

1.解：时间：2017 年 10 月 4 日 农历八月十五（中秋节） 22 时 52 分 40 秒

观测地点 1：Shanghai, China N 31°13'19.99" E 127°27'29.02"

方位角 1/高度角 1：+179°59'52.0"/+54°19'51.5"

观测地点 2：（我也不知道是哪里） S 31°13'19.99" E 127°27'29.02"

方位角 2/高度角 2：+0°00'08.5"/+62°14'15.2"

由地球半径为 6400km，且两处观测地点纬度差为 $31^{\circ}13'19.99'' + 31^{\circ}13'19.99'' = 62^{\circ}26'39.98''$ 得

两处观测地点直线距离为 $d_{12} = 2 \times 6400\text{km} \times \sin(62^{\circ}26'39.98''/2) \approx 6635\text{km}$.

由于两地经度相同，且此时观测地点 1 的方位角约为 180° ，观测地点 2 的方位角约为 0° ，所以月球与两地连线的夹角为 $\theta = (180^{\circ} - 62^{\circ}14'15.2'' - 54^{\circ}19'51.5'') - (62^{\circ}26'39.98'') = 0^{\circ}59'13.32'' \approx 0.01722\text{rad}$.

则地月距离为 $d_{\text{地月}} = d_{12}/\theta \approx 3.852 \times 10^5\text{km}$.

2.（1）解：如图，设自然状态下两小球中心连线与水平线的夹角为 α ，碗中心与两小球切点连线和碗中心与任意小球中心连线所成角为 β .

设碗口平面为零重力势能面.

由几何关系得 $\beta = \arcsin(a/(R - a)) = \pi/4$.

左边小球自然状态下重力势能为 $E_{\text{左}0} = -mg(R - a)\cos(\alpha + \beta) = -\sqrt{2}mg\cos(\alpha + \pi/4)$.

左边小球在侧向偏转 δ 后重力势能为 $E_{\text{左}1} = -mg(R - a)\cos(\alpha + \beta + \delta) = -\sqrt{2}mg\cos(\alpha + \pi/4 + \delta)$.

左边小球在侧向偏转中重力势能变化为 $\Delta E_{\text{左}} = E_{\text{左}1} - E_{\text{左}0} = \sqrt{2}mga[\cos(\alpha + \pi/4) - \cos(\alpha + \pi/4 + \delta)] = \sqrt{2}mga[\cos(\alpha + \pi/4) - \cos(\alpha + \pi/4)\cos\delta + \sin(\alpha + \pi/4)\sin\delta]$.

同理，右边小球自然状态下重力势能为 $E_{\text{右}0} = -2mg(R - a)\cos(\beta - \alpha) = -2\sqrt{2}mg\cos(\pi/4 - \alpha)$.

右边小球在侧向偏转 δ 后重力势能为 $E_{\text{右}1} = -2mg(R - a)\cos(\beta - \alpha - \delta) =$

$$-2\sqrt{2}mg\cos(\pi/4 - \alpha - \delta).$$

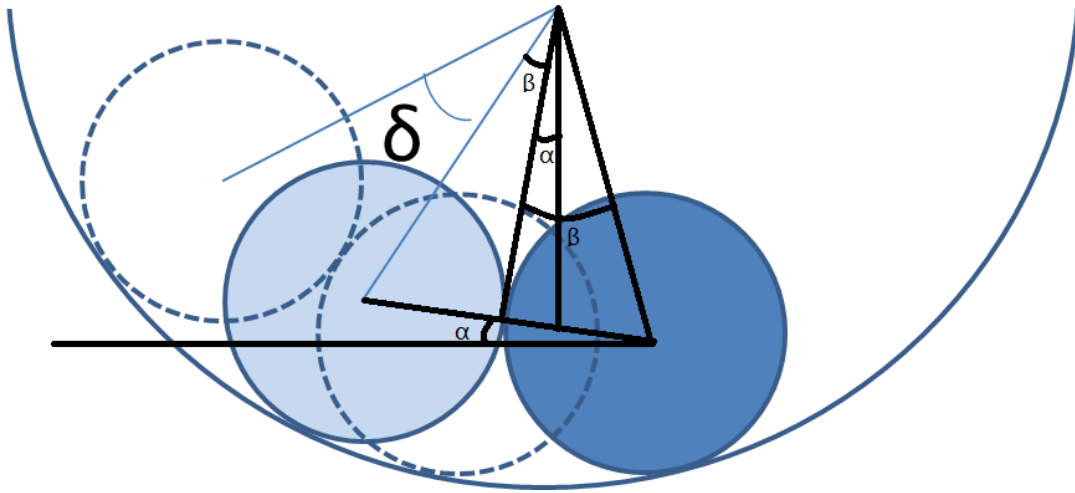
右边小球在侧向偏转中重力势能变化为 $\Delta E_{\text{右}} = E_{\text{右}1} - E_{\text{右}0} = 2\sqrt{2}mga[\cos(\pi/4 - \alpha) - \cos(\pi/4 - \alpha - \delta)] = 2\sqrt{2}mga[\cos(\pi/4 - \alpha) - \cos(\pi/4 - \alpha)\cos\delta - \sin(\pi/4 - \alpha)\sin\delta]$.

(2) 解：为了使两小球平衡，当 $\alpha \rightarrow 0$ 时，应使 $\Delta E_{\text{左}} + \Delta E_{\text{右}} = 0$.

且此时 $\Delta E_{\text{左}} = \sqrt{2}mga\sin\delta(\alpha + \pi/4)$, $\Delta E_{\text{右}} = 2\sqrt{2}mga\delta[-\sin(\pi/4 - \alpha)]$

所以 $\Delta E_{\text{左}} + \Delta E_{\text{右}} = \sqrt{2}mga\delta[\sin(\alpha + \pi/4) - 2\sin(\pi/4 - \alpha)] = mga\delta(3\sin\alpha - \cos\alpha) = 0$.

由此得两小球中心连线与水平线之间的夹角 $\alpha = \arctan(1/3)$.



3.1 : Beta decay has three types:

(1)Beta minus decay: $n \rightarrow p + e^- + \bar{\nu}_e$ A neutron is converted into a proton and an electron and an electron antineutrino. OR ${}^A_ZX \rightarrow {}^A_{Z+1}X + e^- + \bar{\nu}_e$ A atomic nucleus was convert into a nucleus with atomic number increased by one, while emitting an electron and an electron antineutrino.

(2) Beta plus decay: $p \rightarrow n + e^+ + \bar{\nu}_e$ A proton is converted into a neutron and an positron an electron neutrino. OR ${}^A_ZX \rightarrow {}^A_{Z-1}X + e^+ + \bar{\nu}_e$ A atomic nucleus was convert into a nucleus with atomic number subtracted by one, while emitting an electron and an electron antineutrino.

(3)Electron capture: ${}^A_ZX + e^- = {}^A_{Z-1}X + \nu_e$ A nucleus captures one of its atomic electrons, resulting in the emission of a neutrino.

2. Wolfgang Pauli. Neutron(renamed to neutrino by Enrico Fermi later).