## 1. Yokoi connectivity number

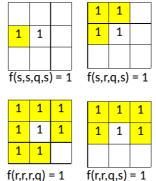
Use Yokoi connectivity number to recognize the property of every pixel

1:edge label
2:connecting label
3:branching label
4:crossing label
5:interior label
0:isolated label

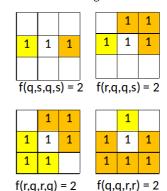




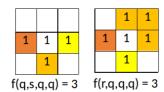
Edge label 1



Connecting label 2



Branching label 3



Crossing label 4



Interior label 5

1	1	1
1	1	1
1	1	1
f(r,r,r,r) = 5		

Step: Binary gray scale lena at 128

downside from 512x512 to 64x64 (choose the top left right pixel in 8x8 grid) do the yokoi algorithm for 4 connectivity

$$h(b,c,d,e) = \begin{cases} q & \text{if } b = c \text{ and } (d \neq b \ \lor e \neq b) \\ r & \text{if } b = c \text{ and } (d = b \land e = b) \\ s & \text{if } b \neq c \end{cases}$$

$$\begin{array}{c|ccc}
 x_7 & x_2 & x_6 \\
 x_3 & x_0 & x_1 \\
 x_8 & x_4 & x_5
 \end{array}$$

## define f function:

$$f(a_{1}, a_{2}, a_{3}, a_{4})$$

$$= \begin{cases} 5 & \text{if } a_{1} = a_{2} = a_{3} = a_{4} = r \\ n & \text{where } n = number of \{a_{k} | a_{k} = q\}, \text{otherwise} \end{cases}$$

to determine the number of label. Result:

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```

Code: follow the yokoi algorithm define h function and f function first

```
def h(b,c,d,e):
    if b==c and ((d != b) or (e != b)):
        return "q"
    elif b==c and ((d==b) and (e==b)):
        return "r"
    elif b != c:
        return "s"
```

```
def f(a1,a2,a3,a4):
    if a1==a2 and a1==a3 and a1==a4 and a1=="r":
        return 5
    else:
        l=[a1,a2,a3,a4]
        #print(l)
        count=l.count("q")
        return count
```

Second define vokoi function

```
def yokoi(img):
     row, col=img. shape
    new=[[" "for i in range(66)] for i in range(66)]
res=[[" "for i in range(66)] for i in range(66)]
     rsize=np.zeros((row,col),dtype=np.int)
     fres=[[" "for i in range(64)] for i in range(64)]
     for i in range(row):
          for j in range(col):
               if img[i][j]==255:
    new[i+1][j+1]=img[i][j]
     for i in range(1,row+1):
          for j in range(1,col+1):
               if new[i][j]==255:
                    1=[]
                    l.append(h(new[i][j],new[i][j+1],new[i-1][j+1],new[i-1][j]))
                   l.append(h(new[i][j],new[i-1][j],new[i-1][j-1],new[i][j-1]))
l.append(h(new[i][j],new[i][j-1],new[i+1][j-1],new[i+1][j]))
                   l.append(h(new[i][j],new[i+1][j],new[i+1][j+1],new[i][j+1]))
                    res[i][j]=f(l[0],l[1],l[2],l[3])
     for i in range(row):
          for j in range(col):
               fres[i][j]=res[i+1][j+1]
     return fres
```

Finally, use pandas to output the matrix

```
bi=bin(img)
ds=downside(bi)
yk=yokoi(ds)
#print(yk)
df=pd.DataFrame(yk)
df.to_csv("hw6.csv")
df=pd.DataFrame(ds)
df.to_csv("ds.csv")
```