```
内能:U = \sum_{l} \varepsilon_{l} a_{l} = \sum_{l} \omega_{l} \varepsilon_{l} e^{-\alpha - \beta \varepsilon_{l}} = e^{-\alpha} \left( -\frac{\partial}{\partial \beta} \sum_{l} \omega_{l} e^{-\beta \varepsilon_{l}} \right) = -\frac{N}{Z_{1}} \frac{\partial Z_{1}}{\partial \beta} = -N \frac{\partial}{\partial \beta} \ln Z_{1}

\Gamma X h : Y = \sum_{l} \frac{\partial \varepsilon_{l}}{\partial y} a_{l} = \sum_{l} \frac{\partial \varepsilon_{l}}{\partial y} \omega_{l} e^{-\alpha - \beta \varepsilon_{l}} = e^{-\alpha} \left( -\frac{1}{\beta} \frac{\partial}{\partial y} \right) \sum_{l} \omega_{l} e^{-\beta \varepsilon_{l}} = -\frac{N}{Z_{1}} \frac{1}{\beta} \frac{\partial Z_{1}}{\partial y} = \frac{\partial}{\partial y} \left( -\frac{1}{\beta} \frac{\partial}{\partial y} \right) \left( -\frac{1}{\beta} \frac{\partial}{\partial y} \right
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   指令・\sin^2\theta・\varphi 2m\mu \pi 
 热客:C_V=\frac{dU}{dT}=\frac{5}{2}Nk;定压热客:C_P=\frac{7}{2}Nk;热客比:\gamma=\frac{7}{5};无法解释低温下H_2的性质,未考虑两原子的相对运动 对固体中的原子振动,原子能量:\varepsilon=\frac{1}{2m}(p_x^2+p_y^2+p_z^2)+\frac{1}{2}m\omega_x^2q_x^2+\frac{1}{2}\omega_y^2q_y^2+\frac{1}{2}m\omega_z^2q_z^2;原子平均能量:\varepsilon=3kT:总内的U=\varepsilon N=3NkT;热容:C_V=\frac{dU}{dT}=3Nk;低温下理论与实验不符合,实验发现C_V=\frac{dU}{dT}=3Nk;低温下理论与实验不符合,实验发现C_V=\frac{dU}{dT}=3Nk
    -rac{N}{eta}rac{\partial}{\partial y}\ln Z_1,其中y-广义坐标;压强:p=rac{N}{eta}rac{\partial}{\partial V}\ln Z_1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     現C_V \downarrow随T \downarrow,终\rightarrow 0,3K以上自由电子的热容可忽略
    アンカ:dW=Ydy=dy\sum_lrac{\partial arepsilon_l}{\partial y}a_l=\sum_la_la_l, 内能全微分:dU=\sum_larepsilon_l e_lda_l+\sum_la_ldarepsilon_l, 其中第一项为能级不变时粒子分布改变引起的内能变化。以dU=dQ+dW得吸
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   对平衡辐射,辐射场可分解为一系列満足周期性边界条件的单色平面波的叠加,E=E_0e^{i(m{k}\cdotm{r}-\omega t)},其中\omega=ck,k_x/y/z=\frac{2\pi}{L}n_x,n_{x/y/z}=0, \pm1,\cdots,E_0有2个相垂且垂直于k的偏振方向;具有一定波
  参数:eta:dQ = dU - Y dy = -Nd \left( \frac{\partial}{\partial \beta} \ln Z_1 \right) + \frac{N}{\beta} \frac{\partial \ln Z_1}{\partial y} dy,两边同乗\beta得\beta dQ = -N\beta d \left( \frac{\partial}{\partial \beta} \ln Z_1 \right) + \frac{N}{\beta} \frac{\partial \ln Z_1}{\partial y} dy,两边同乘\beta得\beta dQ = -N\beta d \left( \frac{\partial}{\partial \beta} \ln Z_1 \right) + \frac{N}{\beta} \frac{\partial \ln Z_1}{\partial y} dy,因Z_1 \beta \beta,y的函数,d(\ln Z_1) = \frac{\partial \ln Z_1}{\partial \beta} d\beta + \frac{\partial \ln Z_1}{\partial y} dy,又d \left( N\beta \frac{\partial \ln Z_1}{\partial \beta} \right) = \frac{\partial \ln Z_1}{\partial \beta} d\beta
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    矢k和一定偏振的单色平面波可视为一自由度,在V内dk_xdk_ydk_z范围内,振动自由度: rac{dk_x}{2\pi/L} rac{dk_y}{2\pi/L} rac{dk_z}{2\pi/L}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     Vdk_xdk_ydk_z/4\pi^3;V內\omega\sim\omega+d\omega范围內,振动自由度:D(\omega)d\omega=rac{V}{4\pi^3}\left(rac{\omega}{2\pi c}
ight)^2d\left(rac{\omega}{2\pi c}
ight)\int_0^\pi\sin	heta d	heta
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            2^{n} d\phi = \frac{V_{cS}}{\pi^2 c^3} \omega^2 d\omega;该范围内总振动能量:U_{\omega} d\omega = D(\omega) k T d\omega = \frac{4\pi^3 (2\pi\varepsilon)^{-0}}{\pi^2 c^3} \omega^2 k T d\omega(讀利)金斯公式);低頻段<sup>1</sup>验符合,高頻段偏差,积分得总能量发散,与斯特藩-玻尔兹曼定律不符,因经典电动力学辐射场有无穷多个振动自由度

5 理想气体的内能和热容 忽略电子运动,观原于分于能量:\varepsilon = \varepsilon^t + \varepsilon^v + \varepsilon^r,其中t,v,r^{-3}/振动/转动分量;配分函数Z_1 = \sum_l \omega_l e^{-\beta \varepsilon_l} = \sum_{t,v,r} \omega^t \omega^v \omega^r e^{-\beta} (\varepsilon^t + \varepsilon^v + \varepsilon^r)
    Nd\left(etarac{\partial\ln Z_1}{\partialeta}
ight) = Neta d\left(rac{\partial\ln Z_1}{\partialeta}
ight) + Nrac{\partial\ln Z_1}{\partialeta}deta,代入前前式得eta dQ = d\left(N\ln Z_1 - Netarac{\partial\ln Z_1}{\partialeta}
ight),这
    说明\beta为一般分因子,嫡式dS=dQ/T说明1/T亦一积分因子,设两者相差一常数k,称<mark>玻尔兹曼常数,\beta=1/kT,应用于理想 ^{\prime} 体得k=R/N_A=1.381 	imes 10^{-23} J \cdot K^{-1}; 嫡:S=Nk\left(\ln Z_1-eta \frac{\partial}{\partial eta} \ln Z_1
ight)</mark>
     坡尔兹曼关系:将N=e^{-\alpha}Z_1\Rightarrow \ln Z_1=\ln N+\alpha  和U=-N\frac{\partial}{\partial \beta}\ln Z_1代入嫡式得S=k(N\ln N-N\alpha+\beta U)=k\left[N\ln N+\sum_l(\alpha+\beta\varepsilon_l)a_l\right]、又a_l=\omega_le^{-\alpha-\beta\varepsilon_l}\Rightarrow \alpha+\beta\varepsilon_l=\ln\frac{\omega_l}{a_l},得S=k(N\ln N-N\alpha+\beta U)=k\left[N\ln N+\sum_l(\alpha+\beta\varepsilon_l)a_l\right]、又a_l=\omega_le^{-\alpha-\beta\varepsilon_l}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    \sum_t \omega^t e^{-\beta \varepsilon^t} \sum_v \omega^v e^{-\beta \varepsilon^v} \sum_r \omega^r e^{-\beta \varepsilon r} \ = \ Z_1^t Z_1^v Z_1^r; \\ \texttt{PME}: U \ = \ -N \frac{\partial}{\partial \beta} \ln Z_1 \ = \ -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1^t) + \ln Z_1^t = -N \frac{\partial}{\partial \beta} (\ln Z_1^t + \ln Z_1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   \ln Z_1^v + \ln Z_1^T) = U^t;定容熱容:C_V = \frac{\partial U}{\partial T} = C_V^t + C_V^v + C_V^T 平动配分函数:Z_V^r = V\left(\frac{2m\pi}{\beta h^2}\right)^{3/2};内能:U^t = -N\frac{\partial}{\partial \beta} \ln Z_1^t = \frac{3N}{2\beta} = \frac{3}{2}NkT;定容热容:C_V^t = \frac{3}{2}Nk
  视相对振动的两原子为线性谐振子,振动能级:e^v_n = \left(n+rac{1}{2}
ight)\hbar\omega;配分函数:Z^v_1 = \sum_{n=0}^\infty e^{-eta\hbar\omega(n+rac{1}{2})} =
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    \frac{e^{-\beta\hbar\omega/2}}{1-e^{-\beta\hbar\omega}}; \textbf{内能}: U^V = -N\frac{\partial}{\partial\beta} \ln Z_1^v = \frac{N\hbar\omega}{2} + \frac{N\hbar\omega}{e^{\beta\hbar\omega}-1} = \frac{Nk\theta_v}{2} + \frac{Nk\theta_v}{e^{\theta_v/T}-1}, \textbf{其中第一}: \textbf{为N个振子的零点能, 与温度无关, 第二项为TFN 个振子的热激发能, 振动特征温度: <math>\theta_v = \frac{\hbar\omega}{k}; \textbf{振动贡献定容热容}: C_V : \textbf{1}
  k \ln N! = k \ln \frac{\Omega_{M,B}}{N!} = k \ln \Omega_{B,E};自由能:F = -NkT \ln Z_1 + kT \ln N!
 经典系统配分函数: Z_1 = \sum_l e^{-\beta \varepsilon_l} \frac{\Delta \omega_l}{h_0^r} = \int e^{-\beta \varepsilon_l} \frac{d\omega_l}{h_0^r} \int \cdots \int e^{-\beta \varepsilon(p,q)} \frac{dq_1 \cdots dq_r dp_1 \cdots \cdots dp_r}{h_0^r}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    \left(\frac{\partial U}{\partial T}\right)_{V} = Nk \left(\frac{\hbar \omega}{kT}\right)^{2} \frac{e^{\hbar \omega/kT}}{(e^{\hbar \omega/kT}-1)^{2}} = Nk \left(\frac{\theta}{T}\right)^{2} \frac{e^{\theta v/T}}{(e^{\theta v/T}-1)^{2}}; \text{ The } W = \theta_{v}, U^{v}
  总粒子数: N=e^{-\alpha}Z_1; 分布: a_l=e^{-\alpha-\beta\varepsilon l} \frac{\Delta\omega_l}{h_0^r}=\frac{N}{Z_1}e^{-\beta\varepsilon l} \frac{\Delta\omega_l}{h_0^r} , h_0^r 与Z_1 中h_0^{-r} 相消, 故分布与h_0^r 值无关
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     rac{Nk	heta_v}{2}+Nk	heta_ve^{-	heta_v/T}, C_V^v=Nk\left(rac{	heta_v}{T}
ight)^2e^{-	heta_v/T},这说明常温下C_V^v	o 0,不参与能量均分
    内能:U=-Nrac{\partial}{\partialeta}\ln Z_1,与h_0取值无关; 广义力:Y=-rac{N}{eta}rac{\partial}{\partial y}\ln Z_1,与h_0取值无关
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     对异核双原子分子(无全同性影响):转动能量:\varepsilon^r = \frac{l(l+1)}{2I}\hbar^2, l = 0, 1, \cdots;简并度:\omega_l = 2l+1;转动配分函
  \beta の \beta
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     温下T \gg \theta_r,令x = l(l+1) \frac{\theta_r}{T},Z_1^r = \int_0^{+\infty} (2l+1) e^{-x} \frac{dx}{(2l+1)(\theta_r/T)} = \frac{T}{\theta_r} = \frac{2I}{\beta \hbar^2},转动贡献内
 e^{-\frac{\beta}{2m}(p_{x}^{2}+p_{y}^{2}+p_{z}^{2})} dx dy dz dp_{x} dp_{y} dp_{z} = \frac{V}{h^{3}} \left(\int_{-\infty}^{+\infty} e^{-\frac{\beta}{2m}p_{x}^{2}} dp_{x}\right)^{3} = V\left(\frac{2m\pi}{\beta h^{2}}\right)^{3/2}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   対同核双原子分子:以氦为例,常温下含3/4兩原子自能平行,以为奇数的正氢,1/4自旋反平行,1個的仲氢,正氢配分函数:Z_{1o}^{r}=\sum_{l=1,3,\cdots}(2l+1)e^{-l(l+1)\theta_{r}/T},仲氢配分函数:Z_{1p}^{r}=\sum_{l=0,2,\cdots}(2l+1)e^{-l(l+1)\theta_{r}/T};转动贡献内能:U^{r}=U_{o}^{r}+U_{p}^{r}=-\frac{3}{4}N\frac{\partial}{\partial\beta}\ln Z_{1o}^{r}-\frac{4}{4}N\frac{\partial}{\partial\beta}\ln Z_{1p}^{r};第溫下T\gg\theta_{r},Z_{1o}^{r}\approx Z_{1p}^{r}\approx\frac{1}{2}\sum_{l=0,1,\cdots}
  压强/物态方程: p=rac{N}{eta}rac{\partial}{\partial V}\ln Z_1=rac{N}{Veta}\Rightarrow pV=kTN=nkTN_A,与pV=nRT比较得R=kN_A
    经典极限条件:将单原子分子理想气体配分函数代入经典极限条件得e^{lpha} \ = \ rac{Z}{N} \ = \ rac{V}{N} \left(rac{2m\pi kT}{\hbar^2}
ight)^{3/2} \ \gg \ 1,这说
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     \frac{1}{2} \int_0^\infty (2l+1) \frac{e^{-x} \, dx}{(2l+1)(\theta_T/T)} = \frac{1}{2} \, \frac{T}{\theta_T} = \frac{I}{\beta \hbar^2},转动贡献内能:U^r \approx -N \frac{\partial}{\partial \beta} \ln Z_{1o}^r = -N \frac{\partial}{\partial \beta} \ln \frac{I}{\beta \hbar^2} = -N \frac{\partial}{\partial \beta} \ln Z_{1o}^r = -N \frac{\partial}{\partial \beta} \ln
    明rac{N}{V}越小(气体越稀薄),T越高,分子质量越大,越趋于经典极限条件;经典极限条件还可表为n\lambda^3 \ll 1,其中分子德布罗意波的
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     rac{N}{eta} = NkT,转动贡献热容:C_V^T = Nk,与能量均分定理的结果一致,低温下不适用,需严格计算级数求和
  热波长 \lambda=\frac{h}{p}=\frac{h}{\sqrt{2marepsilon}}pprox rac{h}{\sqrt{2\pi mkT}},分子数密度 n=\frac{N}{V},即分子热波长《分子间距或在体积 \lambda^3 内平均粒子数《 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    7.6 理想气体的熵 对单原子理想气体,经典统计理论得熵:S=rac{3}{2}Nk\ln T+Nk\ln V+rac{3}{2}Nk\left[1+\ln\left(rac{2\pi mk}{h_{\kappa}^{2}}
ight)
ight],非
  7.3 麦克斯韦速度分布律:单位体积内dv_x dv_y dv_z范围内分子数f(v_x,v_y,v_z) dv_x dv_y dv_z = n \left(rac{m}{2\pi kT}
ight)^{3/2}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 绝对婚,随_0不同而不同,且不満足广廷量要求 经典核限条件下,量子理论得熵:S=k\ln\frac{\Omega_{\mathrm{M.B.}}}{N!}=Nk(\ln Z_1-\beta\frac{\partial}{\partial\beta}\ln Z_1)-k\ln N!,代入Z_1用斯特林公式代
     明:V内dp_xdp_ydp_z范围内,分子平动状态数:\frac{V}{h^3}dp_xdp_ydp_z,分子数:\frac{V}{h^3}e^{-\alpha-\frac{1}{2mkT}}(p_x^2+p_y^2+p_z^2)_{dp_xdp_ydp_z}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     RS=rac{3}{2}Nk\ln T+Nk\lnrac{V}{N}+rac{3}{2}Nk\left[rac{5}{3}+\ln\left(rac{2\pi mk}{h^2}
ight)
ight],是绝对熵,满足广延量要求
  对与凝聚相达平衡的饱和蒸汽,视为理想气体,将理想气体物态方程代入熵式得ln p =
  N\left(\frac{m}{2\pi kT}\right)^{3/2} e^{-\frac{m}{2kT}(v_x^2 + v_y^2 + v_z^2)} dv_x dv_y dv_z,除以V即得
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   \ln \left[ k^{5/2} \left( \frac{2\pi m}{h^2} \right)^{3/2} \right] - \frac{S_{
m gas}}{Nk},用克拉珀龙方程S_{
m vap} - S_{
m con} = \frac{L}{T},足够低T下,S_{
m con} \ll \frac{L}{T},\ln p
  速度空间球坐标中的麦氏速度分布律: f(v, \theta, \phi)v^2 \sin\theta dv d\theta d\phi = n \left(\frac{m}{2\pi kT}\right)^{3/2} e^{-\frac{m}{2kT}v^2}v^2 \sin\theta dv d\theta d\phi;对
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    -\frac{L}{RT}+\frac{5}{2}\ln T+\frac{5}{2}+\ln \left[k^{5/2}\left(rac{2\pi m}{h^2}
ight)^{3/2}
ight](萨库尔-铁特罗特公式),与实验相符
 立体角积分得麦氏速率分布律: f(v)dv=\int_0^{2\pi}\int_0^\pi f(v,\theta,\phi)v^2\sin\theta dv d\theta d\phi=4\pi n\left(\frac{m}{2\pi kT}\right)^{3/2}e^{-\frac{m}{2kT}v^2}v^2v^2中速率分布函数 f(v)满足\int_0^\infty f(v)dv=n
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ,其
理想气体的化学势:一个分子的化学势:\mu = \left(\frac{\partial F}{\partial N}\right)_{T,N},代入F式得\mu = -kT\ln\frac{Z_1}{N},代入Z_1^t得\mu =
  最概然速率:使速率分布函数取极大值的速率,v_{m}=\sqrt{\frac{2kT}{m}};由\frac{df(v)}{dv}=0 \Rightarrow v\left(2-\frac{m}{kT}\right)e^{-\frac{m}{2kT}v^{2}}=
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   kT \ln \left[ rac{N}{V} \left( rac{h^2}{2\pi m k T} 
ight)^{3/2} 
ight],经典极限条件下rac{V}{N} \left( rac{2m \pi k T}{h^2} 
ight)^{3/2} \gg 1,故\mu < 0
  0 \mathbb{E} \frac{d^2 f(v)}{dv^2} < 0 \Rightarrow \left[ \left( 2 - \frac{m}{kT} v^2 \right) + v \left( -2 \frac{m}{kT} v \right) + v \left( 2 - \frac{m}{kT} v^2 \right) \left( -\frac{m}{kT} v \right) \right] e^{-\frac{m}{2kT} v^2} < 0 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   7.7 固体热容的爱因斯坦理论 视固体中原子为3N个相同振动频率的振子,其能级:arepsilon_n=\hbar\omega(n+rac{1}{2}),n=0,1,\cdots,振子定
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   域,故遵从玻尔兹曼分布,配分函数: Z_1=\sum_{n=0}^\infty \omega_1 e^{-\beta\hbar\omega}(n+\frac{1}{2})=\frac{e^{-\frac{1}{2}\beta\hbar\omega}}{1-e^{-\beta\hbar\omega}},内能: U=-3N\frac{\partial}{\partial\beta}\ln Z_1=-3N\frac{\partial}{\partial\beta}\ln Z_1=\frac{3N\frac{\hbar\omega}}{2}+\frac{3N\hbar\omega}{e^{\beta\hbar\omega}-1},其中第一项为零点能,第二项为裁查发能;定义特征温度\theta_E满足k\theta_E=\hbar\omega,内
  平均速率:\bar{v}=\frac{1}{n}\int vf(v)dv=4\pi\left(\frac{m}{2\pi kT}\right)^{3/2}\int_0^\infty e^{-\frac{m}{2kT}v^2}v^3dv=\sqrt{\frac{8kT}{\pi m}}
    方均根速率:\overline{v^2} = \frac{1}{n} \int v^2 f(v) dv = 4\pi \left(\frac{m}{2\pi kT}\right)^{3/2} \int_0^\infty e^{-\frac{m}{2kT}} v^2 v^4 dv = \frac{3kT}{m};平均平动动能:arepsilon
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    能: U=\frac{3}{2}Nk\theta+\frac{3Nk\theta_E}{e^{\theta}E/T-1} , 热容: C_V=\left(\frac{\partial U}{\partial T}\right)_V=3Nk\left(\frac{\theta_E}{T}\right)^2\frac{e^{\theta}E/T}{(e^{\theta}E/T-1)^2} ; 当T\gg\theta_E,e^{\theta}E/T-1
1pprox rac{	heta_E}{T}, C_V = 3Nk;当T \ll 	heta_E, e^{	heta_E/T} - 1 pprox e^{	heta_E/T}, C_V pprox 3Nk \left(rac{	heta}{T}
ight)^2 e^{-	heta_E/T} 
ightarrow 0;因相同振动频
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   1 \approx \frac{\pi}{F} 、CV = 3 いた、 2 = 5 、 CV = 5 いた、 2 = 5 、 CV = 5 いた、 2 = 5 、 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に 2 = 5 に
  n \left( \frac{m}{2\pi kT} \right)^{3/2} \left[ \int_{-\infty}^{+\infty} e^{-\frac{m}{2kT} v_y^2} dv_y \right] \int_0^{+\infty} e^{-\frac{m}{2kT} v_x^2} v_x dv_x = n \sqrt{\frac{kT}{2\pi m}}
  压强:p=rac{n_mRT}{V};证明:在dt内碰到dA上,dv_xdv_ydv_z范围内的分子受到器壁冲量dI=2mv_xd\Gamma dAdt使
  分子速度由v_x变为-v_x,压强dp = (dI/dt)/dA = 2mv_x\Gamma = 2mv_x^2fdv_xdv_ydv_z

p = 2m\int_{-\infty}^{+\infty}dv_y\int_{-\infty}^{+\infty}dv_z\int_{0}^{+\infty}fv_x^2dv_x,由\int_{0}^{+\infty}e^{-\alpha x^2}x^2dx = \frac{\sqrt{\pi}}{4}\alpha^{-3/2}得p
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     \frac{\mu B}{kT}, M = \frac{n\mu^2}{kT}B = \chi H,其中磁化率\chi = n\mu^2\mu_0/kT;强场或低温下, \frac{\mu B}{kT} \gg 1, e^{\mu B/kT} \gg
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    kT , M — kT — 
  2mn \left(\frac{m}{2\pi kT}\right)^{3/2} \left[ \int_{-\infty}^{+\infty} e^{-\frac{m}{2kT} v_y^2} dv_y \right] \int_{0}^{+\infty} e^{-\frac{m}{2kT} v_x^2} dv_x = nkT = \frac{N}{V} kT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     单位体积的熵:s=nk\left(\ln Z_1-\beta\frac{\partial}{\partial\beta}\ln Z_1\right)=nk\left[\ln 2+\ln\cosh\left(\frac{\mu B}{kT}\right)-\left(\frac{\mu B}{kT}\right)\tanh\left(\frac{\mu B}{kT}\right)\right]; 弱
     了。
7.4 能量均分定理:对处在温度为了的平衡态的经典系统,粒子能量中的每一平方项的平均值为kT/2;证明:视系统为经典系统,粒
     子总能量为动能与势能之和\varepsilon=\varepsilon_p+\varepsilon_q=\frac{1}{2}\sum_{i=1}^r a_i p_i^2+\frac{1}{2}\sum_{i=1}^{r'} b_i q_i^2+\varepsilon_q' (q_{r'+1}+a_i,b_i)>0且与p_1,\cdots,p_r,q_1,\cdots,q_r'无关,故分布:a=\frac{1}{h^r}e^{-\alpha-\beta\varepsilon}dp_1\cdots dp_rdq_1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     场/高温下, \frac{\mu B}{kT} 《 1, \tanh\left(\frac{\mu B}{kT}\right) ≈ \frac{\mu B}{kT}, \ln\cosh\left(\frac{\mu B}{kT}\right) ≈ \ln\left[1+\frac{1}{2}\left(\frac{\mu B}{kT}\right)^2\right] ≈ \frac{1}{2}\left(\frac{\mu B}{kT}\right)^2, s
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     nk\ln 2=k\ln 2^n,礦矩消/逆外场方向的概率近似相等,每个礦矩各有2个可能的状态,单位体积微观态数。2^n,强场/低下,\frac{\mu B}{kT}\gg 1,\cosh\left(\frac{\mu B}{kT}\right)\approx \frac{1}{2}e^{\mu B/kT},\tan h\left(\frac{\mu B}{kT}\right)\approx 1,s=0,礦矩均沿外场方向,系统仅1微观态
  \frac{N}{Z_1h^r}e^{-\beta\varepsilon}dp_1\cdots dp_rdq_1\cdots dq_r,其中配分函数 Z_1=\frac{h^r}{h^r}\int\cdots\int_{-\infty}^{+\infty}e^{-\beta\varepsilon}dp_1\cdots dp_rdq_1\cdots dq_r,能量表达式中任意平方项平均值 \frac{1}{2}a_ip_i^2=\frac{1}{N}\int\cdots\int_{-\infty}^{+\infty}\frac{1}{2}a_ip_i^2e^{-\alpha-\beta\varepsilon}\frac{1}{h^r}dp_1\cdots dp_rdq_1\cdots dq_r=\frac{1}{N}\int\cdots\int_{-\infty}^{+\infty}\frac{1}{N}e^{-\alpha-\beta\varepsilon}\frac{1}{N}e^{-\alpha-\beta\varepsilon}\frac{1}{N}e^{-\alpha-\beta\varepsilon}\frac{1}{N}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e^{-\alpha-\beta\varepsilon}e
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    7.9 负温度状态 由dU=TdS+Ydy有rac{1}{T}=\left(rac{\partial S}{\partial U}
ight)_y;当系统的内能增加而熵反而减小时,系统就处在负温度状态
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   \frac{1}{Z_1h^r}\int\cdots\int_{-\infty}^{+\infty}\frac{1}{2}a_ip_i^2e^{-\beta\varepsilon'}-\frac{\beta}{2}a_ip_i^2dp_1\cdots dp_rdq_1\cdots dq_r=\frac{1}{Z_1h^r}\int\cdots\int_{-\infty}^{+\infty}dp_1\cdots dp_{i-1}dp_i
 Nk\left[\ln 2 - rac{1}{2}\left(1 + rac{E}{Narepsilon}
ight)\ln\left(1 + rac{E}{Narepsilon}
ight) - rac{1}{2}\left(1 - rac{E}{Narepsilon}
ight)\ln\left(1 - rac{E}{Narepsilon}
ight)
ight],从前 rac{1}{T} = \left(rac{\partial S}{\partial E}
ight)_B
  \frac{k}{2\varepsilon} \ln \frac{N\varepsilon - E}{N\varepsilon + E}; 当 E < 0, T > 0,正温状态; 当 E < 0, T < 0,负温状态
     dq_1 \cdots dq_r = \frac{1}{2\beta Z_1 h^r} \int \cdots \int_{-\infty}^{+\infty} e^{-\beta \varepsilon} dp_1 \cdots dp_r dq_1 \cdots dq_r = \frac{1}{2\beta} = \frac{1}{2} kT, \exists p \in \mathbb{Z}, \exists p \in
     对单原子分子,质心平动动能:arepsilon=rac{1}{2m}(p_x^2+p_y^2+p_z^2);分子平均能量:arepsilon=rac{3}{2}kT;总内能:U=arepsilon N=0
  容:C_V=rac{dU}{dT}=rac{3}{2}Nk;定压热容:C_p=C_V+Nk=rac{5}{2}Nk;热容比:rac{C_p}{C_V}=rac{5}{3};未考虑原子内电子,需量子理论再解释
  Chap8 玻色统计和费米统计 8.1 热力学量的统计表达式 非简并性条件:e^{\alpha} = \frac{V}{N} \left( \frac{2\pi nkT}{h^2} \right) \ll 1;非简并性气体:满足引
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   内部结构,仅考虑平动自由度,分子能量:\varepsilon = \frac{1}{2m}(p_x^2 + p_y^2 + p_z^2),V内\varepsilon \sim \varepsilon + d\varepsilon范围内分子可能的微观态数:D(\varepsilon)d\varepsilon = g\frac{2\pi V}{h^3}(2m)^{3/2}\varepsilon^{1/2}d\varepsilon,其中g—自旋导致的简并度,拉氏乘子\alpha满足粒子。
  玻色分布:a_l=rac{\omega_l}{e^{lpha+etaarepsilon_l-1}};\;系统平均总粒子数:ar{N}=\sum_lrac{\omega_l}{e^{lpha+etaarepsilon_l-1}};\;系统平均内能:U=\sum_lrac{arepsilon_l\omega_l}{e^{lpha+etaarepsilon_l-1}}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    数:N = g \frac{2\pi V}{h^3} (2m)^{3/2} \int_0^\infty \frac{\varepsilon^{1/2}}{e^{\alpha+\beta\varepsilon+1}},内能:U = g \frac{2\pi V}{h^3} (2m)^{3/2} \int_0^\infty \frac{\varepsilon^{3/2} d\varepsilon}{e^{\alpha+\beta\varepsilon+1}},设尔
  巨配分函数:\Xi = \prod_l [1 - e^{-\alpha - \beta \varepsilon_l}]^{-\omega_l},其对数:\ln \Xi = -\sum_l \omega_l \alpha \ln (1 - e^{-\alpha - \beta \varepsilon_l}) 系统平均总粒子数:\overline{N} = -\frac{\partial}{\partial \alpha} \ln \Xi; 内能:U = \sum_l \varepsilon_l \alpha_l = -\frac{\partial}{\partial \beta} \ln \Xi
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    \beta \varepsilon, N = g \frac{2\pi V}{h^3} (2mkT)^{3/2} \int_0^\infty \frac{x^{1/2}}{e^{\alpha + x} + 1}, U = g \frac{2\pi V}{h^3} (2mkT)^{3/2} kT \int_0^\infty \frac{x^{3/2} dx}{e^{\alpha + x} + 1},被根函
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    数分母 \frac{1}{e^{\alpha+x}\pm 1} = \frac{1}{e^{\alpha+x}(1\pm e^{-\alpha-x})}, \pm e^{-\alpha}, \frac{1}{e^{\alpha+x}\pm 1} \approx e^{-\alpha-x}(1\mp e^{-\alpha-x}), 回代
  广义力:Y = \sum_{l} \frac{\partial \varepsilon_{l}}{\partial y} = \sum_{l} \frac{\partial \varepsilon_{l}}{\partial y} \frac{\omega_{l}}{e^{\alpha + \beta \varepsilon_{l}} - 1};压强:p = \frac{1}{\beta} \frac{\partial}{\partial V} \ln \Xi
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    \#N = g \left(\frac{2\pi mkT}{h^2}\right)^{3/2} Ve^{-\alpha} (1 \mp 2^{-3/2}e^{-\alpha}), U = \frac{3}{2} g \left(\frac{2\pi mkT}{h^2}\right)^{3/2} VkTe^{-\alpha} (1 \mp 2^{-3/2}e^{-\alpha}), U = \frac{3}{2} g \left(\frac{2\pi mkT}{h^2}\right)^{3/2} VkTe^{-\alpha} (1 \mp 2^{-3/2}e^{-\alpha}), U = \frac{3}{2} g \left(\frac{2\pi mkT}{h^2}\right)^{3/2} VkTe^{-\alpha} (1 \mp 2^{-3/2}e^{-\alpha}), U = \frac{3}{2} g \left(\frac{2\pi mkT}{h^2}\right)^{3/2} VkTe^{-\alpha} (1 \mp 2^{-3/2}e^{-\alpha}), U = \frac{3}{2} g \left(\frac{2\pi mkT}{h^2}\right)^{3/2} VkTe^{-\alpha} (1 \mp 2^{-3/2}e^{-\alpha}), U = \frac{3}{2} g \left(\frac{2\pi mkT}{h^2}\right)^{3/2} VkTe^{-\alpha} (1 \mp 2^{-3/2}e^{-\alpha}), U = \frac{3}{2} g \left(\frac{2\pi mkT}{h^2}\right)^{3/2} VkTe^{-\alpha} (1 \mp 2^{-3/2}e^{-\alpha}), U = \frac{3}{2} g \left(\frac{2\pi mkT}{h^2}\right)^{3/2} VkTe^{-\alpha} (1 \mp 2^{-3/2}e^{-\alpha}), U = \frac{3}{2} g \left(\frac{2\pi mkT}{h^2}\right)^{3/2} VkTe^{-\alpha} (1 \mp 2^{-3/2}e^{-\alpha}), U = \frac{3}{2} g \left(\frac{2\pi mkT}{h^2}\right)^{3/2} VkTe^{-\alpha} (1 \mp 2^{-3/2}e^{-\alpha}), U = \frac{3}{2} g \left(\frac{2\pi mkT}{h^2}\right)^{3/2} VkTe^{-\alpha} (1 \mp 2^{-3/2}e^{-\alpha}), U = \frac{3}{2} g \left(\frac{2\pi mkT}{h^2}\right)^{3/2} VkTe^{-\alpha} (1 \mp 2^{-3/2}e^{-\alpha}), U = \frac{3}{2} g \left(\frac{2\pi mkT}{h^2}\right)^{3/2} VkTe^{-\alpha} (1 \mp 2^{-3/2}e^{-\alpha}), U = \frac{3}{2} g \left(\frac{2\pi mkT}{h^2}\right)^{3/2} VkTe^{-\alpha} (1 \mp 2^{-3/2}e^{-\alpha}), U = \frac{3}{2} g \left(\frac{2\pi mkT}{h^2}\right)^{3/2} VkTe^{-\alpha} (1 \mp 2^{-3/2}e^{-\alpha}), U = \frac{3}{2} g \left(\frac{2\pi mkT}{h^2}\right)^{3/2} VkTe^{-\alpha} (1 \mp 2^{-3/2}e^{-\alpha}), U = \frac{3}{2} g \left(\frac{2\pi mkT}{h^2}\right)^{3/2} VkTe^{-\alpha} (1 \mp 2^{-3/2}e^{-\alpha}), U = \frac{3}{2} g \left(\frac{2\pi mkT}{h^2}\right)^{3/2} VkTe^{-\alpha} (1 \mp 2^{-3/2}e^{-\alpha}), U = \frac{3}{2} g \left(\frac{2\pi mkT}{h^2}\right)^{3/2} VkTe^{-\alpha} (1 \mp 2^{-3/2}e^{-\alpha}), U = \frac{3}{2} g \left(\frac{2\pi mkT}{h^2}\right)^{3/2} VkTe^{-\alpha} (1 \mp 2^{-3/2}e^{-\alpha}), U = \frac{3}{2} g \left(\frac{2\pi mkT}{h^2}\right)^{3/2} VkTe^{-\alpha} (1 \mp 2^{-3/2}e^{-\alpha})
     eta\left(dU-Ydy+rac{lpha}{eta}d\overline{N}
ight) = -eta d\left(rac{\partial\ln\Xi}{\partialeta}
ight) + rac{\partial\ln\Xi}{\partial y}dy - alpha d\left(rac{\partial\ln\Xi}{\partiallpha}
ight),因加至为lpha,eta,eta的函数,其
     全徽分:d(\ln \Xi) = \frac{\partial \Xi}{\partial \alpha} d\alpha + \frac{\partial \ln \Xi}{\partial \beta} d\beta + \frac{\partial \ln \Xi}{\partial y} dy,代入前式得\beta \left( dU - Y dy + \frac{\alpha}{\beta} \frac{\partial}{\partial \beta} \overline{N} \right)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    2^{-5/2}e^{-\alpha}) = \frac{3}{2}NkT(1 \pm 2^{-5/2}e^{-\alpha}), e^{-\alpha}零级近似 = \frac{1}{g}\frac{N}{V}\left(\frac{h^2}{2\pi mkT}\right)^{3/2}, U
  d\left(\ln\Xi - \alpha \frac{\partial}{\partial\alpha} \ln\Xi - \beta \frac{\partial}{\partial\beta} \ln\Xi\right), 比较开系热力学基本方程 \frac{1}{T} (dU - Y dy - \mu d\overline{N}) = dS 得 \beta = \frac{1}{kT}, \alpha = 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     \frac{3}{2}NkT\left[1\pm 2^{-5/2}\frac{1}{q}\frac{N}{V}\left(\frac{h^2}{2\pi mkT}\right)^{3/2}\right] = \frac{3}{2}NkT\left(1\pm 2^{-5/2}n\lambda^3\right),其中第一项为内能,第二项为由微观
        -\frac{\mu}{kT}, \text{$\!\!\!\!/} \text{$\!\!\!/} \text{$\!\!\!\!/} \text{$\!\!\!/} \text{$\!\!\!\!/} \text{$\!\!\!\!/} \text{$\!\!\!\!/} \text{$\!\!\!\!/} \text{$\!\!\!/} \text{$\!\!\!\!/} \text{$\!\!\!\!/} \text{$\!\!\!\!/} \text{$\!\!\!\!/} \text{$\!\!\!\!
     機米分布:a_l = \frac{\omega_l}{e^{\alpha+\beta}\varepsilon_{l+1}}; 巨配分函数:\Xi = \sum_l [1 + e^{-\alpha-\beta}\varepsilon_l]^{\omega_l},其对数:\ln\Xi = \sum_l \omega_l \ln(1 + e^{-\alpha-\beta}\varepsilon_l)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     権力主向は原達力能的量)張リスポテス的増加が悪。数本、作的制加がRE> 0、数と (特別的加がRE> 0、など、特別の加がRE> 0、など、RE● 1 は、RE● 1 は、R
```

 $rac{1}{I}(p_{ heta}^2+rac{1}{\sin^2 heta}p_{arphi}^2)+rac{1}{2m\mu}p_r^2+u(r)$;不考虑后两项,分子平均能量: $ar{arepsilon}=rac{5}{2}kT$;总内能: $U=ar{arepsilon}N=ar{arepsilon}$

```
0,\mu由 rac{1}{V}\sum_{l}rac{\omega_{l}}{e^{(arepsilon_{l}-\mu)/kT}-1} = rac{N}{V} = n确定为T和粒子数密度n的函数,足够高T下由D(arepsilon)darepsilon
 \frac{2\pi V}{h^3} (2m)^{3/2} \varepsilon^{1/2} d\varepsilon求和用积分代替,\frac{2\pi}{h^3} (2m)^{3/2} \int_0^\infty \frac{\varepsilon^{1/2} d\varepsilon}{e^{(\varepsilon-\mu)/kT} - 1} = n, \mu \uparrow 随 T \downarrow, \exists T \to 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      对费米分布,能量\epsilon的1个量子态上平均电子数:f=\frac{1}{e^{(\varepsilon-\mu)/kT}+1};T=0下,f=1, \varepsilon
> \mu_0;电子自旋在动量方向上的投影有两个值,V内d\varepsilon内电子的量子态数: \frac{4\pi V}{h^3}(2m)^{3/2}\varepsilon^{1/2}d\varepsilon,平均电子
 式化为\frac{2\pi}{h^3}(2mkT_c)^{3/2}\int_0^\infty \frac{x^{1/2}dx}{e^x-1} = n \Rightarrow T_c = \frac{2\pi}{2.612^{2/3}}\frac{\hbar^2}{mk}n^{2/3},当T < T_c, \mu = \frac{2\pi}{2.612^{2/3}}\frac{\hbar^2}{mk}n^{2/3}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   数: \frac{4\pi V}{\hbar^3}(2m)^{3/2}\frac{\varepsilon^{1/2}}{e(\varepsilon-\mu)/kT+1},给定 N,T,V 下 \mu 满足 总电子数: N=\frac{4\pi V}{\hbar^3}(2m)^{3/2}\int_0^\infty\frac{\varepsilon^{1/2}}{e(\varepsilon-\mu)/kT+1} ; T=\frac{2\pi V}{\hbar^3}(2m)^{3/2}\int_0^\infty\frac{\varepsilon^{1/2}}{e(\varepsilon-\mu)/kT+1}
 0, \frac{2\pi}{h^3} (2m)^{3/2} \int_0^\infty \frac{\varepsilon^{1/2} d\varepsilon}{e^{(\varepsilon-\mu)/kT} - 1} < n,产生这一矛盾是因为用积分代替求和,忽略了\varepsilon = 0项,足够高T下,能
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   0 \top, N \ = \ \int_0^{\mu(0)} \ \Rightarrow \ \text{费米能级} : T \ = \ O \top, \\ \text{电子最大能量} \\ \mu(0) \ = \ \frac{\hbar^2}{2m} \left(3\pi^2 \frac{N}{V}\right)^{2/3},  对常温T, \mu(T) \ \sim \ \mu_0 \ \ll 1
                                    = 0上粒子数相比总粒子数为一可忽略的小量,足够低T下,能级arepsilon = 0上粒子数可观,不可忽略,当T < T_c,n_0(T) +
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        -\mu/kT\ll 1,这说明金属中自由电子高度简并;费米动量:p_F=\sqrt{2m\mu(0)}=(3\pi^2n)^{1/3}\hbar;费米速
 总内能:U = \frac{4\pi V}{h^3} (2m)^{3/2} \int_0^{\mu(0)} \varepsilon^{3/2} d\varepsilon = \frac{3}{5} N\mu(0),分子平均能量:\frac{3}{5}\mu(0),电子气体的简并压:p(0)
   级上粒子数密度n_{arepsilon>0}=rac{2\pi}{h^3}(2mkT)^{3/2}\int_0^\inftyrac{x^{1/2}dx}{e^x-1}=n\left(rac{T}{T_c}
ight)^{3/2};玻色-爱因斯坦凝聚:当T< T_c与总粒子数
意文 -1 (T_C) (T
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     显著差异,从而对热容有贡献;能量在\mu附近kT范围内对热容有贡献的有效电子数:N有效 pprox rac{kT}{\mu}N,将能量均分定理用于有效电
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     子,每一有效电子贡献热容 \frac{3}{2} k,金屬中自由电子热容的贡献:C_V = \frac{3}{2}Nk\left(\frac{kT}{\mu}\right),室温下 \frac{kT}{\mu} \ll 1 N 和U均可写为I = \int_0^\infty \frac{\eta(\varepsilon)d\varepsilon}{e^{(\varepsilon-\mu)/k\mu}+1},其中\eta(\varepsilon)分别= C\varepsilon^{1/2},C\varepsilon^{3/2},C = \frac{4\pi V}{h^3}(2m)^{3/2},设\varepsilon - \mu = 1
    弱作用玻色气体凝聚:临界条件:n\lambda^3=n\left(rac{h}{\sqrt{2\pi mkT_C}}
ight)=2.612;当热波长与分子何平均距离具有相同量级,量子关联起决
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      kTz, I = \int_{-\mu/kT}^{\infty} \frac{\eta(\mu + kTz)}{e^2 + 1} kTdz = kT \int_{0}^{\mu/kT} \frac{\eta(\mu - kTz)}{e^{-z} + 1} dz + kT \int_{0}^{\infty} \frac{\eta(\mu + kTz)}{e^2 + 1} dz = kT \int_{0}^{\infty} \frac{\eta(\mu + kTz)}{e^2 + 1} dz
                                                          kT \int_{0}^{\mu/kT} \eta(\mu - kTz) dz - kT \int_{0}^{\mu/kT} \frac{\eta(\mu - kTz)}{e^{z} + 1} dz + kT \int_{0}^{\infty} \frac{\eta(\mu + kTz)}{e^{z} + 1} dz = \int_{0}^{\mu} \eta(\varepsilon) \varepsilon^{-\frac{1}{2}} dz
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      kT \int_0^{\mu/kT} \frac{\eta(\mu - kTz)}{e^z + 1} dz + kT \int_0^{\infty} \frac{\eta(\mu + kT)}{e^z + 1} dz, \exists \mu/kT \gg 1, I = \int_0^{\mu} \eta(\varepsilon) d\varepsilon
          「 大石闕偏振V内p\sim p+dp范围内,光子量子态數: \frac{8\pi V}{h^3}\,p^2dp,\omega\sim\omega+d\omega范围内,光子量子态數 \frac{V}{\pi^2c^3}\omega^2d\omega,"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   kT \int_0^\infty \frac{\eta(\mu + kTz) - \eta(\mu - kTz)}{e^z + 1} \, dz,  分子泰勒关于z展开得I = \int_0^\mu \eta(\varepsilon) d\varepsilon + 2(kT)^2 \eta'(\mu) \int_0^\infty \frac{zdz}{e^z + 1} + \cdots = \int_0^\mu \eta(\varepsilon) d\varepsilon + \frac{\pi^2}{6} (kT)^2 \eta'(\mu) + \cdots,  故U = \frac{2}{5} C \mu^{5/2} \left[ 1 + \frac{5\pi^2}{8} \left( \frac{kT}{\mu} \right)^2 \right],  N = \frac{\pi^2}{6} (kT)^2 \eta'(\mu) + \cdots + \frac{\pi
   均光子数: \frac{V}{\pi^2 c^3} \frac{\omega^2 d\omega}{e^{\hbar \omega/kT} - 1}, 普朗克公式: V内d\omega内, 辐射场的内能U(\omega, T)d\omega = \frac{V}{\pi^2 c^3} \frac{\hbar \omega^3 d\omega}{e^{\hbar \omega/kT} - 1}; 低频范
围,\frac{\hbar\omega}{kT} 《 1,e^{\hbar\omega/kT} ≈ 1+\frac{\hbar\omega}{kT}, 普氏公式近似为瑞利-金斯公式: U(\omega,T)d\omega=\frac{V}{\pi^2c^3}\omega^3kTd\omega; 高频范围,\frac{\hbar\omega}{kT} 》 1,e^{\hbar\omega/kT} 》 1,e^{\hbar\omega/k
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      \frac{2}{3} \, C \mu^{3/2} \left[ 1 + \frac{\pi^2}{8} \left( \frac{kT}{\mu} \right)^2 \right] \quad \Rightarrow \quad \mu \quad = \quad \frac{\hbar^2}{2m} \left( \frac{3N\pi^2}{V} \right)^{2/3} \left[ 1 + \frac{\pi^2}{8} \left( \frac{kT}{\mu} \right)^2 \right]^{-2/3} , \text{代入} \mu_0  式且在
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   第二項中用 \frac{kT}{\mu_0} 代替 \frac{kT}{\mu} 得 \mu = \mu_0 \left[1 + \frac{\pi^2}{8} \left(\frac{kT}{\mu_0}\right)^2\right]^{-2/3} \approx \mu_0 \left[1 - \frac{\pi^2}{12} \left(\frac{kT}{\mu_0}\right)^2\right];内能:U = \frac{\pi^2}{12} \left(\frac{kT}{\mu_0}\right)^2
 能:U=rac{V}{\pi^2c^3}\int_0^\inftyrac{\hbar\omega^3d\omega}{e^{\hbar\omega/kT}-1}d\omega,设y=rac{\hbar\omega}{kT} , U=rac{V\hbar}{\pi^2c^3}\left(rac{kT}{\hbar}
ight)\int_0^\inftyrac{y^3dy}{e^y-1}=rac{\pi^2k^4}{15c^3\hbar^3}VT^4 (斯-玻定
 律);能量密度极值满足 \frac{d}{dy}\left(\frac{y^3}{e^y-1}\right)=0 \Rightarrow 3-3e^{-y}=y \Rightarrow \frac{\hbar\omega_m}{kT}\approx 2.822
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     \frac{2}{5}C\mu_0^{5/2} \left[1 - \frac{\pi}{12} \left(\frac{kT}{\mu_0}\right)^2\right]^{5/2} \left[1 + \frac{5\pi^2}{8} \left(\frac{kT}{\mu_0}\right)^2\right] \\ = \frac{3}{5}N\mu_0 \left[1 + \frac{5}{12}\pi^2 \left(\frac{kT}{\mu_0}\right)^2\right]; \text{e}\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{--}5\text{
 光子气体的巨配分函数:\ln\Xi = -\sum_s \omega_l \ln(1-e^{-\beta\varepsilon}l) = -\frac{V}{\pi^2c^3} \int_0^\infty \omega^2 \ln(1-e^{-\beta\hbar\omega})d\omega、设x=0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      容:C_V = \left(\frac{\partial U}{\partial T}\right)_V = Nk^2\frac{\pi^2}{2}\left(\frac{kT}{\mu_0}\right) = \gamma_0 T;低温下金属热容:电子和离子振动贡献热容之和C_V = \gamma T + AT^3
   \frac{\hbar \omega}{kT}, \ln \Xi = -\frac{V}{\pi^2 c^3} \left(\frac{1}{\beta \hbar}\right)^3 \int_0^\infty x^2 \ln(1 - e^{-x}) dx = \frac{\pi^2 V}{45 c^3} \left(\frac{1}{\beta \hbar}\right)^3, 内能: U = -\frac{\partial}{\partial \beta} \ln \Xi = -\frac{\hbar \omega}{\hbar V}
    \frac{\pi^2 k^4 V}{15 c^3 \hbar^3} T^4, 压强: p = -\frac{1}{\beta} \frac{\partial}{\partial V} \ln \Xi = \frac{\pi^2 k^4}{45 c^3 \hbar^3} T^4 = \frac{1}{3} \frac{U}{V},  熵: S = k (\ln \Xi - \beta U)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     \frac{5}{2}\,Nk, E(N,S,V) \ = \ \frac{3h^2\,N^{5/3}}{4\pi m V^{2/3}}e^{\frac{2S}{3Nk}-\frac{5}{3}}, T \ = \ \left(\frac{\partial E}{\partial S}\right)_{N,V} \ = \ \frac{2}{3Nk}\,E, E \ = \ \frac{3}{2}\,NkT, p \ 
          2hap9 系综理论 9.1 相空间刘维尔定理 最概然统计方法:适用于近独立粒子系统;系综理论:可处理粒子间有相互作用的系统计系综:一定宏观条件下,大量性质现结构完全相同的处于各种微观状态的各自独立的系统的集合 
统理论的两点假设:宏观量是相应微观量的时间平均,时间平均等价于系统平均;平衡孤立系的一切可能微观态出现概率相等
个粒子自由度:r,水个全间粒子组成的系统自由度:f=Nr;任一时刻系统微观态由f个广义坐标q_1, \dots, q_f和f个相应的
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      -\left(\frac{\partial E}{\partial V}\right)_{N,S}=rac{2}{3}rac{E}{V},以上两式联立得pV=NkT,S=Nk\ln\left[rac{V}{N}\left(rac{2\pi mkT}{h^2}
ight)^{3/2}
ight]+rac{5}{2}Nk
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     9.4 正则条综 证则分布:有峒定N,V,江阳系统的가中函权 设有确定N,V,T的系统与大热源接触,热源很大,能交不改变热源温度,E^{(0)}=E+E_r,E\ll E^{(0)},平衡后两者温度相 E_r,平衡态下每个可能微观状态出观概率相等,故系统处于状态E_r的概率E_r0 E_r1 E_r1 E_r2 E_r3 E_r3 E_r4 E_r5 E_r6 E_r7 E_r7 E_r8 E_r9 E
   \overline{E} (1) ある。 \overline{G} (1) カステンス (1) カステンス (1) カステンス (2) カステンス (2) カステンス (3) カステンス (4) カステンス (4) カステンス (5) カステンス (5) カステンス (5) カステンス (6) カステンス (
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   \ln \Omega_T(E^{\left(0\right)}) - \beta E_S,其中\beta = \left(\frac{\partial \ln \Omega_T}{\partial E_T}\right)_{E_T=E^{\left(0\right)}} = \frac{1}{kT},T-热灏温度,因达热平衡,亦系统温度,故\rho_S \propto T
    刘维尔定理: \frac{d\rho}{dt} = 0;证:\rho(q_i + \dot{q}_i dt, p_i + \dot{p}_i dt, t + dt) = \rho + \frac{d\rho}{dt} dt, \frac{d\rho}{dt} = \frac{\partial \rho}{\partial t}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      e^{-eta E_S},归一化得
ho_S=rac{1}{2}e^{-eta E_S},其中配分函数:Z=\sum_S e^{-eta E_S},\sum_S为对(N,V)的系统的所有微观态求》
 \sum_i \left[ rac{\partial 
ho}{\partial q_i} \dot{q}_i + rac{\partial 
ho}{\partial p_i} \dot{p}_i 
ight] , d\Omega以2f对平面q_i, q_i + dq_i; p_i, p_i + dp_i (i = 1, \cdots, f)为边界,t时
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     统处于微观态s的概率仅与E_s有关;若E_l表示系统各个能级,\Omega_l表示其简并度,则系统处于E_l的概率:
ho_l = rac{1}{Z}\Omega_l e^{-eta E_l},其
                                                                                                                                             + dt时刻代表点数:\left(\rho+\frac{\partial\rho}{\partial t}dt\right)d\Omega,dt内代表点数增加\frac{\partial\rho}{dt}dtd\Omega,d\Omega在平面q_i上的
   边界面积:dA = dq_1 \cdots dq_{i-1} dq_{i+1} \cdots dq_f dp_1 \cdots dp_f,dt内经dA入d代表点数:\rho \dot{q}_i dt dA,经平面q_i + dq_i出d\Omega代表点数:(\rho \dot{q}_i)_{q_i+dq_i} dt dA = \left[ (\rho \dot{q}_i)_{q_i} + \frac{\partial}{\partial q_i} (\rho \dot{q}_i) dq_i \right] dt dA,以上两式相減
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      T கால்கZ = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = Z = 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      9.5 正则系综理论的热力学公式 内能:U=\overline{E}=rac{1}{Z}\sum_s E_s e^{-eta E_s}=rac{1}{Z}\left(-rac{\partial}{\partialeta}
ight)\sum_s e^{-eta E_s}=-rac{\partial}{\partialeta}\ln Z
   得dt内经一对平面q_i,q_i + dq_i净入d\Omega代表点数:-\frac{\partial}{\partial q_i}(\rho \dot{q}_i)dq_i^{\dagger}dtdA = -\frac{\partial}{\partial q_i}(\rho \dot{q}_i)dtd\Omega,同理经一对平
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   广义力: Y=rac{1}{Z}\sum_{s}rac{\partial E_{s}}{\partial y}e^{-eta E_{s}}=rac{1}{Z}\left(-rac{1}{eta}rac{\partial}{\partial y}
ight)\sum_{s}e^{-eta E_{s}}=-rac{1}{eta}rac{\partial}{\partial y}\ln Z; 压强: p=rac{1}{eta}rac{\partial}{\partial V}\ln Z
 面p_i和p_i + dp_i净入d\Omega代表点数:-\frac{\partial}{\partial p_i}(\rho\dot{p}_i)dtd\Omega,以上两式相加并对i求和得在dt内净入d\Omega代表点数:\frac{\partial \rho}{\partial t}dtd\Omega =
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      eta(dU-Ydy) \,=\, -eta d\left(rac{\partial}{\partialeta}\ln Z
ight) + rac{\partial}{\partial y}\ln Zdy,因Z为eta,y的函数,\ln Z的全微分为d\ln Z \,=\, rac{\partial}{\partialeta}\ln Zdeta +
 -\sum_{i}\left[\frac{\partial(\rho\dot{q}_{i})}{\partial q_{i}}+\frac{\partial(\rho\dot{p}_{i})}{\partial p_{i}}\right]dtd\Omega \Rightarrow \frac{\partial\rho}{\partial t}+\sum_{i}\left[\frac{\partial(\rho\dot{q}_{i})}{\partial q_{i}}+\frac{\partial(\rho\dot{p}_{i})}{\partial p_{i}}\right]=0,由正则方程有 \frac{\partial\dot{q}_{i}}{\partial q_{i}}+\frac{\partial\dot{p}_{i}}{\partial p_{i}}=0,从
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      \frac{\partial}{\partial y} \ln Z dy,代入前式得\beta (dU - Y dy) = d \left( \ln Z - \beta \frac{\partial}{\partial \beta} \ln Z \right),这说明\beta为dU - Y dy的积分因子,与热力学公
 而 \frac{d\rho}{dt} = \frac{\partial \rho}{\partial t} + \sum_i \left[ \frac{\partial \rho}{\partial q_i} \dot{q}_i + \frac{\partial \rho}{\partial p_i} \dot{p}_i \right] = 0,这说明若随一代表点在相空间中运动,其邻域内代表点密度恒定;刘氏定理(另
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      式 rac{1}{T}(dU-Ydy)=dS比较得eta=rac{1}{kT},S=k\left(\ln Z-etarac{\partial}{\partialeta}\ln Z
ight);自由能:F=U-TS=-kT\ln Z
m \overline{dt} = \overline{\partial t} + \Sigma_i \left[ \overline{\partial q_i} q_i + \overline{\partial p_i} p_i \right] = 0, \Sigma \overline{\partial t} = 0, \Sigma \overline{\partial t} = -\Sigma_i \left[ \overline{\partial q_i} \overline{\partial p_i} - \overline{\partial p_i} \overline{\partial q_i} \right] = 0, \Sigma \overline{\partial t} = 0; \overline{\partial t} = 0; \overline{\partial t} = -\Sigma_i \left[ \overline{\partial q_i} \overline{\partial p_i} - \overline{\partial p_i} \overline{\partial q_i} \right] = 0, \overline{\partial t} = 0; \overline{\partial t} = 0; \overline{\partial t} = -\Sigma_i \left[ \overline{\partial t} - \overline{\partial t} - \overline{\partial t} - \overline{\partial t} \right] = 0, \overline{\partial t} = 0; \overline{\partial t} = -\Sigma_i \left[ \overline{\partial t} - \overline{\partial t} - \overline{\partial t} - \overline{\partial t} - \overline{\partial t} \right] = 0, \overline{\partial t} = 0; \overline{\partial t} = -\Sigma_i \left[ \overline{\partial t} - \overline{\partial t} \right] = 0, \overline{\partial t} = -\Sigma_i \left[ \overline{\partial t} - \overline{\partial t} \right] = 0, \overline{\partial t} = -\Sigma_i \left[ \overline{\partial t} - \overline{\partial t} -
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      \sum_{s} 
ho_{s} \left[ E_{s}^{2} - 2\overline{E}E_{s} + (\overline{E})^{2} \right] = \sum_{s} 
ho_{s} E_{s}^{2} - 2\overline{E} \sum_{s} 
ho_{s} E_{s} + (\overline{E})^{2} \sum_{s} 
ho_{s} = \overline{E^{2}} - (\overline{E})^{2};对正则分布, \frac{\partial \overline{E}}{\partial eta} = \overline{E^{2}} - (\overline{E})^{2}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      -\frac{\partial \overline{E}}{\partial \beta} = kT^2 \frac{\partial \overline{E}}{\partial T} = kT^2 C_V, \text{能量相对涨落} : \frac{\overline{(E-\overline{E})^2}}{\overline{(E)^2}} = \frac{kT^2 C_V}{\overline{(E)^2}}, \text{这说明} C_V > 0; \\ \text{其中广廷量}\overline{E}, C_V \propto N, \text{故z}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     相对涨落反比N,对单原子分子理想气体,\overline{E}=rac{3}{2}NkT,C_V=rac{3}{2}Nk,,\overline{(E-\overline{E})^2}=rac{2}{3N},故宏观系统(N\sim 10^{23})可忽略
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      能量相对涨落
9.6 实际气体的物态方程 (分子间作用不能忽略) 推导方法:(1)建立实际气体微观模型;(2)系统能量表达式;(3)配分函数;(4)物方
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      单原子分子气体能量:E=\sum_{k=1}^{3N}rac{p_k^2}{2m}+\sum_{i< j}arphi(r_{ij}),配分函数:Z=rac{1}{N!h^{3N}}\int e^{-eta E}dqdp
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   \frac{N_2, V_2, E_2, \Omega_2(N_{23}N_2, \frac{F_2}{2m})), \forall j}{\frac{1}{N!h^{3N}} \int e^{-\beta \sum_{k=1}^{N} \frac{F_2}{2m}} dp \int e^{-\beta \sum_{i < j} \varphi(r_{ij})} dq = \frac{1}{N!h^{3N}} AQ, \exists j \neq k = \prod_{k=1}^{3N} \int_{-\infty}^{+\infty} e^{-\beta \frac{P_k^2}{2m}} dp \int e^{-\beta \sum_{i < j} \varphi(r_{ij})} dq = \frac{1}{N!h^{3N}} AQ = \frac{1}{N!h^{3N}} \int_{-\infty}^{+\infty} e^{-\beta \frac{P_k^2}{2m}} dp \int e^{-\beta \sum_{i < j} \varphi(r_{ij})} dq = \frac{1}{N!h^{3N}} \int_{-\infty}^{+\infty} e^{-\beta \sum_{i < j} \varphi(r_{ij})} dq = \frac{1}{N!h^{3N}} \int_{-\infty}^{+\infty} e^{-\beta \sum_{i < j} \varphi(r_{ij})} dq = \frac{1}{N!h^{3N}} \int_{-\infty}^{+\infty} e^{-\beta \sum_{i < j} \varphi(r_{ij})} dq = \frac{1}{N!h^{3N}} \int_{-\infty}^{+\infty} e^{-\beta \sum_{i < j} \varphi(r_{ij})} dq = \frac{1}{N!h^{3N}} \int_{-\infty}^{+\infty} e^{-\beta \sum_{i < j} \varphi(r_{ij})} dq = \frac{1}{N!h^{3N}} \int_{-\infty}^{+\infty} e^{-\beta \sum_{i < j} \varphi(r_{ij})} dq = \frac{1}{N!h^{3N}} \int_{-\infty}^{+\infty} e^{-\beta \sum_{i < j} \varphi(r_{ij})} dq = \frac{1}{N!h^{3N}} \int_{-\infty}^{+\infty} e^{-\beta \sum_{i < j} \varphi(r_{ij})} dq = \frac{1}{N!h^{3N}} \int_{-\infty}^{+\infty} e^{-\beta \sum_{i < j} \varphi(r_{ij})} dq = \frac{1}{N!h^{3N}} \int_{-\infty}^{+\infty} e^{-\beta \sum_{i < j} \varphi(r_{ij})} dq = \frac{1}{N!h^{3N}} \int_{-\infty}^{+\infty} e^{-\beta \sum_{i < j} \varphi(r_{ij})} dq = \frac{1}{N!h^{3N}} \int_{-\infty}^{+\infty} e^{-\beta \sum_{i < j} \varphi(r_{ij})} dr = \frac{1}{N!h^{3N}} \int_{-\infty}^{+\infty} e^{-\beta \sum_{i < j} \varphi(r_{ij})} dr = \frac{1}{N!h^{3N}} \int_{-\infty}^{+\infty} e^{-\beta \sum_{i < j} \varphi(r_{ij})} dr = \frac{1}{N!h^{3N}} \int_{-\infty}^{+\infty} e^{-\beta \sum_{i < j} \varphi(r_{ij})} dr = \frac{1}{N!h^{3N}} \int_{-\infty}^{+\infty} e^{-\beta \sum_{i < j < j} \varphi(r_{ij})} dr = \frac{1}{N!h^{3N}} \int_{-\infty}^{+\infty} e^{-\beta \sum_{i < j < j < j} \varphi(r_{ij})} dr = \frac{1}{N!h^{3N}} \int_{-\infty}^{+\infty} e^{-\beta \sum_{i < j < j < j} \varphi(r_{ij})} dr = \frac{1}{N!h^{3N}} \int_{-\infty}^{+\infty} e^{-\beta \sum_{i < j < j < j} \varphi(r_{ij})} dr = \frac{1}{N!h^{3N}} \int_{-\infty}^{+\infty} e^{-\beta \sum_{i < j < j < j} \varphi(r_{ij})} dr = \frac{1}{N!h^{3N}} \int_{-\infty}^{+\infty} e^{-\beta \sum_{i < j < j < j} \varphi(r_{ij})} dr = \frac{1}{N!h^{3N}} \int_{-\infty}^{+\infty} e^{-\beta \sum_{i < j < j < j} \varphi(r_{ij})} dr = \frac{1}{N!h^{3N}} \int_{-\infty}^{+\infty} e^{-\beta \sum_{i < j < j < j} \varphi(r_{ij})} dr = \frac{1}{N!h^{3N}} \int_{-\infty}^{+\infty} e^{-\beta \sum_{i < j < j < j} \varphi(r_{ij})} dr = \frac{1}{N!h^{3N}} \int_{-\infty}^{+\infty} e^{-\beta \sum_{i < j < j < j} \varphi(r_{ij})} dr = \frac{1}{N!h^{3N}} \int_{-\infty}^{+\infty} e^{-\beta \sum_{i < j < j} \varphi(r_{ij})} dr = \frac{1}{N!h^{3N}} \int_{-\infty}^{+\infty} e^{-\beta \sum_{i < j < j < j} \varphi(r_{ij})} dr = \frac{1}{N!h^{3N}
              系统仅能交,无物交和体积变化,E^{(0)}=E_1+E_2,\Omega^{(0)}(E_1,E_2)=\Omega_1(E_1)\Omega_2(E_2)=\Omega_1(E_1)\Omega_2(E^{(0)})
              _1),对给定_{E}^{(0)},_{\Omega}^{(0)}取决于_{1},即总微观态数取决于能量在两子系统间的分配,由等概率原理,平衡态下孤立系统所有可能微
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        \left(\frac{2\pi m}{\beta}\right)^{3N/2}, Q = \int e^{-\beta \sum_i < j \; \varphi(r_{ij})} dq = \int \cdots \int e^{-\beta \sum_i < j \; \varphi(r_{ij})} d	au_1 \cdots d	au_N,配分函
 数:Z=rac{1}{N!}\left(rac{2\pi m}{eta h^2}
ight)^{3N/2}Q,对每对分子引入函数f_{ij}=e^{-eta arphi}(r_{ij})-1,当r_{ij}>互作用力程(个
 \frac{\partial \Omega_1(E_1)}{\partial E_1}\Omega_2(E_2) - \Omega_1(E_1)\frac{\partial \Omega_2(E_2)}{\partial E_2} = 0 \Rightarrow \left(\frac{\partial \ln \Omega_1(E_1)}{\partial E_1}\right)_{N_1,V_1} = \left(\frac{\partial \ln \Omega_2(E_2)}{\partial E_2}\right)_{N_2,V_2}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      10^{-10\sim -9} m),\varphi(r_{ij})=0,f_{ij}=0,当r_{ij}<为程,f_{ij}\neq0,集团展开:Q=\int\prod_{i< j}(1+f_{ij})d	au
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      \int (1 + \sum_{i < j} f_{ij} + \sum_{i < j} \sum_{i' < j'} f_{ij} f_{i'j'} + \cdots) d	au,若仅保留首项,即不计分子互作用,Q
 子系统间达热平衡,\beta = \left(\frac{\partial \ln \Omega(N,V,E)}{\partial E}\right)_{N,V} 必相等,热平衡条件:\beta_1 = \beta_2;对照热力学中热平衡条
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   为理想气体,第二項仪当1对分子(i,j)在力程内才\neq 0,第三项仪当2对分子(i,j)、(i',j')均在力程内才\neq 0,对稀薄气体,2个以上分子同时相碰的概率极小,故仅保留前两项:Q=\int (1+\sum_{i< j}f_{ij})\tau=V^N+\int \sum_{i< j}f_{ij}d\tau,第二项化为\int \sum_{i< j}f_{ij}\tau=\sum_{i< j}\int f_{ij}d\tau=\sum_{i< j}V^{N-2}\iint f_{ij}d\tau_id\tau_j=N^2V^{N-2}\iint f_{12}d\tau_1\tau_2,引入相
 件: \left(\frac{\partial S_1}{\partial U_1}\right)_{N_1,V_1}=\left(\frac{\partial S_2}{\partial U_2}\right)_{N_2,V_2}=\frac{1}{T} 得 \beta=\frac{1}{kT} 和熵: S=k\ln\Omega (将最概然分布理论在近
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   対性标r=r_2-r_1,质心坐标r_C=rac{m_1r_1+m_2r_2}{m_1+m_2},从而∬ f_{12}d\tau_1d	au_2=\iint f_{12}rdr_C=V\int f_{12}dr_Q=
              立系统中的结论推广到了粒子间相互作用的系统);两子系统间还可物交和改变体积,V^{(0)}=V_1+V_2,N^{(0)}=0
\begin{array}{lll} N_1 \,+\, N_2, \\ \mathbb{M} \overline{n} \left( \frac{\partial \ln \Omega}{\partial V_1} \right)_{N_1,\,E_1} &=\, \left( \frac{\partial \ln \Omega_2}{\partial V_2} \right)_{N_2,\,E_2}, \\ \left( \frac{\partial \ln \Omega_1}{\partial N_1} \right)_{E_1,\,V_1} &=\, \left( \frac{\partial \ln \Omega_2}{\partial N_2} \right)_{E_2,\,V_2}, \\ \mathbb{X} \gamma &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{N,E}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial N} \right)_{V,E}, \\ \end{array} \\ \mathbf{y}_{E_2} = \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{N_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial N} \right)_{V_1,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln \Omega(N,V,E)}{\partial V} \right)_{V_2,E_2}, \\ \alpha &=\, \left( \frac{\partial \ln 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      V^N \left[1 + \frac{N^2}{2V} \int f_{12} dr\right], \ln Q = N \ln V + \ln \left[1 + \frac{N^2}{2V} \int f_{12} dr\right], 假设 \frac{N^2}{2V} \int f_{12} dr \ll 1, \ln Q = 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     N \ln V \ + \ \frac{N^2}{2V} \int f_{12} d{m r},物态方程:p = \frac{1}{eta} \frac{\partial}{\partial V} \ln Z \ = \ \frac{1}{eta} \frac{\partial}{\partial V} \ln Q \ = \ \frac{1}{eta} \frac{N}{V} \left[ 1 - \frac{N}{2V} \int f_{12} d{m r} \right],比
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     较二阶近似的昂尼斯方程:pV = NkT\left[1+rac{nB}{V}
ight]得第2位力系数B = -rac{N_A}{2}\int f_{f 12}dm{r};纳德·琼斯半经验
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     公式:两分子互作用势:\phi(r) = \phi_0 \left[ \left( \frac{r_0}{r} \right)^{12} - 2 \left( \frac{r_0}{r} \right)^6 \right],近似为\phi(r) = +\infty, r < r_0, \phi(r) =
 地下地球ボー・1=12(N年十期)、P_1=P_2(D7年期)、P_1=P_2)(N7年間)、P_2 大田 は P_2 大田 に P_2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     -\phi_0\left(\frac{r_0}{r}\right)^6, \\ \exists B = -\frac{N_A}{2}\int (e^{-\frac{\phi(r)}{kT}}-1)r^2\sin\theta dr d\theta d\phi = -2\pi N_A\int_0^\infty (e^{-\frac{\phi(r)}{kT}}-1)r^2 dr = -\frac{N_A}{2}\int (e^{-\frac{\phi(r)}{kT}}-1)r^2 dr
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   2\pi N \left[ \int_0^{r_0} r^2 dr - \int_{r_0}^{\infty} (e^{-\frac{\phi(r)}{kT}} - 1) r^2 dr \right],若T足够高,分子热激发>互作用势,e^{-\frac{\phi}{kT}} = 1 - \frac{\phi}{kT}, B = 1 - \frac{\phi}{kT}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   2\pi N_A \left\lceil \frac{r_0^3}{3} - \frac{\phi_0 r_0^3}{3kT} \right\rceil, \\ \\ \Leftrightarrow B = b - \frac{a}{N_A kT}, \\ \\ \\ \sharp + b = \frac{2\pi}{3} N_A r_0^3 = 4N_A v = 4V_{0m}, \\ \\ a = \frac{2\pi}{3} N_A^2 \phi_0 r_0^3 = 4N_A v = 4V_{0m}, \\ a = \frac{2\pi}{3} N_A^2 \phi_0 r_0^3 = 4N_A v = 4V_{0m}, \\ a = \frac{2\pi}{3} N_A^2 \phi_0 r_0^3 = 4N_A v = 4V_{0m}, \\ a = \frac{2\pi}{3} N_A^2 \phi_0 r_0^3 = 4N_A v = 4V_{0m}, \\ a = \frac{2\pi}{3} N_A^2 \phi_0 r_0^3 = 4N_A v = 4V_{0m}, \\ a = \frac{2\pi}{3} N_A^2 \phi_0 r_0^3 = 4N_A v = 4V_{0m}, \\ a = \frac{2\pi}{3} N_A^2 \phi_0 r_0^3 = 4N_A v = 4V_{0m}, \\ a = \frac{2\pi}{3} N_A^2 \phi_0 r_0^3 = 4N_A v = 4V_{0m}, \\ a = \frac{2\pi}{3} N_A^2 \phi_0 r_0^3 = 4N_A v = 4V_{0m}, \\ a = \frac{2\pi}{3} N_A^2 \phi_0 r_0^3 = 4N_A v = 4V_{0m}, \\ a = \frac{2\pi}{3} N_A^2 \phi_0 r_0^3 = 4N_A v = 4V_{0m}, \\ a = \frac{2\pi}{3} N_A^2 \phi_0 r_0^3 = 4N_A v = 4V_{0m}, \\ a = \frac{2\pi}{3} N_A^2 \phi_0 r_0^3 = 4N_A v = 4V_{0m}, \\ a = \frac{2\pi}{3} N_A^2 \phi_0 r_0^3 = 4N_A v = 4V_{0m}, \\ a = \frac{2\pi}{3} N_A v = 4V_{0m}, \\ a = \frac{2\pi}{3} N_
   设理想气体含N个单原子分子,哈密顿量:H=\sum_{i=1}^{3N}rac{p_i^2}{2m},则\Omega=rac{1}{N!h^{3N}}\int_{E}\leq H(q,p)\leq E+\Delta E\;dqdp,系
 4N_A\phi_0V_{0m}与分子引力有关,物态方程近似为pV=NkT\left[1+rac{nb}{V}
ight]-rac{n^2a}{V}或\left(p+rac{n^2a}{V^2}
ight)rac{V}{1+rac{nb}{V^2}}=
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     NkT,因 \frac{nb}{V} \ll 1, \frac{1}{1+\frac{nb}{V}} = 1 - \frac{nb}{V},物态方程近似为\left(p + \frac{n^2a}{V}\right)(V-nb) = NkT
 \frac{\pi^{3N/2}}{\left(\frac{3N}{2}\right)!}等于3N维空间中半径为1的球体积,故\Sigma(E) = \left(\frac{V}{h^3}\right)^N \frac{(2\pi m E)^{3N/2}}{N!\left(\frac{3N}{2}\right)!},能竞E \sim E + \Delta E内
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     9.7 固体的热容 固体原子间相互作用很强,各原子在一定平衡位置附近做三维非简谐微振动
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      系统能量由原子振动动能\sum_{i=1}^{3N} \frac{p_{\xi_i}^2}{2m}和势能(原子偏离平衡位置位移的幂级数,近似至二阶)\phi = \phi_0 + \sum_i \left(\frac{\partial \phi}{\partial \xi_i}\right)_0 \xi_i +
   \frac{1}{2} \sum_{i,j} \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right) \xi_i \xi_j \text{ 组成}, 因所有原子均处于平衡位置附近,} \left( \frac{\partial \phi}{\partial \xi_i} \right)_0 = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, E = 0, \\ \diamondsuit a_{ij} = \left( \frac{\partial^2 \phi}{\partial \xi_i \partial \xi_j} \right)_0, \\ \diamondsuit a_{ij
   \frac{5}{2}Nk + k \left[ \ln \left( \frac{3N}{2} \right) + \ln \left( \frac{\Delta E}{E} \right) \right], \\ \mathbb{E}\lim_{N \to \infty} \frac{\ln N}{N} = 0, \\ S = Nk \ln \left[ \frac{V}{h^3 N} \left( \frac{4\pi mE}{3N} \right)^{3/2} \right] + \frac{1}{N} \left[ \frac{N}{N} \left( \frac{N}{N} \right) \right] + \frac{N}{N} \left[ \frac{N}{N} \left( \frac{N}{N} \right) \right] +
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+ \frac{1}{2}\sum_{i,j}a_{ij}\xi_i\xi_j + \varphi_0,用线性变换将各\xi_i组合为简正坐标q_i,上式化为平方和:E=\frac{1}{2}\sum_{i=1}^{3N}(p_i)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      \Omega_r(N^{(0)}, E^{(0)} - E_s);将\ln \Omega_r \epsilon N^{(0)}, E^{(0)}处展开为N, E_s的幂级数,取到1阶项,\ln \Omega_r(N^{(0)} - N, E^{(0)})
                                                                 \phi_0,这3N个简正坐标的运动是相互独立的简正振动,特征频率:\omega_i,由量子理论,3N个谐振子的能量:E=
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                \begin{array}{lll} \Omega_T(N^0,E^0) &= E_S \text{ [spin Magnin Magni
能:U=-\frac{\partial}{\partial\beta}\ln Z=U_0+\sum_{i=1}^{3N}\frac{\hbar\omega_i}{e^{\beta\hbar\omega_i}-1},其中结合能:U_0=\phi_0+\sum_{i=1}^{3N}\frac{\hbar\omega_i}{2},零点能:\sum_{i=1}^{3N}\frac{\hbar\omega_i}{2},热
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     数:\Xi=\sum_{N=0}^{\infty}\sum_{s}e^{-\alpha N-\beta E_{s}},巨正则分布的经典表达式:
ho_{N}dqdp=\frac{1}{N!h^{Nr}}\frac{e^{-\alpha N-\beta E(q,p)}}{\Xi}d\Omega,其中巨
   运动能量:\sum_{i=1}^{3N} \frac{\hbar \omega_i}{\beta \hbar \omega_{i-1}},需简正振动的频率分布(振动频谱),才能求出内能;爱因斯坦模型:假设固体中所有原子均独立地
   做頻率相同的简谐运动、U=3N\frac{\hbar\omega}{2}+\frac{3N\hbar\omega}{e^{\beta \hbar\omega}-1};德拜固体理论:视固体为连续弹性媒介,3N个简正振动是其基本被动,对一定的被矢k。阅体中的被动含仅一种振动方式的数读和两种振动方式(两个正交方向上的偏振的模读,可用被矢和偏振方向标志3N个简正振动状态,两种被的色散关系:\omega=c_tk、\omega=c_tk、V 中\omega\sim\omega+d\omega范围内简正振动数:D(\omega)d\omega=
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   9.11 巨正则系線理论的热力学公式 系統平均粒子数:给定V,T,\mu下所有可能微观态粒子数的平均值,\overline{N}=\sum_N\sum_sN\rho_{Ns}=\frac{1}{\Xi}\sum_N\sum_sNe^{-\alpha N-\beta Es}=\frac{1}{\Xi}\left(-\frac{\partial}{\partial\alpha}\right)\sum_N\sum_se^{-\alpha N-\beta Es}=\frac{1}{\Xi}\left(-\frac{\partial}{\partial\alpha}\right)\Xi=-\frac{\partial}{\partial\alpha}\ln\Xi 内能:U=\overline{E}=\frac{1}{\Xi}\sum_N\sum_sE_se^{-\alpha N-\beta Es}=\frac{1}{\Xi}\left(-\frac{\partial}{\partial\beta}\right)\Xi=-\frac{\partial}{\partial\beta}\ln\Xi
   \frac{V}{2\pi^2} \left( \frac{1}{c_f^3} + \frac{2}{c_f^3} \right) \omega^2 d\omega, \\ \forall B = \frac{V}{2\pi^2} \left( \frac{1}{c_f^3} + \frac{2}{c_f^3} \right), \\ \exists \text{ LM} \\ \exists \phi \in D, \\ \exists 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   广义カ: Y = \frac{1}{\Xi} \sum_{N} \sum_{s} \frac{\partial E_{s}}{\partial y} e^{-\alpha N - \beta E_{s}} = \frac{1}{\Xi} \left( -\frac{1}{\beta} \frac{\partial}{\partial y} \right) \Xi = -\frac{1}{\beta} \frac{\partial}{\partial y} \ln \Xi : 压强: p = \frac{1}{\beta} \frac{\partial}{\partial \beta} \ln \Xi
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   \beta(dU - Ydy + \frac{\alpha}{\beta}d\overline{N}) = -\beta d\left(\frac{\partial \ln \Xi}{\partial \beta}\right) + \frac{\partial \ln \Xi}{\partial y}dy - \alpha d\left(\frac{\partial}{\partial \alpha}\ln \Xi\right), \operatorname{Bln}\Xi h\alpha, \beta, y的 函数,其全微分为d \ln \Xi = \frac{\partial \ln \Xi}{\partial \beta}d\beta + \frac{\partial \ln \Xi}{\partial \alpha}d\alpha + \frac{\partial \ln \Xi}{\partial y}dy, \text{故}\beta\left(dU - Ydy + \frac{\alpha}{\beta}d\overline{N}\right) = 0
   \omega_D, D(\omega) d\omega = 0, \omega \geq \omega_D, \int_0^{\omega_D} B\omega^2 d\omega = 3N \Rightarrow \omega_D = \frac{9N}{B}, \text{phi}: U = U_0 + \int_0^{\omega} D(\omega) \frac{\hbar \omega}{e^{\beta} \hbar \omega - 1} d\omega = 0
d\left(\ln\Xi - \alpha \frac{\partial\Xi}{\partial\alpha} - \beta \frac{\partial\ln\Xi}{\partial\beta}\right),开系热力学基本方程 \frac{1}{T}(dU - Ydy - \mu d\overline{N}) = dS说明1/T为\left(dU - Ydy + \mu d\overline{N}\right)的
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    \frac{\partial \alpha}{\partial \alpha} \frac{\partial \beta}{\partial \beta}  积分因子,故\beta = \frac{1}{kT}, \alpha = -\frac{\mu}{kT}, S = k \left( \ln \Xi - \alpha \frac{\partial \ln \Xi}{\partial \alpha} - \beta \frac{\partial \ln \Xi}{\partial \beta} \right)  粒子数涨落:(N - \overline{N})^2 = \overline{N^2} - \overline{N^2}, \exists \overline{N} = \frac{1}{\Xi} \sum_N \sum_S N^2 e^{-\alpha N - \beta E_S}   \frac{1}{\Xi} \left( -\frac{\partial}{\partial \alpha} \right) \sum_N \sum_S N e^{-\alpha N - \beta E_S} = \frac{1}{\Xi} \left[ \frac{\partial}{\partial \alpha} (\overline{N}\Xi) \right] = -\frac{1}{\Xi} \left[ \Xi \frac{\partial \overline{N}}{\partial \alpha} + \overline{N} \frac{\partial \Xi}{\partial \alpha} \right] 
    温下,T \gg \theta_D, y 《 1, e^y = 1 + y, \mathscr{D}(x) \approx \frac{3}{x^3} \int_0^x y^2 dy = 1,内能:U = U_0 + 3NkT,热
    容:C_V=3Nk,与经典统计理论结果一致;低温下,T~\ll~	heta_D,x~\gg~1, \mathscr{D}(x)~pprox~rac{3}{x^3}\int_0^\inftyrac{y^3dy}{e^y-1}~=~rac{\pi^4}{5x^3},内
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     能:U=U_0+3Nk\frac{\pi^4}{5}\frac{T^3}{\theta J},C_V=3Nk\frac{4\pi^4}{5}\left(\frac{T}{\theta D}\right)^3(德拜T^3律);符合非金属和T\geq 3K下金属固体,T\leq 3K下金属固体不能忽略电子对热容的影响,德拜仅考虑其原子部分,且视固体为连续弹性介质,忽略了其中原子的离散结构;对\lambda\gg a(—原
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      \frac{kT}{\overline{N}^2} \left( \frac{\partial \overline{N}}{\partial \mu} \right)_{T,V} ; \\ \exists dG = -SdT + Vdp + \mu dn \\ \exists d(\overline{N}\mu) = -(\overline{N}s)dT + (\overline{N}v)dp + \mu d\overline{N} \\ \Rightarrow d\mu = -(\overline{N}s)dT + (\overline{N}v)dp + \mu d\overline{N} \\ \Rightarrow d\mu = -(\overline{N}s)dT + (\overline{N}v)dp + \mu d\overline{N} \\ \Rightarrow d\mu = -(\overline{N}s)dT + (\overline{N}v)dp + \mu d\overline{N} \\ \Rightarrow d\mu = -(\overline{N}s)dT + (\overline{N}v)dp + \mu d\overline{N} \\ \Rightarrow d\mu = -(\overline{N}s)dT + (\overline{N}v)dp + \mu d\overline{N} \\ \Rightarrow d\mu = -(\overline{N}s)dT + (\overline{N}v)dp + \mu d\overline{N} \\ \Rightarrow d\mu = -(\overline{N}s)dT + (\overline{N}v)dp + \mu d\overline{N} \\ \Rightarrow d\mu = -(\overline{N}s)dT + (\overline{N}v)dp + \mu d\overline{N} \\ \Rightarrow d\mu = -(\overline{N}s)dT + (\overline{N}v)dp + \mu d\overline{N} \\ \Rightarrow d\mu = -(\overline{N}s)dT + (\overline{N}v)dp + \mu d\overline{N} \\ \Rightarrow d\mu = -(\overline{N}s)dT + (\overline{N}v)dp + \mu d\overline{N} \\ \Rightarrow d\mu = -(\overline{N}s)dT + (\overline{N}v)dp + \mu d\overline{N} \\ \Rightarrow d\mu = -(\overline{N}s)dT + (\overline{N}v)dp + \mu d\overline{N} \\ \Rightarrow d\mu = -(\overline{N}s)dT + (\overline{N}v)dp + \mu d\overline{N} \\ \Rightarrow d\mu = -(\overline{N}s)dT + (\overline{N}v)dp + \mu d\overline{N} \\ \Rightarrow d\mu = -(\overline{N}s)dT + (\overline{N}v)dp + \mu d\overline{N} \\ \Rightarrow d\mu = -(\overline{N}s)dT + (\overline{N}v)dp + \mu d\overline{N} \\ \Rightarrow d\mu = -(\overline{N}s)dT + (\overline{N}v)dp + \mu d\overline{N} \\ \Rightarrow d\mu = -(\overline{N}s)dT + (\overline{N}v)dp + \mu d\overline{N} \\ \Rightarrow d\mu = -(\overline{N}s)dT + (\overline{N}v)dp + \mu d\overline{N} \\ \Rightarrow d\mu = -(\overline{N}s)dT + (\overline{N}v)dT + (\overline{N}v)d
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      vdp-sdT,因d\mu=rac{\partial\mu}{\partial v}dv+rac{\partial u}{\partial T}dT,故\left(rac{\partial\mu}{\partial v}
ight)_T=v\left(rac{\partial p}{\partial v}
ight)_T,注意v=rac{V}{N},当V不变而\overline{N}变,\left(rac{\partial\mu}{\partial v}
ight)_T=0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   化,相当于不同状态的声子不断产生和湮灭,声子数不守恒,声子气体化学势=0,由玻色分布U=U_0+\sum_{i=1}^{3N} -1
         oldsymbol{n}8. oldsymbol{n}8. oldsymbol{m}^4 He- 數色子, He 原子间相互作用很弱,原子质量很小,故零点振动能很大,常压下 炎近 oldsymbol{n}6 K 时仍可保持液态,此时量子相应主导,液 He 为量子液体
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         -rac{kT}{Vv}\left(rac{\partial v}{\partial p}
ight)_T=rac{kT}{V}\kappa_T;因广延量V\propto \overline{N},当\kappa_T有限,相对涨落反比\overline{N},故宏观系统涨落很小
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     用巨正则分布求熱力學量相当于选自受量为\mu,V,T的巨熱力学勢J为粹性函數;正则分布相当于选F(N,V,T)
9.12 巨正则系综理论的简单应用 吸附现象:表面有N_0个吸附中心,各可吸附一气体分子,分子吸附后能量为-\varepsilon_0,视气体为
热源和粒子源,被吸附分子组成与之能交和物交的系统,遵从巨正则分布,当N个分子吸附,系统能量:-N\varepsilon_0,巨配分函数:\Xi
      \lambda相变:正常相^4He I沿饱和蒸气压曲线降温,在T_\lambda=2.18K和比容v_\lambda=46.2Å^3/a	ext{tom}处相变为He II,相变处无潜热/体
                  \S化,比熱以对數形式→ +\infty,为二級相变,比熱线像入,故名之,T^3附近,比热以T^3形式→ 0

{\bf 1e} I1的特性:1超流性:能沿极细的毛细管流动而无粘滞性,临界速度之上,超流性破坏;2.用细丝悬薄圆盘浸入并使盘做扭转振
测得粘滞系数与正常相相似,比毛细法所得大门10^6倍,强烈依赖于温度,→ 0随T → 0K;3. 力热效应:从容器A经多孔塞或极细毛
管流由时,A内余液T 个,其逆过程称热力效应;4. 热导率很大,为室温下Cu800倍,不以普通流体~温度梯度
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   \sum_{N=0}^{N_0} \sum_s e^{-\alpha N - \beta E_s} = \sum_{N=0}^{N_0} e^{\beta(\mu + \varepsilon_0)N} \frac{N_0!}{N!(N_0 - N)!} = [1 + e^{\beta(\mu + \varepsilon_0)}]^{N_0}, 平均吸附分子
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   数: \overline{N} = -\frac{\partial}{\partial \alpha} \ln \Xi = kT \frac{\partial}{\partial \mu} \ln \Xi = \frac{N_0}{1+e^{-\beta}(\varepsilon_0 + \mu)}, 达平衡时吸附和未吸附分子的\mu, T相等, 理想气体化学
                                                                      7 演帖日 II由正常流体和超流体组成。超流体工精滞性和熵,正常流体有, \rho_s, \rho_n一超)正常流体质量密度、v_s, v_n一两者密度, \rho_s, \rho_n一超)工能流体和显流体, v_s, v_n一两者密度, \rho_s, \rho_n一超流体, v_s, \rho_n一超流体, v_s, v_n一两者密度, v_s, \rho_n一超流体, v_s, v_n一两者密度, v_s, \rho_n为温度的函数, v_s, v_n一两者密度, v_s, v_n0、以, v_s, v_n0、以, v_s, v_n0、以, v_s0、以, 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     势:\mu = kT \ln \left[ \frac{N}{V} \left( \frac{h^2}{2\pi m kT} \right)^{3/2} \right],故戦附率:\theta = N/N_0 = \left[ 1 + \frac{kT}{p} \left( \frac{2\pi m kT}{h^2} \right)^{3/2} e^{-\epsilon_0/kT} \right]^{-1}
                                                  1 < 1_{\lambda} \rho_S \rho_
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     近独立粒子平均分布:系统仅含一种近独立粒子,能级为\varepsilon_1,、、、、、\varepsilon_l,、、、、无简并,当分布为\{a_l\},总粒子数:N=\sum_l c能能:E=\sum_l c_l (\alpha+\beta\varepsilon_l) a_l
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   \begin{split} & \sum_{\{a_l\}} \prod_l e^{-(\alpha+\beta\varepsilon_l)a_l} = \prod_l \sum_{\{a_l\}} e^{-(\alpha+\beta\varepsilon_l)a_l} = \prod_l \sum_{l} \sum_{l} \sum_{l} \sum_{s} a_l e^{-(\alpha+\beta\varepsilon_l)a_l}, \\ & \underbrace{\mathbb{E}_{\{a_l\}} \prod_l e^{-(\alpha+\beta\varepsilon_l)a_l}}_{= \sum_{l} \sum_{s} a_l e^{-\alpha N - \beta E_s} = \frac{1}{\Xi} \sum_{l} \sum_{s} a_l e^{-(\alpha+\beta\varepsilon_l)a_l} \\ & \underbrace{\mathbb{E}_{\{a_m\}} \left[a_l \prod_m e^{-(\alpha+\beta\varepsilon_m)a_m}\right]}_{= \sum_{l} \sum_{l} \sum_{s} a_l e^{-(\alpha+\beta\varepsilon_l)a_l} \prod_{l} \sum_{l} e^{-(\alpha+\beta\varepsilon_l)a_l} \\ & \underbrace{\mathbb{E}_{\{a_m\}} \left[a_l e^{-(\alpha+\beta\varepsilon_l)a_l} \prod_{m \neq l} e^{-(\alpha+\beta\varepsilon_l)a_l}\right]}_{= \sum_{l} \sum_{s} a_l a_l e^{-(\alpha+\beta\varepsilon_l)a_l} = \frac{1}{\Xi} \sum_{l} \sum_{s} a_l a_l e^{-(\alpha+\beta\varepsilon_l)a_l} = \frac{1}{\Xi} \sum_{l} \sum_{s} a_l a_l e^{-(\alpha+\beta\varepsilon_l)a_l} = \frac{1}{\Xi} \sum_{s} \sum_{s
          0玻色元激发—声子/旋子,1、实验发现当T 《 T》,比熱随T^3变化,此为声子特征、能谱。 = cp,c—声子速度(2、实验发现(3温度稍高,比热有一如\exp[-\Delta/k_BT]的附加项,\Delta = const.故推测对较大动量,元激发能量有-\Delta能瞭,该动量范围内能
    \ddot{a}: arepsilon(p) = \hbar \omega_k = \Delta + rac{(p-p_0)^2}{2m^*} = \Delta + rac{\hbar^2(k-k_0)^2}{2m^*}, m^*-族子有效质量;准粒子在能量\hbar \omega_k的平均占
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      \frac{1}{\Xi_l} \left( -\frac{\partial}{\partial \alpha} \right) \Xi_l \ = \ -\frac{\partial}{\partial \alpha} \ln \Xi_l, \forall \text{ $\mathbf{x}$ } \text{ $\mathbf{x
    据数:\langle n_k \rangle = 1/(e^{\beta\hbar\omega_k} - 1),内能:U = E_0 + \sum_k \hbar\omega_k \langle n_k \rangle = E_0 + \frac{V}{2\pi^2} \int_0^\infty \frac{k^2\hbar\omega_k dk}{e^{\beta\hbar\omega_k} - 1},定容
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  比热:C_V = \left(\frac{\partial U}{\partial T}\right)_V,声子贡献比热:\frac{C_{\mathrm{phonon}}}{Nk_B} = \frac{2\pi^2 v(k_BT)^3}{15(\hbar c)^3},当k_BT/\Delta较小,旋子贡献比热 \frac{C_{\mathrm{roton}}}{Nk_B} = \frac{2\pi^2 v(k_BT)^3}{15(\hbar c)^3}
    \frac{2\sqrt{m^*}(k_0\Delta)^2ve^{-\Delta/k_BT}}{2\sqrt{2}},这些结果与实验符合得很好
    \left[\sum_{a_m} a_m e^{-(\alpha+\beta\varepsilon_m)a_m}\right] \left[\prod_{k\neq l, m} \sum_{a_k} e^{-(\alpha+\beta\varepsilon_k)a_k}\right] = \frac{1}{\Xi_l} \frac{1}{\Xi_m} \left[\sum_{a_l} a_l e^{-(\alpha+\beta\varepsilon_l)a_l}\right]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      \left[\sum_{a_m}a_me^{-(\alpha+\beta\varepsilon_m)a_m}
ight]=ar{a}_lar{a}_m,故\overline{(a_l-ar{a}_l)(a_m-ar{a}_m)}=0,不同能级上涨落不相关
 Chap10 涨落理论 10.1 涨落的准热力学理论 涨落分2类:宏观量围绕平均值的涨落(:宏观量瞬时值与平均值的偏差)和布朗运动 设系统E,V,S各有平衡值\overline{E},\overline{V},\overline{S},若某微观态有\Delta E = \frac{E-\overline{E},\Delta V}{E-\Delta E-p\Delta V} = V-\overline{V},\Delta S = S-\overline{S},该 微观态出现概率为W(\Delta S,\Delta E,\Delta V) = W_m \epsilon \frac{T\Delta S-\Delta E-p\Delta V}{kT}(基本公式\mathbf{1})或W(\Delta S,\Delta E,\Delta V) = \Delta p\Delta V-\Delta T\Delta S
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      当于分子对静止布朗颗粒的碰撞作用力,平均值=0)),从而mrac{d^2x}{dt^2}=-lpharac{dx}{dt}+F(t)+G(t)(郎之万方程),当无其它t
   力,m\frac{d^2x}{dt^2} = -\alpha\frac{dx}{dt} + F(t),两边同乘x并用x\ddot{x} = \frac{d}{dt}(x\dot{x}) - \dot{x}^2 = \frac{1}{2}\frac{d^2}{dt^2}x^2 - \dot{x}^2 得 \frac{1}{2}\frac{d^2}{dt^2}(mx^2) - m\dot{x}^2 = \frac{1}{2}\frac{d^2}{dt^2}x^2 + \frac{1}{2}\frac{d
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      -\frac{\alpha}{2}\frac{d}{dt}x^2 + xF(x),因(1)求平均与对时间求导可交换: \frac{d}{dt}x^2 = \frac{d}{dx}\overline{x^2}, \frac{d}{dt}mx^2 = \frac{d}{dt}\overline{mx^2},(2)涨落力与颗粒位置无
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      关:\overline{xF(t)}=\bar{x}\overline{F(t)}=\bar{x}\cdot 0=0,(3)当颗粒与介质达热平衡,由均分定理,颗粒平均动能:\frac{1}{2}\overline{m\dot{x}^2}=\frac{1}{2}kT,得 \frac{d^2}{dt^2}\overline{x^2}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      \frac{\alpha}{m}\frac{d}{dt}\overline{x^2} - \frac{2kT}{m} = 0,方程通解为\overline{x^2} = \frac{2kT}{\alpha}t + C_1e^{-\frac{\alpha}{m}t} + C_2,设m = \frac{4}{3}\pi\rho a^3,则\frac{\alpha}{m} = \frac{9\eta}{2a^2\rho},因\frac{\alpha}{m}
    量偏差\Delta E = E(S,V) - \overline{E}(\overline{S},\overline{V})在(\overline{S},\overline{V})展开并保留到二阶项得\Delta E = \left(\frac{\partial E}{\partial S}\right)_V \Delta S + \left(\frac{\partial E}{\partial V}\right)_S \Delta V + \left(\frac{\partial E}{\partial V}\right)_S \Delta V
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     10^7 s^{-1},故很短时间(> 10^{-6} s)后,通解中第二项便可忽略,设x(0) = 0得C_2 = 0,从而得\overline{x^2} = \frac{2kT}{\alpha} t(爱因斯坦公式)
    \frac{1}{2} \left[ \left( \frac{\partial^2 E}{\partial S^2} \right)_V (\Delta S)^2 + 2 \frac{\partial^2 E}{\partial S \partial V} \Delta S \Delta V + \left( \frac{\partial^2 E}{\partial V^2} \right)_S (\Delta V)^2 \right], \\ \text{其中各级偏导取} S = \overline{S}, V = \overline{V} \text{ brind}, \\ \text{代
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     从扩散观点看布朗运动:一维情况下,菲克定律: J = -D \nabla n,连续方程: \frac{\partial D}{\partial t} + \nabla \cdot J = 0,其中n(x,t)-布朗颗粒密度分布,J(x,t)-布朗颗粒流量(单位时间通过单位截面的颗粒数),\Rightarrow \frac{\partial n}{\partial t} = D \nabla^2 n,设x(0) = 0即x(0) = 0
      \lambda \left( \frac{\partial E}{\partial S} \right)_V = T, \left( \frac{\partial E}{\partial V} \right)_S = -p得\Delta E = T\Delta S - p\Delta V + \frac{1}{2}(\Delta T\Delta S - \Delta p\Delta V),将上式代入I得基公II
    基公的应用:基公\Pi中4个偏差仅2个独立,可选2个变量X,Y作自变量,利用基公\Pi求\overline{(\Delta X)^2},\overline{(\Delta Y)^2},\overline{(\Delta Y)^2}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     N\delta(x),则n(x,t) = \frac{N}{2\sqrt{\pi Dt}}e^{-\frac{x^2}{4Dt}},这说明颗粒密度分布为与t有关的高斯分布,\overline{x^2} = \int x^2 \rho(x) dx =
   以T,V为自变量,\Delta S = \left( \frac{\partial S}{\partial T} \right)_V \Delta T + \left( \frac{\partial S}{\partial V} \right)_T \Delta V = \frac{C_V}{T} \Delta T + \left( \frac{\partial p}{\partial T} \right)_V \Delta V, \Delta p = \left( \frac{\partial p}{\partial T} \right)_V \Delta T + \left( \frac{\partial p}{\partial T} \right)_V \Delta V
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     \int x^2 \frac{n(x,t)}{N} dx = \frac{1}{\sqrt{\pi Dt}} \int_{-\infty}^{+\infty} x^2 e^{-\frac{x^2}{4Dt}} dx = 2Dt,与爱因斯坦方程形式一致,比较得D = \frac{kT}{\alpha} = \frac{kT}{6\pi\alpha\eta}
   oxed{10.6} 布朗颗粒动量的扩散和时间关联 系综平均:某物理量对大量布朗粒子的平均\overline{A(t)}=rac{1}{N}\sum_{i=1}^{N}A_i(t),其中i-第i个粒子
   \mathbb{E}(\overline{\Delta T})^{2} = \frac{\int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} (\Delta T)^{2} W(\Delta T, \Delta V) d(\Delta T) d(\Delta V)}{\int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} W(\Delta T, \Delta V) d(\Delta T) d(\Delta V)} = \frac{\int_{-\infty}^{+\infty} (\Delta T)^{2} \exp\left[-\frac{C_{V}}{2kT^{2}}(\Delta T)^{2}\right] d(\Delta T)}{\int_{-\infty}^{+\infty} \exp\left[-\frac{C_{V}}{2kT^{2}}(\Delta T)\right]} d(\Delta T) d(\Delta
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   涨落力的时间关联函数: F(t)F(t+\tau)=\frac{1}{N}\sum_{i=1}^{N}F_i(t)F_i(t+\tau),当\tau是够长, F_i(t)和F_i(t+\tau)三不分联, F(t)F(t+\tau)=0,及之相互依赖, 由此引入涨落力的关联时间\tau_c区分两种情况; 关联时间尺度上: 关联时间与涨落力的升
                                                                                                                                                                                                                                                                                                                                                                                                                           \frac{\int_{-\infty}^{+\infty} \exp\left[-\frac{C_V}{2kT^2}(\Delta T)\right] }{ \int_{-\infty}^{+\infty} \exp\left[-\frac{C_V}{2kT^2}(\Delta T)\right] } 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   均周期一般有相同數量級,对在	au_c量级时间内仅有微小变化的物理量,F(t)F(t+	au)=2D_p\delta(	au),其中2D_p-涨落力强度的量度(公成)不同时刻漆落力不关联,长时间平均值:\langle F(t)F(t+	au)\rangle=\lim_{T_0\to\infty}\frac{1}{T_0}\int_0^T F(t)F(t+	au)dt,长时间内,颗
   \frac{kT^2}{CV},\overline{(\Delta V)^2} = \frac{\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}(\Delta V)^2W(\Delta T,\Delta V)d(\Delta T)d(\Delta V)}{\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}(\Delta V)^2\exp\left[\frac{1}{2kT}\left(\frac{\partial p}{\partial V}\right)_T(\Delta V)\right]d(\Delta T)} = \frac{\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}(\Delta V)^2\exp\left[\frac{1}{2kT}\left(\frac{\partial p}{\partial V}\right)_T(\Delta V)\right]d(\Delta T)}{\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}(\Delta V)^2\exp\left[\frac{1}{2kT}\left(\frac{\partial p}{\partial V}\right)_T(\Delta V)\right]d(\Delta T)d(\Delta T)} = \frac{\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}(\Delta V)^2W(\Delta T,\Delta V)d(\Delta T)d(\Delta V)}{\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}(\Delta V)^2\exp\left[\frac{1}{2kT}\left(\frac{\partial p}{\partial V}\right)_T(\Delta V)\right]d(\Delta T)d(\Delta T)} = \frac{\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}(\Delta V)^2W(\Delta T,\Delta V)d(\Delta T)d(\Delta T)}{\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}(\Delta V)^2\exp\left[\frac{1}{2kT}\left(\frac{\partial p}{\partial V}\right)_T(\Delta V)\right]d(\Delta T)d(\Delta T)} = \frac{\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}(\Delta V)^2\exp\left[\frac{1}{2kT}\left(\frac{\partial p}{\partial V}\right)_T(\Delta V)\right]d(\Delta T)}{\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}\int_{-\infty}^{+\infty}
                                                                                                                        \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} W(\Delta T, \Delta V) d(\Delta T) d(\Delta V)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                (本将経历各种可能的涨落力作用,故长时间均值与系综平均相等,\langle F(t)F(t+	au) 
angle = \overline{F(t)F(t+	au)}
                                                                                                                                                                                                                                                                                                                                                                                                                  \int_{-\infty}^{+\infty} \exp \left| \frac{1}{2kT} \left( \frac{\partial p}{\partial V} \right)_T (\Delta V)^2 \right| dV
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  动量平均值和散差: 无外力时郎之万方程为 \frac{dp}{dt} = -\gamma p + F(t) , 其中 \gamma = \alpha/m , \Rightarrow \frac{d}{dt}(pe^{-\gamma t}) = e^{\gamma t}F(t) \Rightarrow p(t) = p(0)e^{-\gamma t} + e^{-\gamma t}\int_0^t e^{-\gamma \xi}F(\xi)d\xi , 因\overline{F}(\xi) = 0 得动量平均值: \overline{p}(t) = p(0)e^{-\gamma t} , 动量散差: \overline{(\Delta p)^2} = \frac{1}{2}
   -kT\left(\frac{\partial V}{\partial p}\right)_T = kTV\kappa_T, \overline{\Delta T\Delta V} = \overline{\Delta T} \ \overline{\Delta V} = 0,这说明T和V统计独立
   以S,p为自变量,W(\Delta S,\Delta p)=W_{m}\exp\left[-\frac{1}{2kC_{p}}(\Delta S)^{2}+\frac{1}{2kT}\left(\frac{\partial V}{\partial p}\right)_{S}(\Delta p)^{2}\right],于是\overline{(\Delta S)^{2}}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   \overline{[p(t) - \overline{p(t)}]^2} \ = \ \int_0^t d\xi' \int_0^t \overline{F(\xi) F(\xi')} e^{-\gamma (t - \xi)} e^{-\gamma (t - \xi')} d\xi \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} d\xi \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} d\xi \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} d\xi \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} d\xi \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} d\xi \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} d\xi \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} d\xi \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} d\xi \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} d\xi \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} d\xi \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} d\xi \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} d\xi \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} d\xi \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} d\xi \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} d\xi \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} d\xi \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} d\xi \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} d\xi \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} d\xi \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} d\xi \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} d\xi \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} d\xi \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} d\xi \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} d\xi \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} d\xi \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} dt \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} dt \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} dt \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} dt \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} dt \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} dt \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} dt \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} dt \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} dt \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} dt \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} dt \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} dt \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} dt \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} dt \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} dt \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} dt \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} dt \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} dt \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} dt \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} dt \ = \ 2 D_p \delta(\tau) \int_0^t e^{-2\gamma (t - \xi)} dt \ = \ 2 D_p \delta(\tau) \int_0
    kC_p, \overline{(\Delta p)^2} = -kT\left(\frac{\partial p}{\partial V}\right)_S, \overline{\Delta S \Delta p} = \overline{\Delta S \Delta p} = 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      rac{D_p}{\gamma}[1-e^{-2\gamma t}];当	au_c 《 t 《 1/\gamma,\overline{(\Delta p)^2} = 2D_p t,动量散差与位移平方平均值有类似规律,D_p-
    其他相关函数:以T,V为自变量,\Delta T \Delta S = \left( \frac{\partial S}{\partial T} \right)_V \left( \Delta T \right)^2 + \left( \frac{\partial S}{\partial V} \right)_T \Delta T \Delta V, \overline{\Delta T \Delta S} = \left( \frac{\partial S}{\partial T} \right)_V \overline{(\Delta T)^2} + \overline{(\Delta T)^2}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      动量扩散系数;当t \gg 1/\gamma, p(t) = 0, \overline{(\Delta p)^2} = \overline{p^2} = \frac{D_p}{\gamma}, \overline{\frac{p^2}{2m}} = \frac{1}{2}kT
    \left(\frac{\partial S}{\partial V}\right)_{T}\overline{\Delta T \Delta V} = \frac{C_{V}}{T}\overline{(\Delta T)^{2}} = kT, \overline{\Delta V \Delta p} = -kT, \overline{\Delta S \Delta V} = kT\left(\frac{\partial V}{\partial T}\right)_{p}, \overline{\Delta T \Delta p} = \frac{kT}{C_{V}}\left(\frac{\partial p}{\partial T}\right)_{V}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     \alpha kT,阻尼系数\infty动量扩散系数,粘滞阻力导致颗粒动能耗散和颗粒与介质达平衡,涨落力导致动量扩散;当t
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   1/\gamma, p(t) \approx e^{-\gamma t} \int_0^t e^{\gamma \xi} F(\xi) d\xi, \overline{p(t)p(t')} = e^{-\gamma (t+t')} \int_0^t d\xi \int_0^{t'} d\xi' \overline{F(\xi)F(\xi')} e^{\gamma (\xi+\xi')} = 2D_p \int_0^t d\xi \int_0^{t'} d\xi' \delta(\xi-\xi') e^{-\gamma (t-\xi)} e^{-\gamma (t'-\xi')}, \overline{p(t)p(t')} = \frac{D_p}{\gamma} [e^{-\gamma (t-t')} - e^{-\gamma (t+t')}], (t > t')
   粒子数N的涨落:当N固定,nV=N\Rightarrow rac{\Delta n}{n}+rac{\Delta V}{V}=0,粒子数密度相对涨落:rac{(\Delta n)^2}{n^2}=rac{(\Delta V)^2}{V^2}=rac{kT}{V}\kappa_T;当V固
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      (t'), \overline{p(t)p(t')} = \frac{Dp}{\gamma} [e^{-\gamma(t'-t)} - e^{-\gamma(t'+t)}], (t < t'), \overline{p(t)p(t')} = \frac{Dp}{\gamma} [e^{-\gamma(t'-t)} - e^{-\gamma(t'+t)}] \approx \frac{Dp}{\gamma} [e^{-\gamma(t'-t)} - e^{-\gamma(t'+t)}]
   能量E的涨落:以T,V为自变量,\Delta E = \left(\frac{\partial E}{\partial T}\right)_V \Delta T + \left(\frac{\partial E}{\partial V}\right)_T \Delta V = C_V \Delta T + \left(\frac{\partial E}{\partial V}\right)_T \Delta V \Rightarrow \overline{(\Delta E)^2}:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      rac{D_p}{\sim}e^{-\gamma|t'-t|}=\stackrel{'}{=}mkTe^{-\gamma|t'-t|},(t,t'>1/\gamma),不同时刻的涨落力无关联,不同时刻的动量却相互关联,因为动量是
   C_V^2\overline{(\Delta T)^2} + 2C_V\left(\frac{\partial E}{\partial V}\right)_T\overline{\Delta T \Delta V} + \left(\frac{\partial E}{\partial V}\right)_T\overline{(\Delta V)^2} = kT^2C_V + kTV\kappa_T\left(\frac{\partial E}{\partial V}\right)_T^2, \\ \pm N \mathcal{K}
      \mathfrak{E}, \mathbb{H}\left(\frac{\partial E}{\partial V}\right)_T = \frac{N}{V} \left(\frac{\partial E}{\partial N}\right)_T \tilde{\mathbb{H}}(\overline{\Delta E})^2 = kT^2C_V + \frac{N^2}{V}kT\kappa_T \left(\frac{\partial E}{\partial N}\right)_T^2 = kT^2C_V + \overline{(\Delta N)^2} \left(\frac{\partial E}{\partial N}\right)_T T
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      布朗颗粒的位移:经时间t后,位移:x(t)=rac{1}{m}\int_0^t p(\xi)d\xi,位移平方平均值:\overline{x^2(t)}=rac{1}{m^2}\int_0^t d\xi \int_0^t d\xi' \overline{p(\xi)p(\xi')}=
                         5 布朗运动:处于气或液体中的微小颗粒因受周围气或液体分子碰撞而产生的不规则随机运动;布朗粒子通常很小(直径10<sup>--</sup>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      \frac{kT}{m}\int_0^t d\xi \int_0^t d\xi' e^{-\gamma |\xi-\xi'|} = \frac{2kT}{m}t = \frac{2kT}{\alpha}t,与布朗理论结果相同
 I(n) \ = \ \int_0^\infty \frac{x^{n-1}}{e^x-1} \, dx, \\ I(2) \ = \ \frac{\pi^2}{6}, \\ I(3) \ = \ 2 \sum_{k=1}^\infty \frac{1}{k^3} \ \approx \ 2.404, \\ I(4) \ = \ \frac{\pi^4}{15}, \\ I(\frac{3}{2}) \ 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   \frac{\sqrt{\pi}}{2} \sum_{k=1}^{\infty} \frac{1}{k^{3/2}} = \frac{\sqrt{\pi}}{2} \times 2.612, I(\frac{5}{2}) = \frac{3\sqrt{\pi}}{4} \sum_{k=1}^{\infty} \frac{1}{k^{5/2}} = \frac{3\sqrt{\pi}}{4} \times 1.341 \qquad \int_{0}^{\infty} \frac{x dx}{e^{x} + 1} = \frac{\pi^{2}}{12} \frac{1}{2} \left( \frac{x^{2}}{2} + \frac{1}{2} \right) \frac{1}{2} \left( \frac{x^{2}}{2} + \frac{1}{2} + \frac{1}{2} \right) \frac{1}{2} \left( \frac{x^{2}}{2} + \frac{1}{2} + \frac{1}{2} + \frac{1}{2} \right) \frac{1}{2} \left( \frac{x^{2}}{2} + \frac{1}{2} + \frac
    \frac{\sqrt{\pi}}{4\alpha^{3/2}}, I(3) = \frac{1}{2\alpha^{2}}, I(4) = \frac{3\sqrt{\pi}}{8\alpha^{5/2}}, I(5) = \frac{1}{\alpha^{3}}
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1.2 热平衡定律(热0律):若A,B各与处于同一状态C达热平衡,若A,B热接触,两者亦热平衡
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   \frac{V}{C_p}(T\alpha - 1); 绝热膨胀:\mu_S = \left(\frac{\partial T}{\partial p}\right)_S = \frac{T}{C_p} \left(\frac{\partial V}{\partial T}\right)_p = \frac{VT\alpha}{C_p}
  1.3 定压膨胀系数:\alpha=\frac{1}{V}\left(\frac{\partial V}{\partial T}\right)_p;定容压力系数:\beta=\frac{1}{p}\left(\frac{\partial p}{\partial T}\right)_V;等温压缩系数:\kappa_T=-\frac{1}{V}\left(\frac{\partial V}{\partial p}\right)_T
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                \mathbf{2.4}\ dU = C_V \, dT + \left[T \left(\frac{\partial p}{\partial T}\right)_V - p\right] \, dV \Rightarrow U = \int \left\{C_V \, dT + \left[T \left(\frac{\partial p}{\partial T}\right)_V - p\right] \, dV\right\} + U_0
 \left(\frac{\partial y}{\partial x}\right)_z \left(\frac{\partial x}{\partial z}\right)_y \left(\frac{\partial z}{\partial y}\right)_x = -1; \left(\frac{\partial y}{\partial x}\right)_z \left(\frac{\partial x}{\partial y}\right)_z = 1; \left(\frac{\partial y}{\partial x}\right)_z = \left(\frac{\partial y}{\partial w}\right)_z \left(\frac{\partial w}{\partial x}\right)_z 玻意耳定律:当T, n, pV = C; 阿伏伽德罗定律:相同T, p下任何气体V_m均相同,V_{m0} = 22.4 L/\text{mol}(1\text{atm}, 273\text{K})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                dS = \frac{C_V}{T} \, dT + \left(\frac{\partial p}{\partial T}\right)_V \, dV \Rightarrow S = \int \left[\frac{C_V}{T} \, dT + \left(\frac{\partial p}{\partial T}\right)_V\right] + S_0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             dH = C_p dT + \left[V - T\left(\frac{\partial V}{\partial T}\right)_p\right] dp \Rightarrow H = \int \left\{C_p dT + \left[V - T\left(\frac{\partial V}{\partial T}\right)_p\right] dp\right\} + H_0
 理想气体物态方程:pV = nRT,(R = 8.3145 \text{J} \cdot \text{mol}^{-1} \cdot \text{K}^{-1}); 非理想气体状态方程:范德瓦尔斯方程:(p + \frac{an^2}{V^2})(V - \frac{an^2}{V^2})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               dS = \frac{C_P}{T} dT - \left(\frac{\partial V}{\partial T}\right)_p dp \Rightarrow S = \int \left[\frac{C_P}{T} dT - \left(\frac{\partial V}{\partial T}\right)_p dp\right] + S_0 计算要点:1.已知物态方程和C_V, C_P,可得U, SnH; 2.由此得其他热力学函数; 3.C_V(T,V) = C_V(T,V_0) +
  nb)=nRT; 昂尼斯方程:p=rac{nRT}{V}\left[1+rac{n}{V}B(T)+\left(rac{n}{V}
ight)^2C(T)+\cdots
ight], (B,C-第2,3位力系数)
1.4 体积功:dW=-pdV,W=-\int_{V_1}^{V_2}pdV; 功的一般表达式:dW=\sum_{i=1}^{I}Y_idy_i(Y_i一广义之标) 1.5 热力学第一定律:自然界一切物质都具有能量,能量有各种不同的形式,可以从一种形式转化为另一种形式,从一个物体传递到另一个物体,在传递和转化中能量的数量不变;\Delta U=W+Q或dU=dW+dQ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             T \int_{V_0}^{V} \left( \frac{\partial^2 p}{\partial T^2} \right)_{V} dV, C_p(T, p) = C_p(T, p_0) - T \int_{p_0}^{p} \left( \frac{\partial^2 V}{\partial T^2} \right)_{p} dp
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                2.5 F(T,V)作特性函数,S=-\left(\frac{\partial F}{\partial T}\right)_{V}, p=-\left(\frac{\partial F}{\partial V}\right)_{T}, U=F-T\left(\frac{\partial F}{\partial T}\right)_{V}(吉布斯-亥姆霍兹方程),H=
  1.6\ \text{等容热容量}: C_V = \lim_{\Delta T \to 0} \left(\frac{\Delta Q}{\Delta T}\right)_V = \left(\frac{\partial U}{\partial T}\right)_V;\ \text{等压热容量}: C_p = \lim_{\Delta T \to 0} \left(\frac{\Delta Q}{\Delta T}\right)_p
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       \frac{(\partial T)_{V}}{G(T,p)} + \frac{(\partial V)_{T}}{(\partial T)_{p}} + \frac{(\partial L)_{V}}{(\partial T)_{p}} + H = G - T \left(\frac{\partial G}{\partial T}\right)_{p} (  [古
 焓:H=U+pV;C_p=\left(\frac{\partial H}{\partial T}\right)_p 对理想气体,C_p-C_V=nR,C_V=\frac{nR}{\gamma-1},(热容比\gamma=\frac{C_p}{C_V})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                布斯-亥姆霍兹方程),F = G - pV, U = G - pV + TS
 1.8 理想气体的绝热过程:pV^{\gamma}=C_1, TV^{\gamma-1}=C_2, p^{\gamma-1}T^{-\gamma}=C_3 1.10 热力学第二定律 开介文表述:\tau可能从单一热源吸热使之完全变为有用功而不引起其他变化 克劳修斯表述:\tau可能把能量从低温物体传到高温物体而不引起其他变化
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                {f 2.6} 平衡辐射特性的热力学函数:辐射压力和能量密度之间的关系:p=u/3,内能:U=aVT^4,熵:S=rac{4}{3}aT^3V,自由
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                能:F = -\frac{1}{3}aVT^4,焓:H = \frac{4}{3}aVT^4,吉布斯函数:G = F + pV = 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               1.11 卡诺定理:所有工作在一定温度间的热机,以可逆热机效率最高,\eta=1-rac{Q_2}{Q_1}\leq 1-rac{T_2}{T_1}(对可逆热机=,不可逆热机<)
1.11 年間起生河打土中圧 足血収円的が高れいの以上が収入を取り、カー I - Q_1 = I - T_1、のうなたのでも、ことのなり、日、1.14 嫡変:S_B - S_A = \int_A^B \frac{dQ}{T}(沿可逆过程积分、不可逆过程的嫡変可用相同初末态的可逆过程计算) 1.16 嫡増加展理系統经色維过程从一状态到另一状态、其嫡水不减少。考过程可逆,则嫡保持不变,若不可逆,则嫡增;推论:孤立系统内部任何自发过程总朝着嫡增方向进行。当嫡达最大,系统平衡 1.18 自由能:F = U - TS:最大功原理、等温过程中,系统对外做功不大于其自由能的减少,W \le F_A - F_B,自由能判据、等温等容条件下,F水不增加、不可逆反应总朝F 上的方向进行:古布斯函数:G = F + pV = U - TS + pV;古布斯函数增据:等温度过程中,统不增加、不可逆反应总朝F 上的方向进行:1. 执行季基本微分方程:dU = TdS - pdV,H = TdS + Vdp,dF = -SdT - pdV,dG = -SdT + Vdp 麦克斯韦关系:\left(\frac{\partial U}{\partial S}\right)_V = T, \left(\frac{\partial U}{\partial P}\right)_S = -p \Rightarrow \left(\frac{\partial T}{\partial V}\right)_S = -p \Rightarrow \left(\frac{\partial F}{\partial V}\right)_V = -S, \left(\frac{\partial F}{\partial V}\right)_T = -p \Rightarrow \left(\frac{\partial S}{\partial V}\right)_T = \left(\frac{\partial F}{\partial V}\right)_T = -p \Rightarrow \left(\frac{\partial S}{\partial V}\right)_T = -p \Rightarrow \left(\frac{\partial
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   -SdT + \mu_0 \mathcal{H}dm, G = F - \mu_0 \mathcal{H}m = U - TS - \mu_0 \mathcal{H}m, dG = -SdT - \mu_0 md\mathcal{H}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                \mu_0 \left( \frac{\partial \mathcal{H}}{\partial S} \right)_m, \left( \frac{\partial T}{\partial \mathcal{H}} \right)_S = -\mu_0 \left( \frac{\partial m}{\partial S} \right)_{\mathcal{H}}, \left( \frac{\partial S}{\partial m} \right)_T = -\mu_0 \left( \frac{\partial \mathcal{H}}{\partial T} \right)_m, \left( \frac{\partial S}{\partial \mathcal{H}} \right)_T = \mu_0 \left( \frac{\partial m}{\partial T} \right)_{\mathcal{H}}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               3.2 开系的热力学基本方程:dU = TdS - pdV + \mu dn, \mu = \left(\frac{\partial U}{\partial n}\right)_{S,V}; dG = -SdT + Vdp + \mu dn,其
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             中化学势 \mu = \left(\frac{\partial G}{\partial n}\right)_{T,p} G(T,p,n) = n\mu;dH = TdS + Vdp + \mu dn, \mu = \left(\frac{\partial H}{\partial n}\right)_{S,p};dF = 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             「のか T,p」 「のか S,p」 「した S,p
 \left(\frac{\partial p}{\partial T}\right)_{V}^{};\quad \left(\frac{\partial G}{\partial T}\right)_{p}=-S, \left(\frac{\partial G}{\partial p}\right)_{T}=V \Rightarrow \left(\frac{\partial S}{\partial p}\right)_{T}=-\left(\frac{\partial V}{\partial T}\right)_{p}
\mathbf{2.2} \, \text{內能方程}: dU \, = \, T \, \left( \frac{\partial S}{\partial T} \right)_V \, dT \, + \, \left[ T \, \left( \frac{\partial p}{\partial T} \right)_V \, - \, p \right] \, dV \, ; C_V \, = \, T \, \left( \frac{\partial S}{\partial T} \right)_V \, , \, \left( \frac{\partial U}{\partial V} \right)_T \, = \, T \, \left( \frac{\partial p}{\partial T} \right)_V \, - \, p \, dV \, ; C_V \, = \, T \, \left( \frac{\partial S}{\partial T} \right)_V \, , \, \left( \frac{\partial U}{\partial V} \right)_T \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, - \, p \, dV \, ; C_V \, = \, T \, \left( \frac{\partial S}{\partial T} \right)_V \, , \, \left( \frac{\partial U}{\partial V} \right)_T \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, - \, p \, dV \, ; C_V \, = \, T \, \left( \frac{\partial S}{\partial T} \right)_V \, , \, \left( \frac{\partial U}{\partial V} \right)_T \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, - \, p \, dV \, ; C_V \, = \, T \, \left( \frac{\partial S}{\partial T} \right)_V \, , \, \left( \frac{\partial U}{\partial V} \right)_T \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, - \, p \, dV \, ; C_V \, = \, T \, \left( \frac{\partial S}{\partial T} \right)_V \, , \, \left( \frac{\partial U}{\partial V} \right)_T \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, - \, p \, dV \, ; C_V \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, , \, C_V \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, - \, p \, dV \, ; C_V \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, , \, C_V \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, , \, C_V \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, , \, C_V \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, , \, C_V \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, , \, C_V \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, , \, C_V \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, , \, C_V \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, , \, C_V \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, , \, C_V \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, , \, C_V \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, , \, C_V \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, , \, C_V \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, , \, C_V \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, , \, C_V \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, , \, C_V \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, , \, C_V \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, , \, C_V \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, , \, C_V \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, , \, C_V \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, , \, C_V \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, , \, C_V \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, , \, C_V \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, , \, C_V \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, , \, C_V \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, , \, C_V \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, , \, C_V \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, , \, C_V \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, , \, C_V \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, , \, C_V \, = \, T \, \left( \frac{\partial P}{\partial T} \right)_V \, , \, C
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               的平衡性质 克拉珀龙方程:沿相平衡曲线,\frac{dp}{dT} = \frac{S_m^\beta - S_m^\alpha}{V_m^\beta - V_m^\alpha} = \frac{L}{T(V_m^\beta - V_m^\alpha)},相变潜热. L = T(S_m^\beta - S_m^\alpha) 4.8 热力学第三定律 能斯特定理.\lim_{T\to 0} (\Delta S)_T = 0; 热力学第三定律:不可能通过有限的步骤使一个物体冷却到绝对温度
端方程:dH = T\left(\frac{\partial S}{\partial T}\right)_p dT + \left[V - T\left(\frac{\partial V}{\partial T}\right)_p\right] dp \Rightarrow C_p = T\left(\frac{\partial S}{\partial T}\right)_p, \\ \left(\frac{\partial H}{\partial p}\right)_T = V - T\left(\frac{\partial V}{\partial T}\right)_p
 定压与定容热容量之差:C_P-C_V=T\left(\frac{\partial S}{\partial V}\right)_T\left(\frac{\partial V}{\partial T}\right)_p=T\left(\frac{\partial p}{\partial T}\right)_V\left(\frac{\partial V}{\partial T}\right)_p=TVp\alpha\beta=\frac{VT\alpha^2}{\kappa_T}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                的零度;推论:\lim_{T\to 0}\left(\frac{\partial V}{\partial T}\right)_p = -\lim_{T\to 0}\left(\frac{\partial S}{\partial p}\right) = 0, \lim_{T\to 0}\left(\frac{\partial P}{\partial T}\right)_V = \lim_{T\to 0}\left(\frac{\partial S}{\partial V}\right)_T = 0
 2.3 节流过程:气体由高压流至低压并达定常状态,为等焓过程; 焦汤系数:\mu = \left(\frac{\partial T}{\partial p}\right)_H = \frac{1}{C_p} \left[T\left(\frac{\partial V}{\partial T}\right)_p - V\right] =
7-4试证、对遵从玻尔兹曼分布的定域系统,熵可表为S=-Nk\sum_S P_S \ln P_S、式中P_S—粒子处在量子态。的極率,P_S=e^{-\alpha-\beta\varepsilon_S}/N=e^{-\beta\varepsilon_S}/Z_1,\sum_s—对粒子所有量子态求和、对满足经典核服条件的非定域系统,熵的表达式有何不同? P_S满足归一化条件\sum_S P_S=1,\ln P_S=-\ln Z_1-\beta\varepsilon_S,粒子平均能量:E=\sum_S P_S\varepsilon_S,定域系统的熵:S=Nk(\ln Z_1-\beta\frac{\partial}{\partial\beta}\ln Z_1)=Nk(\ln Z_1+\beta\varepsilon)=Nk\sum_S P_S(\ln Z_1+\beta\varepsilon_S)=Nk\sum_S P_S\ln P_S,对满
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                \sum_{S}an_{x},n_{y},n_{z},\mu\uparrow他T\downarrow,T_{C}下,N=\sum_{n_{x},n_{y},n_{z}}(e^{\tilde{n}_{x}+\tilde{n}_{y}+\tilde{n}_{z}}-1)^{-1},其中\tilde{n}_{i}=(\hbar\omega_{i}/kT_{c})n_{i},题设
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                极限下化求和为积分,N=(kT_C/\hbarar{\omega})\int dar{n}_xdar{n}_ydar{n}_z/(e^{ar{n}_x+ar{n}_y+ar{n}_z}-1),将被积函数如上题展开即得
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               8-7来下下V內光子气体的平均总光子數 V內\omega \sim \omega + d\omega范围內光子的量子态數:D(\omega)d\omega = (V/\pi^2c^3)\omega^2d\omega,平均光子數:\overline{N}(\omega,T)d\omega = D(\omega)d\omega/(e^{\hbar\omega/kT}-1),总光子數:\overline{N}(T) = (V/\pi^2c^3)\int_0^{+\infty}\omega^2d\omega/(e^{\hbar\omega/kT}-1)
  是经典极限条件的定域系统,S=Nk(\ln Z_1-\beta\partial\ln Z_1/\partial\beta)-k\ln N!=-Nk\sum_sP_s\ln P_s-k\ln N!=-Nk\sum_sP_s\ln P_s-Nk(\ln N-1)7-6晶体含N个原子,当原子离开正常位置,晶体中就出现了空位和间隙原子,晶体的这种缺陷称福仑克尔缺陷,(a)假设正常位置和见
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               1), \forall x = \hbar \omega / k T, \overline{N}(T) = (V/\pi^2 c^2) (kT/\hbar)^3 \int_0^{+\infty} x^2 dx / (e^x - 1) = 2.404 (k^3/\pi^2 c^3 \hbar^3) V T^3, n = \overline{N}/V, n (1000) \approx 2 \times 10^{16} \, \mathrm{m}^{-3}, n (3) \approx 5.5 \times 10^8 \, \mathrm{m}^{-3}
(\hat{\sigma}, (\partial V/\partial p)_T) = (\partial V/\partial p)_S
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                8-26由N个自旋极化的粒子组成的理想费米气体处在径向频率\omega_r,轴向频率\lambda\omega_r的磁光陷阱内,粒子能量:\varepsilon
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             (N-n)\ln(N-n)],严德志子极小要求\partial F/\partial n=W-kT\ln(N-n/n)=0,因n(N-n)],严德志子极小要求\partial F/\partial n=W-kT\ln(N-n/n)=0,因n(N-n)],严德志子极小要求\partial F/\partial n=W-kT\ln(N-n/n)=0,因n(N-n),因n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n),因为n(N-n)。因为n(N-n),因为n(N-n),因为n(N-n)。因为n(N-n),因为n(N-n)。因为n(N-n),因为n(N-n)。因为n(N-n) 和n(N-n) 和n(N-n)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             EN = \sum_{n_x, n_y, n_z} (e^{\beta(\varepsilon_x + \varepsilon_y + \varepsilon_z - \mu)} + 1), \exists \varepsilon_i = n_i \text{nor}, i \varepsilon
     mv_2, \varepsilon_1 + mv_1^2/2 + \hbar\omega = \varepsilon_2 + mv_2^2/2,式(1)平方并处以2m得mv_1^2/2 + \hbar^2k^2/2m + \hbar v_1 \cdot k = mv_2 \cdot k
    \frac{1}{2}mv_2^2,代入式(2)得\hbar\omega_0 = \hbar\omega - \hbar v_1 \cdot \mathbf{k} - \hbar^2 k^2/2m,或\omega_0 = \omega - v_{1z}\omega/c - \hbar\omega^2/2mc^2,考
  度m\sim 10^{-26}{\rm kg}, v_{1z}\sim 3\times 10^2 {\rm m\cdot s^{-1}}, \omega\sim 10^{15}{\rm s^{-1}}有1 \gg v_{1z}\gg \hbar\omega/2mc^2, 右側第三 项可忽略, \omega=\omega/(1-v_{1z}/c) \approx \omega_0(1+v_{1z}/c), T下气体原子速度z分量在v_z\sim v_z+dv_z范围内的
域中感転, \omega = \omega/(1 - v_{1z}/c) \approx \omega_0(1 + v_{1z}/c), T ト气体原子速度を分量在v_z \sim v_z + dv_z范制内的 概率\propto e^{-mv_z^2/2kT} dv_z, \omega \sim \omega + d\omega范围内概率\propto e^{-(m/2kT)(c^2(\omega-\omega_0)^2/\omega_0^2)} c/\omega_0 d\omega, 归一化 得F(\omega) = (2\pi\delta^2)^{-1/2} e^{-(\omega-\omega_0)^2/2\delta^2}, \delta = \omega(kT/mc^2)^{1/2} 7-11表面活性物质的分子在液面熵作二维自由运动,可视为二维气体,试写出二维气体中分子的速度分布和速率分布,并求平均速度v。根据速率v_m和方均根速率v_s 速度分布:(m/2\pi kT)e^{-m(v_x^2+v_y^2)/2kT} dv_x dv_y,速率分 \frac{2}{2} 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             田四一化木叶\sum_S \rho_S = 1和以 = 1/\rho_S物う = k \ln \mathcal{Q} = k \sum_S \rho_S \ln \mathcal{Q} = 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            \pi: (m/kT)e^{-mv^2/2kT}vdv, \bar{v} = (m/kT)\int_0^\infty e^{-mv^2/2kT}vdv = \sqrt{\pi kT/2m}, \bar{v}^2 = (m/kT)
  \int_{0}^{+\infty} e^{-mv^2/2kT} v^3 dv = 2kT/m, v_s = \sqrt{2kT/m}, d(e^{-mv^2/2kT} v)/dv = 0 \Rightarrow v_m = \sqrt{kT/m}
  oldsymbol{v}^{	au} oldsymbol{v}^{	a
  分子1和分子2各自处在速度间隔dv_1和dv_2的概率:dW = dW_1 \cdot dW_2 = (m/2\pi kT)^{3/2} e^{-mv^2/2kT} dv_1 ·
(m/2\pi kT)^{3/2}e^{-mv^2/2kT}dv_2, 熊心速度:v_c=(m_1v_1+m_2v_2)/(m_1+m_2), 相対速度:v_r=v_2-v_1. 当m_1=m_2=m, 简化为v_c=(v_1+v_2)/2, v_r=v_2-v_1. 动能:E_k=m_1v_1^2/2+m_2v_2^2/2=v_1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                \frac{2i=1}{(1/N!h^{2N})}(2\pi m/\beta h^2)^N Q, 其中Q = \int e^{-\beta\sum_i < j} \frac{\phi(r_{ij})}{dr_1 \cdots dr_N}, \forall f_{ij} = e^{-\beta\phi(r_{ij})}
 m'v_c^2/2 + \mu v_r^2/2,其中m' = m_1 + m_2, \mu = m_1 m_2/(m_1 + m_2),当m_1 = m_2 = m, m' = 2m, \mu = m/2,dW = (m'/2\pi kT)^{3/2}e^{-m'v_c^2/2kT}dv_c \cdot (\mu/2\pi kT)^{3/2}e^{-\mu v_r^2/2kT}dv_r = dW_c dW_r,相对速度
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             \begin{array}{ll} (1/Nm^{2})(2\pi m/\beta h^{2}) & \text{Gr}_{3} + \text{Gr}_{4} & \text{Gr}_{3} + \text{Gr}_{4} & \text{Gr}_
 的概率分布dW_r=(\mu/2\pi kT)^{3/2}e^{-\mu v_r^2/2kT}dv_r相对速率的分布:4\pi(\mu/2\pi kT)^{3/2}e^{-\mu v_r^2/2kT}v_r^2dv_r,相
对速率的平均值:\bar{v}_r=4\pi(\mu/2\pi kT)^{3/2}\int_0^\infty e^{-\mu v_r^2/2kT}v_r^2dv_r=\sqrt{8kT/\pi\mu}7-14分子从器壁的小孔中射出,求在射出的分子束中,分子的平均速率/方均根速率/平均能量
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                dk内:(L^2/2\pi)kdk,\omega \sim \omega + d\omega范围内振动模式数:D(\omega)d\omega = 2(L/2\pi)(1/c) = B_2\omega d\omega,满
 面积器壁上v\sim v+dv范围内的分子数:d\Gamma(v)=\pi n(m/2\pi kT)^{3/2}e^{-mv^2/2kT}v^3dv,平均速率:\bar{v}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                \mathbb{E}B_2\int_0^{\omega_D}\omega d\omega = 3N,德拜頻率:\omega_D^2 = 6N/B_2,内能:U = U_0 + B_2\int_0^{\omega_D}\hbar\omega^2 d\omega/(e^{\hbar\omega/kT}-1),高
 (\int_0^{+\infty} v \, d\Gamma(v))/(\int_0^{+\infty} d\Gamma) = \sqrt{9\pi kT/8m}, \\ v^2 = (\int_0^{+\infty} v^5 e^{-mv^2/2kT} \, dv)/(\int_0^{+\infty} v^3 e^{-mv^2/2kT} \, dv)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             4kT/m, v_S = \sqrt{\overline{v^2}} = \sqrt{4kT/m},平均动能:m\overline{v^2}/2 = 2kT
  7-17已知粒子遵经典玻尔兹曼分布,其能量表达式:ε = (p_x^2 + p_y^2 + p_z^2)/2m + ax^2 + bx,求粒子的平均能量
 方\varepsilon = (p_x^2 + p_y^2 + p_z^2)/2m + a(x+b/2a)^2 - b^2/4a,能量均分定理:\varepsilon = 2kT - b^2/4a
7-23对双原子分子,常温下kT ≫转动的能级间距,求转动熵 转动配分函数:Z_1^r = (1/h^2)\int e^{-\beta}(p_\theta^2 + p_\varphi^2/\sin^2\theta)/2I dp_\theta dp_\varphi d\theta d\varphi = 2I/\beta h^2, S^r = Nk(\ln Z_1^r - \beta\partial(\ln Z_1^r)/\partial\beta) = Nk[\ln(2I/\beta h^2) + 1] 7-28晶体中原子密度n,角动量量子数1,外场B下,原子磁矩可有三种不同取向,忽略磁矩向相互作用,求T下,磁化强度M,及其在高温弱场和低温强场下近似 配分函数:Z_1 = e^\beta \mu B + 1 + e^{-\beta} \mu B = 1 + 2\cosh(\beta \mu B), 磁化强度M = (n/\beta)\partial(\ln Z_1)/\partial B = n\mu(2\sinh\beta\mu B)/(1 + 2\cosh\beta\mu B), 高温弱场下, <math>\beta\mu B \ll 1, S_1 S_2 S_2 S_3 S_4 S_
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                B(kT/\hbar)^{5/2} \hbar \int_0^{+\infty} x^{3/2} dx/(e^x - 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               9-20试证在巨正则系综理论中熵可表为S=-k\ln_n\ln_s\rho_{N,s}, \lim\rho_{N,s}, \lim\rho_{N,s}=(1/\Xi)e^{-\alpha N-\beta E_S}系统 有N个粒子,处在状态。的概率 由归一化条件\sum_{N,s}\rho_{N,s}=1和\ln\rho_{N,s}=-(\ln\Xi+\alpha N+\beta E_S)有S=
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               N(m) = 1 (N(m) = 1 ) N(m) = 1 (N(m) = 1 (N(m) = 1 ) N(m) = 1 (N(m) = 1 (N(m) = 1 ) N(m) = 1 (N(m) = 1 ) N(m) = 1 (N(m) = 1 (N(m) = 1 ) N(m) = 1 (N(m) = 1 (N(m) = 1 ) N(m) = 1 (N(m) = 1 (N(m) = 1 ) N(m) = 1 (N(m) = 1 (N(m) = 1 (N(m) = 1 ) N(m) = 1 (N(m) = 1 (N(m) = 1 ) N(m) = 1 (N(m) = 1 (N(m) = 1 ) N(m) = 1 (N(m) = 1 (N(m) = 1 (N(m) = 1 ) N(m) = 1 (N(m) = 1 (N(m) = 1 (N(m) = 1 ) N(m) = 1 (N(m) = 
度M=(n/\beta)\partial(\ln Z_1)/\partial B=n\mu(2\sinh \beta\mu B)/(1+2\cosh \beta\mu B),高温弱頻下,\beta\mu B\ll 1,\sinh \beta\mu B\approx \beta\mu B,\cosh \beta\mu B\approx 1,M=(2/3)(n\mu^2/kT)B,反之,\sinh \beta\mu B\approx \cosh \beta\mu B\approx e^{\beta\mu}B/2,M\approx n\mu 8年8と3院、理想要来系統的嫡可表为S_{\Gamma,D}=-k\sum_s[f_s\ln f_s+(1-f_s)\ln(1-f_s)],其中f_s=\frac{1}{2}干态ま上的平均粒子载,\sum_s 对各量子态求和,并证当f_s\ll 1,S_{B,E}\approx S_{\Gamma,D}\approx S_{M,B}=-k\sum_s[f_s\ln f_s-f_s) 理想要来系統的第:S_{\Gamma,D}=k\sum_l[\omega_l\ln\omega_l-\alpha_l\ln\alpha_l-(\omega_l-\alpha_l)\ln(\omega_l-\alpha_l)]=-k\sum_l[(\omega_l-\alpha_l)\ln((\omega_l-\alpha_l))+\alpha_l\ln\alpha_l-(\omega_l)-\alpha_l)\ln(1-\alpha_l/\omega_l)-(\alpha_l/\omega_l)\ln(\alpha_l/\omega_l)],或件的一个数字能数求和,因f_s=a_l/\omega_l,\sum_l\sim s,S_{\Gamma,D}=-k\sum_s[f_s\ln f_s+(1-f_s)\ln(1-f_s)],当f_s\ll 1,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                (1/n!)Z_1^n—n个粒子的正则配分函数,\ln\Xi=e^{-\alpha}Z_1,\bar{n}=-\partial(\ln\Xi)/\partial\alpha=e^{-\alpha}Z_1=\ln\Xi,代入得
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                9-23单原子分子理想气体与固体吸附面接触达平衡,被吸附分子可在吸附面上二维运动,能量:p^2/2m
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               数 Z_1=(1/\hbar^2)\int e^{-eta(p^2/2m-arepsilon_0)}dxdydp_xdp_y=A(2\pi m/eta\hbar^2)e^{eta arepsilon_0-单粒子配分函数,代入得至=\exp[e^{-lpha}A(2\pi m/eta\hbar^2)e^{eta arepsilon_0}],\overline{N}=A(2\pi mkT/\hbar^2)e^{(arepsilon+\mu)/kT},代入单原子分子理想气体化学势并处以A得
  8-4试证,在热力学极限下均匀二维理想玻色气体不会发生玻-爱凝聚
                                                                                                                                                                                                                                                                                               临界温度由\int_{0}^{+\infty} D(\varepsilon)d\varepsilon/(e^{\varepsilon/kT_c}-1) = n确
  定,态密度:D(\varepsilon)d\varepsilon = (2\pi L/h^2)md\varepsilon,代入得(2\pi L^2/h^2)m\int_0^{+\infty} d\varepsilon/(e^{\varepsilon/kT_c} - 1) = n,令x
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               9-25试证玻尔兹曼分布的涨落:(a_l - \bar{a}_l)^2 = \bar{a}_l 视能级\varepsilon_l上的粒子为一开系,(a_l - \bar{a}_l)^2 = -\partial \bar{a}_l/\partial \alpha得 9-26试证光子气体,(a_l - \bar{a}_l)^2 = -(1/\beta)\partial \bar{a}_l/\partial \varepsilon_l \Xi = \sum_{a_l} e^{-\beta \varepsilon_l a_l}, \bar{a}_l
 \varepsilon/kT_{c}, (2\pi L^{2}/h^{2})mkT_{c}\int_{0}^{+\infty}dx/(e^{x}-1) = n, \mathbb{R}H1/(e^{x}-1) = 1/(e^{x}(1-e^{-x})) = 1/(e^{x}(1-e^{-x}))
e^{-x}(1+e^{-x}+\cdots),\int_0^\infty dx/(e^x-1)=\sum_{n=1}^\infty 1/n,級數发散意味着有限温度下化学势不可能趋于0,故 8-5约束在磁光陷阱中的理想原子气体,在三维谐振势场V=m(\omega_x^2x^2+\omega_y^2y^2+\omega_z^2z^2)/2中运动,若为玻色子,试
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                (1/\Xi)\sum_{a_l}a_le^{-\beta\varepsilon_la_l}=(\sum_{a_l}a_le^{-\beta\varepsilon_la_l})/(\sum_{a_l}e^{-\beta\varepsilon_la_l}),求导即得,可代入\bar{a}_l=1/(e^{\beta\varepsilon_l}-1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                -10-8=4\pm6\pi0 நூக்க புறியூர் கட்கு நடிக்க பிறிய கட்க நடிக்க நடிக்
证T \le T_c下,有大量原子凝聚在基态,T_c满足N = 1.202(kT_c/\hbar\omega)^3 三维谐振子能量:\varepsilon = \hbar\omega_x(n_x + 1/2) + \hbar\omega_y(n_y + 1/2) + \hbar\omega_z(n_z + 1/2), n_x/y/z = 0, 1, \cdots,在量子态n_x, n_y, n_z上的粒子
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                0, \overline{F_i(t)F_j(t')} = 2m\gamma kT\delta_{ij}\delta(t-t'),试证t后位移平方平均值\overline{[{m x}-{m x}(0)]^2} = \sum_i \overline{[x_i-x_i(0)]^2} = 6kTt/m\gamma
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一维布朗: $[x_i - x_i(0)]^2 = 2kTt/m\gamma$,即得

数: $a_{n_x,n_y,n_z}=(e^{(\varepsilon-\mu)/kT}-1)^{-1}$,化学势 $\mu<\varepsilon_0=(\hbar/2)(\omega_x+\omega_y+\omega_z)$,且满足N=