Adapted from Graham's lecture slides.

第一章: 概论

函数,函数式程序设计, 历史回顾,Haskell的特点和例子 课程内容概览



## 函数

 In Haskell, a function is a mapping that takes one or more arguments and produces a single result.

double 
$$x = x + x$$



Computation by function application

```
double 3
= { applying double }
  3 + 3
= { applying + }
6
```



### Computation by function application

```
double (double 2)
= { applying the inner double }
  double (2 + 2)
= { applying + }
  double 4
= { applying double }
  4 + 4
= { applying + }
  8
```



### Computation by function application

```
double (double 2)
    { applying the outer double }
  double 2 + double 2
= { applying the first double }
 (2 + 2) + double 2
= { applying the first + }
 4 + double 2
  { applying double }
 4 + (2 + 2)
= { applying the second + }
  4 + 4
= {applying + }
  8
```



## 函数式程序设计

 Functional programming is <u>style</u> of programming in which the basic method of computation is the application of functions to arguments;

 A functional language is one that <u>supports</u> and <u>encourages</u> the functional style.



## 例子

## Summing the integers 1 to 10 in Java:

```
int total = 0;
for (int i = 1; i ≤ 10; i++)
  total = total + i;
```

The computation method is variable assignment.

Summing the integers 1 to 10 in Haskell:

```
sum [] = 0
sum (x:xs) = x + sum xs
sum [1..10]
```

The computation method is <u>function application</u>.

#### 1930s:



Alonzo Church develops the <u>lambda calculus</u>, a simple but powerful theory of functions.



1950s:



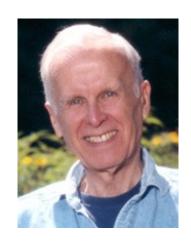
John McCarthy develops <u>Lisp</u>, the first functional language, with some influences from the lambda calculus, but retaining variable assignments.

#### 1960s:



Peter Landin develops <u>ISWIM</u>, the first *pure* functional language, based strongly on the lambda calculus, with no assignments.

#### 1970s:



John Backus develops <u>FP</u>, a functional language that emphasizes *higher-order functions* and *reasoning about programs*.

#### 1970s:



Robin Milner and others develop ML, the first modern functional language, which introduced *type inference* and *polymorphic types*.

1970s - 1980s:



David Turner develops a number of *lazy* functional languages, culminating in the <u>Miranda</u> system.

1987:



An international committee starts the development of <u>Haskell</u>, a standard lazy functional language.

1990s:



Phil Wadler and others develop *type classes* and *monads*, two of the main innovations of Haskell.

2003:



The committee publishes the <u>Haskell Report</u>, defining a stable version of the language; an updated version was published in 2010.

#### 2010-date:



Standard distribution, library support, new language features, development tools, use in industry, influence on other languages, etc.

## Haskell的特点

- 简洁(声明式):第2章,第4章
- 强有力的类型系统: 第3章, 第8章
- List comprehensions: 第5章
- 递归函数:第6章
- 高阶函数: 第7章
- 表达副作用的函数: 第10章, 第12章
- Generic函数: 第12章, 第14章
- 惰性计算: 第15章
- 程序推理: 第16章, 第17章



## 例1:序列求和

```
sum [] = 0
sum (n:ns) = n + sum ns
```

```
sum [1,2,3]
= { applying sum }"
1 + sum [2,3]
= { applying sum }
1 + (2 + sum [3])
= { applying sum }
1 + (2 + (3 + sum []))
= { applying sum }
1 + (2 + (3 + o))
= { applying + }
6
```



## 例2: 快速排序



# 例3: 序列求"和"一般化: 高阶函数

```
sum [] = 0

sum (n:ns) = n + sum ns
```



foldr plus zero [] = zero foldr plus zero (n:ns) = plus n (foldr plus zero ns)

sum = foldr(+) o

练习:用foldr定义(1)计算数字列表的乘积;(2)计算列表的长度。\_



## 例4: 生成无限序列

```
cyclic = let x = o : y

y = 1 : x

in x
```

ns = o : foldr f o nswhere f n r = (1+n) : r



如何构造出一个正确而且高效的解决最大子段和问题?

#### Maximum Segment Sum Problem

Given a list of numbers, find the maximum of sums of all *consecutive* sublists.

- $[-1,3,3,-4,-1,4,2,-1] \implies 7$
- $[-1, 3, 1, -4, -1, 4, 2, -1] \implies 6$
- $[-1, 3, 1, -4, -1, 1, 2, -1] \implies 4$



```
mss=0; s=0;
for(i=0;i<n;i++){
    s += x[i];
    if(s<0) s=0;
    if(mss<s) mss= s;
}</pre>
```



• 课程第一部分(Haskell):利用高阶函数等的组合描述要做什么

```
mss = maximum . map sum . segs
where
    maximum = foldr max (-inf)
    sum = foldr (+) o
    segs = concat . map tails . inits
    concat = ...
    tails = ...
    inits = ...
```



• 课程第二部分 (Agda): 构建序列上的演算理论

```
map : \forall {A B : Set} \rightarrow (A \rightarrow B) \rightarrow List A \rightarrow List B map f [] = [] map f (x :: xs) = f x :: map f xs
```



• 课程第二部分 (Agda): 构建序列上的演算理论



• 课程第二部分 (Agda): 程序推理/程序演算 (+记号设计)



## 作业:

- **【1-1】** Define a function *product* that produces the product of a list of numbers, and show using your definition that product[2,3,4] = 24.
  - [1-2] Define list length function using foldr.
- 【1-3】 How should the definition of the function qsort be modified so that it produces a reverse sorted version of a list?

