1 Introduction

In recent years, predicting student performance has become increasingly important for both educators and policymakers. In this project, we seek to determine the most influential predictors on a student's final grade in Portuguese secondary schools using a combination of students' physical and school-related factors.

1.1 Research Question of Interest

Our research question is: Can we accurately predict students' final grades based on their time of study, family members' education level, students' health condition and number of absences? This question was formulated considering its potential implications for early interventions in a student's academic journey. For instance, understanding what non-academic factors contribute significantly to final grades could help schools and policymakers design effective support systems to improve student performance.

1.2 Background and Source of the Data Set

The data we use in this project was collected from two Portuguese secondary schools and includes a variety of student grades, family-related and school-related attributes. In this report, we start by providing a descriptive analysis of the data, then move on to fit and interpret multiple regression models to answer our research question, and finally discuss our findings and their implications. The variables include:

```
- Medu:
              Mother's education
                                      numeric: 1 - none, 2 - primary, 3 - secondary, 4 - college
- Fedu:
              Father's education
                                      numeric: 1 - none, 2 - primary, 3 - secondary, 4 - college
- studytime:
              Weekly study time
                                      numeric: 1 - <2 hours, 2 - 2 to 5 hours, 3 - 5 to 10 hours, 4 - >10 hours
- health:
                                      numeric: from 1 - very bad to 5 - very good
              Current health status
                                      numeric: from 0 to 93
- absences:
              Number of absences
- G1:
              First-period grade
                                      numeric: from 0 to 20
- G2:
              Second-period grade
                                      numeric: from 0 to 20
- G3:
                                      numeric: from 0 to 20
              Final grade
- Gtotal:
              Total grade
                                      numeric: from 0 to 60
```

The latest version of this project report, datasets and R source code files are available at: https://blog.nus.edu.sg/chenguoyi/modules/st3131/

1.3 Explain the method chosen to model the relationship

While modeling the relationship between different variables, we begin with the Multiple Linear Regression (MLR) and diagnostic plots. To better the model, we use transformation and model selection for MLR. After getting the final model, we check the improvements by viewing the general diagnostic plots.

1.4 Overview of the structure of our research

We begin the paper with scatter plots for the data to show the general relationship between the response variable (Gtotal) and all predictors. Then we use the R results to comment on the fit of the linear model and find a better model for the data set. Finally, we summarize the results by discussing the limitations and expectations of our model.

2 Data Description

The Figure 2.1 shows the correlations relationship between each variable.

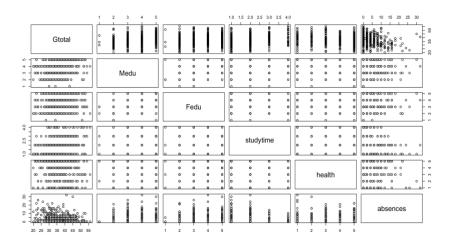


Fig 2.1 Scatter plot matrix of the original variables

The summary statistics of these variables such as mean, standard deviation, distribution of each variable and relationships among the variables using appropriate graphs are attached in *Appendix II*.

3 Results and Interpretation

3.1 Original Model Diagnostics

Based on the scatter plot (Figure 2.1) and summary result (Tab 3.1), we learn about the relationship between response variable and all predictors. We can learn from scatter plot and summary result that except for the educational levels of fathers, all other variables are statistically significant.

Tab 3.1 Summary Result of Original Model

```
Call:
lm(formula = Gtotal ~ Medu + Fedu + studytime + health + absences,
    data = student)
Residuals:
               10
                    Median
                                  30
    Min
                                          Max
-18.5097
         -4.4600
                   -0.2166
                              4.0884
                                      17.7181
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) 31.09306
                        1.73540 17.917 < 2e-16 ***
                         0.38351
Medu
             1.21202
                                   3.160 0.001691 **
             0.25086
                        0.37613
                                   0.667 0.505165
Fedu
                                   4.694 3.64e-06 ***
studytime
             1.82387
                         0.38853
```

```
health -0.67388 0.22628 -2.978 0.003070 **
absences -0.24260 0.06267 -3.871 0.000126 ***
---
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 '' 1
Residual standard error: 6.564 on 417 degrees of freedom
Multiple R-squared: 0.1634, Adjusted R-squared: 0.1534
F-statistic: 16.29 on 5 and 417 DF, p-value: 1.089e-14
```

Based on the diagnostic plots (see *Appendix I*, Figure I.1), we know that the variance of residuals is not constant and there are some bad leverage points. Thus, this model is not valid and needs to be modified. Then we use the R code result (Table 3.2) to determine the transformation needed for each variable. Since for the variable of absence, there are 0 values that hinder our function, we add 1 to all absence values.

Tab 3.2 Transformation Results for each variable

```
bcPower Transformations to Multinormality
          Est Power Rounded Pwr Wald Lwr Bnd Wald Upr Bnd
                           1.00
Gtotal
             0.6166
                                     0.2193
                                                    1.0140
             1.2951
                          1.00
                                                    1.5956
Medu
                                     0.9946
             0.7896
                          1.00
Fedu
                                     0.5172
                                                   1.0619
studytime
           0.1993
                           0.00
                                     -0.0206
                                                    0.4192
health
            1.4179
                           1.42
                                      1.1839
                                                   1.6518
            -0.0531
                           0.00
                                     -0.1634
                                                    0.0572
Likelihood ratio test that transformation parameters are equal to 0
 (all log transformations)
                                    LRT df
                                                  pval
LR test, lambda = (0\ 0\ 0\ 0\ 0\ 0)\ 304.811\ 6 < 2.22e-16
Likelihood ratio test that no transformations are needed
                                     LRT df
LR test, lambda = (1 \ 1 \ 1 \ 1 \ 1) \ 468.6497 \ 6 < 2.22e-16
```

Based on the rounded power in R result, we can get the transformed model to be: $Gammath{total} = \beta_0 + \beta_1 \times Medu + \beta_2 \times Fedu + \beta_3 \times \log(studytime) + \beta_4 \times health^{1.42} + \beta_5 \times \log(absences + 1)$

Tab 3.3 Summary Result of Transformed Model

```
Call:
lm(formula = Gtotal ~ Medu + Fedu + log(studytime) + I(health^(1.4)) +
    log(absences + 1), data = student)
Residuals:
    Min    1Q    Median    3Q    Max
```

```
-18.8946 -4.3599 -0.0842
                           4.2985 17.9949
Coefficients:
               Estimate Std. Error t value Pr(>|t|)
                32.2162
                             1.5458 20.842 < 2e-16 ***
(Intercept)
                  1.2536
                             0.3830 3.273 0.00115 **
Medu
                           0.3760 0.602 0.54754
Fedu
                  0.2263
log(studytime)
                 3.6824
                           0.7561 4.870 1.59e-06 ***
I(health^(1.4))
                -0.2907
                           0.1030 -2.822 0.00501 **
log(absences + 1) -1.1697 0.3278 -3.569 0.00040 ***
___
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 6.565 on 417 degrees of freedom
Multiple R-squared: 0.1631, Adjusted R-squared: 0.153
F-statistic: 16.25 on 5 and 417 DF, p-value: 1.189e-14
```

3.2 Final Model Diagnostics

After figuring out the variable transformation, we should then move on to the variable selection process. We can use the forward stepwise method to find out the best subset model.

Tab 3.4 Result of Forward Stepwise Method

```
Start: AIC=1663.25
Gtotal ~ 1
                  Df Sum of Sq
                                RSS
                                       AIC
+ log(studytime) 1 1608.67 19867 1632.3
                   1 1153.63 20322 1641.9
+ Medu
+ log(absences + 1) 1 942.13 20534 1646.3
+ I(health^(1.4)) 1
                       476.34 20999 1655.8
                  1 446.32 21029 1656.4
+ Fedu
                               21476 1663.2
<none>
Step: AIC=1632.31
Gtotal ~ log(studytime)
                  Df Sum of Sq RSS
                                       ATC
+ Medu
                   1 1022.92 18844 1612.0
+ log(absences + 1) 1 576.25 19291 1621.9
+ Fedu
                       468.35 19399 1624.2
+ I(health^(1.4)) 1 321.10 19546 1627.4
<none>
                               19867 1632.3
Step: AIC=1611.95
```

```
Gtotal ~ log(studytime) + Medu
                  Df Sum of Sq RSS AIC
+ log(absences + 1) 1 518.66 18325 1602.2
+ I(health^(1.4)) 1 312.59 18532 1606.9
<none>
                              18844 1612.0
           1 3.80 18840 1613.9
+ Fedu
Step: AIC=1602.15
Gtotal ~ log(studytime) + Medu + log(absences + 1)
                Df Sum of Sq RSS
+ I(health^(1.4)) 1 335.94 17990 1596.3
<none>
                           18325 1602.2
          1 8.38 18317 1604.0
+ Fedu
Step: AIC=1596.32
Gtotal ~ log(studytime) + Medu + log(absences + 1) + I(health^(1.4))
      Df Sum of Sq RSS
                          AIC
                  17990 1596.3
<none>
+ Fedu 1
           15.618 17974 1598.0
```

Based on the AIC values, we know that when the model is $Gtotal \sim log(studytime) + Medu + log(absences + 1) + I(health^{1.4})$, AIC get the smallest value. Therefore, the final model should be: $Gtotal = \beta_0 + \beta_1 \times Medu + \beta_2 \times log(studytime) + \beta_3 \times health^{1.42} + \beta_4 \times log(absences + 1)$. Checking on this final model, we can get the summary and diagnostic plots (see *Appendix I*, Figure I.2).

Tab 3.5 Summary Result of Final Model

```
Call:
Х
Residuals:
         10 Median 30
    Min
                                  Max
-18.7267 -4.3258 -0.1429 4.2414 17.6855
Coefficients:
              Estimate Std. Error t value Pr(>|t|)
                          1.4991 21.639 < 2e-16 ***
               32.4402
(Intercept)
                1.3991
                         0.2969 4.712 3.35e-06 ***
Medu
log(studytime) 3.6628 0.7548 4.852 1.72e-06 ***
                         0.1028 -2.794 0.005447 **
I(health^(1.4))
               -0.2871
```

Based on the plots and summary, we know that all transformed variables in the final model are significant. Also, the variance of residuals becomes more constant, and the model has less bad leverage points.

4 Summary and Further Analysis

In order to get the final model about the relationship between students' academic performance, which is shown as the final grades in our project, and the time of study, family members' education levels, students' health conditions and number of absences, we use multiple linear regression model and the proper transformation and selection methods to find out the best model for our data set.

Based on our model, we find out that the students' final grades are highly related to all transformed variables except the educational level of fathers. Therefore, we know that the educational levels of fathers have no relationship with students' final grades. For the educational levels of mothers, the slope coefficient is 1.3991, which means that as mothers have higher education levels, students generally have higher final grades. Similarly, the study time also has a positive association with final grades, which indicates that as students study more, they get a better grade. However, the transformed variable of absence has a significant negative relationship with the total grades, so as students have more times of absences, they get a lower grade. The transformed variable of health also has a negative relationship with total grades, but the coefficient is not large enough. In this case, we can assume that when students have better health conditions, they perform worse academically, but this actually has little impact on the academic performance. We think our model makes sense in real life. Fathers hardly ever pay attention to their kids' study so the fathers' educational level has no relationship with students' academic scores. However, mothers devote most of their time to kids, so their educational levels will greatly affect how they treated their kids' study. Therefore, as mothers have higher educational levels, like college, they pay more attention and more money for kids' study, which greatly improves their academic performance. It's obvious that absences will negatively influence students' final scores because they miss some key points while they are away from class. Poorer health conditions may be related with higher graders because unhealthy kids have more time staying at home and learning things.

Despite all the achievements we have made, our project has some drawbacks. We want to study how different variables affect students' final grades and academic performance. However, we only get the data from two Portuguese secondary schools which means we cannot apply this model to all secondary schools students. If some elements are different, like the size of the school or even the place where the school is located, the result may be very different. Therefore, in order to improve the model, we should collect students' data from secondary schools of different sizes and at different places.

Appendix I Diagnostic Diagrams

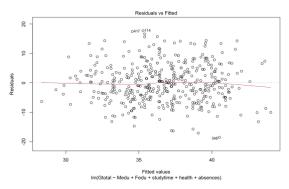
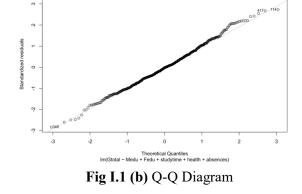


Fig I.1 (a) Residuals Plot



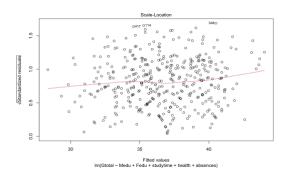


Fig I.1 (c) Sqrt Standard Residuals Plot

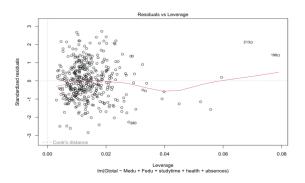


Fig I.1 (d) Leverage Plot

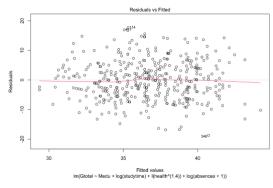


Fig I.2 (a) Residuals Plot

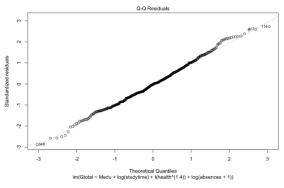


Fig I.2 (b) Q-Q Diagram

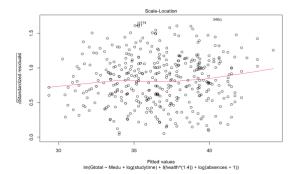


Fig I.2 (c) Sqrt Standard Residuals Plot

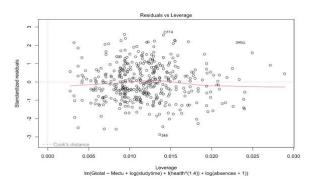


Fig I.2 (d) Leverage Plot

Appendix II Variable Statistics

II.0 Overall Correlations

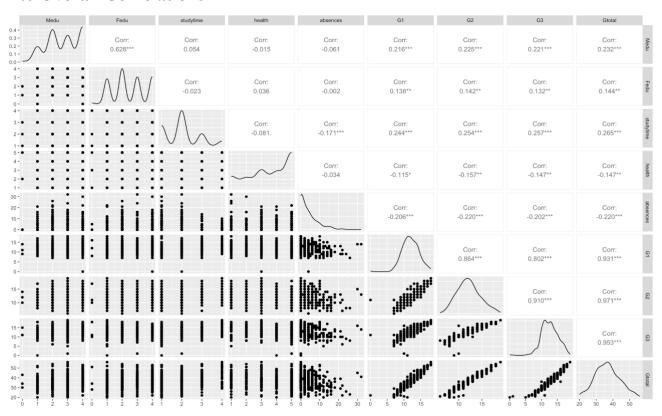


Fig II.1 Correlation matrix of the original variables

II.1 Medu

Mother's education numeric: 1 - none, 2 - primary, 3 - secondary, 4 - college

Mean	3.72576832	140				
STD	1.0764941	120		124		135
MAX	5	100			102	
MIN	1	80				
Mode	5	60	62			
1 Q	3	20				
Medium	4	0	[1 0]	(2, 2]	/2 4]	(4.5)
3 Q	5		[1, 2]	(2, 3]	(3, 4]	(4, 5]

II.2 Fedu

Father's education numeric: 1 - none, 2 - primary, 3 - secondary, 4 - college

Mean	3.4751773	140				
STD	1.09662274	120		129		
MAX	5	100	95		99	100
MIN	1	80	30			
Mode	3	60				
1 Q	3	20				
Medium	3	0				
3 Q	4		[1, 2]	(2, 3]	(3, 4]	(4, 5]

II.3 studytime

Weekly study time numeric: 1 - <2 hours, 2 - 2 to 5 hours, 3 - 5 to 10 hours, 4 - >10 hours

Mean	2.0141844	500				
STD	0.84021394					
MAX	4	400			412	
MIN	1	300				
Mode	2	200		213		
1 Q	1	100	108			119
Medium	2	0		3	2	1
3 Q	2		4			1

II.4 health

Current health status numeric: from 1 - very bad to 5 - very good

Mean	3.59810875	180				
STD	1.42063207	160	60			167
MAX	5	140 — 120 —				
MIN	1	100	100			
Mode	5	60		83	73	
1 Q	3	40 20				
Medium	4	0	F4 03	(0, 01	(0.47	(4. 53
3 Q	5		[1, 2]	(2, 3]	(3, 4]	(4, 5]

II.5 absences

Number of absences numeric: from 0 to 93

Mean	4.21513002	350
STD	5.19191478	300
MAX	32	250 293
MIN	0	200
Mode	0	150
1 Q	0	50 88
Medium	2	0 13 5 2 1
3 Q	6	[0, 5] (5, 10] (10, 15] (15, 20] (20, 25] (25, 30] (30, 35]

II.6 G1First-period grade numeric: from 0 to 20

Mean	11.9858156	300 -				
STD	2.41829269	250			273	
MAX	18	200				
MIN	0	150				
Mode	11	100		116		
1 Q	10	50 -				
Medium	12	0	1	/F 401	(40, 45)	33
3 Q	14		[0, 5]	(5, 10]	(10, 15]	(15, 20]

II.7 G2Second-period grade numeric: from 0 to 20

Mean	12.144208	250			
STD	2.45152207	200		225	
MAX	19		175		
MIN	6	150			
Mode	12	100			
1 Q	10	50			
Medium	12	0			23
3 Q	14		[6, 11]	(11, 16]	(16, 21]

II.8 G3

Final grade numeric: from 0 to 20

Mean	12.5768322	300				
STD	2.62563599	250			279	
MAX	19	200				
MIN	0	150				
Mode	11	100				
1 Q	11	50 -		82		59
Medium	13	0 -	3			
3 Q	14		[0, 5]	(5, 10]	(10, 15]	(15, 20]

II.9 Gtotal

Total grade numeric: from 0 to 60

Mean	36.7068558	140
STD	7.13373438	120
MAX	56	100 104
MIN	20	80
Mode	37	60 61 66
1 Q	32	20 23
Medium	37	0
3 Q	41	[20, 25] (25, 30] (30, 35] (35, 40] (40, 45] (45, 50] (50, 55] (55, 60]

Appendix III R File

```
# Project: STATS101A Group Project Report
# Authors: Yining Xu, Guoyi Chen, Yuexuan Wu
# Code is available online @https://blog.nus.edu.sg/chenguoyi/modules/st3131/
# Install Dependency Packages
install.packages("car")
library(car)
# Load data
student <- read.csv("student-por.csv", header = TRUE)</pre>
# <Fig 2.1> Scatter plot matrix using base R
pairs (Gtotal ~ Medu + Fedu + studytime + health + absences, data = student)
# <Tab 3.1> Summary result of original model
model <- lm(Gtotal~Medu + Fedu + studytime + health + absences, data = student)</pre>
summary(model)
# <Tab 3.2> Transformation Results for each variable
transform xy <-
powerTransform(cbind(Gtotal, Medu, Fedu, studytime, health, (absences+1))~1, data =
student)
summary(transform xy)
# <Tab 3.3> Summary Result of Final Model
model2 \leftarrow lm(Gtotal\sim Medu + Fedu + log(studytime) + I(health^(1.4)) +
log(absences+1), data = student)
summary(model2)
# <Tab 3.4> Result of Forward Stepwise Method
nullm <- lm(Gtotal~1, data = student)</pre>
forwardAIC <- step(nullm, scope=list(lower=~1, upper=~Medu + Fedu +</pre>
\log(\text{studytime}) + I(\text{health}^{(1.4)}) + \log(\text{absences}+1)), direction="forward", data = 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 100
student)
# <Tab 3.5> Summary Result of Final Model
model3 <- model2 <- lm(Gtotal~Medu + Fedu + log(studytime) + I(health^(1.4)) +
log(absences+1), data = student)
summary(model3)
```