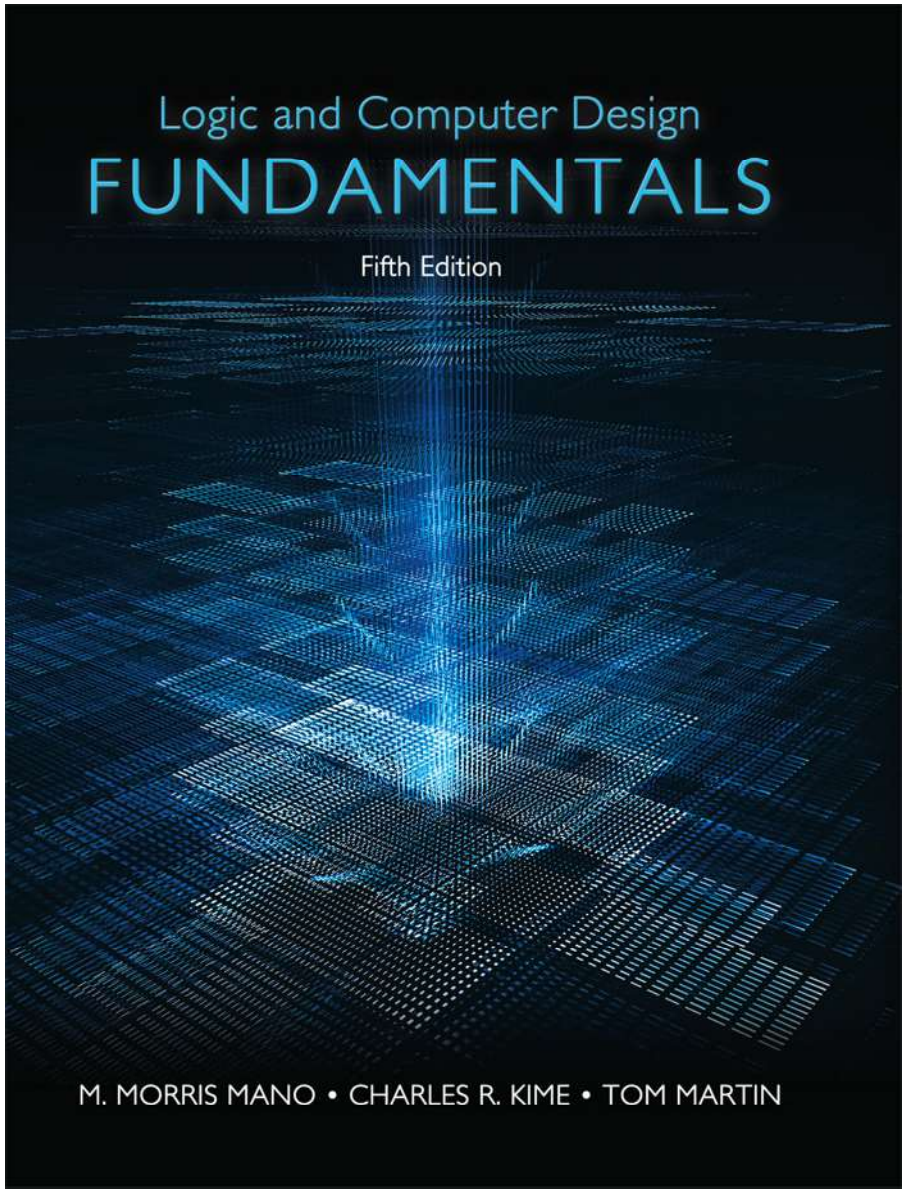
Logic and Computer Design
FUNDAMENTALS
Fifth Edition
M. MORRIS MANO • CHARLES R. KIME • TOM MARTIN

Logic and Computer Design Fundamentals

Fifth Edition

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