

### **Poisson Distribution :**

$$p(y) = \frac{\lambda^y}{y!} e^{-\lambda}$$

### **Tchebysheff's Theorem :**

$$P(|Y - \mu| < k\sigma) \geq 1 - \frac{1}{k^2}$$

or

$$P(|Y - \mu| \geq k\sigma) \leq \frac{1}{k^2}$$

### **Probability Distribution for a Continuous Random Variable :**

$$E(Y) = \int_{-\infty}^{\infty} yf(y) dy$$

### **Uniform Probability Distribution**

$$\mu = E(Y) = \frac{\theta_1 + \theta_2}{2}$$

$$\sigma^2 = V(Y) = \frac{(\theta_2 - \theta_1)^2}{12}$$

### **Exponential Distribution**

$$\mu = \frac{1}{\lambda}$$

$$V(Y) = \frac{1}{\lambda^2}$$

$$f(x) = \lambda e^{-\lambda x}, \text{ for } x \geq 0$$

### **Bivariate Distribution**

$$p(y_1, y_2) = P(Y_1 = y_1, Y_2 = y_2), \quad -\infty < y_1 < \infty, -\infty < y_2 < \infty$$

## Continuous Random Variables with Joint Distribution Function

$$F(y_1, y_2) = \int_{-\infty}^{y_1} \int_{-\infty}^{y_2} f(t_1, t_2) dt_2 dt_1$$

## Marginal Probability and Density Functions

$$p_1(y_1) = \sum_{all y_2} p(y_1, y_2) \text{ and } p_2(y_2) = \sum_{all y_1} p(y_1, y_2)$$

$$f_1(y_1) = \int_{-\infty}^{\infty} f(y_1, y_2) dy_2 \text{ and } f_2(y_2) = \int_{-\infty}^{\infty} f(y_1, y_2) dy_1$$

$$p(y_1|y_2) = P(Y_1 = y_1|Y_2 = y_2) = P(Y_1 = y_1, Y_2 = y_2) = p(y_1, y_2), P(Y_2 = y_2) p_2(y_2)$$

$$F(y_1|y_2) = P(Y_1 \leq y_1|Y_2 = y_2)$$

$$f(y_1|y_2) = f \frac{(y_1, y_2)}{f_2(y_2)}$$

$$f(y_2|y_1) = f \frac{(y_1, y_2)}{f_1(y_1)}$$

## Independent Random Variables

$$F(y_1, y_2) = F_1(y_1)F_2(y_2)$$