

1. If we want to analyze only players who were regularly involved in the season, how can we use set theory to define eligibility?

We define two sets:

- Set A: Players who averaged more than 20 minutes per game ($|A| = 268$)
- Set B: Players who played at least 41 games ($|B| = 340$)

The set of qualified players is their intersection:

- $S = A \cap B = 226$

This filters out part-time or minimally used players, ensuring valid comparisons.

2. What's the probability a player is average in 0 or 1 of the 5 main categories?

From the data:

- $P(0 \text{ categories}) = 0.323$ (32.3%)
- $P(1 \text{ category}) = 0.363$ (36.3%)

So the combined probability:

$P(0 \text{ or } 1 \text{ categories}) = 0.323 + 0.363 = 0.686$ (68.6%)

Most players are average in 1 or no categories statistical balance is rare.

3. What is the chance the most average player is not selected in 3 random picks?

Lets assume the chance of selecting the target player = 0.5 per trial.

The probability of not selecting them in 3 trials:

$P = (1 - 0.5)^3 = 0.125$

So there's a 12.5% chance the most average player is overlooked in 3 random attempts.

4. In how many ways can 9 players be grouped into levels of averageness?

We want to arrange 9 players into groups of 3 (highly average), 5 (moderately average), and 1 (perfectly average):

Use permutations with repetition:

$\text{Ways} = 9! / (3! * 5! * 1!) = 504$

5. If a player is average in points, how likely are they to also be average in another stat?

From conditional counts:

- $P(\text{TRB} | \text{PPG}) = 0.414$
- $P(\text{AST} | \text{PPG}) = 0.276$
- $P(\text{STL} | \text{PPG}) = 0.259$
- $P(\text{BLK} | \text{PPG}) = 0.190$

Conclusion: Being average in one stat doesn't strongly imply averageness elsewhere.

6. Are points and rebounds independent?

We compare:

- $P(\text{PPG}) = 58 / 226 = 0.257$
- $P(\text{TRB}) = 65 / 226 = 0.288$
- $P(\text{PPG} \cap \text{TRB}) = 24 / 226 = 0.106$
- If independent: $0.257 * 0.288 = 0.074$

Since $0.106 \neq 0.074$, they are not independent a weak positive relationship exists.

7. If a player is average in points, what's the probability they're a big man?

We apply Bayes Rule:

- $P(\text{PPG}) = 58 / 226 = 0.257$
- $P(\text{Big}) = 84 / 226 = 0.372$
- $P(\text{PPG} | \text{Big}) = 19 / 84 = 0.226$

Bayes: $P(\text{Big} \mid \text{PPG}) = (0.226 * 0.372) / 0.257 = 0.327$

So ~32.7% of average scorers are big men.

8. Whats the expected number of categories a player is average in?

Using the formula:

$$E(X) = [x * P(x)] = 0 * 0.323 + 1 * 0.363 + 2 * 0.217 + 3 * 0.075 + 4 * 0.022 = 1.11$$

So, the average player is statistically average in ~1.1 categories.

9. What is the probability of being average in all 5 categories?

Using binomial formula:

$n = 5$, $p = 0.222$ (prob. of being average in 1 category)

$$P(X = 5) = C(5, 5) * 0.222^5 = 0.00054$$

Very rare (<0.1%).

10. Whats the chance the first average player appears on the 5th try?

Geometric formula:

$$P = (1-p)^{(k-1)} * p = (1-0.097)^4 * 0.097 = 0.06449$$

So, 6.4% chance it takes 5 tries to find the first one.

11. On average, how many players do you need to find 3 average ones?

Negative binomial expected value:

$$E(X) = r / p = 3 / 0.097 = 30.93$$

So expect to examine ~31 players to find 3 average ones.

12. If 4 players are randomly selected, what's the chance all are average scorers?

Using hypergeometric:

$$P = [C(58, 4) * C(168, 0)] / C(226, 4) = 0.01806$$

Only ~1.8% of 4-player groups are all average in scoring.

13. Do blocks follow a Poisson distribution?

Yes the distribution is count-based, right-skewed.

$$- (\text{bigs}) = 0.859$$

$$- (\text{non-bigs}) = 0.370$$

Most non-bigs had 0 blocks, which is expected for low- Poisson variables.

14. How many players fall within 1.5 standard deviations of average PPG?

Tchebysheffs bound:

$$P(|X - \mu| < 1.5) \geq 1 - 1/k = 1 - 1/2.25 = 0.556$$

Actual observed: 87.2% much higher than guaranteed bound.

15. Whats the probability a player is within 15% of average PPG?

Normal model:

$$= 14.18, = 5.96$$

Interval: 12.05 X 16.31

$$P = 0.2788 \text{ (27.9\%)}$$

16. What are the expected value and variance for PPG?

Computed from sample:

Mean = 14.18 points per game

Variance = 35.52

17. What's the chance a player is in the average AST range assuming a uniform distribution?

$U(0, 10)$ width = 10

Interval = [2.77, 3.75] width = 0.98

$P = 0.98 / 10 = 0.0979$ (9.8%)

18. Do any NBA stat categories follow a Gamma (or Exponential) distribution?

Yes. Stats that are right-skewed and involve counts of rare events like blocks or steals often resemble a Gamma distribution.

- For example, blocks per game among non-bigs had $\lambda = 0.370$, heavily right-skewed.
 - Most players have 0 or 1 block per game, but a few have much higher values, creating the tail.
- This shape is typical of Gamma or Exponential distributions, which makes them suitable for modeling rare but variable events in NBA stats.