

$$\begin{aligned} 1. \quad f(x) &= 3x^4 - 8x^3 + 10 \\ f'(x) &= 12x^3 - 24x^2 \\ &= 12x^2(x - 2) \\ f''(x) &= 36x^2 - 48 \\ &= 12x(3x - 4) \end{aligned}$$

$$a. \quad \begin{array}{c|c|c} - & - & + \\ \hline & 0 & 2 \end{array}$$

$\therefore f(x)$ turun pada $(-\infty, 0) \cup (0, 2)$
 $f(x)$ naik pada $(2, \infty)$

b. hanya ada minimum lokal pada $x=2$

c. hanya ada minimum global pada $x=2$

$$d. \quad \begin{array}{c|c|c} + & - & + \\ \hline & 0 & \frac{4}{3} \end{array}$$

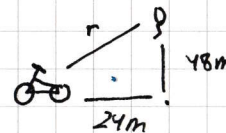
$\therefore f(x)$ cekung keatas pada $(-\infty, 0) \cup (\frac{4}{3}, \infty)$
 $f(x)$ cekung kebawah pada $(0, \frac{4}{3})$

e. karena pangkat terbesar genap maka $f(x) \rightarrow \infty$
Saat $x \rightarrow \infty$ dan $x \rightarrow -\infty$

2. a. Setelah 3 detik :

\rightarrow balon berada 48m dari titik awal

\rightarrow pesepeda berada 24m dari titik awal

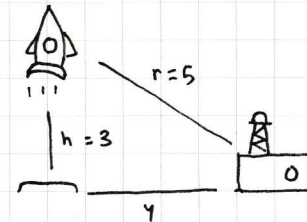


$$r^2 = 48^2 + 24^2$$

$$r = 24\sqrt{5}$$



3.



dit. $\frac{dh}{dt}$ saat $h=3$

$$\therefore \frac{dr}{dt} = 3600$$

$$r^2 = h^2 + 16$$

jawab:

$$\frac{dr}{dt} = \frac{dh}{dr} \cdot \frac{dr}{dt}$$

$$2r \, dr = 2h \, dh$$

$$\rightarrow \frac{dh}{dr} = \frac{2r}{2h} = \frac{r}{h} = \frac{\sqrt{h^2+16}}{h}$$

$$\therefore \frac{dh}{dt} = \frac{5}{3} \cdot 3600 = 6000 \quad \boxed{\text{shaded}}$$

$$h=3$$

$$\begin{aligned} \text{4. } V_{\text{balok}} &= s^2 l = 13500 \rightarrow l = \frac{13500}{s^2} \\ \text{total material} &= 4sl + s^2 \\ &= s^2 + \frac{54000}{s} = L \end{aligned}$$

$$L' = 2s - \frac{54000}{s^2} = 0$$

$$s = 30, l = 15 \quad \boxed{\text{shaded}}$$

$$\text{5. a. } 4 \text{ kali / 15 menit} = 4^4 \text{ kali / jam}$$

$$\therefore \text{Setelah 3 jam} = 10.256^3$$

$$\text{b. } 10^3 = 10.256^t$$

$$10^8 = 256^t$$

$$8 \ln 10 = t \ln 256$$

$$t = \frac{8 \ln 10}{\ln 256} = 3.3219280 \dots \text{jam} \quad \boxed{\text{shaded}}$$