7. Water is slightly soluble in liquid nitrogen. At -196°C (the boiling point of liquid nitrogen), the mole fraction of water in a saturated solution is  $1.00 \times 10^{-5}$ . Compute the mass of water that can dissolve in 1.00 kg of boiling liquid nitrogen.

Water is the solute, and liquid nitrogen is the solvent, but the definition of mole fraction works the same. Use it to write the equation

$$X_{\rm H_2O} = 1.00 \times 10^{-5} = \frac{n_{\rm H_2O}}{n_{\rm N_2} + n_{\rm H_2O}} = \frac{n_{\rm H_2O}}{35.6972 + n_{\rm H_2O}}$$

where 35.6972 is the number of moles of  $N_2$  in 1.00 kg of  $N_2$  (non-significant figures are carried along deliberately). Solving the equation for  $n_{\rm H_2O}$  is simplified by noting that  $n_{\rm H_2O}$  can be neglected in the denominator. Thus, the 1.00 kg of  $N_2(l)$  contains 3.5697  $\times$  10<sup>-4</sup> mol of dissolved H<sub>2</sub>O. This amounts to 0.00643 g of H<sub>2</sub>O.

- **10**. A perchloric acid solution is 60.0% HClO<sub>4</sub> by mass. It is simultaneously 9.20 M at 25°C.
  - (a) Compute the density of this solution.
  - (b) What volume of this solution should be used in mixing 1.00 L of a 1.00 M perchloric acid solution?
- a) Consider a 1 kg sample of the perchloric acid solution. It contains 600 g of HClO<sub>4</sub>. Dividing 600 g by 100.46 g mol<sup>-1</sup>, the molar mass of HClO<sub>4</sub>, establishes that the solution contains 5.973 mol HClO<sub>4</sub> per kg. It simultaneously contains 9.20 mol of HClO<sub>4</sub> per liter (its molarity). Dividing the second of these two measures of composition by the first gives a density. To do the division, invert the divisor and multiply

$$\rho = \left(\frac{9.20 \text{ mol HClO}_4}{1 \text{ L solution}}\right) \times \left(\frac{1 \text{ kg solution}}{5.973 \text{ mol HClO}_4}\right) = 1.54 \text{ kg L}^{-1} = 1.54 \text{ g mL}^{-1}$$

- b) To prepare 1.00 L of a solution that contains 1.00 mol of the solute requires 1.00 mol of the HClO<sub>4</sub>. The 9.20 M solution is quite concentrated: 1000 mL of it supplies 9.20 mol of HClO<sub>4</sub>. It follows that 1000/9.20 = 108.7 mL of solution supplies 1.00 mol of solute.
- **14.** Rewrite the following balanced equations as net ionic equations.

(a) 
$$Na_2SO_4(aq) + BaCl_2(aq) \longrightarrow BaSO_4(s) + 2 NaCl(aq)$$

(b) 
$$6 \text{ NaOH}(aq) + 3 \text{ Cl}_2(g) \longrightarrow$$

$$NaClO_3(aq) + 5 NaCl(aq) + 3 H_2O(\ell)$$

(c) 
$$Hg_2(NO_3)_2(aq) + 2 KI(aq) \longrightarrow Hg_2I_2(s) + 2 KNO_3(aq)$$

(d) 
$$3 \text{ NaOCl}(aq) + \text{KI}(aq) \longrightarrow$$

$$NaIO_3(aq) + 2 NaCl(aq) + KCl(aq)$$

Net ionic equations omit all ions not specifically reacting:

a) 
$$Ba^{2+}(aq) + SO_4^{2-}(aq) \to BaSO_4(s)$$

**b)** 
$$3 \operatorname{Cl}_2(g) + 6 \operatorname{OH}^-(aq) \to \operatorname{ClO}_3^-(aq) + 5 \operatorname{Cl}^-(aq) + 3 \operatorname{H}_2 \operatorname{O}(l)$$

c) 
$$\operatorname{Hg}_{2}^{2+}(aq) + 2\operatorname{I}^{-}(aq) \to \operatorname{Hg}_{2}\operatorname{I}_{2}(s)$$

d) 
$$3 \text{ OCl}^-(aq) + \text{I}^-(aq) \rightarrow \text{IO}_3^-(aq) + 3 \text{ Cl}^-(aq)$$

- **24.** Phosphorus pentachloride reacts violently with water to give a mixture of phosphoric acid and hydrochloric acid.
  - (a) Write a balanced chemical equation for this reaction.
  - (b) Determine the concentration (in moles per liter) of each of the acids that result from the complete reaction of 1.22 L of phosphorus pentachloride (measured at 215°C and 0.962 atm pressure) with enough water to give a solution volume of 697 mL.

a) 
$$PCl_5 + 4H_2O \rightarrow H_3PO_4 + 5HCl.$$

b)

$$\begin{split} n_{\rm PCl_5} &= \frac{PV}{RT} = \frac{(0.962~{\rm atm})~(1.22~{\rm L})}{(0.08206~{\rm L}~{\rm atm}~{\rm mol}^{-1}{\rm K}^{-1})~(215 + 273.15)~{\rm K}} = 0.0293~{\rm mol}~{\rm PCl_5} \\ n_{\rm HCl} &= 0.0293~{\rm mol}~{\rm PCl_5} \times \frac{5~{\rm mol}~{\rm HCl}}{1~{\rm mol}~{\rm PCl_5}} = 0.1465~{\rm mol}~{\rm HCl} = 0.146~{\rm mol}~{\rm HCl} \\ n_{\rm H_3PO_4} &= 0.0293~{\rm mol}~{\rm PCl_5} \times \frac{1~{\rm mol}~{\rm H_3PO_4}}{1~{\rm mol}~{\rm PCl_5}} = 0.0293~{\rm mol}~{\rm H_3PO_4} \end{split}$$

Both acids are collected in enough water so that the final volume of the solution is 697 mL

$$c_{\text{HCI}} = \frac{0.1465 \text{ mol}}{0.697 \text{ L}} = 0.210 \text{ mol L}^{-1}$$
  $c_{\text{H}_3 \text{PO}_4} = \frac{0.0293 \text{ mol}}{0.697 \text{ L}} = 0.0420 \text{ mol L}^{-1}$ 

- **34.** Complete and balance the following equations for reactions taking place in basic solution.
  - (a)  $OCl^{-}(aq) + I^{-}(aq) \longrightarrow IO_{3}^{-}(aq) + Cl^{-}(aq)$
  - (b)  $SO_3^{2-}(aq) + Be(s) \longrightarrow S_2O_3^{2-}(aq) + Be_2O_3^{2-}(aq)$
  - (c)  $H_2BO_3^-(aq) + Al(s) \longrightarrow BH_4^-(aq) + H_2AlO_3^-(aq)$
  - (d)  $O_2(g) + Sb(s) \longrightarrow H_2O_2(aq) + SbO_2^-(aq)$
  - (e)  $\operatorname{Sn}(OH)_6^{2-}(aq) + \operatorname{Si}(s) \longrightarrow \operatorname{HSnO}_2^{-}(aq) + \operatorname{SiO}_3^{2-}(aq)$

In basic solution, OH<sup>-</sup> and H<sub>2</sub>O may take part either as reactants or as products.

a) 
$$3 \text{ OCl}^-(aq) + \text{I}^-(aq) \to \text{IO}_3^-(aq) + 3 \text{ Cl}^-(aq)$$

**b)** 
$$2 \operatorname{SO}_3^{2-}(aq) + 2 \operatorname{Be}(s) \to \operatorname{S}_2 \operatorname{O}_3^{2-}(aq) + \operatorname{Be}_2 \operatorname{O}_3^{2-}(aq)$$

c) 
$$3 H_2 BO_3^-(aq) + 8 Al(s) + 8 OH^-(aq) + 7 H_2 O(l) \rightarrow 3 BH_4^-(aq) + 8 H_2 AlO_3^-(aq)$$

d) 
$$3O_2(g)+2Sb(s)+2OH^{-}(aq)+2H_2O(1)\rightarrow 3H_2O_2(aq)+2SbO_2^{-}(aq)$$
   
或  $2O_2(g)+2Sb(s)+2OH^{-}(aq)\rightarrow H_2O_2(aq)+2SbO_2^{-}(aq)$    
…

e) 
$$2 \operatorname{Sn}(OH)_{6}^{2-}(aq) + \operatorname{Si}(s) \to 2 \operatorname{HSnO}_{2}^{-}(aq) + \operatorname{SiO}_{3}^{2-}(aq) + 5 \operatorname{H}_{2}O(l)$$

- **64.** At 300 K, the vapor pressure of pure benzene ( $C_6H_6$ ) is 0.1355 atm and the vapor pressure of pure *n*-hexane ( $C_6H_{14}$ ) is 0.2128 atm. Mixing 50.0 g of benzene with 50.0 g of *n*-hexane gives a solution that is nearly ideal.
  - (a) Calculate the mole fraction of benzene in the solution.
  - **(b)** Calculate the total vapor pressure of the solution at 300 K.
  - (c) Calculate the mole fraction of benzene in the vapor in equilibrium with the solution.
- a) The chemical amount of benzene ( $\mathcal{M}=78.11~\mathrm{g~mol^{-1}}$ ) in 50.0 g is 0.640 mol. The chemical amount of *n*-hexane ( $\mathcal{M}=86.18~\mathrm{g~mol^{-1}}$ ) is 0.580 mol. The mole fraction of benzene in the solution is

$$X_{\text{benzene}} = \frac{0.640 \text{ mol}}{(0.640 + 0.580) \text{ mol}} = 0.525$$

b) The total vapor pressure above the solution is

$$P_{\text{tot}} = P_{\text{benzene}} + P_{\text{hexane}}$$
  
=  $X_{\text{benzene}} P_{\text{benzene}}^{\circ} + X_{\text{hexane}} P_{\text{hexane}}^{\circ}$   
=  $0.525(0.1355 \text{ atm}) + (1 - 0.525)(0.2128 \text{ atm}) = 0.172 \text{ atm}$ 

- c)  $X_{\text{benzene}}$  (vapor) = 0.525(0.1355 atm)/0.172 atm = 0.414.
- 78. Ethylene glycol ( $CH_2OHCH_2OH$ ) is used in antifreeze because, when mixed with water, it lowers the freezing point below 0°C. What mass percentage of ethylene glycol in water must be used to reduce the freezing point of the mixture to -5.0°C, assuming ideal solution behavior?

The molality of the required antifreeze solution of ethylene glycol is

$$m = -\frac{\Delta T}{K_{\rm f}} = -\frac{(-5.0)}{1.86} = 2.69 \text{ mol kg}^{-1}$$

Such a solution has 2.69 mol of  $CH_2OHCH_2OH$  ( $\mathcal{M}=62.07~g$  mol<sup>-1</sup>) dissolved in 1000 g of water. This chemical amount of ethylene glycol equals 167 g. There is thus 167 g of ethylene glycol for every 1167 g of solution. The percentage by mass of the ethylene glycol in the solution is  $167/1167 \times 100\% = 14.3\%$ . Note the assumption that ethylene glycol neither dissociates into two or more particles nor associates in aqueous solution (in addition to the assumption of ideal solution behavior).

- **11.** Using the law of mass action, write the equilibrium expression for each of the following reactions.
  - (a)  $Zn(s) + 2 Ag^{+}(aq) \iff Zn^{2+}(aq) + 2 Ag(s)$
  - (b)  $VO_4^{3-}(aq) + H_2O(\ell) \iff VO_3(OH)^{2-}(aq) + OH^{-}(aq)$
  - (c)  $2 \text{ As}(OH)_6^{3-}(aq) + 6 \text{ CO}_2(g) \iff \text{As}_2O_3(s) + 6 \text{ HCO}_3^{-}(aq) + 3 \text{ H}_2O(\ell)$

Pure solids and liquids are omitted from the expressions because their activities equal 1.

a) 
$$\frac{a_{\mathrm{Zn^{2+}}}}{a_{\mathrm{Ag^{+}}}^{2}} = K$$
 b)  $\frac{a_{\mathrm{VO_3(OH)^{2-}}} a_{\mathrm{OH^{-}}}}{a_{\mathrm{VO_3^{3-}}}} = K$  c)  $\frac{(a_{\mathrm{HCO_3^{-}}})^6}{(a_{\mathrm{As(OH)_6^{3-}}})^2 (a_{\mathrm{CO_2}})^6} = K$ 

In all three parts, the concentrations of the solutes divided by the standard state concentration(1 M) approximates the activity of the solute. Also, the partial pressures of the gases divided by the standard-state press (1atm) approximate the activity of the gas. This allows rewriting the answers as

$$\mathbf{a}) \quad \frac{[\mathrm{Zn^{2+}}]}{\left[\mathrm{Ag^{+}}\right]^{2}} = K \qquad \mathbf{b}) \quad \frac{[\mathrm{VO_{3}}(\mathrm{OH})^{2-}][\mathrm{OH^{-}}]}{[\mathrm{VO_{4}^{3-}}]} = K \qquad \mathbf{c}) \quad \frac{[\mathrm{HCO_{3}^{-}}]^{6}}{[\mathrm{As}(\mathrm{OH})_{6}^{3-}]^{2}P_{\mathrm{CO_{2}}}^{6}} = K$$

27. The dehydrogenation of benzyl alcohol to make the flavoring agent benzaldehyde is an equilibrium process described by the equation

$$C_6H_5CH_2OH(g) \iff C_6H_5CHO(g) + H_2(g)$$

At 523 K, the value of its equilibrium constant is K = 0.558.

- (a) Suppose 1.20 g of benzyl alcohol is placed in a 2.00-L vessel and heated to 523 K. What is the partial pressure of benzaldehyde when equilibrium is attained?
- (b) What fraction of benzyl alcohol is dissociated into products at equilibrium?

a) Calculate the chemical amount of the gaseous  $C_6H_5CH_2OH$ . Then use the ideal-gas law to calculate its initial partial pressure. Abbreviate the formula of benzyl alcohol as  $BzOH^1$ 

$$\begin{split} n_{\rm BzOH} &= 1.20~{\rm g~BzOH} \times \left(\frac{1~{\rm mol~BzOH}}{108~{\rm g~BzOH}}\right) = 0.0111~{\rm mol~BzOH} \\ P_{\rm BzOH} &= \frac{n_{\rm BzOH}RT}{V} = \frac{(0.0111~{\rm mol})(0.08206~{\rm L~atm~mol^{-1}K^{-1}})(523~{\rm K})}{2.00~{\rm L}} = 0.238~{\rm atm} \end{split}$$

The following three-line table shows how the partial pressures of benzyl alcohol and its products change as equilibrium is approached

Substitute the final pressures in the mass-action expression

$$\frac{P_{\text{C}_0\text{H}_5\text{CHO}}P_{\text{H}_2}}{P_{\text{BzOH}}} = 0.558 = \frac{(x)(x)}{(0.238 - x)} \qquad \text{from which} \qquad x^2 + 0.558x - 0.133 = 0$$

Use the quadratic formula to solve for x

$$x = \frac{-(0.558) \pm \sqrt{(0.558)^2 - 4(1)(-0.133)}}{2(1)} = \frac{-0.558 \pm 0.918}{2}$$
$$x = 0.180 \quad \text{and} \quad x = -0.738$$

Disregard the solution x = -0.738 because it leads to impossible partial pressures for all three gases. The answer is  $P_{\text{C}_{6}\text{H}_{5}\text{CHO}} = \boxed{0.180 \text{ atm}}$ .

b) The fraction of the benzyl alcohol dissociated at equilibrium equals the amount dissociated divided by the initial amount. These amounts are respectively proportional to the decrease in partial pressure of the benzyl alcohol and the initial partial pressure of the benzyl alcohol. Hence

$$f = \frac{\text{amount of BzOH dissociated}}{\text{original amount of BzOH}} = \frac{0.180 \text{ atm}}{0.238 \text{ atm}} = \boxed{0.756}$$

**53.** Explain the effect of each of the following stresses on the position of the following equilibrium:

$$3 \text{ NO}(g) \iff \text{N}_2\text{O}(g) + \text{NO}_2(g)$$

The reaction as written is exothermic.

- (a)  $N_2O(g)$  is added to the equilibrium mixture without change of volume or temperature.
- **(b)** The volume of the equilibrium mixture is reduced at constant temperature.
- (c) The equilibrium mixture is cooled.
- (d) Gaseous argon (which does not react) is added to the equilibrium mixture while both the total gas pressure and the temperature are kept constant.
- (e) Gaseous argon is added to the equilibrium mixture without changing the volume.

Chemical systems always tend toward equilibrium.<sup>2</sup> If a stress is applied to a system at equilibrium, the system reacts to minimize the stress and to reach a new equilibrium.

- a) The stress is the addition of  $N_2O(g)$ . The system reacts to decrease the concentration of  $N_2O$ . The reaction proceeds from right to left until a new equilibrium is reached.
- b) The stress is the reduction in volume. The partial pressures of all the compounds will momentarily rise. The equilibrium will then shift in such a way as to reduce the number of molecules of gas (chemical amount of gas) in the container and reduce the total pressure. There are three moles of gas on the reactant side of the equation and two moles of gas on the product side. The equilibrium will thus shift from left to right.
- c) The reaction is exothermic. Cooling the mixture shifts the equilibrium from left to right (to favor the products).
- d) In order to maintain a constant pressure, the volume of the system must have increased. Thus, the reaction will shift from right to left.
- e) The partial pressures of the reacting gases are unchanged by the addition of an inert gas, and the equilibrium law is independent of total pressure. There is no effect on the position of the equilibrium.