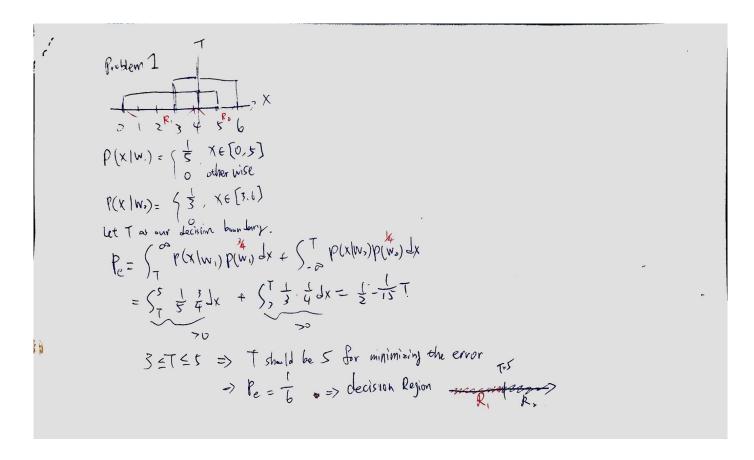
DLCV hw1 r06946003 湯忠憲

Problem1



Problem2

```
In [1]:
```

```
from os import listdir
import imageio
import numpy as np
import matplotlib.pyplot as plt
from sklearn.decomposition import PCA
from sklearn.neighbors import KNeighborsClassifier
from sklearn.model_selection import GridSearchCV
from sklearn.metrics import accuracy_score
% matplotlib inline
```

In [2]:

```
# training & set name
train_set_name = [str(i)+"_"+str(j)+".png" for i in range(1,41) for j in range(1,7)]
test_set_name = [str(i)+"_"+str(j)+".png" for i in range(1,41) for j in range(7,11)]
```

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In [3]:

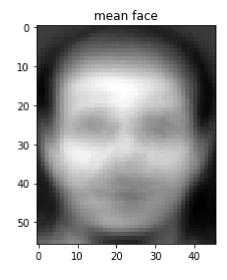
```
train_X = [imageio.imread("hw1_dataset/"+n) for n in train_set_name]
train_X = np.array(train_X).reshape(240,-1)
train_y = [i for i in range(1,41) for _ in range(1,7)]

test_X = [imageio.imread("hw1_dataset/"+n) for n in test_set_name]
test_X = np.array(test_X).reshape(160,-1)
test_y = [i for i in range(1,41) for _ in range(7,11)]
```

(a)

In [4]:

```
# mean face
mean_face_vector = train_X.mean(axis=0)
plt.title("mean face")
plt.imshow(mean_face_vector.reshape(56,46), cmap='gray')
plt.show()
```



In [5]:

```
# PCA and plot first three eigenfaces
pca = PCA()
output = pca.fit(train_X - mean_face_vector)
output.components_.shape
```

Out[5]:

(240, 2576)

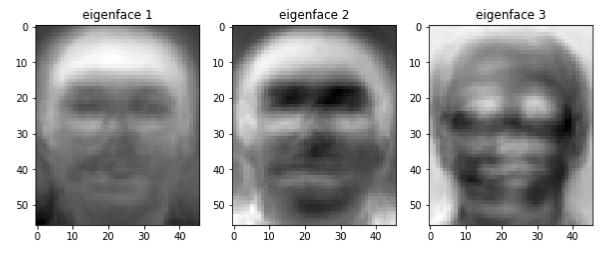
In [6]:

```
e1 = (output.components_[0]).reshape(56,46)
e2 = (output.components_[1]).reshape(56,46)
e3 = (output.components_[2]).reshape(56,46)
```

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In [7]:

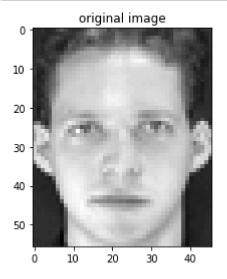
```
plt.figure(figsize=(10,6))
plt.subplot(131)
plt.imshow(e1,cmap='gray')
plt.title("eigenface 1")
plt.subplot(132)
plt.imshow(e2,cmap='gray')
plt.title("eigenface 2")
plt.subplot(133)
plt.imshow(e3,cmap='gray')
plt.title("eigenface 3")
plt.show()
```



(b)

In [8]:

```
input_img = imageio.imread("hw1_dataset/1_1.png").reshape(1,-1)
plt.title("original image")
plt.imshow(input_img.reshape(56,46), cmap="gray")
plt.show()
```



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```
In [9]:
```

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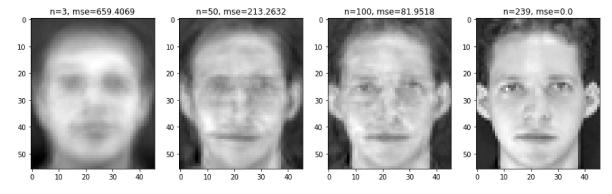
```
projected = pca.transform(input_img - mean_face_vector)
print(projected.shape)
```

(1, 240)

In [10]:

```
plt.figure(figsize=(15,6))

for j,i in enumerate([ 3, 50, 100, 239]):
    recon_f = (projected[:,:i] @ output.components_[:i]) + mean_face_vector
    mse = np.mean((recon_f - input_img)**2)
    plt.subplot(1,4,j+1)
    tit = "n="+str(i)+", mse="+str(np.round(mse,4))
    plt.title(tit)
    plt.imshow(recon_f.reshape(56,46), cmap = "gray")
plt.show()
```



(c)

In [11]:

```
k=1 k=3 k=5

n= 3 [ 0.70833333 0.5875 0.4875 ]

n= 50 [ 0.92916667 0.875 0.775 ]

n= 159 [ 0.925 0.87083333 0.74583333]
```

From the above gridsearch output with 3-fold cross validation, we can find out the best parameters should be k=1 and n=50.

In [12]:

```
# real test
test_X_reduced = pca.transform(test_X - mean_face_vector)
knn = KNeighborsClassifier(n_neighbors=1)
knn.fit(train_X_reduced[:,:50], train_y)
pred_y = knn.predict(test_X_reduced[:,:50])
```

In [13]:

```
acc = accuracy_score(y_pred=pred_y, y_true=test_y)
print("The accuracy on testing set:", acc)
```

The accuracy on testing set: 0.9625

Bonux

```
Let A be a dxd symmetric matric with distinct eigenvalue.

(i.e. 7, -12 x ...)

Since. A is symmetric metric, it's diagonalizable which exists deigenvectors corresponding to deigenvalues.

(X1, X2... X2)

Here we set a initial vector Uo and Uo = C1X1+C2X2+...+CnXn

Based on Uo; U1 = A·Uo = C1·71·X1+C2X2X2...+C171·X3

Uk = C171·X1+C2X2/2+...+C171·X3

> Uk = 71·C1X1+C2X2/2+...+C171·X3

as k become large, (21)

Thus. Uk 2 71·C1X1, ...

Uk coverges to the same lirection of X1. which is the 1 se eigenvector, Then we an normalize Uk to get the approximation of X1.
```

In []: