, j)
            new[i][j] = s1
    for i in range(row):
        for j in range(col):
            if new[i][j] > threshold:
                for X in range(-1, 2):
                    for Y in range(-1, 2):
                        if X+i >= 0 and X+i < row and j+Y >= 0 and j+Y < col:
                            if new[i+X][j+Y] < -1 * threshold:
                                res[i][j] = 255
    return res

```

Discussion:

we can find that the bigger kernel has function not only on finding contour but also remove the noise. However, it's also need more time to process the image.

I regard Laplace of Gaussian as the best performance.

I think this is because zero crossing check more constrains such as whether it's neighbor is less than threshold, which increases the correctness of finding contour. Besides, Gaussian distribution also a good model to describe the image pixels distribution.

