## 期末考试

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成绩:

第 1 题 得分: \_\_\_\_\_\_\_. 单模热光场的密度算符为  $\rho = (1 - e^{-\beta}) \exp(-\beta a^{\dagger} a), \ \beta = \hbar \omega / kT$ . 求其密度算符的 Q表示.

解: 单模热光场的密度算符可化为

$$\rho = (1 - e^{-\beta}) \exp(-\beta a^{\dagger} a) \sum_{n} |n\rangle \langle n|$$
$$= (1 - e^{-\beta}) \sum_{n} \exp(-n\beta) |n\rangle \langle n|.$$

Q 表示为

$$Q(\alpha) = \frac{1}{\pi} \langle \alpha | \rho | \alpha \rangle = \frac{1}{\pi} \langle \alpha | (1 - e^{-\beta}) \sum_{n} \exp(-n\beta) | n \rangle \langle n | \alpha \rangle$$

$$= \frac{1 - e^{-\beta}}{\pi} \sum_{n} \exp(-n\beta) | \langle n | \alpha \rangle |^{2}$$

$$= \frac{1 - e^{-\beta}}{\pi} \sum_{n} \exp(-n\beta) \left| e^{-|\alpha|^{2}/2} \frac{\alpha^{n}}{\sqrt{n!}} \right|^{2}$$

$$= \frac{1 - e^{-\beta}}{\pi} e^{-|\alpha|^{2}} \sum_{n} \exp(-n\beta) \frac{|\alpha|^{2n}}{n!}$$

$$= \frac{1 - e^{-\beta}}{\pi} e^{-|\alpha|^{2}[1 - \exp(-\beta)]}.$$
(1)

第 2 题 得分: \_\_\_\_\_. 一光场处于这样的叠加态:  $|\psi\rangle=N(|\alpha\rangle+e^{i\theta}|-\alpha\rangle).$ 

- (1) 计算归一化常数 N.
- (2) 若  $\theta = \pi$ , 判断其是否为泊松分布, 为什么?
- (3) 若  $\theta = 0$ ,  $\alpha$  为纯虚数, 判断其是否有压缩现象, 为什么? (提示: 计算  $(\Delta X_1)^2$ ,  $X_1 = (\alpha + \alpha^{\dagger})/2$ ,  $X_2 = (\alpha \alpha^{\dagger})/2i$ .)

解: (1) 由归一化条件,

$$\langle \psi | \psi \rangle = |N|^{2} \left( \langle \alpha | + e^{-i\theta} \langle -\alpha |) (|\alpha \rangle + e^{i\theta} | -\alpha \rangle \right)$$

$$= |N|^{2} \left( \langle \alpha | \alpha \rangle + \langle \alpha | -\alpha \rangle e^{i\theta} + \langle -\alpha | \alpha \rangle e^{-i\theta} + \langle -\alpha | -\alpha \rangle \right)$$

$$= |N|^{2} \left[ 1 + \exp(-2 |\alpha|^{2}) e^{i\theta} + \exp(-2 |\alpha|^{2}) e^{-i\theta} + 1 \right]$$

$$= 2 |N|^{2} \left[ 1 + \exp(-2 |\alpha|^{2}) \cos \theta \right]$$

$$= 1,$$
(2)

$$\implies N = [2 + 2\exp(-2|\alpha|^2)\cos\theta]^{-1/2}.$$
 (3)

(2) 若  $\theta = \pi$ , 则叠加态为

$$|\psi\rangle = N(|\alpha\rangle - |-\alpha\rangle),\tag{4}$$

二阶相关度

$$g^{(2)}(0) = \frac{\langle a^\dagger a^\dagger a a \rangle}{\langle a^\dagger a \rangle^2} = \frac{\langle \psi | a^\dagger a^\dagger a a | \psi \rangle}{\langle \psi | a^\dagger a | \psi \rangle^2}$$

$$= \frac{|N|^{2} (\langle \alpha | - \langle -\alpha |) a^{\dagger} a^{\dagger} a a (|\alpha \rangle - |-\alpha \rangle)}{[|N|^{2} (\langle \alpha | - \langle -\alpha |) a^{\dagger} a (|\alpha \rangle - |-\alpha \rangle)]^{2}} 
= \frac{[(\alpha^{*})^{2} \langle \alpha | - (\alpha^{*})^{2} \langle -\alpha |] [\alpha^{2} | \alpha \rangle - \alpha^{2} |-\alpha \rangle]}{|N|^{2} \{ [\alpha^{*} \langle \alpha | + \alpha^{*} \langle -\alpha |] [\alpha | \alpha \rangle + \alpha |-\alpha \rangle] \}^{2}} 
= \frac{|\alpha|^{4} (1 - \exp(-2|\alpha|^{2}) - \exp(-2|\alpha|^{2}) + 1)}{|N|^{2} \{ |\alpha|^{2} (1 + \exp(-2|\alpha|^{2}) + \exp(-2|\alpha|^{2}) + 1) \}^{2}} 
= \frac{1 - \exp(-2|\alpha|^{2})}{2|N|^{2} [1 + \exp(-2|\alpha|^{2})]^{2}} 
= \frac{[1 - \exp(-2|\alpha|^{2})][1 + \exp(-2|\alpha|^{2})\cos\theta]}{[1 + \exp(-2|\alpha|^{2})]^{2}} < 1,$$
(5)

故该叠加态为亚泊松分布.

## (3) 若 $\theta = 0$ , 叠加态为

$$|\psi\rangle = N(|\alpha\rangle + |-\alpha\rangle),\tag{6}$$

其中

$$N = [2 + 2\exp(-2|\alpha|^2)]^{-1/2} \tag{7}$$

 $X_1$  的均值为

$$\langle X_{1} \rangle = N^{*}(\langle \alpha | + \langle -\alpha |) \frac{1}{2} (\alpha + \alpha^{\dagger}) N(|\alpha\rangle + |-\alpha\rangle)$$

$$= \frac{|N|^{2}}{2} [(\langle \alpha | + \langle -\alpha |) (\alpha | \alpha\rangle - \alpha | -\alpha\rangle) + (\alpha^{*} \langle \alpha | -\alpha^{*} \langle -\alpha |) (|\alpha\rangle + |-\alpha\rangle)]$$

$$= \frac{|N|^{2}}{2} [\alpha (1 - \exp(-2 |\alpha|^{2}) + \exp(-2 |\alpha|^{2}) - 1) + \alpha^{*} (1 + \exp(-2 |\alpha|^{2}) - \exp(-2 |\alpha|^{2}) - 1)]$$

$$= 0.$$
(8)

 $X_1^2$  的均值为

$$\begin{split} \langle X_1^2 \rangle = & N^*(\langle \alpha | + \langle -\alpha |) \left[ \frac{1}{2} (a + a^\dagger) \right]^2 N(|\alpha\rangle + |-\alpha\rangle) \\ = & \frac{|N|^2}{4} (\langle \alpha | + \langle -\alpha |) (aa + aa^\dagger + a^\dagger a + a^\dagger a^\dagger) (|\alpha\rangle + |-\alpha\rangle) \\ = & \frac{|N|^2}{4} (\langle \alpha | + \langle -\alpha |) (aa + 2a^\dagger a + 1 + a^\dagger a^\dagger) (|\alpha\rangle + |-\alpha\rangle) \\ = & \frac{|N|^2}{4} [(\langle \alpha | + \langle -\alpha |) (\alpha^2 | \alpha\rangle + \alpha^2 | -\alpha\rangle) + 2(\alpha^* \langle \alpha | - \alpha^* \langle -\alpha |) (\alpha | \alpha\rangle - \alpha | -\alpha\rangle) \\ & + (\langle \alpha | + \langle -\alpha |) (|\alpha\rangle + |-\alpha\rangle) + ((\alpha^*)^2 \langle \alpha | + (\alpha^*)^2 \langle -\alpha |) (|\alpha\rangle + |-\alpha\rangle)] \\ = & \frac{|N^2|}{4} [\alpha^2 (1 + \exp(-2|\alpha|^2) + \exp(-2|\alpha|^2) + 1) + 2|\alpha|^2 (1 - \exp(-2|\alpha|^2) - \exp(-2|\alpha|^2) + 1) \\ & + (1 + \exp(-2|\alpha|^2) + \exp(-2|\alpha|^2) + 1) + (\alpha^*)^2 (1 + \exp(-2|\alpha|^2) + \exp(-2|\alpha|^2) + 1)] \\ = & \frac{|N|^2}{2} [(\alpha^2 + (\alpha^*)^2 + 1) (1 + \exp(-2|\alpha|^2)) + |\alpha|^2 (1 - \exp(-2|\alpha|^2))] \\ = & \frac{1}{4} \left[ 1 + \alpha^2 + (\alpha^*)^2 + |\alpha|^2 \frac{1 - \exp(-2|\alpha|^2)}{1 + \exp(-2|\alpha|^2)} \right], \end{split} \tag{9}$$

由于  $\alpha$  为纯虚数, 故

$$\langle X_1^2 \rangle = \frac{1}{4} \left[ 1 - |\alpha|^2 \frac{1 + 3 \exp(-2|\alpha|^2)}{1 + \exp(-2|\alpha|^2)} \right] < \frac{1}{4}.$$
 (10)

 $X_1$  的涨落为

$$\Delta X_1 = \sqrt{\langle X_1^2 \rangle - \langle X_1 \rangle^2} = \sqrt{\langle X_1^2 \rangle} < \frac{1}{2},\tag{11}$$

故有压缩.

第 3 题 得分: \_\_\_\_\_. 简述:

- (1) 偶极近似的适用条件;
- (2) 旋转波近似的含义;
- (3) 马尔可夫近似的含义;
- (4) 自发辐射和受激辐射的不同点;
- (5) Hanbry-Brown-Twiss 实验与迈克尔逊干涉实验的不同之处.
- 解: (1) 偶极近似的适用条件: 讨论的系统尺寸远小于光的波长.
  - (2) 旋转波近似的含义: 光场频率相对于系统的本征频率具有大失谐的分量在足够长时间的积分下对系统演化的 贡献平均为零.
  - (3) 马尔科夫近似:系统无记忆,系统的当前状态与其历史无关,即关联时间为 0,该近似适用于热库非常大且系统与热库相互作用持续的情形.
  - (4) (a) 自发辐射由真空中电磁场的涨落扰动引起,受激辐射需要外界辐射场的激励才能发生;
    - (b) 自发辐射的发生时间、相位、方向和偏振是随机的, 受激辐射的相位、方向和偏振与诱导光子相同.
  - (5) HBT 实验是二阶相干, 是光子与光子之间的相干, 体现了光源的光子数分布特性; 迈克尔逊干涉实验是一阶相干, 是光子自身的相干, 体现了光源频谱的单色性.

第 4 题 得分: \_\_\_\_\_\_. 单个二能级原子 (上下能级分别为  $|a\rangle$ ,  $|b\rangle$ ) 同单模光场 (频率  $\nu = \omega_{ab}$ ) 共振相互作用. 考虑偶极近似和旋转波近似, 假设相互作用系数为实数.

- (1) 写出半经典理论描述的原子-光场系统哈密顿量.
- (2) 写出全量子理论描述的原子-光场哈密顿量.
- (3) 原子初态为  $|a\rangle$ , 光场初态为真空态, 利用全量子理论的描述求 t 时刻的原子布居数反转数  $W(t) = |c_a|^2 |c_b|^2$ .
- (4) (附加题) 若原子初态为  $\frac{1}{\sqrt{2}}(|a\rangle |b\rangle)$ , 光场的初态为真空态, 求 W(t).
- 解: (1) 半经典理论描述的原子-光场系统哈密顿量为

$$H = \hbar \omega_a |a\rangle\langle a| + \hbar \omega_b |b\rangle\langle b| - (\mu_{ab}|a\rangle\langle b| + \mu_{ba}|b\rangle\langle a|)\mathcal{E}\cos\nu t \tag{12}$$

其中电偶极矩算符的对角项

$$\mu_{ab} = \langle a|\mu|b\rangle, \quad \mu_{ba} = \langle b|\mu|a\rangle.$$
 (13)

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## (2) 全量子理论描述的原子-光场哈密顿量为

$$H = H_0 + H_1. (14)$$

其中无微扰哈密顿量

$$H_0 = \hbar \nu a^{\dagger} a + \frac{1}{2} \hbar \omega_{ab} \sigma_z, \tag{15}$$

相互作用哈密顿量

$$H_1 = \hbar g(\sigma_+ a + a^{\dagger} \sigma_-). \tag{16}$$

## (3) 相互作用表象下, 系统的相互作用哈密顿量为

$$\hat{V} = e^{i\hat{H}_0 t/\hbar} H_1 e^{-i\hat{H}_0 t/\hbar} = \hbar g(\sigma_+ a e^{i\Delta t} + a^{\dagger} \sigma_- e^{-i\Delta t}), \tag{17}$$

其中频率失谐  $\Delta = \omega_{ab} - \nu$ . 系统演化遵循相互作用表象下薛定谔方程:

$$i\hbar \frac{\partial}{\partial t} |\psi(t)\rangle = \hat{V}|\psi(t)\rangle,$$
 (18)

代入系统的量子态

$$|\psi(t)\rangle = \sum_{n=0}^{\infty} [C_{a,n}(t)|a,n\rangle + C_{b,n}|b,n\rangle], \tag{19}$$

有

$$\dot{C}_{a,n}(t) = -igC_{b,n+1}\sqrt{n+1}e^{i\Delta t},\tag{20}$$

$$\dot{C}_{b,n+1}(t) = -igC_{a,n}\sqrt{n+1}e^{-i\Delta t},$$
(21)

解得

$$C_{a,n}(t) = \left\{ C_{a,n}(0) \left[ \cos \left( \frac{\Omega_n t}{2} \right) - \frac{i\Delta}{\Omega_n} \sin \left( \frac{\Omega_n t}{2} \right) \right] - \frac{2ig\sqrt{n+1}}{\Omega_n} C_{b,n+1}(0) \sin \left( \frac{\Omega_n t}{2} \right) \right\} e^{i\Delta t/2}, \tag{22}$$

$$C_{b,n+1}(t) = \left\{ C_{b,n+1}(0) \left[ \cos \left( \frac{\Omega_n t}{2} \right) + \frac{i\Delta}{\Omega_n} \sin \left( \frac{\Omega_n t}{2} \right) \right] - \frac{2ig\sqrt{n+1}}{\Omega_n} C_{a,n}(0) \sin \left( \frac{\Omega_n t}{2} \right) \right\} e^{-i\Delta t/2}, \tag{23}$$

其中

$$\Omega_n^2 = \Delta^2 + 4g^2(n+1). \tag{24}$$

原子初态为  $|a\rangle$ , 即  $C_{a,0}=1$ , 将其代入上面两式得

$$C_{a,0}(t) = \left[\cos\left(\frac{\Omega_0 t}{2}\right) - \frac{i\Delta}{\Omega_0}\sin\left(\frac{\Omega_0 t}{2}\right)\right]e^{i\Delta t/2},\tag{25}$$

$$C_{b,1}(t) = -\frac{2ig}{\Omega_0} \sin\left(\frac{\Omega_0 t}{2}\right) e^{-i\Delta t/2}.$$
 (26)

t 时刻的原子布居数反转为

$$W(t) = |c_a|^2 - |c_b|^2 = |C_{a,0}(t)|^2 - |C_{b,1}(t)|^2 = \cos^2\left(\frac{\Omega_0 t}{2}\right) + \frac{\Delta^2 - 4g^2}{\Omega_0^2}\sin^2\left(\frac{\Omega_0 t}{2}\right).$$
 (27)

由于  $\nu = \omega_{ab}$ , 故  $\Delta = 0$ ,  $\Omega_0^2 = 4g^2$ ,

$$W(t) = \cos^2(gt) - \sin^2(gt) = \cos(2gt). \tag{28}$$

(4) 若原子初态为  $\frac{1}{\sqrt{2}}(|a\rangle - |b\rangle)$ , 光场的初态为真空态, 则  $C_{a,0}(0) = \frac{1}{\sqrt{2}}$ ,  $C_{b,0} = \frac{1}{\sqrt{2}}$ ,

$$C_{a,0}(t) = \frac{1}{\sqrt{2}} \left[ \cos \left( \frac{\Omega_0 t}{2} \right) - \frac{i\Delta}{\Omega_0} \sin \left( \frac{\Omega_0 t}{2} \right) \right] e^{i\Delta t/2}, \tag{29}$$

$$C_{b,1}(t) = -\frac{\sqrt{2}ig}{\Omega_0} \sin\left(\frac{\Omega_0 t}{2}\right) e^{-i\Delta t/2},\tag{30}$$

$$C_{b,0}(t) = \frac{1}{\sqrt{2}}. (31)$$

t 时刻的原子布居数反转为

$$W(t) = |c_a(t)|^2 - |c_b(t)|^2 = |C_{a,0}(t)|^2 - |C_{b,1}|^2 - |C_{b,0}(t)|^2$$

$$= \frac{1}{2}\cos^2\left(\frac{\Omega_0 t}{2}\right) + \frac{\Delta^2 - 4g^2}{2\Omega_0^2}\sin^2\left(\frac{\Omega_0 t}{2}\right) - \frac{1}{2}.$$
(32)

由于  $\nu = \omega_{ab}$ , 故  $\Delta = 0$ ,  $\Omega_n^2 = 4g^2(n+1)$ ,

$$W(t) = \frac{1}{2}\cos^2(gt) - \frac{1}{2}\sin^2(gt) - \frac{1}{2} = \frac{\cos(2gt) - 1}{2}.$$
 (33)

第 5 题 得分: \_\_\_\_\_\_\_. 单模光场与热平衡辐射场热库相互作用, 其密度算符的运动方程为:

$$\dot{\rho} = -\frac{\gamma}{2}\bar{n}(aa^{\dagger}\rho - 2a^{\dagger}\rho a + \rho aa^{\dagger}) - \frac{\gamma}{2}(\bar{n} + 1)(a^{\dagger}a\rho - 2a\rho a^{\dagger} + \rho a^{\dagger}a).$$

求 t 时刻光场的粒子数平均值  $\langle a^\dagger(t)a(t) \rangle$ . [提示:  $\frac{\mathrm{d}\langle a^\dagger a \rangle}{\mathrm{d}t} = \mathrm{Tr}(\dot{\rho}a^\dagger a)$ ]

解:

$$\begin{split} &\frac{\mathrm{d}\langle a^{\dagger}a\rangle}{\mathrm{d}t} = \mathrm{Tr}(\dot{\rho}a^{\dagger}a) \\ &= \mathrm{Tr}\left\{\left[-\frac{\gamma}{2}\bar{n}(aa^{\dagger}\rho - 2a^{\dagger}\rho a + \rho aa^{\dagger}) - \frac{\gamma}{2}(\bar{n}+1)(a^{\dagger}a\rho - 2a\rho a^{\dagger} + \rho a^{\dagger}a)\right]a^{\dagger}a\right\} \\ &= \mathrm{Tr}\left\{-\frac{\gamma}{2}\bar{n}(aa^{\dagger}\rho a^{\dagger}a - 2a^{\dagger}\rho aa^{\dagger}a + \rho aa^{\dagger}a^{\dagger}a) - \frac{\gamma}{2}(\bar{n}+1)(a^{\dagger}a\rho a^{\dagger}a - 2a\rho a^{\dagger}a^{\dagger}a + \rho a^{\dagger}aa^{\dagger}a)\right\} \\ &= \mathrm{Tr}\left\{\rho\left[-\frac{\gamma}{2}\bar{n}(a^{\dagger}aaa^{\dagger} - 2aa^{\dagger}aa^{\dagger} + aa^{\dagger}a^{\dagger}a) - \frac{\gamma}{2}(\bar{n}+1)(a^{\dagger}aa^{\dagger}a - 2a^{\dagger}a^{\dagger}aa + a^{\dagger}aa^{\dagger}a)\right]\right\} \\ &= \mathrm{Tr}\left\{\rho\left[-\frac{\gamma}{2}\bar{n}(a^{\dagger}a(a^{\dagger}a + 1) - 2(a^{\dagger}a + 1)(a^{\dagger}a + 1) + (a^{\dagger}a + 1)a^{\dagger}a) - \frac{\gamma}{2}(\bar{n}+1)(2a^{\dagger}(a^{\dagger}a + 1)a - 2a^{\dagger}a^{\dagger}aa)\right]\right\} \\ &= \mathrm{Tr}\left\{\rho\left[\gamma\bar{n}(a^{\dagger}a + 1) - \gamma(\bar{n}+1)a^{\dagger}a\right]\right\} \\ &= \mathrm{Tr}\left\{\gamma\rho(\bar{n}-a^{\dagger}a)\right\} \\ &= \gamma(\bar{n}-\langle a^{\dagger}a\rangle), \end{split}$$

解得 t 时刻光场的粒子数平均值为

$$\langle a^{\dagger}(t)a(t)\rangle = (\langle a^{\dagger}(0)a(0)\rangle - \bar{n})e^{-\gamma t} + \bar{n}. \tag{35}$$

第 6 题 得分: \_\_\_\_\_. 单模光场与热平衡辐射场热库相互作用的 Langevin 方程为

$$\dot{\tilde{a}}(t) = -\frac{\gamma}{2}\tilde{a}(t) + F_{\tilde{a}}(t),$$

且已知:  $\langle F_{\tilde{a}}^{\dagger}(t)\tilde{a}(t)\rangle_{R} + \langle \tilde{a}^{\dagger}(t)F_{\tilde{a}}(t)\rangle_{R} = \gamma \bar{n}$ . 试求  $\langle \tilde{a}^{\dagger}(t)\tilde{a}(t)\rangle_{R}$ .

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解: Langevin 方程的共轭为

$$\dot{\tilde{a}}^{\dagger}(t) = -\frac{\gamma^*}{2}\tilde{a}^{\dagger}(t) + F_{\tilde{a}}^{\dagger}(t). \tag{36}$$

 $\langle \tilde{a}^{\dagger}(t)\tilde{a}(t)\rangle$  遵循演化方程:

$$\frac{\mathrm{d}\langle \tilde{a}^{\dagger}(t)\tilde{a}(t)\rangle_{R}}{\mathrm{d}t} = \left\langle \frac{\mathrm{d}\tilde{a}^{\dagger}(t)\tilde{a}(t)}{\mathrm{d}t} \right\rangle_{R} = \left\langle \frac{\mathrm{d}\tilde{a}^{\dagger}(t)}{\mathrm{d}t}\tilde{a}(t) + \tilde{a}^{\dagger}(t)\frac{\mathrm{d}\tilde{a}(t)}{\mathrm{d}t} \right\rangle_{R}$$

$$= \left\langle \left[ -\frac{\gamma^{*}}{2}\tilde{a}^{\dagger}(t) + F_{\tilde{a}}^{\dagger}(t) \right] \tilde{a}(t) + \tilde{a}^{\dagger}(t) \left[ -\frac{\gamma}{2}\tilde{a}(t) + F_{\tilde{a}}(t) \right] \right\rangle_{R}$$

$$= -\frac{\gamma^{*} + \gamma}{2} \langle \tilde{a}^{\dagger}(t)\tilde{a}(t)\rangle_{R} + \langle F_{\tilde{a}}^{\dagger}(t)\tilde{a}(t)\rangle_{R} + \langle \tilde{a}^{\dagger}(t)F_{\tilde{a}}(t)\rangle_{R}$$

$$= -\frac{\gamma^{*} + \gamma}{2} \langle \tilde{a}^{\dagger}(t)\tilde{a}(t)\rangle_{R} + \gamma\bar{n}, \tag{37}$$

解得

$$\langle \tilde{a}^{\dagger}(t)\tilde{a}(t)\rangle_{R} = \left[\langle \tilde{a}^{\dagger}(0)\tilde{a}(0)\rangle - \frac{2\gamma}{\gamma^{*} + \gamma}\right]e^{-\frac{\gamma^{*} + \gamma}{2}t} + \frac{2\gamma}{\gamma^{*} + \gamma}\bar{n}.$$
 (38)

第 7 题 (附加题) 得分: \_\_\_\_\_\_. 如何理解原子谱线宽度和寿命的不确定性关系  $\Delta\omega \propto 1/\tau$ .

解: 原子上能级具有有限的寿命  $\tau$ , 由不确定性原理, 其能量值具有不确定性  $\Delta E$ , 满足

$$\Delta E \cdot \tau \sim \frac{\hbar}{2},\tag{39}$$

故原子谱线, 即原子由上能级跃迁至下能级辐射的光子频率具有不确定性

$$\Delta\omega = \frac{\Delta E}{\hbar} \propto \frac{1}{\tau}.\tag{40}$$

第8题 (附加题) 得分: \_\_\_\_\_. 谈谈你对信息的理解.

解:信息即不确定度的减少,信息的量用香农熵

$$H = -\sum_{k=1}^{n} p_k \log_2 p_k \tag{41}$$

来衡量.

**第9题 (附加题)得分:** \_\_\_\_\_. 简述量子光学主要是研究什么问题? 在经典物理学中主要用哪一些学科研究 这些内容 (例如可举普通物理和四大力学中的学科和工具).

解:量子光学主要研究光场的量子化和光与物质的相互作用.

经典物理学中有光学、原子物理学、电动力学来研究这些内容.