

1. Yokoi connectivity number

Use Yokoi connectivity number to recognize the property of every pixel

- 1:edge label
- 2:connecting label
- 3:branching label
- 4:crossing label
- 5:interior label
- 0:isolated label

Isolated label 0

	1	

$$f(s,s,s,s) = 0$$

Edge label 1

1	1	

$$f(s,s,q,s) = 1$$

1	1	
1	1	

$$f(s,r,q,s) = 1$$

1	1	1
1	1	1
1	1	

$$f(r,r,r,q) = 1$$

1	1	1
1	1	1

$$f(r,r,r,q,s) = 1$$

Connecting label 2

1	1	1

$$f(q,s,q,s) = 2$$

	1	1
1	1	1

$$f(r,q,q,s) = 2$$

	1	1
1	1	1
1	1	

$$f(r,q,r,q) = 2$$

	1	
1	1	1
1	1	1

$$f(q,q,r,r) = 2$$

Branching label 3

1	1	1
	1	

$$f(q,s,q,q) = 3$$

	1	1
1	1	1
	1	

$$f(r,q,q,q) = 3$$

Crossing label 4

	1	
1	1	1
	1	

$$f(q,q,q,q) = 4$$

Interior label 5

1	1	1
1	1	1
1	1	1

$$f(r,r,r,r) = 5$$

Step: Binary gray scale lena at 128

downside from 512x512 to 64x64 (choose the top left right pixel in 8x8 grid)

do the yokoi algorithm for 4 connectivity

$$h(b,c,d,e) = \begin{cases} q & \text{if } b = c \text{ and } (d \neq b \vee e \neq b) \\ r & \text{if } b = c \text{ and } (d = b \wedge e = b) \\ s & \text{if } b \neq c \end{cases}$$

$$a1=h(b,c,d,e)=h(x0,x1,x6,x2)$$

$$a2=h(b,c,d,e)=h(x0,x2,x7,x3)$$

$$a3=h(b,c,d,e)=h(x0,x3,x8,x4)$$

$$a4=h(b,c,d,e)=h(x0,x4,x5,x1)$$

x_7	x_2	x_6
x_3	x_0	x_1
x_8	x_4	x_5

define f function:

$$f(a_1, a_2, a_3, a_4) = \begin{cases} 5 & \text{if } a_1 = a_2 = a_3 = a_4 = r \\ n & \text{where } n = \text{numberof}\{a_k | a_k = q\}, \text{otherwise} \end{cases}$$

Result:



define h function and f function first

```
def h(b,c,d,e):  
    if b==c and ((d != b) or (e != b)):  
        return "q"  
    elif b==c and ((d==b) and (e==b)):  
        return "r"  
    elif b != c:  
        return "s"
```

```
def f(a1,a2,a3,a4):
    if a1==a2 and a1==a3 and a1==a4 and a1=="r":
        return 5
    else:
        l=[a1,a2,a3,a4]
        #print(l)
        count=l.count("q")
        return count
```

Second define yokoi function

```
def yokoi(img):
    row,col=img.shape
    new=[" "for i in range(66)] for i in range(66)]
    res=[" "for i in range(66)] for i in range(66)]
    #new=np.zeros((row+2,col+2),dtype=np.int)
    #res=np.zeros((row+2,col+2),dtype=np.int)
    rsize=np.zeros((row,col),dtype=np.int)
    fres=[" "for i in range(64)] for i in range(64)]
    for i in range(row):
        for j in range(col):
            if img[i][j]==255:
                new[i+1][j+1]=img[i][j]
    for i in range(1,row+1):
        for j in range(1,col+1):
            if new[i][j]==255:
                l=[]
                l.append(h(new[i][j],new[i][j+1],new[i-1][j+1],new[i-1][j]))
                l.append(h(new[i][j],new[i-1][j],new[i-1][j-1],new[i][j-1]))
                l.append(h(new[i][j],new[i][j-1],new[i+1][j-1],new[i+1][j]))
                l.append(h(new[i][j],new[i+1][j],new[i+1][j+1],new[i][j+1]))
                res[i][j]=f(l[0],l[1],l[2],l[3])
    for i in range(row):
        for j in range(col):
            fres[i][j]=res[i+1][j+1]

    return fres
```

Finally, use pandas to output the matrix

```
bi=bin(img)
ds=downside(bi)
yk=yokoi(ds)
#print(yk)
df=pd.DataFrame(yk)
df.to_csv("hw6.csv")
df=pd.DataFrame(ds)
df.to_csv("ds.csv")
```