CS 5/7320 Artificial Intelligence

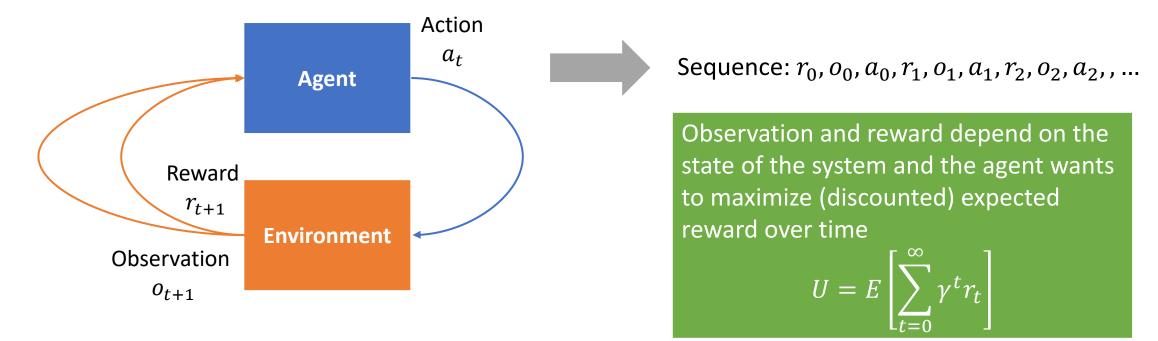
Reinforcement Learning AIMA Chapter 17&21

Slides by Michael Hahsler with figures from the AIMA textbook.



Chapter 17. Sequential Decision Problems

- **Utility-based agent**: The agent's utility depends on a sequence of decisions.
- Sequential decision problems incorporate utilities, uncertainty, and sensing.



Markov Decision Process (MDP)

- Fully observable environment: The agent's observation is the state $o_t = s_t$.
- A MDP defines a sequential decision problem with
 - a finite set of states S (initial state S_0)
 - a set actions ACTIONS(s) in each state s of actions
 - a transition model P(s' | s, a) where $a \in ACTIONS(s)$
 - a reward function R(s)
- The goal is to find an **optimal policy** π^* that prescribes for each state the optimal action $\pi(s)$ to maximize the expected utility over time.

Example: 4x3 Grid World

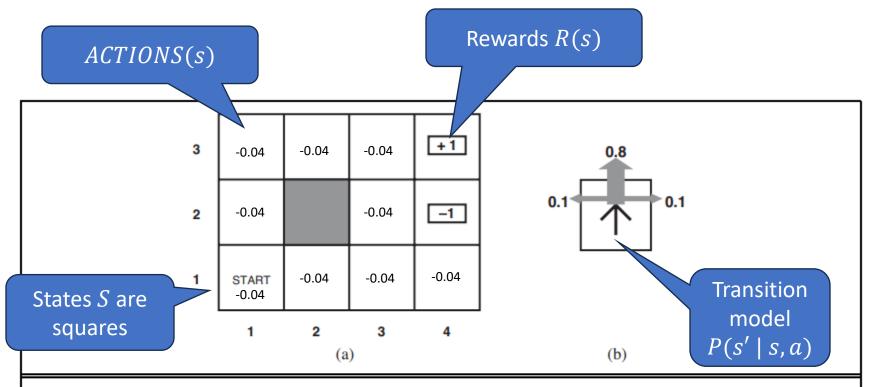
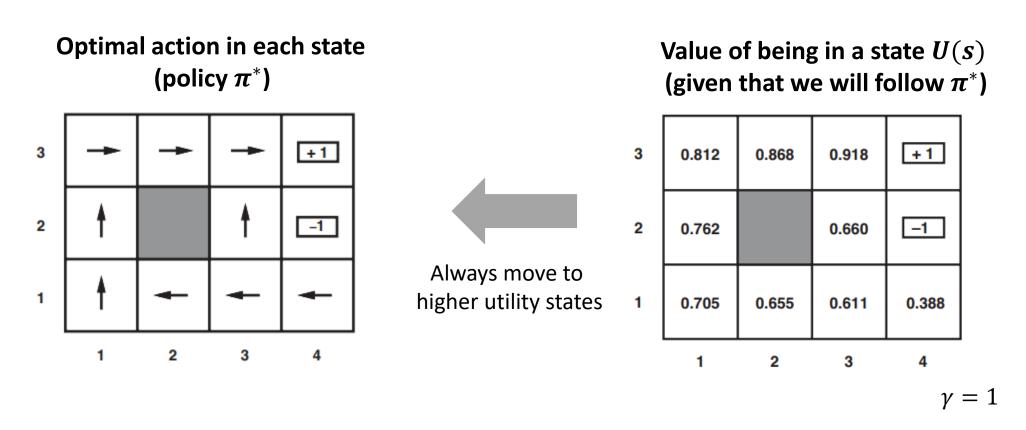


Figure 17.1 (a) A simple 4×3 environment that presents the agent with a sequential decision problem. (b) Illustration of the transition model of the environment: the "intended" outcome occurs with probability 0.8, but with probability 0.2 the agent moves at right angles to the intended direction. A collision with a wall results in no movement. The two terminal states have reward +1 and -1, respectively, and all other states have a reward of -0.04.

Goal: What direction should we go in each square?

 $\pi(s)$

Solution: 4x3 Grid World



Question: How to we find the optimal value function/optimal policy?

Value Iteration

```
function VALUE-ITERATION(mdp, \epsilon) returns a utility function
 inputs: mdp, an MDP with states S, actions A(s), transition model P(s' \mid s, a),
              rewards R(s), discount \gamma
          \epsilon, the maximum error allowed in the utility of any state
 local variables: U, U', vectors of utilities for states in S, initially zero
                     \delta, the maximum change in the utility of any state in an iteration
 repeat
     U \leftarrow U'; \delta \leftarrow 0
                                                                                          Bellman update
     for each state s in S do
         U'[s] \leftarrow R(s) + \gamma \max_{a \in A(s)} \sum_{s'} P(s' \mid s, a) \ U[s']
         if |U'[s] - U[s]| > \delta then \delta \leftarrow |U'[s] - U[s]|
 until \delta < \epsilon(1-\gamma)/\gamma
 return U
                                                                                        U converges to U^{\pi^*}
```

Policy Iteration

```
function POLICY-ITERATION(mdp) returns a policy
 inputs: mdp, an MDP with states S, actions A(s), transition model P(s' \mid s, a)
 local variables: U, a vector of utilities for states in S, initially zero
                      \pi, a policy vector indexed by state, initially random
repeat
                                                                         Calculate U given current policy
      U \leftarrow \text{POLICY-EVALUATION}(\pi, U, mdp)
                                                                         (eighter solve an LP or iterative solution)
      unchanged? \leftarrow true
     for each state s in S do
          \inf_{a \in A(s)} \max_{s'} \sum_{s'} P(s' \mid s, a) \ U[s'] > \sum_{s'} P(s' \mid s, \pi[s]) \ U[s'] \text{ then do} \pi[s] \leftarrow \operatorname*{argmax}_{a \in A(s)} \sum_{s'} P(s' \mid s, a) \ U[s']
                                                                                                          Policy
                                                                                                          Improvement
               unchanged? \leftarrow false
 until unchanged?
                                                                                              U converges to U^{\pi^*}
 return \pi
                                                                                            and \pi converges to \pi^*
```

Partially Observable Markov Decision Model (POMDP)

- If the environment is partially observable then the model is expanded by
 - a sensor model $P(o \mid s)$ for receiving observation o given being in state s.
- This makes things a lot more complicated and we have to work with **belief states**. A belief state is a distribution over states. Example: For a problem with three states, the belief state b=<.2,.8,0> means the agent beliefs that is 20% in state 1 and 80% in state 2.
- This leads to a belief MDP that has an infinite number of states (the belief states).
- The solution of a POMDP is a policy with the optimal action for a set of belief states.
- For all but tiny problems, POMDPs can only be solved approximately.

Chapter 21: Reinforcement Learning

The basis of reinforcement learning are MDPs.

- What if we do not have a transition model $P(s' \mid s, a)$?
- Now we cannot solve the MDP (estimate the state utility function/policy) because we cannot predict future states!

 The agent needs to explore (try actions) and use the reward signal to update its belief about the utility of states and actions (i.e., this is also called learning or estimation)

Q-Learning

- Q-Learning learns the state-action utility function Q(s, a).
- Relationship with the state utility function:

$$U(s) = \max_{a} Q(s, a) .$$

```
function Q-LEARNING-AGENT(percept) returns an action inputs: percept, a percept indicating the current state s' and reward signal r' persistent: Q, a table of action values indexed by state and action, initially zero N_{sa}, a table of frequencies for state—action pairs, initially zero s, a, r, the previous state, action, and reward, initially null
```

if TERMINAL?(s) **then** $Q[s, None] \leftarrow r'$ Make Q[s, a] a little more similar to the received reward + the best Q-value of the successor state.

increment $N_{sa}[s, a]$

return a

$$Q[s, a] \leftarrow Q[s, a] + \alpha(N_{sa}[s, a])(r + \gamma \max_{a'} Q[s', a'] - Q[s, a])$$

$$s, a, r \leftarrow s', \operatorname{argmax}_{a'} f(Q[s', a'], N_{sa}[s', a']), r'$$

f is the exploration function and decides on the next action. As N increases it can exploit good actions more.

Summary

- Agents can learn the value of being in a state from reward signals.
- Rewards can be delayed (e.g., at the end of a game).
- Not being able to fully observe the state makes the problem more difficult (POMDP).
- Unknown transition models lead to the need of exploration by trying actions (model free methods like Q-Learning).
- All these problems are computationally very expensive and often can only be solved approximately.
- All functions (U, Q, etc.) can be approximated with (deep) artificial neural networks.