

$$\ddot{x} = \omega \sin \alpha (A e^{\omega \sin \alpha t} - B e^{-\omega \sin \alpha t}) = \dot{x}(t).$$

由(7)第一式得 $\ddot{x} - (\omega \sin \alpha)^2 x' = 0$, $\ddot{x}' = \frac{dx'}{dt} = \cancel{x} \frac{dx'}{dx} \dot{x} \frac{dx'}{dx} = (\omega \sin \alpha)^2 x'$

$$\cancel{\dot{x}} dx' \dot{x} dx' = (\omega \sin \alpha)^2 x' dx', \quad x'^2 = (\omega \sin \alpha)^2 x^2 + C.$$

在 $t=0$ 时, $x=0$, $\dot{x}=0$, $\dot{x}' = \dot{x} = 0$, $x' = x + k = k$.

$$\therefore C = -k^2 (\omega \sin \alpha)^2, \quad \dot{x}'^2 = (\omega \sin \alpha)^2 (x'^2 - k^2)$$

$$\dot{x}^2 = (\omega \sin \alpha)^2 [(x+k)^2 - k^2] = (\omega \sin \alpha)^2 (x+2k)x.$$

$$\dot{x} = \sqrt{(\omega \sin \alpha)^2 \left(x + \frac{2g \cos \alpha}{\omega^2 \sin^2 \alpha}\right) x} = \sqrt{(\omega^2 x \sin^2 \alpha + 2g \cos \alpha) x} \quad (9)$$

由(7)式第二式, 得 $F_{Ny} = mg \sin \alpha - m \omega^2 x \sin \alpha \cos \alpha$

$$\dot{x} = \sqrt{(\omega \sin \alpha)^2 \left(x + \frac{2g \cos \alpha}{\omega^2 \sin^2 \alpha}\right) x} = \sqrt{(\omega^2 \sin^2 \alpha x + 2g \cos \alpha) x} \quad (9).$$

$$\Rightarrow F_{Nz} = -2m \omega \sin \alpha \sqrt{(2g \cos \alpha + \omega^2 x \sin^2 \alpha) x}$$

把 $x=s$ 代入质点对圆锥槽的作用力为:

$$\begin{aligned} \vec{F}_N &= -F_{Ny} \vec{j} - F_{Nz} \vec{k} \\ &= mg \sin \alpha (\omega^2 s \cos \alpha - g) \vec{j} + 2m \omega \sin \alpha \sqrt{\omega^2 s^2 \sin^2 \alpha + 2g s \cos \alpha} \vec{k} \end{aligned}$$