

# Fundamentos de los Sistemas Operativos (FSO)

Departamento de Informática de Sistemas y Computadoras (DISCA)  
*Universitat Politècnica de València*

## Part 4: Memory management

### Seminar 12

### Virtual memory exercises (II)

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- **Exercise S10-1: 2nd chance replacement algorithm**
  - Exercise S10-1.1: 2nd chance basic
  - Exercise S10-1.2: 2nd chance complete
- **Exercise S10-2: Working set**
  - Exercise S10-2.1: Getting the working set

- In a **demand paging** system with **global replacement** policy, **5 frames** are allocated to all **processes**. Pages (and frames) have a size of **16K pages**. The initial state of the system and the page sequence generated by the CPU is detailed below.

Page Sequence	P1,0	P1,3	P2,3	P2,4	P1,3	P2,1	P1,4	P1,0	P2,2
Time	21	22	23	24	25	26	27	28	29

Initial frame allocation	
0	P1,1
1	P2,2
2	P1,2
3	P1,3
4	--

Obtain what pages are allocated on every frame when the next global scope algorithms are applied

- LRU based on Counters considering the initial counters state
- LRU based on stack considering the initial stack state
- LRU based in bit reference and 2nd oportunity considering the initial bit state

# Exercise S10-1.1

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  - Obtain what pages are allocated on every frame when the next global scope algorithms are applied
- LRU based on Counters**
  - LRU based on stack
  - LRU based in bit reference and 2nd opportunity.

		Inicio	P1,0	P1,3	P2,3	P2,4	P1,3	P2,1	P1,4	P1,0	P2,2
tiempo		20	21	22	23	24	25	26	27	28	29
0		P1,1	P1,1	P1,1	P2,3	P2,3	P2,3	P2,3	P2,3	P1,0	P1,0
1		P2,2	P2,2	P2,2	P2,2	P2,4	P2,4	P2,4	P2,4	P2,4	P2,2
2		P1,2	P1,2	P1,2	P1,2	P1,2	P1,2	P2,1	P2,1	P2,1	P2,1
3		P1,3	P1,3	P1,3	P1,3	P1,3	P1,3	P1,3	P1,3	P1,3	P1,3
4		--	P1,0	P1,0	P1,0	P1,0	P1,0	P1,0	P1,4	P1,4	P1,4
0		10	10	10	23	23	23	23	23	28	28
1		11	11	11	11	24	24	24	24	24	29
2		12	12	12	12	12	12	26	26	26	26
3		13	13	22	22	22	25	25	25	25	25
4		--	21	21	21	21	21	21	27	27	27

Counter of  
page in  
frame

Faults: 7 Replacements: 6

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  - LRU based on Counters
  - LRU based on stack**
  - LRU based in bit reference and 2nd opportunity.

	Inicio	P1,0	P1,3	P2,3	P2,4	P1,3	P2,1	P1,4	P1,0	P2,2
tiempo	20	21	22	23	24	25	26	27	28	29
0	P1,1	P1,1	P1,1	P2,3	P2,3	P2,3	P2,3	P2,3	P1,0	P1,0
1	P2,2	P2,2	P2,2	P2,2	P2,4	P2,4	P2,4	P2,4	P2,4	P2,2
2	P1,2	P1,2	P1,2	P1,2	P1,2	P1,2	P2,1	P2,1	P2,1	P2,1
3	P1,3	P1,3	P1,3	P1,3	P1,3	P1,3	P1,3	P1,3	P1,3	P1,3
4	--	P1,0	P1,0	P1,0	P1,0	P1,0	P1,0	P1,4	P1,4	P1,4
Stack	head	P1,3	P1,0	P1,3	P2,3	P2,4	P1,3	P2,1	P1,4	P1,0
		P1,2	P1,3	P1,0	P1,3	P2,3	P2,4	P1,3	P2,1	P1,4
		P2,2	P1,2	P1,2	P1,0	P1,3	P2,3	P2,4	P1,3	P2,1
		P1,1	P2,2	P2,2	P1,2	P1,0	P2,3	P2,4	P1,3	P2,1
	tail		P1,1	P1,1	P2,2	P1,2	P1,0	P2,3	P2,4	P1,3

Faults: 7 Replacements: 6

# Exercise S10-1.1

- In a **demand paging** system with **local replacement** policy, **5 frames** are allocated to all **processes**. Pages (and frames) have a size of **16K pages**. The initial state of the system and the page sequence generated by the CPU is detailed below.
- Obtain what pages are allocated on every frame when the next global scope algorithms are applied
  - LRU based on Counters
  - LRU based on stack
  - LRU based in bit reference and 2nd opportunity.**

	Inicio	P1,0	P1,3	P2,3	P2,4	P1,3	P2,1	P1,4	P1,0	P2,2
tiempo	20	21	22	23	24	25	26	27	28	29
0	P1,1	P1,1	P1,1	P2,3	P2,3	P2,3	P2,3	P2,3	P2,3	P2,2
1	P2,2	P2,2	P2,2	P2,2	P2,4	P2,4	P2,4	P2,4	P2,4	P2,4
2	P1,2	P1,2	P1,2	P1,2	P1,2	P1,2	P2,1	P2,1	P2,1	P2,1
3	P1,3	P1,3	P1,3	P1,3	P1,3	P1,3	P1,3	P1,3	P1,0	P1,0
4	--	P1,0	P1,0	P1,0	P1,0	P1,0	P1,0	P1,4	P1,4	P1,4
0	1	1	1	1	1	1	1	1	0	1
1	1	1	1	0	1	1	1	1	0	0
2	1	1	1	0	0	0	1	1	0	0
3	1	1	1	0	0	1	1	0	1	1
4	--	1	1	0	0	0	0	1	1	0

Reference bit of page in frame

1

Pointer to the page

Faults: 7 Replacements: 6

## • Comparative

LRU based on  
Counters

	Inicio	P1,0	P1,3	P2,3	P2,4	P1,3	P2,1	P1,4	P1,0	P2,2
tiempo	20	21	22	23	24	25	26	27	28	29
0	P1,1	P1,1	P1,1	P2,3	P2,3	P2,3	P2,3	P2,3	P1,0	P1,0
1	P2,2	P2,2	P2,2	P2,2	P2,4	P2,4	P2,4	P2,4	P2,4	P2,2
2	P1,2	P1,2	P1,2	P1,2	P1,2	P1,2	P2,1	P2,1	P2,1	P2,1
3	P1,3	P1,3	P1,3	P1,3	P1,3	P1,3	P1,3	P1,3	P1,3	P1,3
4	--	P1,0	P1,0	P1,0	P1,0	P1,0	P1,0	P1,4	P1,4	P1,4

LRU based on  
stack

	Inicio	P1,0	P1,3	P2,3	P2,4	P1,3	P2,1	P1,4	P1,0	P2,2
tiempo	20	21	22	23	24	25	26	27	28	29
0	P1,1	P1,1	P1,1	P2,3	P2,3	P2,3	P2,3	P2,3	P1,0	P1,0
1	P2,2	P2,2	P2,2	P2,2	P2,4	P2,4	P2,4	P2,4	P2,4	P2,2
2	P1,2	P1,2	P1,2	P1,2	P1,2	P1,2	P2,1	P2,1	P2,1	P2,1
3	P1,3	P1,3	P1,3	P1,3	P1,3	P1,3	P1,3	P1,3	P1,3	P1,3
4	--	P1,0	P1,0	P1,0	P1,0	P1,0	P1,0	P1,4	P1,4	P1,4

LRU based on  
reference bit and  
2nd opportunity

	Inicio	P1,0	P1,3	P2,3	P2,4	P1,3	P2,1	P1,4	P1,0	P2,2
tiempo	20	21	22	23	24	25	26	27	28	29
0	P1,1	P1,1	P1,1	P2,3	P2,3	P2,3	P2,3	P2,3	P2,3	P2,2
1	P2,2	P2,2	P2,2	P2,2	P2,4	P2,4	P2,4	P2,4	P2,4	P2,4
2	P1,2	P1,2	P1,2	P1,2	P1,2	P1,2	P2,1	P2,1	P2,1	P2,1
3	P1,3	P1,3	P1,3	P1,3	P1,3	P1,3	P1,3	P1,3	P1,0	P1,0
4	--	P1,0	P1,0	P1,0	P1,0	P1,0	P1,0	P1,4	P1,4	P1,4

- In a **demand paging** system with **local replacement** policy, **4 frames** are allocated to **every process**. The **maximum logical size** of a process is de **4K pages** (3 hexadecimal digits), page size is **64Kbyte**. Suppose that the following table contains all the information related to process P3 at a given time t.

Process P3 information at time t					
Frame (Hexadecimal)	Page (Hexadecimal)	Loading time	Last reference time	Reference bit	Modified bit
E7	B72	60	161	1	0
E8	B71	130	160	1	1
E9	B70	26	162	0	0
EA	B73	20	163	1	1

Then process P3 generates the logical address **B745A7C**. Obtain **the physical address** corresponding to this logical address supposing a replacement policy based on 2nd chance replacement algorithm.



- In a **demand paging** system with **local replacement** policy, **4 frames** are allocated to **every process**. The **maximum logical size** of a process is de **4K pages** (3 hexadecimal digits), page size is **64Kbyte**. Suppose that the following table contains all the information related to process P3 at a given time  $t=164$ .

Process P3 information at time t					
Frame (Hexadecimal)	Page (Hexadecimal)	Loading time	Last reference time	Reference bit	Modified bit
E7	B72	60	161	1	0
E8	B71	130	160	1	1
E9	B70	26	162	0	0
EA	B73	20	163	1	1

Then process P3 generates the logical address **B745A7C**. Obtain **the physical address** corresponding to this logical address supposing a replacement policy based on 2nd chance replacement algorithm.

**4K pages => 12 bits ; Page size 64K => 16 bits; L. address  $12 + 16 = 28$  bits.**

**0xB745A7C => Page: 0xB74 Offset: 0x5A7C**

27	26	25	24	23	22	21	20	19	18	17	16	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0

**0xB74**

**0x5A7C**

**Page B74 => page fault; Assuming that pointer => E7**

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Then process P3 generates the logical address **B745A7C**. Obtain the **physical address** corresponding to this logical address supposing a replacement policy based on 2nd chance replacement algorithm.

4K pages => 12 bits ; Page

27	26	25	24	23	22	21	20	19	18	17	16	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0

0xB745A7C => Page: 0xB74 Offset: 0x5A7C

Page B74 => page fault; Assuming that pointer => E7

Process P3 information at time t					
Frame (Hexadecimal)	Page (Hexadecimal)	Loading time	Last reference time	Reference bit	Modified bit
E7	B72	60	161	0	0
E8	B71	130	160	0	1
E9	B74	164	164	1	0
EA	B73	20	163	1	1

- Suppose a **virtual memory system** based on **demand paging**, where **logical addresses are 24 bit wide** and **page size is 1 KByte**. The system can handle up to **1MB of main memory**. The replacement algorithm used is **local 2<sup>nd</sup> opportunity**
  - a) Get the **physical and logical address formats** in this system, indicating the bit number and name of every field
  - b) Suppose that at time  $t = 0$  a user requests the execution of process A and the system allocates to it frames 0, 1, 2 and 3. The frames are initially empty and they are allocated in increasing order. Show the **evolution of the physical memory content and how many page faults** would generate the following sequence of logical addresses:

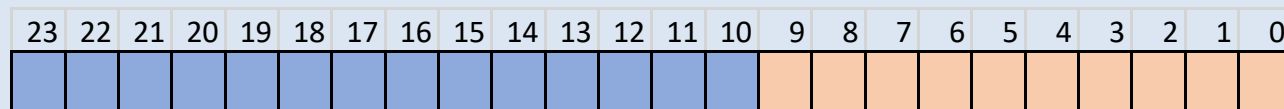
**1000, 3000, 5000, 6000, 7000, 2900, 4900, 900**

- Suppose a **virtual memory system** based on **demand paging**, where **logical addresses are 24 bit wide** and **page size is 1 KByte**. The system can handle up to **1MB of main memory**. The replacement algorithm used is **local 2<sup>nd</sup> opportunity**
  - Get the **physical and logical address formats** in this system, indicating the bit number and name of every field

Logical Address size: 24 bits

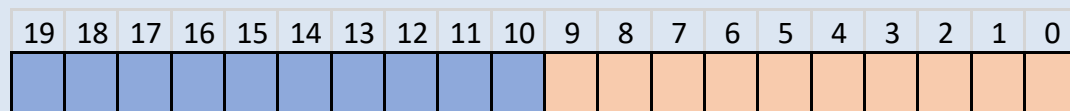
Page size = frame size: 1KB => 10 bits

Logical Address: 14 bits (page) + 10 bits (offset)



Main memory size: 1MB => 20 bits

Physical Address: 10 bits (frame) + 10 bits (offset)



- Suppose a **virtual memory system** based on **demand paging**, where **logical addresses are 24 bit wide** and **page size is 1 KByte**. The system can handle up to **1MB of main memory**. The replacement algorithm used is **local 2<sup>nd</sup> opportunity**

b) Suppose that at time  $t = 0$  a user requests the execution of process A and the system allocates to it frames 0, 1, 2 and 3. The frames are initially empty and they are allocated in increasing order. Show the **evolution of the physical memory content** and **how many page faults** would generate the following sequence of logical addresses:

Dec	1000	3000	5000	6000	7000	2900	4900	900
Hex	3E8	BB8	1388	1770	1B58	B54	1324	384
<b>Page</b>	<b>0</b>	<b>2</b>	<b>4</b>	<b>5</b>	<b>6</b>	<b>2</b>	<b>4</b>	<b>0</b>
offset	1000	952	904	880	856	852	804	900

t	0	1	2	3	4	5	6	7
<b>Page</b>	<b>0</b>	<b>2</b>	<b>4</b>	<b>5</b>	<b>6</b>	<b>2</b>	<b>4</b>	<b>0</b>
0	0	0	0	0	6	6	6	6
1		2	2	2	2	2	2	2
2			4	4	4	4	4	4
3				5	5	5	5	0
0	1	1	1	1	1	1	1	1
1		1	1	1	0	1	1	0
2			1	1	0	0	1	0
3				1	0	0	0	1

- Exercise S10-1: 2nd chance replacement algorithm
  - Exercise S10-1.1: 2nd chance basic
  - Exercise S10-1.2: 2nd chance complete
- **Exercise S10-2: Working set**
  - Exercise S10-2.1: Getting the working set

- In a virtual memory system has been decided to use a **working set model** to control physical memory allocation. There are **3 processes A, B y C** in execution. Every memory access is encoded in two characters that represent the process and the page accessed, respectively.
  - a) Supposing that the **working set window size ( $\Delta$ ) is 4**, obtain the **working set for every process** at the instant when the last reference happens in the following reference string:  
**A0,B2,C3,A0,A1,A5,B2,C4,C2,A2,B1,B3,C0,A1  
C1,B0,A1,C0,B1,B2,C4,A0,B3,B3, C3,A1,C4**
  - b) Considering that the system has **6 frames**, are they enough to allocate the working sets of all processes till the end?

- In a virtual memory system has been decided to use a **working set model** to control physical memory allocation. There are **3 processes A, B y C** in execution. Every memory access is encoded in two characters that represent the process and the page accessed, respectively.

- Supposing that the **working set window size ( $\Delta$ )** is **4**, obtain the **working set for every process** at the instant when the last reference happens in the following reference string:

**A0,B2,C3,A0,A1,A5,B2,C4,C2,A2,B1,B3,C0,A1**

**C1,B0,A1,C0,B1,B2,C4,A0,B3,B3, C3,A1,C4**

	A0	B2	C3	A0	A1	A5	B2	C4	C2	A2	B1	B3	C0	A1	C1	B0	A1	C0	B1	B2	C4	A0	B3	B3	C3	A1	C4	
	A	A0			A0	A1	A5				A2				A1			A1					A0				A1	
	A						{0,1,5}				{0,1,2,5}				{1,2,5}			{1,2,5}					{0,1,2}				{0, 1}	
	B		B2					B2				B1	B3				B0			B1	B2			B3	B3			
	B												{1,2,3}				{0,1,2,3}			{0,1,2,3}	{0,1,2,3}			{0,1,2,3}	{1,2,3}			
	C			C3					C4	C2				C0		C1			C0			C4				C3		C4
	C												{0,2,3,4}		{0,1,2,4}			{0,1,2}			{0,1,4}				{0,1,3,4}		{0,3,4}	



- Fundamentos de los Sistemas Operativos

- The sum of all WSSs is always higher than 6.

# Fundamentos de los Sistemas Operativos (FSO)

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## Consolidation Exercises 3

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A disk partition has a size of 8 Gbytes being formatted with a MINIX file system. The file system has been configured with the following parameters:

- 1 block = 2 KByte
- 1 zone = 1 blocks
- i-node size = 64 bytes with pointers of 32 bits (7 direct, 1 indirect and 1 double indirect)
- 32 bit directory entry
- 16384 i-nodes

The file system structure is :

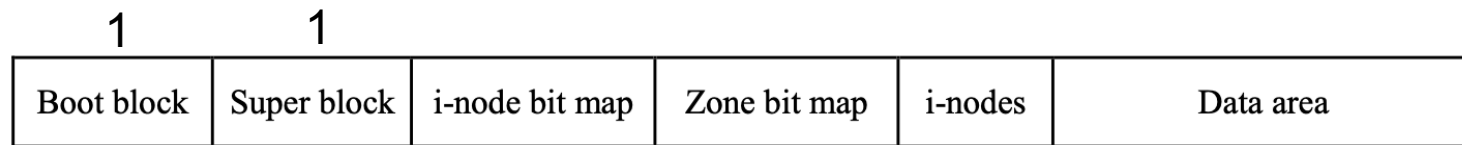
Boot block	Super block	i-node bit map	Zone bit map	i-nodes	Data area
------------	-------------	----------------	--------------	---------	-----------

a) Define the sizes of the different file system components

A disk partition has a size of 8 Gbytes being formatted with a MINIX file system. The file system has been configured with the following parameters:

- 1 block = 2 KByte
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- i-node size = 64 bytes with pointers of 32 bits (7 direct, 1 indirect and 1 double indirect)
- 32 bit directory entry
- 16384 i-nodes

The file system structure is :



a) Define the sizes of the different file system components

i-node bit map: Number of nodes: 16384      16384 bits are needed

In 1 block how many bits are?

1 block => 2 Kbytes =>  $2 * 1024 * 8 \text{ bits} = 16384 \text{ bits}$

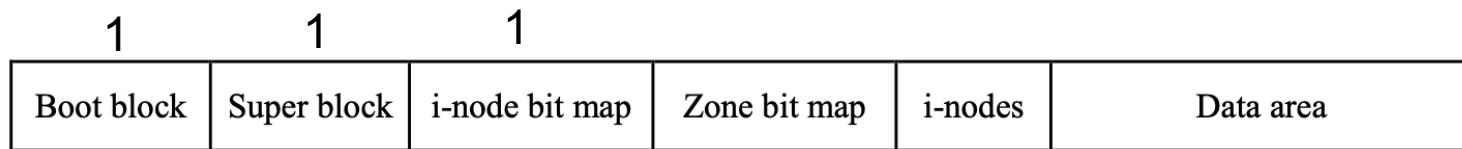
1 block is sufficient for the i-node bit map

$$\text{ceiling}(16384 / (2 * 1024 * 8)) = 1$$

A disk partition has a size of 8 Gbytes being formatted with a MINIX file system. The file system has been configured with the following parameters:

- 1 block = 2 KByte
- 1 zone = 1 blocks
- i-node size = 64 bytes with pointers of 32 bits (7 direct, 1 indirect and 1 double indirect)
- 32 bit directory entry
- 16384 i-nodes

The file system structure is :



a) Define the sizes of the different file system components

i-nodes      Number of nodes: 16384      16384 \* 64 bytes are needed

In 1 block how many i-nodes can be allocated?

1 block => 2 Kbytes => ceiling (2 \* 1024 / 64) = 32 i-nodes

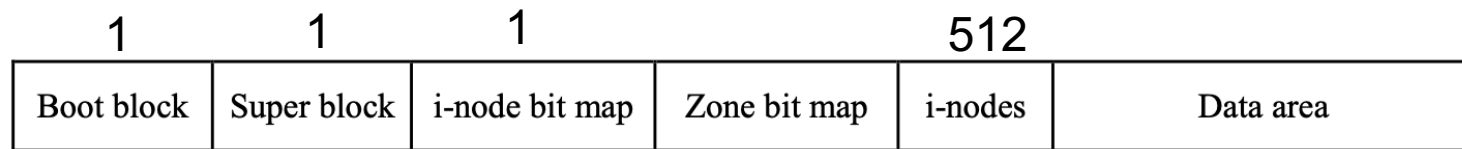
So, we need to allocate 16384 i-nodes considering that in each block 32 i-nodes can be allocated

**ceiling (16384 / 32) = 512 blocks**

A disk partition has a size of 8 Gbytes being formatted with a MINIX file system. The file system has been configured with the following parameters:

- 1 block = 2 KByte
- 1 zone = 1 block
- i-node size = 64 bytes with pointers of 32 bits (7 direct, 1 indirect and 1 double indirect)
- 32 bit directory entry
- 16384 i-nodes

The file system structure is :



a) Define the sizes of the different file system components

How many block are in the file system?

The device has 8GB  $\Rightarrow$  ceiling (8GB / 2KB) = 4 \* 1024 \* 1024 Blocks

How many zone bitmap blocks are needed?

ceiling (n. zones / bits per area) = ceiling (4 \* 1024 \* 1024 / 2 \* 1024 \* 8) =  
256 blocks

# Exercise 3.1

A disk partition has a size of 8 Gbytes being formatted with a MINIX file system. The file system has been configured with the following parameters:

- 1 block = 2 KByte
- 1 zone = 1 block
- i-node size = 64 bytes with pointers of 32 bits (7 direct, 1 indirect and 1 double indirect)
- 32 bit directory entry
- 16384 i-nodes

The file system structure is :

1	1	1	256	512	4.193.533
Boot block	Super block	i-node bit map	Zone bit map	i-nodes	Data area

a) Define the sizes of the different file system components

**Total blocks :**  $4 * 1024 * 1024$  Blocks = 4.194.304

**Data area:**  $= 4.194.304 - (1 + 1 + 1 + 256 + 512) = 4.193.533$  blocks

A disk partition has a size of 8 Gbytes being formatted with a MINIX file system. The file system has been configured with the following parameters:

- 1 block = 2 KByte
- 1 zone = 1 block
- i-node size = 64 bytes with pointers of 32 bits (7 direct, 1 indirect and 1 double indirect)
- 32 bit directory entry
- 16384 i-nodes

b) The root directory contains:

- 12 subdirectories (5 empty directories and 2 with 1 regular file of 9KB)
- 5 regular files (size < 1KB)
- 10 regular files (4KB < size < 6KB)
- 2 regular files (size = 20K)
- 1 regular file (size = 1MB)

How many i-nodes are used and how many blocks are occupied.

	i-node	entries	dir areas	pointer block	total areas
root		1 1+1+12+5+10=29	ceiling(29/32) = 1		1
5 empty directories		5 1+1 = 2		1	5
5 reg files (< 1K)	5			1	5
10 reg files [4,6}	10		ceiling(6K /2K) = 3		30
2 reg files [20K}	2		ceiling(20K /2K) =10	1	22
1 reg file (1MB)	1		ceiling(1M/2K) = 512	1	513
2 non empty dirs		2 1+1+1 = 3		1	2
1 regular files	2		ceiling(9K/2K) = 5		10
	28				588



A system has 512 MB of logical addressing space, with 4 KB page size and with 64 MB of physical memory.

- a) If memory is managed by paging, with a maximum number of 4 pages per process, the following translation between logical and physical addresses has been done along the execution of process A.

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Fill the page table of process A

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Logical address	27C9	1C	36E2	1C50
Physical address	1C27C9	1901C	16E2	6C50

	2   7C9	0   01C	3   6E2	1   C50
	1c2   7C9	19   01C	1   6E2	6   C50

	hex	dec	validity
0	19	25	1
1	6	6	1
2	1C2	450	1
3	1	1	1

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b) Describe the logical address format if **segmentation with paging** is applied with a maximum of 32 segments per process.

512 MB =  $2^{29}$  B  $\Rightarrow$  29 bits

32 segments =  $2^5$  segments.  $\Rightarrow$  5 bits

Offset 4KB =  $2^{12}$  Bytes.  $\Rightarrow$  12 bits

**Logical address 29 bits = 5 (segment) + [12 (page) + 12 (offset)]**

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c) In the previous **segmentation with paging** model, and considering the following page table of segment 1 for a given process, obtain the logical addresses that correspond to physical addresses 8220 and 25096 in that process.

Segment 1			
page	frame	Valid	
0	4	1	
1	5	1	
2	6	1	
3	2	1	

8220	25096
201C	6208

8220 => 0x201C => 2 | 01C. Frame 2 allocates page 3 of segment 1  
 Logical address S1, 3 | 01C = S1, 3 \* 4096 + 28 = S1, 12316

25096 => 0x6208 => 6 | 208. Frame 6 allocates page 2 of segment 1  
 Logical address S1, 2 | 208 = S1, 2 \* 4096 + 520 = S1, 8712