

Abstract

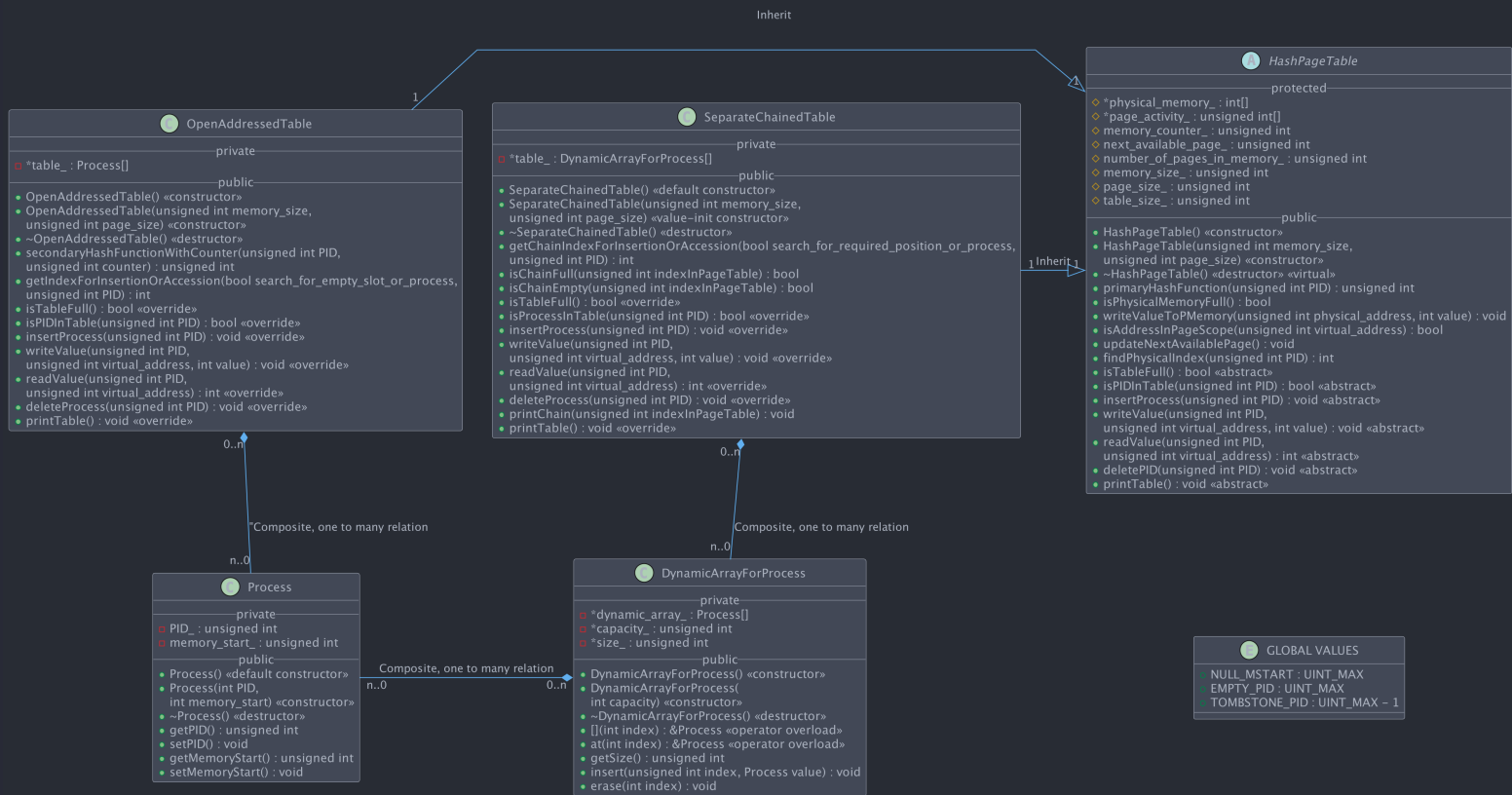
This is the design document of Chaitanya Sharma for Project 2 for ECE 250's Winter 2023 offering.

1 Introduction

My program consisted of a base abstract class `HashPageTable`, and two derived classes, namely `OpenAddressedTable` and `SeparateChainedTable` with dynamic array class for Chaining called `DynamicArrayForProcess`. Also, according to the first word in the test case, the `main` function calls either of `OpenAddressedTableDriver` or `ChainedTableDriver` for which I follow the parsing designs given by the ECE 250 staff. I have three **GLOBAL VALUES** defined, which act as placeholders for empty and deleted values, there values are **EMPTY_PID**= 0, **NULL_MSTART**= `UINT_MAX` = 4294967295 and **TOMBSTONE_PID**= `UINT_MAX` = 4294967295.

I've tested all edge test cases possible and also used the test cases provided by the jekelaugrader on <https://github.com/JZJisawesome/ece250-testcases>.

Hashed Page Table Implementation With Ordered Separate Chaining And Open Addressing Via Double Hashing



2 Class Structure

2.1 class Process

This is a very simple class which only holds two pieces of information, the `PID_` and the `memory_start_`, and I've provided the appropriate `constructors()`, a default `destructor()` and getters and setters for the two variables. The `memory_start_` is like a virtual pointer to an index(or address) in the physical memory. And in the abstract design, two processes should neither ever have the same `PID_` or the same `memory_start_`, except when they're deleted or initialized to by the default constructor which would give them the value of **TOMBSTONE_PID** or **EMPTY_PID** respectively and a memory start of **NULL_MSTART**.

2.2 class HashPageTable

In this class most of the functions are actually pure virtual functions, except the `constructor()`, `destructor()`, status boolean helper functions like `isPhysicalMemoryFull`, the helper functions which deal with the physical memory like `findPhysicalIndex` and obviously the `primaryHashFunction()`. I've allocated all types of data structures which I would need, but aren't unique to the derived classes, in this class like the `physical_memory_[]`, `page_activity_[]` and more. I've used the `page_activity_[]` to keep track of the statuses of each page in physical memory, and used a virtual pointer called `next_available_page_` which I update using `updateNextAvailablePage()`. I'll explain all other logic since they're unique to the derived classes. The runtime of all functions defined in this class are $O(1)$ since they all just use the `primaryHashFunction()` to their operations, and the `primaryHashFunction()` is $O(1)$, and the `updateNextAvailablePage()` is dependant on the hash function, so due to our assumption of even spread, it is also $O(1)$.

For the destructor, I delete all appropriate dynamically allocated objects and equal them to `nullptr`.

2.3 class DynamicArrayForProcess

Instead of using the bloated `std::vector` class, I've created my own dynamic array class which is dynamically allocated process array, and for it's design, I've taken inspiration from the actual `std::vector` class, and I've used the same logic for the `DynamicArrayForProcess` class. Since I would only be using the functions `insert()`, `erase()`, `size()` and the appropriate operators overloads `operator[]` and `at`, I've only implemented those functions. When referring to `std::vector` class, as "bloated", I mean that for the purpose of a Page Table, most of its functionalities would be useless, and hence I've created my own class. Since even when using `std::vector`, we were assuming the insertion, deletion and copy operations(for increasing size), we were assuming the runtime of the functionalities to be insignifigant, inside the concept of Hashing. Hence, the runtime of all the functions in this class are $O(n)$ but considered $O(1)$ for the abstraction purpose of this project. This class will produce an aggregation object of the `Process` class's objects.

For the destructor, I delete all appropriate dynamically allocated objects.

2.4 class SeparateChainedTable

The main component of this class is a pointer which when initialized properly is an a dynamic array object of type

`DynamicArrayForProcess` with the size $\frac{N(\text{memory size})}{P(\text{page size})}$. Hence, it essentially acts as a 2D array. Since the `DynamicArrayForProcess` object itself initializes without an element and resizes according to need, I do not initialize the internal index `DynamicArrayForProcess` objects with a specified

size. In this class, I have an empty constructor which just calls the empty `constructor()` of the `HashPageTable` class and initializes `table__` to `nullptr`, a value-init `constructor()`, which calls the value-init `constructor()`, but at the same time, initializes the `table__` with the value $\frac{N}{P}$.

For the destructor, I delete all appropriate dynamically allocated objects as well as call the destructor of the `HashPageTable` class.

Then there are chain status boolean functions like `isChainEmpty()` and `isChainFull()` whose names are self-descriptive, and functions like `isTableFull()` and `isProcessInTable()` which returns boolean values.

2.4.1 `int getChainIndexForInsertionOrAccession(bool search_for_required_position_or_process, unsigned int PID)` ★ a special feature of my code ★

I call this function a double option finder function, as function serves two purposes, one for insertion and one for accession, decided by the `bool` parameter. I've created this in such a way so that this is the single most iterative function in this whole class, and such that it first gets the `table__`'s index using the `primaryHashFunction()` and then then iterates through the `DynamicArrayForProcess` object at that index, and returns the index of the `DynamicArrayForProcess` object which is either empty or has the same PID as the one passed in the parameter according to the `bool` parameter. The amortized runtime analysis of this function is $O(1)$ which means that the runtime is $O(1)$ on average, with a worst-case runtime of $O(n)$. The `bool` parameter is used with the value `true` for insertion and `false` for accession. All my other major functions look like `one-liners` due to the ease of use of this function. Hence, I find this function to be the most important function in this class.

2.4.2 `void insertProcess(unsigned int PID)`

This function takes in the PID of the process to be inserted, and then calls the `getChainIndexForInsertionOrAccession` function with the `bool` parameter as `true` and then inserts the process at the index returned by the function using the `insert` function of my `DynamicArrayForProcess` class. It also prompts the virtual pointer to move to the next empty spot using the `updateNextAvailablePage()` on the `page_activity__` array and then it decrements the `number_of_pages_in_memory__` by one. The amortized runtime analysis of this function is $O(1)$ since it works by directly using the `getChainIndexForInsertionOrAccession()` function.

2.4.3 `void writeValue(unsigned int PID, unsigned int virtual_address, unsigned int value)`

This function modifies the value of `physical_memory__` array at the index calculated by using `getMemoryStarty()` `getChainIndexForInsertionOrAccession()` on `table__` array's index decided by the `primaryHashFunction()` and adding an offset of `virtual_address` to it. The amortized runtime analysis of this function is $O(1)$ similar to the `insertProcess()` function.

2.4.4 `int readValue(unsigned int PID, unsigned int virtual_address)`

This function operates in a similar fashion to the `writeValue()` function, but instead of modifying the value, it returns that value. The amortized runtime analysis of this function is $O(1)$ similar to the `insertProcess()` function.

2.4.5 `void deleteProcess(unsigned int PID)`

It uses the `erase()` function of my `DynamicArrayForProcess` class to delete the process from the `table__` array's index decided by the `primaryHashFunction()`. Then it decrements the `number_of_pages_in_memory__` by the number of pages the process occupied, changes the status of the page in the `page_activity__` array to 0 and then prompts the virtual pointer to move to the next empty spot using the `updateNextAvailablePage()` function. The amortized runtime analysis of this function is $O(1)$ similar to the `insertProcess()` function.

2.4.6 `void printChain()`

This function initiates a for loop which iterates through the `table__`'s index decided by the `primaryHashFunction()` and then prints the PID of the processes. The amortized runtime analysis of this function is $O(1)$ since it only operates on the `DynamicArrayForProcess` object at the index decided by the `primaryHashFunction()` with the assumption of uniform spread of the PID values.

2.4.7 `void printTable()` CONVENIENCE FUNCTION: beautifully prints the page table

2.5 `class OpenAddressedTable`

This table acts as a hash table structure, but instead of resolving collisions using chaining, it uses open addressed via double hashing. A core feature of this class is that it uses Lazy Deletion methodology, which I've declared globally using the `#define` directive. The structures of the constructors and destructor are similar to the `ChainedTable` class, but the value-init `constructor` creates a `table__` array of `Process` objects, and the `destructor` deletes the `table__` array and other dynamically allocated objects. Similar to the `ChainedTable` class, this class also has a `table__` array of `Process` objects, and there is also a double option finder function. For the destructor, I delete all appropriate dynamically allocated objects as well as call the destructor of the `HashPageTable` class. I have helper boolean functions like `isTableFull()` and `isProcessInTable()` which are used to check the status of the table.

2.5.1 `unsigned int secondaryHashFunctionWithCounter(unsigned int PID, unsigned int counter)`

This function is the secondary hash function used in conjunction with the primary hash function. It uses the `secondaryHashFunction()` function to calculate the index, and then it adds the `counter` to it. This function is used most importantly in the double option finder function.

2.5.2 `int getIndexForInsertionOrAccession(bool search_for_empty_slot_or_process, unsigned int PID)`

This function is the double option finder function. It takes in the PID of the process to be inserted or accessed, and then it uses the `primaryHashFunction()` function to calculate the index. I've implemented a `lambda function` called `index()` inside this function to calculate the result of the `secondaryHashFunctionWithCounter()` function in conjunction with the `primaryHashFunction()` function. I implemented a `Hash Path concept` in this function along with `Lazy Deletion` methodology. I consider the hash path to be the sequence of indexes that the `index()` function returns on incrementing the `counter` variable.

I've implemented Lazy Deletion by deciding to have values which have been pre-used empty to have the `UINT_MAX` and ever-empty slots to have the 0 value since we're given that all PIDs > 0. This way, I decide to ignore the re-used empty when searching a process, and stop when I see an empty slot, and in while searching for insertion i.e. an empty slot, I stop when I see a slot which has been pre-used empty or an ever-empty slot.

Along with this, I also implemented a non-empty counter inside this function, which is incremented every time I see a non-empty slot, and keep comparing this value to the total number of active processes in the page table. This lets me stop much before if I keep seeing pre-used empty slots, while searching for a process if I've already seen the total number of active processes in the page table, since I. All of this makes my function run on an amortized $O(1)$ time complexity which is the best.

2.5.3 `void other functions(unsigned int PID)`

All other corresponding functions are similar to the `ChainedTable` class and overridden from the base `HashPageTable` class, but they operated on the 1D array `table__` instead of the 2D array `table__`. And since all of them are directly dependant on the `getIndexForInsertionOrAccession()` they all run on an amortized $O(1)$ time complexity.

2.5.4 `void printTable()` CONVENIENCE FUNCTION: beautifully prints the page table