

Objectives

- Work with higher order functions
- Work with the `plot` package

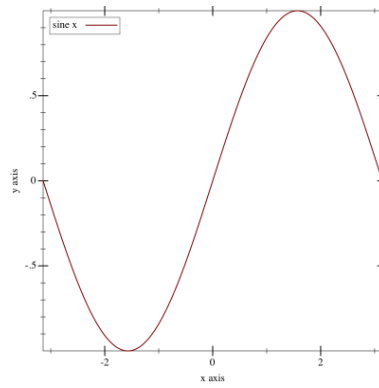
Activities

1. Let f and g be two functions, mapping integers to integers. Define a function `dominate` so that `(dominate f g)` outputs the smallest positive integer k for which $f(k) > g(k)$. Thus, if $f(1) > g(1)$, `(dominate f g)` should output 1. If $f(1) \leq g(1)$ but $f(2) > g(2)$, then `(dominate f g)` should output 2, etc.
2. **[SICP Exercise 1.41]**
Define a procedure `double` that takes a procedure of one argument as an argument and returns a procedure that applies the original procedure twice. For example, if `inc` is a procedure that adds 1 to its argument, then `(double inc)` should be a procedure that adds 2. What value is returned by `((double (double double)) inc) 5)`?
3. So far this semester, we have written several functions which find the n^{th} number in a sequence which satisfies some property (e.g. the n^{th} even number). It would be helpful if we wrote a higher order function which could take a function which generated the sequence and a function which tested for the property in which we are interested as well as the integer n and returned the n^{th} value in that sequence which satisfied the property (i.e. the `test` function returns true when passed that value).
 - (a) Write a function, named `find`, which takes three parameters (`sequence`, `test`, and `n`) and returns the n^{th} value in `sequence` for which the `test` function returns true (`#t`) when passed a value in `sequence`.
 - (b) Test your program with by finding the 5th of even number and the 5th of odd number. Verify your results with the solutions to the problem sets and in the lecture slides.
 - (c) A Fibonacci prime is a Fibonacci number which is prime. Use your higher-order function to find the 5th Fibonacci prime.
4. Racket also provides a graphing package, named `plot`, with which you can graph the functions you write in SCHEME. With Racket 5.2.1, change your language to “Use the language declared in the source” and add `#lang racket` as the first line in your Definitions window. To plot a function, start with the following two instructions which will import the plotting functions and create graphs in a new window.

```
(require plot)
```

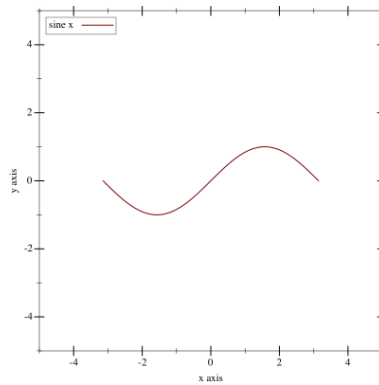
Next you can graph a function by using `plot`:

```
(plot (function sin (- pi) pi #:label "sine_x"))
```



where $(-\pi)$ and π determine the x-axis bounds. Additional plot keywords can be used to specify additional features of the plotted functions such as a legend and x and y bounds of the graph (separate from the bounds of the function to be graphed):

```
(plot (function sin (- pi) pi #:label "sine_x")
      #:x-min -5 #:x-max 5 #:y-min -5 #:y-max 5)
```



Plot the following function in the interval $[-5, 5]$, using Racket's plot capabilities:

```
(define (f x) (+ (* (sin x) (- 3 x)) 1))
```