


# **V. CLASSIFICATION WITH K-NEAREST NEIGHBORS**

	continuous	categorical
supervised	regression	
classification		
unsupervised	reduction dimension	clustering

	continuous	categorical
supervised	regression	
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150  
observations  
( $n = 150$ )

Fisher's *Iris* Data

Sepal length ⇅	Sepal width ⇅	Petal length ⇅	Petal width ⇅	Species ⇅
5.1	3.5	1.4	0.2	<i>I. setosa</i>
4.9	3.0	1.4	0.2	<i>I. setosa</i>
4.7	3.2	1.3	0.2	<i>I. setosa</i>
4.6	3.1	1.5	0.2	<i>I. setosa</i>
5.0	3.6	1.4	0.2	<i>I. setosa</i>
5.4	3.9	1.7	0.4	<i>I. setosa</i>
4.6	3.4	1.4	0.3	<i>I. setosa</i>
5.0	3.4	1.5	0.2	<i>I. setosa</i>



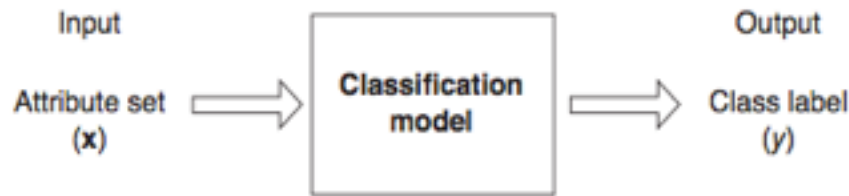
response



4 predictors ( $p = 4$ )

Q: How does a classification problem work?

A: Data in, predicted labels out.

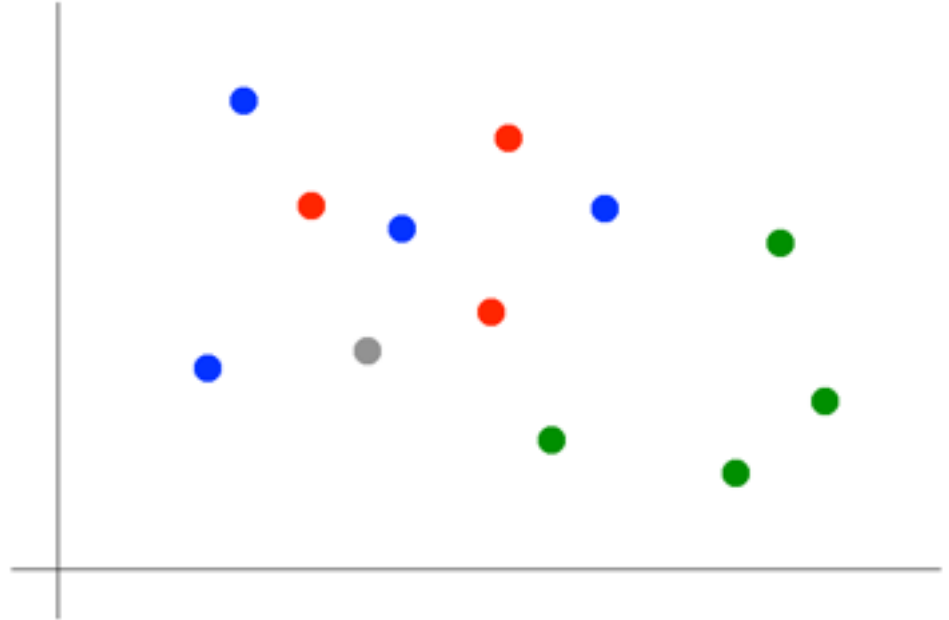


**Figure 4.2.** Classification as the task of mapping an input attribute set  $x$  into its class label  $y$ .

Suppose we want to predict the color of the gray dot.

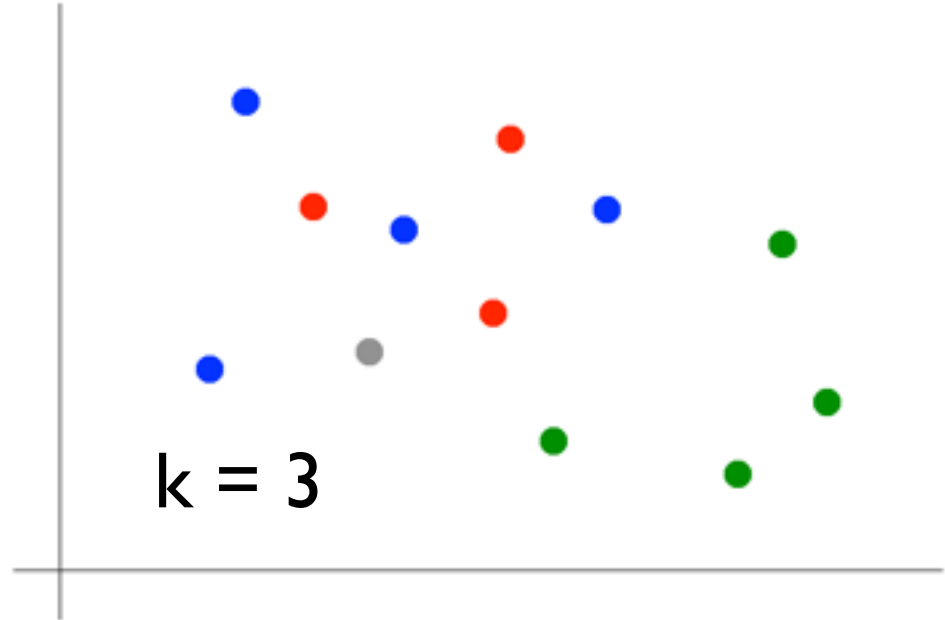
**QUESTION:**

What are the predictors?  
What is the response?



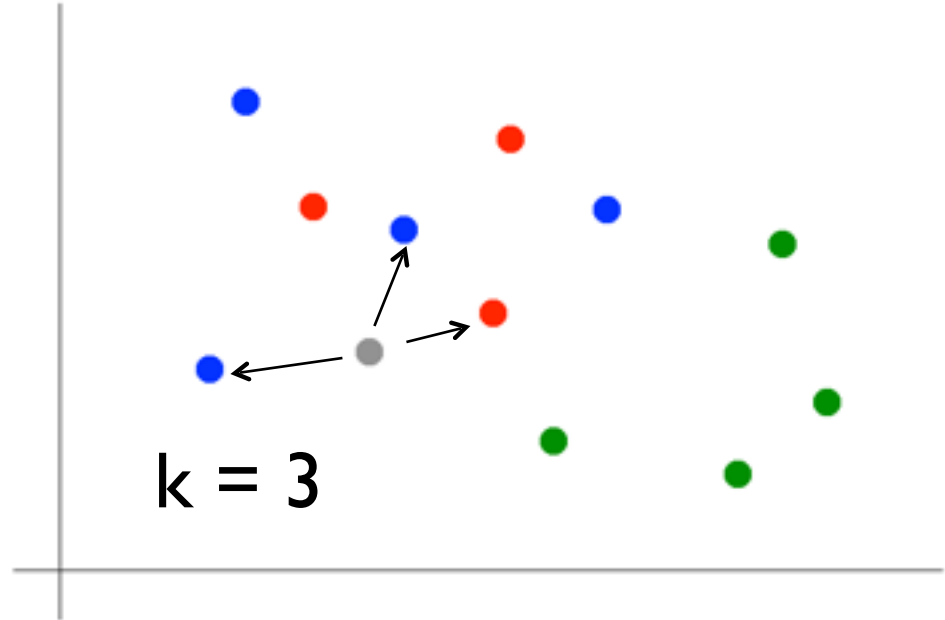
Suppose we want to predict the color of the gray dot.

1) Pick a value for  $k$ .



Suppose we want to predict the color of the gray dot.

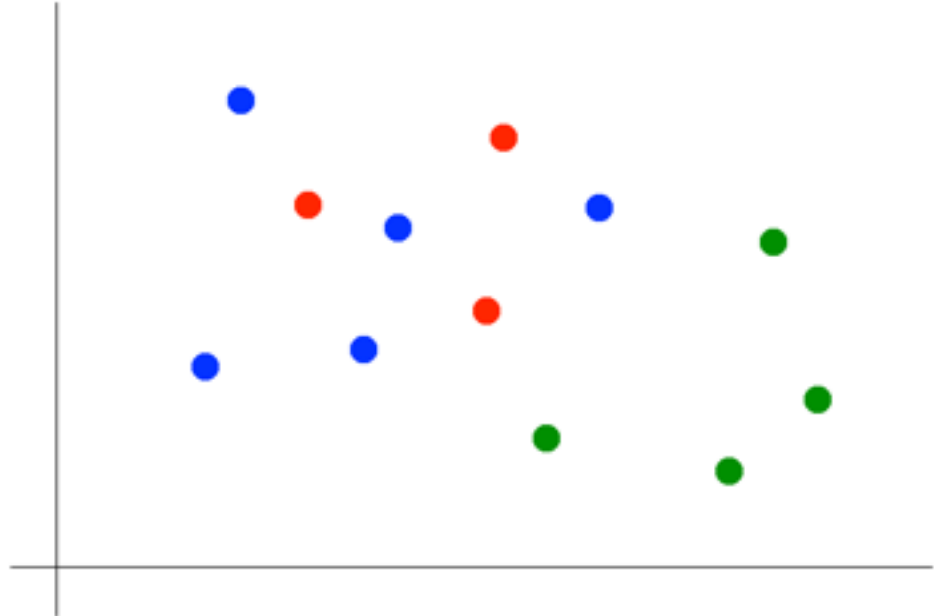
- 1) Pick a value for  $k$ .
- 2) Find colors of  $k$  nearest neighbors.





Suppose we want to predict the color of the gray dot.

- 1) Pick a value for  $k$ .
- 2) Find colors of  $k$  nearest neighbors.
- 3) Assign the most common color to the gray dot.

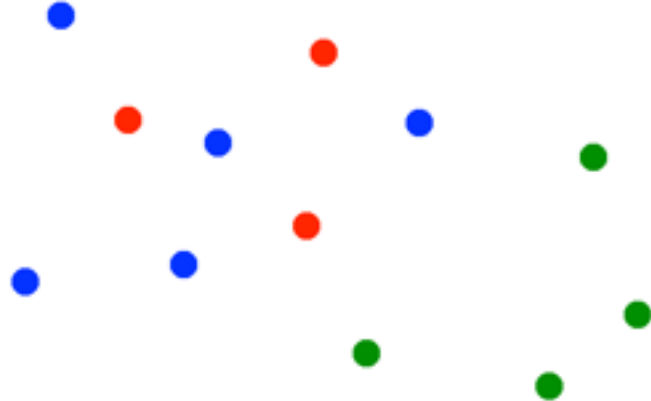


Suppose we want to predict the color of the gray dot.

- 1) Pick a value for  $k$ .
- 2) Find colors of  $k$  nearest neighbors.
- 3) Assign the most common color to the gray dot.

NOTE:

Our definition of "nearest" implicitly uses the *Euclidean distance function*.



### Advantages of KNN:

- Simple to understand and explain
- Model training phase is fast
- Non-parametric (does not presume a “form” of the “decision boundary”)

### Disadvantages of KNN:

- Prediction phase can be slow when  $n$  is large
- Sensitive to irrelevant features

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# DATA SCIENCE

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