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在KOTO實驗中尋找無質量暗光子： $K_L^0 \rightarrow \gamma\bar{\gamma}$

Search for a massless dark photon in $K_L^0 \rightarrow \gamma\bar{\gamma}$ at the
KOTO Experiment

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MASTER THESIS

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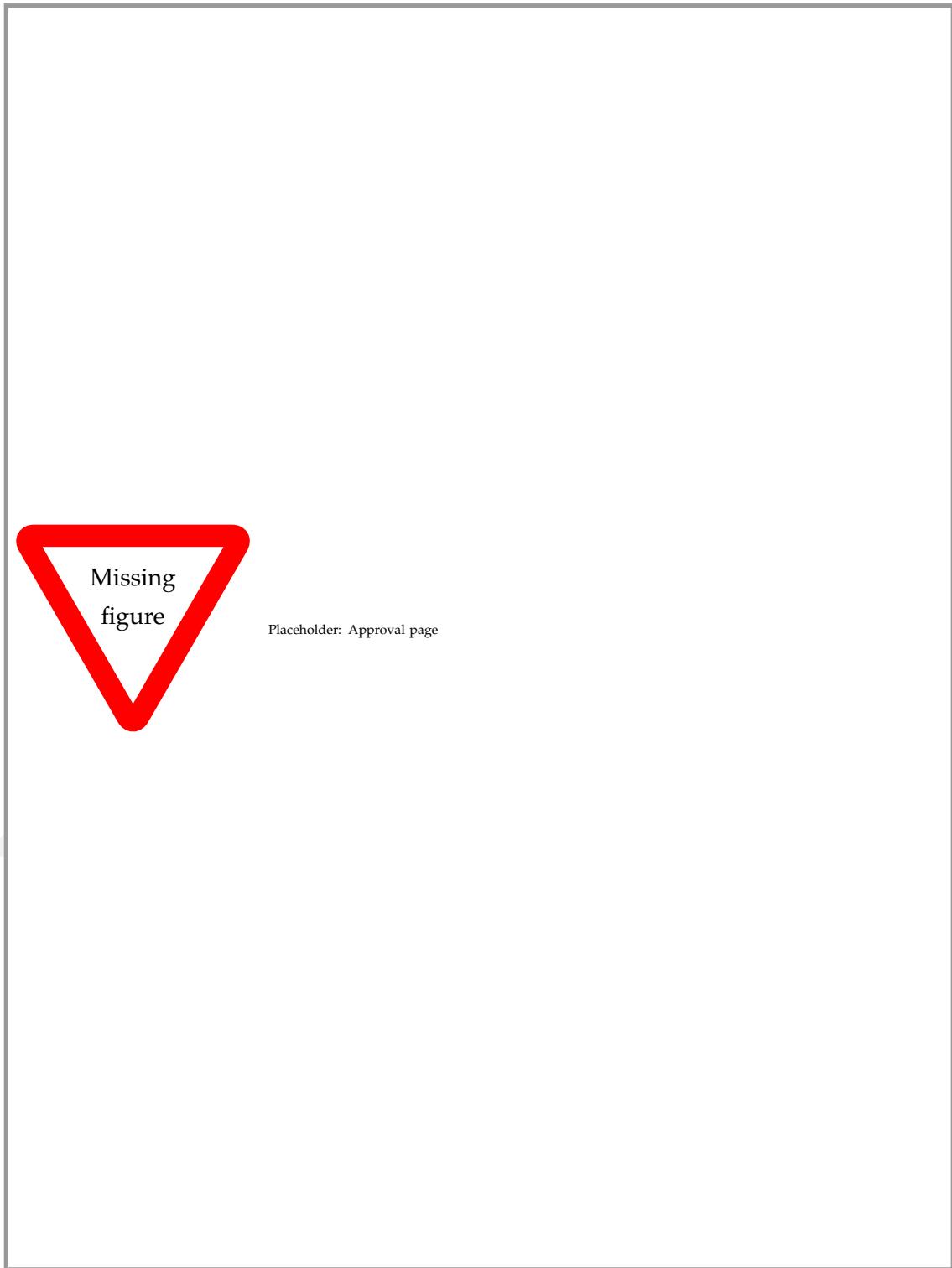


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Thanks all

DRAFT

中文摘要

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關鍵詞：暗光子、新物理。

Abstract

This thesis presents the search for the massless dark photon ($\bar{\gamma}$) in the $K_L^0 \rightarrow \gamma\bar{\gamma}$ decay at the J-PARC KOTO experiment, based on the special data collected in 2020.

Distinguished from the massive dark photon, the massless one does not directly mix with the ordinary photon but could interact with Standard Model (SM) particles through direct coupling to quarks. Some theoretical models propose that the branching ratio (\mathcal{BR}) of the $K_L^0 \rightarrow \gamma\bar{\gamma}$ decay could reach up to $\mathcal{O}(10^{-3})$.

The number of K_L^0 decays that had been collected in the special run is estimated to be $(1.29 \pm 0.02_{stat.}) \times 10^{10}$. The single event sensitivity is calculated to be $(2.91 \pm 0.02_{stat.}) \times 10^{-8}$. The total background level prediction is $(12.65 \pm 4.61_{stat.})$ with the agreement from the side-band region. We uncovered the blind region and observed 13 events. The Feldman-Cousins method is used to calculate the upper limit of the $K_L^0 \rightarrow \gamma\bar{\gamma}$ branching ratio to be $< 2.15 \times 10^{-7}$ (90%C.L.).

Keywords: Dark Photon, beyond Standard Model.

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■ Present the upper limit at 90% confidence level.	xv
■ Should I include the detail of direct detection formalism? It will be based on PDG Sec.27.6.2	1
■ \section{Energy and Timing reconstruct from Waveform}	13
■ Present the upper limit at 90% confidence level.	54

¹ Chapter 1

² Introduction

³ 1.1 Dark Matter and Dark Photons

⁴ Dark matter (DM) is posited to constitute approximately 26.4% of the universe's critical
⁵ density, according to cosmological observations [1]. At this moment the fundamental na-
⁶ ture of dark matter remains one of the most profound mysteries in physics. The Standard
⁷ Model (SM) of particle physics provides no viable explanation for dark matter, prompt-
⁸ ing the motivation to explore physics beyond the Standard Model (BSM). Recent years
⁹ have seen a surge in research aimed at probing the dark sector, with numerous astrophys-
¹⁰ ical and high-energy physics (HEP) experiments making intensified efforts to explore the
¹¹ dark matter.

¹² The dark photon is one of the most promising candidates in the dark sector, it is a new
¹³ type of gauge boson. Theatrical there are two kinds of dark photons, the massive dark
¹⁴ photon and the massless dark photon. The massive dark photon (A') could mix coupling
¹⁵ with visible photons, to interact with the ordinary particles [1], which means the massive
¹⁶ dark photon is possible to be detected in the experiments. Consequently, the massive
¹⁷ dark photon gets most of the attention in the experimental search for dark photons [2].

¹⁸ However, the massive dark photon has been searched by several experiments, and no
¹⁹ evidence has been observed so far, the parameter space for the massive dark photon
²⁰ has been increasingly constrained. Therefore, our investigation shifts focus towards the
²¹ search for the massless dark photon.

²² The massless dark photon, denoted as $\bar{\gamma}$ in this thesis, is different from the massive
²³ dark photon, it will not directly couple with the Standard Model(SM) particles, and only
²⁴ interact with the SM particles by coupling to the quark. [2] Therefore the massless dark
²⁵ photon is more challenging to be searched in the experiments because it is undetectable.

²⁶ 1.2 Theoretical Predictions

²⁷ There are some theoretical calculations predict that the existence of massless dark pho-
²⁸ tons in the Kaon decay [3]. Assuming the flavor-changing neutral current (FCNC) cou-
²⁹ pling to the d and s quarks, the Kaon meson can decay with missing energy by a massless
³⁰ dark photon. The theories consider the neutral Kaon decay and the charge Kaon channels
³¹ shown in the below Table 1.1.

Should I include the details¹⁶ of direct detection formalism? It will be based on PDG Sec.27.6.2

17

TABLE 1.1: Theoretical predictions for the branching fractions of the Kaon decays involving massless dark photons. [3]

Decay Channel	Branching Fraction
$K_L \rightarrow \gamma\bar{\gamma}$	$< 1.2 \times 10^{-3}$
$K_S \rightarrow \gamma\bar{\gamma}$	$< 2.1 \times 10^{-6}$
$K_L \rightarrow \pi^0\gamma\bar{\gamma}$	$< 1.0 \times 10^{-6}$
$K_S \rightarrow \pi^0\gamma\bar{\gamma}$	$< 1.8 \times 10^{-9}$
$K_L \rightarrow \pi^+\pi^-\bar{\gamma}$	$< 9.8 \times 10^{-6}$
$K_S \rightarrow \pi^+\pi^-\bar{\gamma}$	$< 1.7 \times 10^{-8}$
$K^+ \rightarrow \pi^+\gamma\bar{\gamma}$	$< 5.6 \times 10^{-7}$
$K^+ \rightarrow \pi^+\pi^0\bar{\gamma}$	$< 2.4 \times 10^{-6}$

32 Some decay channels decay by KLz is potentially searched in the KOTO experiment.
 33 KOTO Experiment is a rare kaon decay experiment, it is designed to search for the $K_L^0 \rightarrow$
 34 $\pi^0\nu\bar{\nu}$ decay, which is a rare long-lifetime decay that can provide valuable insights into
 35 the CP violation in the Standard Model. $K_L^0 \rightarrow \pi^0\nu\bar{\nu}$ decay has neutrinos in the final
 36 state, it will perform as the missing energy in the detector because it is undetectable.
 37 To probe the missing energy of the neutrino pair, a hermetic veto system was designed
 38 to enclose the kaon decay volume. This design can avoid the energy missing from the
 39 detectable particle as much as possible, which is beneficial to the search for the missing
 40 energy model.

41 1.3 Basic Strategy of the $K_L^0 \rightarrow \gamma\bar{\gamma}$ Search

42 From the theoretical perspective shown above, the massless dark photon can be produced
 43 in the $K_L^0 \rightarrow \gamma\bar{\gamma}$ decay with the branching fraction of this model up to 10^{-3} . This is well
 44 within the sensitivity of the KOTO experiment and is the search Objective of this thesis.

45 In the $K_L^0 \rightarrow \gamma\bar{\gamma}$ decay, the final state is a photon and a massless dark photon, the
 46 photon is detectable in the detector, and the massless dark photon is undetectable.

47 1.3.1 Signal Identification

48 $K_L^0 \rightarrow \gamma\bar{\gamma}$ decay requires only one photon cluster to hit the CsI calorimeter and without
 49 any in-time hit in the rest of the detector. A single cluster can only provide the energy
 50 and position information. The lack of kinematic constraints will be the challenge of this
 51 study. Moreover, single cluster signatures are easily mimicked by some unknown arbi-
 52 trary background. Requiring a high photon energy may help to suppress this kind of
 53 background but also reduce the signal efficiency.

54 1.3.2 Major Background Sources

55 The major background sources are K_L^0 decay background and neutron-like background.

⁵⁶ **K_L^0 decay background**

⁵⁷ Table 6.1 shows the main K_L^0 decay backgrounds. Other decay channels are unnecessary to be considered because of the low branching ratio. Only $K_L^0 \rightarrow \pi^\pm e^\mp \nu_e$ and $K_L^0 \rightarrow \pi^\pm \mu^\mp \nu_\mu$ are considered for the decay channel of charged particles in the final state, due to the high branching ratio. To suppress the K_L^0 decay background, studying these decay channels and understanding their characteristics are important. All of these decay channels produce more than one photon in the final state. Therefore, it is easy to suppress these decay channels with the KOTO detector. Except for the decay of $K_L^0 \rightarrow 2\gamma$, whose final state is similar to the signal signature and may be a potentially non-eliminable source of background.

TABLE 1.2: Main K_L^0 decay background modes and their branching ratios.

Decay mode	Branching Ratio
$K_L \rightarrow \pi^\pm e^\mp \nu_e$	$(40.55 \pm 0.11)\%$
$K_L \rightarrow \pi^\pm \mu^\mp \nu_\mu$	$(27.04 \pm 0.07)\%$
$K_L \rightarrow 3\pi^0$	$(19.52 \pm 0.12)\%$
$K_L \rightarrow \pi^+ \pi^- \pi^0$	$(12.54 \pm 0.05)\%$
$K_L \rightarrow 2\pi^0$	$(8.64 \pm 0.06) \times 10^{-4}$
$K_L \rightarrow 2\gamma$	$(5.47 \pm 0.04) \times 10^{-4}$

⁶⁶ **Neutron-like background**

⁶⁷ The neutron originating from the beamline poses a significant background challenge. Accurately simulating the in-beam neutron background is nearly impossible, especially without a defined mechanism to avoid it. The primary method to mitigate this background involves distinguishing the cluster from the photon event.

⁷¹ **1.4 Thesis Overview**

⁷² This thesis presents a detailed study of the $K_L^0 \rightarrow \gamma\bar{\gamma}$ decay in the KOTO experiment. We begin with an overview of the KOTO experiment, describing its detector components and data acquisition (DAQ) system. The analysis section follows, where we elucidate the event reconstruction methods and Monte Carlo simulation techniques employed in the KOTO experiment. Special attention is given to the unique approaches developed for this particular analysis. Subsequently, we delve into the crucial process of Kaon yield estimation and provide an in-depth exploration of the $K_L^0 \rightarrow \gamma\bar{\gamma}$ analysis. This includes background estimation and systematic uncertainty evaluation. In conclusion, we summarize our findings and discuss their implications. The thesis culminates with an outlook on the prospects of the $K_L^0 \rightarrow \gamma\bar{\gamma}$ search within the KOTO experiment, considering potential improvements and challenges.

⁸³ **Chapter 2**

⁸⁴ **KOTO Experiment**

⁸⁵ The KOTO Experiment is a rare decay experiment. The main goal of this experiment is
⁸⁶ to search for the $K_L \rightarrow \pi^0 \nu \bar{\nu}$ decay. The branching ratio of this decay is predicted to be
⁸⁷ $(3.00 \pm 0.30) \times 10^{-11}$ by the Standard Model (SM) [4]. The branching ratio of this decay
⁸⁸ is sensitive to the new physics beyond the SM because of the accuracy. Therefore, the
⁸⁹ KOTO experiment is a good place to search for new physics.

⁹⁰ This chapter will introduce the KOTO detector, outlining the sequence from proton
⁹¹ generation through to data capture within the detector.

⁹² **2.1 J-PARC and Proton Beamlne**

⁹³ The KOTO experiment is located at the Japan Proton Accelerator Research Complex (J-
⁹⁴ PARC)[5] Hadron Experimental Facility (HEF) in Tokai, Japan. Figure 2.1 shows the flow
⁹⁵ of proton beam acceleration, HEF (Hadron Beam Facility) is one of the delivered exper-
⁹⁶ iment facilities. The proton beam has been generated at the end of the linear particle
⁹⁷ accelerator (LINAC)[6], then into a 3 GeV rapid cycling synchrotron (RCS)[7], and finally
⁹⁸ into the main ring synchrotron (MR) to accelerate to 30 GeV[8]. At the end extracted from
⁹⁹ the synchrotron and directed to the HEF, as shown in Figure 2.2.

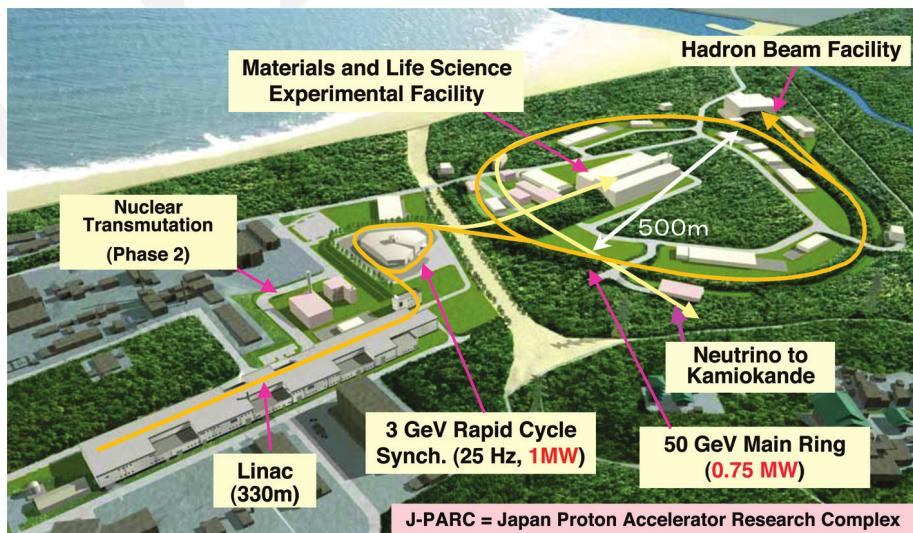


FIGURE 2.1: The entire view of J-PARC. [5]

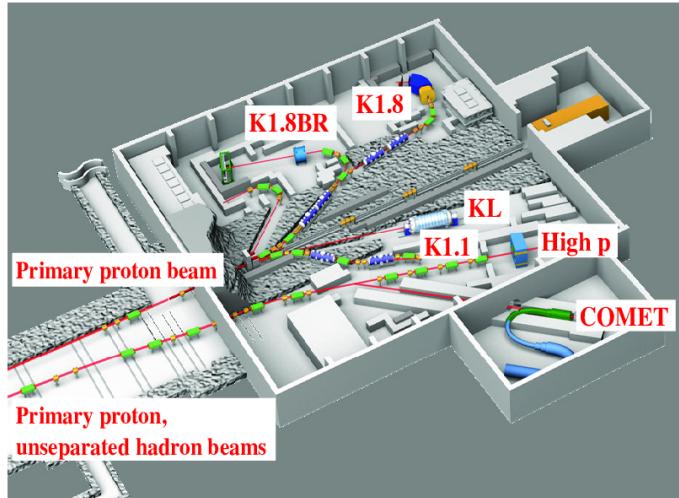


FIGURE 2.2: Illustration of the Hadron Experimental Facility (HEF) at J-PARC.[9] The KL in the Figure indicated the KOTO detector

100 To reduce the instantaneous rate of particles coming into detectors to prevent the event
 101 pileup, a slow-extraction (SX) technique is used. The proton beam was extracted for 2
 102 seconds as a "spill" every 4.22 seconds in 2024 for the beam power of 82 kW. The beam
 103 power is calculated by

$$\text{Beam Power} = E_{\text{proton}} F_{\text{proton}}, \quad (2.1)$$

$$F_{\text{proton}} = N_{\text{spill}}^{\text{proton}} / s_{\text{spill}} \quad (2.2)$$

104 where E_{proton} is the extracted energy of the proton beam, F_{proton} is the protons flux,
 105 $N_{\text{spill}}^{\text{proton}}$ is the number of protons per spill, and s_{spill} is the spill duration.

106 In HEF, the extracted proton beam collides with the T1 target to produce secondary
 107 particles. As shown in Figure 2.3, the T1 target consists of two 66 mm long gold bars with
 108 dimensions of 15×11 mm in cross-section. One bar is used for production and the other
 109 one is a spare. The secondary particles are then directed to the KOTO detector at a 16° to
 110 the beamline.

111 2.2 K_L^0 Beamline

112 After the p-gold collides, a 16° to the beamline was chosen to direct the Kaon beamline
 113 for KOTO. Figure 2.4 shows the schematic diagram of the K_L^0 beamline. To reduce the
 114 photon in the beamline, a 7 cm thick lead photon absorber was installed after the T1
 115 target. Two collimators follow that to narrow the beamline and make it pencil-like. A
 116 sweeping magnet with a 1.2 T magnetic field was installed between the two collimators to
 117 reduce the charged particles in the beamline. A rotatable beam plug is placed between the
 118 sweeping magnet and the 2nd collimator, it is made of brass that could stop the beamline
 119 with most particles. The total length of the beamline is 20 m, which is long enough to
 120 allow the short-life particles, such as the K_s and hyperons, to decay before reaching the
 121 KOTO detector. Figure 4.1 shows the possible remaining particle at the end of the 2nd

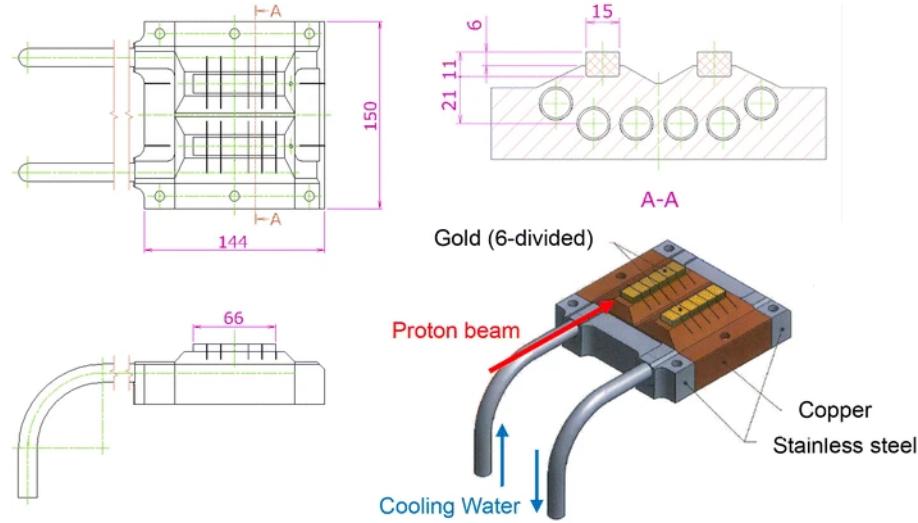


FIGURE 2.3: Structural drawings of the T1 production target [10]. One bar is used for production and the other is a spare.

122 collimator in the beamline which is estimated by the beamline simulation. These particles
123 will enter the KOTO detector.

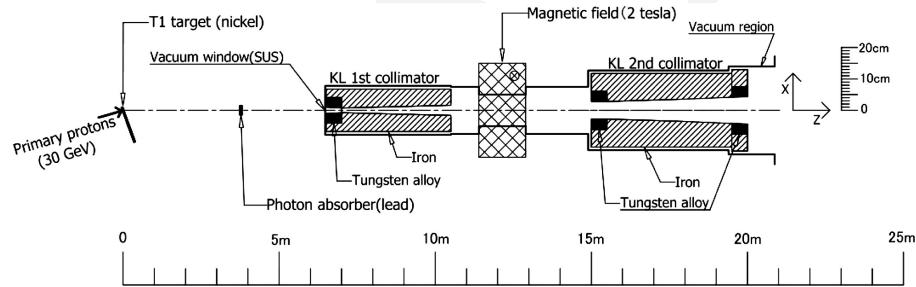


FIGURE 2.4: Schematic diagram of the K_L^0 beamline.[11]

124 2.3 Detectors

125 The KOTO detector is designed to study the decay of K_L^0 particles. Its main components
126 are an electromagnetic calorimeter and a hermetic veto system. As K_L^0 particles enter the
127 detector, they decay within a highly evacuated volume maintained at 5×10^{-5} Pa. The
128 resulting decay products are then detected by various subdetectors. The electromagnetic
129 calorimeter, positioned perpendicular to the beamline, serves primarily as a photon de-
130 tector. Surrounding the decay volume, the hermetic veto system comprises multiple veto
131 counters, including barrel vetoes, charge vetoes, and additional specialized veto coun-
132 ters. This comprehensive veto system ensures efficient detection and differentiation of
133 particle interactions. Figure 2.7 provides a schematic overview of the KOTO detector's
134 layout and components. In this section, the Calorimeter and some important veto coun-
135 ters will be introduced in detail.

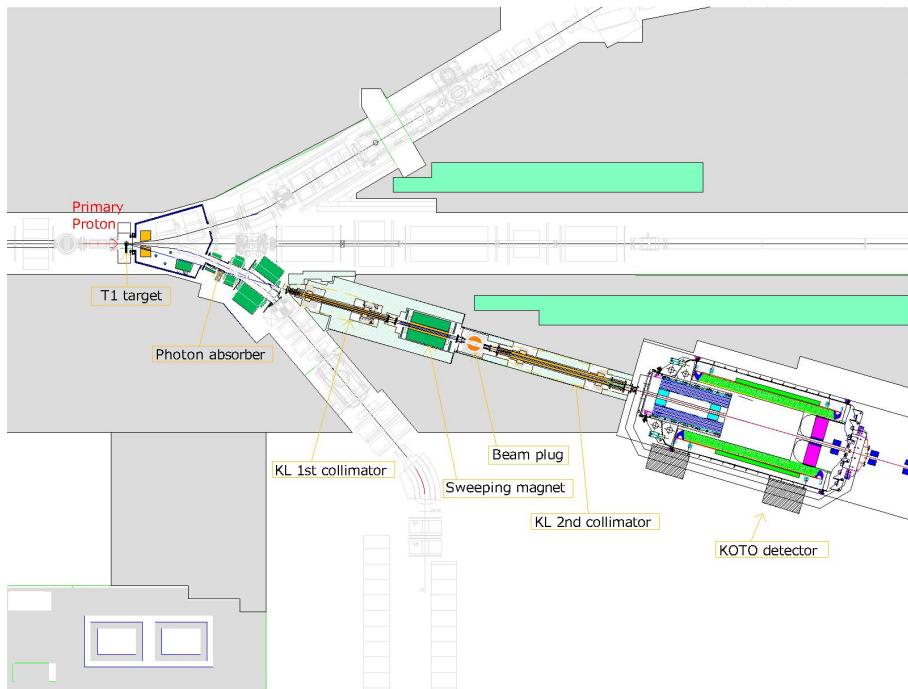


FIGURE 2.5: Beamlne layout

¹³⁶ 2.3.1 CsI

¹³⁷ The electromagnetic calorimeter is the main detector of the KOTO experiment. It is used
¹³⁸ to detect the photon from the K_L decay. The electromagnetic calorimeter consists of 2716
¹³⁹ undoped cesium iodide crystals (CsI). The cross-section of crystals has 2 types of units:
¹⁴⁰ the small crystal is 25×25 mm with 2240 crystals, and the large one is 50×50 mm with
¹⁴¹ 476 crystals. The arrangement of those crystals is shown in Figure 2.6. The depth of the
¹⁴² crystal is 500 mm corresponding to 27 radiation lengths(X_0), in which the X^0 of CsI is
¹⁴³ 18.5 mm. The large crystal depth can contain all the photon energy that can allow us to
¹⁴⁴ ignore the detection inefficiency of the photon. The small crystal size is smaller than the
¹⁴⁵ Molère radius of 35.7 mm, which provides a good resolution of position and the cluster
¹⁴⁶ shape in the x-y plant. That allows us to use the shower shape to distinguish the different
¹⁴⁷ types of clusters on CsI.

¹⁴⁸ A both-end readout system was used in the CsI calorimeter. A photon multiplier tube
¹⁴⁹ (PMT) was connected to the end of each CsI crystal. When a photon hits the CsI, the EM
¹⁵⁰ shower will be induced and the PMT can observe the deposited energy on each crystal.
¹⁵¹ In front of the CsI crystal, 4096 Multi-pixel photon counters (MPPC) were glued. It could
¹⁵² detect the signal of the photon hit from the front end. This readout system can be used to
¹⁵³ measure the shower depth in the calorimeter, by evaluating the time difference between
¹⁵⁴ both ends of the crystal. Which is potentially useful for discriminating the photon cluster
¹⁵⁵ and hadronic-like cluster. Because a hadronic shower is generally deeper than an EM
¹⁵⁶ shower cluster.

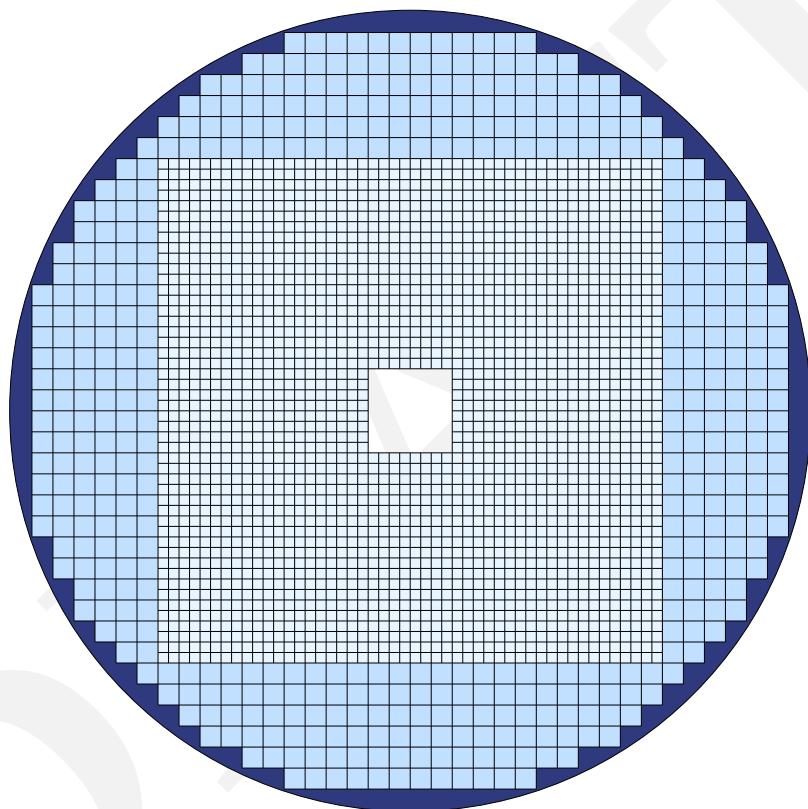


FIGURE 2.6: Schematic diagram of CsI layout.

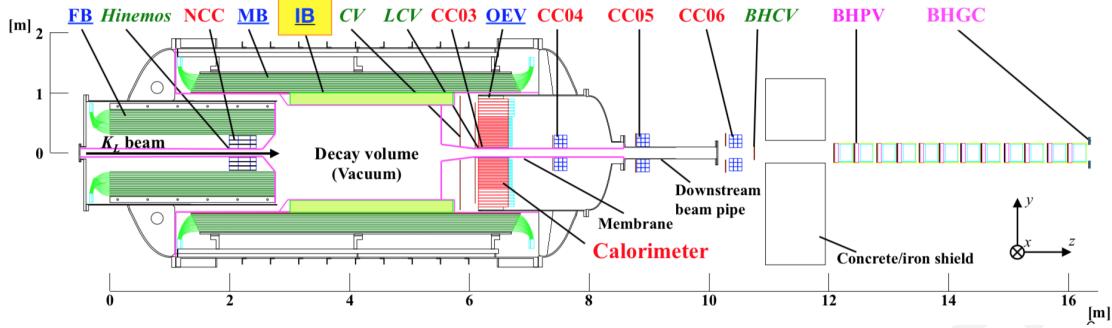


FIGURE 2.7: KOTO detector layout

157 2.3.2 Charge Veto Counter

158 The Charge Veto Counter (CV) is placed in front of the CsI [12, 13, 14]. It is a plant com-
 159 posed of plastic scintillator strips, the arrangement of the strips is shown in Figure 2.8.
 160 Because the CV plant is also perpendicular to the beamline, a square hole was made in
 161 the center of the CV to allow the beamline to pass through. The CV consists of two layers
 162 of 3-mm thick scintillator strips and wavelength-shifting (WLS) fibers, the direction of
 163 the two layers' strips is perpendicular to each other. The front CV is placed 30 cm up-
 164 stream of the CsI, and the Rare CV is placed 5 cm upstream. An MPPC was attached to
 165 both ends of the strip to detect the light emitted by the scintillator.

166 This veto counter was used to detect the charged particle that could hit the CsI calorime-
 167 ter. Because the $K_L^0 \rightarrow \pi^\pm e^\mp \nu_e$ and $K_L^0 \rightarrow \pi^\pm \mu^\mp \nu_\mu$ have a very large branching ratio, the
 168 charged particle could hit the CsI calorimeter and produce a fake photon cluster. The
 169 main purpose of the CV is to veto the charged particle and reduce these two decay chan-
 170 nels. The inefficiency of the CV to a single charge particle is 1.5×10^{-5} .

171 2.3.3 Barrel Veto Counter

172 The Barrel veto counters surround the decay volume which is the main body of the her-
 173 metic veto system to ensure all the photons will not escape from the detector. There are
 174 3 Barrel Veto Counters in the KOTO detector, Front Barrel(FB), Main Barrel(MB), and In-
 175 ner Barrel(IB). The place relation of the three barrel veto counters was shown in Figure
 176 2.9. The MB covered the decay volume, and the IB was placed in the center of the MB,
 177 these two veto counters are used to detect the photon hit escape from the CsI calorime-
 178 ter. The front barrel covers the upstream of the decay region to veto the event decay in
 179 the upstream region. All the barrel veto counters are composed of the lead-scintillator
 180 sandwich structure, as shown in Figure 2.9. The lead was used to absorb the photon and
 181 the scintillator was used to emit the light when the photon hit. After the light emitted by
 182 the scintillator, it will be transferred to the PMT attached to the end of the barrel by WSL
 183 fiber. At the innermost of the MB and IB, a 10 mm thick Charge Veto is attached, which is
 184 called MBCV and IBCV. The MBCV and IBCV consisted of the scintillator and WLS fiber,
 185 which was used to veto the charged particle.

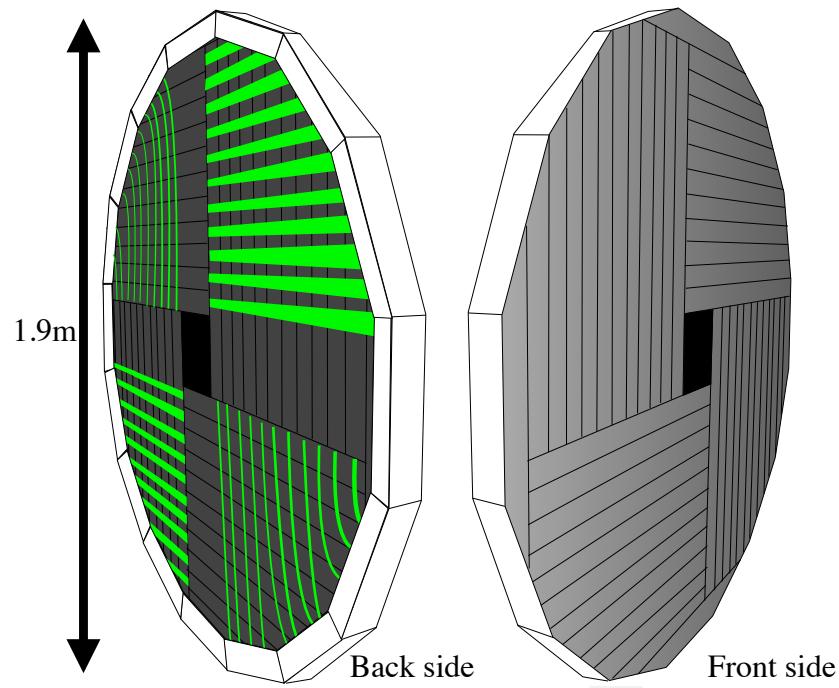


FIGURE 2.8: The Schematic Diagram of Charge Veto Structure.

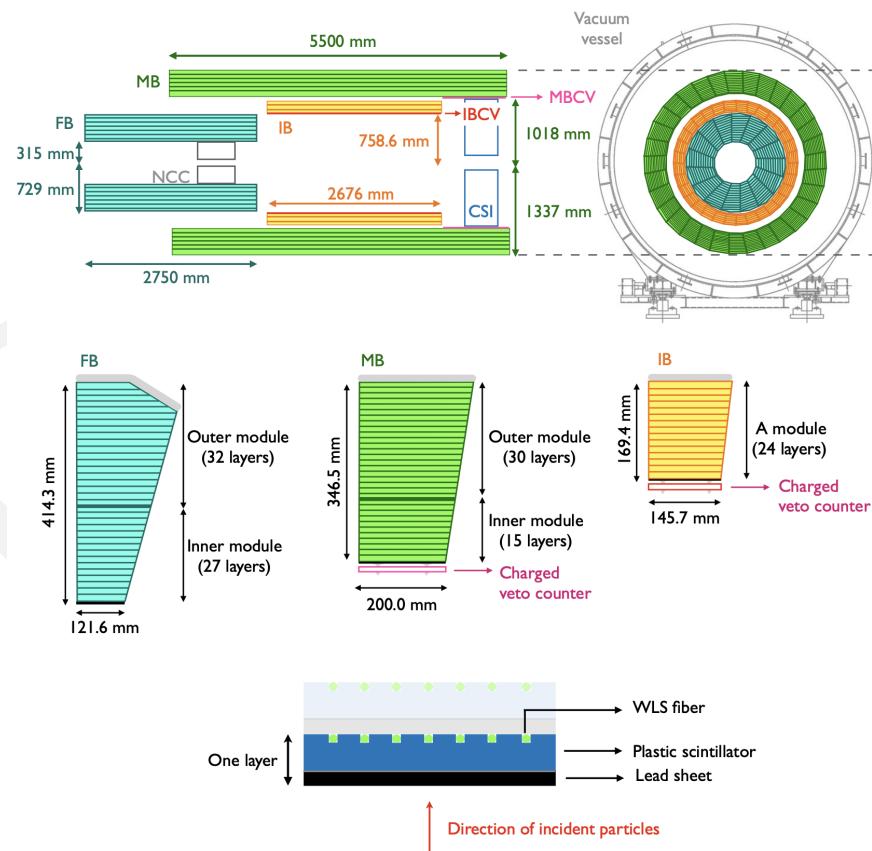


FIGURE 2.9: The Schematic Diagram of Barrel Veto Structure. Figure courtesy of [15].

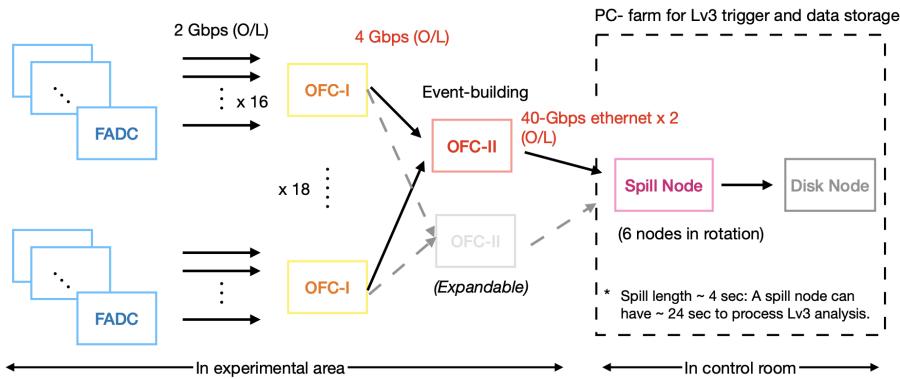


FIGURE 2.10: The architecture of the KOTO DAQ system. [16]

¹⁸⁶ 2.4 Data Acquisition System

¹⁸⁷ When a particle hits the detectors, the electronic signal will be generated. To determine
¹⁸⁸ whether this signal is interesting, a trigger system is used to decide the candidate events.
¹⁸⁹ If an event passes any trigger criteria, the data acquisition system (DAQ) will collect and
¹⁹⁰ store the data.

¹⁹¹ The DAQ system of the KOTO experiment consists of 3 levels: the first-level (L1) and
¹⁹² second-level (L2) trigger placed in the experiment area, and the third-level trigger (L3) at
¹⁹³ the PC farm. The architecture of the DAQ system is shown in Figure 2.10.

¹⁹⁴ KOTO detector has nearly 4000 channels in total, all these channels are connected to
¹⁹⁵ the flash analog-to-digital converter (FADC) board to digitize the signal. There are two
¹⁹⁶ types of FADC boards in the KOTO detector, with 125 MHz and 500 MHz sampling rates.
¹⁹⁷ We have a total of 288 FADC boards and separate them into 18 crates with 16 boards in
¹⁹⁸ each crate.

¹⁹⁹ For the 125 MHz FADC, 16 channels are connected to each board, and the 500 MHz
²⁰⁰ FADC has 4 channels on each board.

201 **Chapter 3**

202 **Event Reconstruction**

203 Event reconstruction is a crucial step in the analysis of decay events. After the reconstruction,
204 the kinematic variable of the K_L^0 , such as the decay vertex, energy, and momentum,
205 can be obtained. With kinematic information, precise event selection can be achieved and
206 the performance of physical analysis can be improved.

207 To reconstruct a K_L^0 decay event, it is necessary to accurately model the decay process.
208 The primary strategy involves initially identifying photon clusters. Subsequently, the
209 clusters' energy, timing, and position on the CsI are utilized to reconstruct the parent
210 particle. This includes determining kinematic properties such as the decay vertex, energy,
211 and momentum of the parent particle. The specific details of the reconstruction process
212 vary depending on the decay mode. For channels involving pions, such as $K_L^0 \rightarrow 3\pi^0$ and
213 $K_L^0 \rightarrow \pi^0\pi^0$, the photon clusters are mapped to pions, which are then used to reconstruct
214 the Kaon. In simpler decay channels like $K_L^0 \rightarrow 2\gamma$, the K_L^0 is directly reconstructed from
215 the photon data.

216 \section{Energy and Timing reconstruct from Waveform}

217 **3.1 Photon Cluster Finding**

218 In this step, we need to find the photon cluster and then reconstruct the energy, timing,
219 and the hit position of the cluster. This process is called "clustering".

220 First, need to find the cluster. The crystal which has deposited energy larger than 3
221 MeV and the hit timing is within 150 ns is considered a "seed crystal". Then, scanning
222 the neighboring crystals in a 140 mm wide square box around the seed crystal. The
223 neighboring crystals will add to the same cluster if the neighboring crystal is also a seed
224 crystal. And do the same scanning process for the neighboring crystals of the neighboring
225 crystals, til there is not a neighboring friend that can be found. This process will be
226 applied to all the seed crystals that have not been assigned to any cluster yet. A seed
227 crystal without any neighboring friend will be defined as an "isolated crystal hit". The
228 isolated crystal hit will be used in the CsI veto. The algorithm is illustrated in Figure 3.1.

229 Because of the wide 150 ns timing window, the cluster may contain the hits not belong
230 to the cluster shower. A seed crystal is assigned to a cluster, but it does not come from

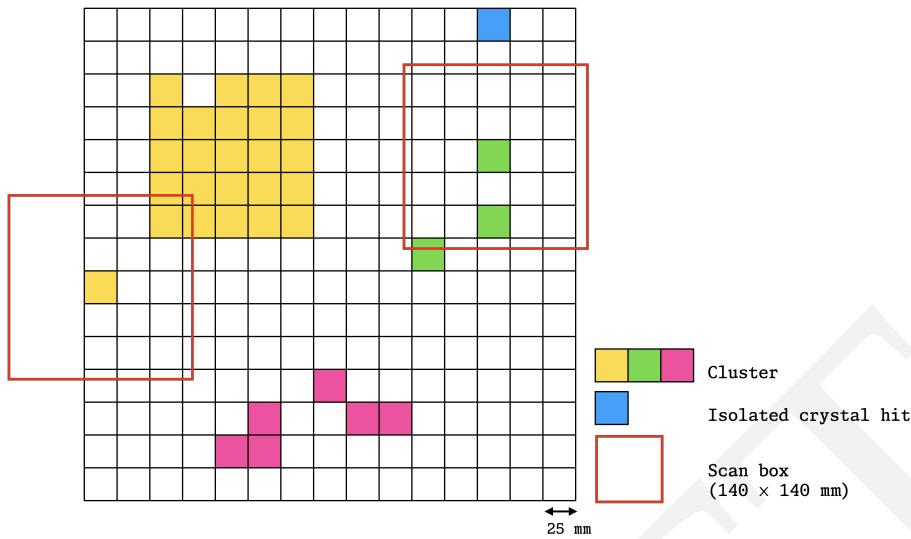


FIGURE 3.1: The illustration of the cluster finding process. All the color crystals are the seed crystals, and the crystals with the same color belong to the same cluster. The black crystal is the isolated crystal hit.

231 the cluster shower will be defined as an "accidental hit" and should be removed from the
 232 cluster. To avoid the accidental hit, the cluster timing was used to do the selection. The
 233 cluster timing ($T_{cluster}$) is defined by the equation 3.1.

$$T_{cluster} = \frac{\sum_{i=1}^n T_i / \sigma_t^2}{\sum_{i=1}^n 1 / \sigma_t^2} \quad (3.1)$$

$$\sigma_t = 0.13 \oplus \frac{3.63}{\sqrt{E_i}} \oplus \frac{5}{E_i} \quad (3.2)$$

234 Where n is the number of crystals in the cluster, i is the i -th crystal, and e is the energy
 235 of the cluster. The σ_t is the timing uncertainty of each crystal, which is a function of
 236 the energy of each crystal[17]. If a seed crystal from a cluster with timing outside the
 237 $\pm 5\sigma$ boundary of its cluster timing, it will be defined as an accidental hit and will be
 238 removed. Figure 3.2 shows the timing boundary for a crystal seed after subtracting the
 239 cluster timing. The cluster timing will recalculate after removing the accidental hit and
 240 iterate this process until all accidental hits have been removed.

241 Moreover, a timing selection will apply to the clusters. Because the cluster should be
 242 produced by the same Kaon decay, the timing of the cluster should be within a certain
 243 range. Therefore, the maximum timing difference between all clusters should be within
 244 30 ns. Otherwise, the cluster that has the largest timing difference with the average timing
 245 of all clusters will be removed. This process will be repeated until all clusters satisfy the
 246 timing selection.

247 The cluster after the above process will be used in the next step of the reconstruction.
 248 The below information on the cluster will be calculated and provided to the next step.

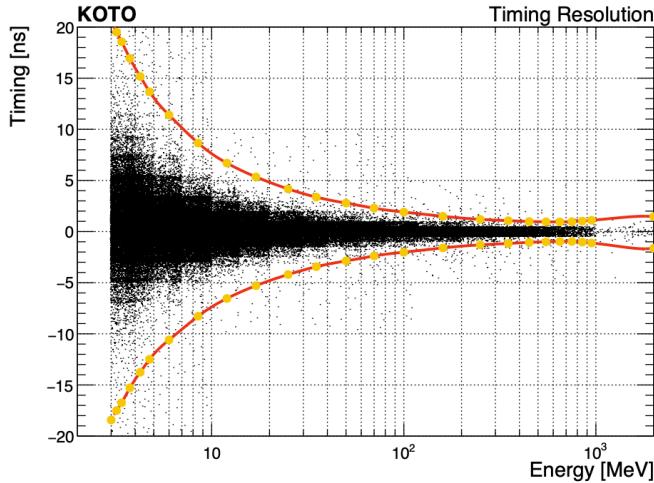


FIGURE 3.2: Timing boundary for a cluster seed based on the scattered plot of crystal timing versus energy deposit. A Gaussian function is fitted at each energy bin and the boundary is defined by $\mu \pm 5\sigma$, where μ and σ are the Gaussian mean and standard deviation. The orange points indicate the boundary at the associated energy bin. The red curve connects all the points for the interpolation of the boundary value between the points. (Figure courtesy of [15])

249 **Cluster Energy ($E_{cluster}$)**

250 The energy of the cluster is the sum of the energy of all crystals in the cluster.

$$E_{cluster} = \sum_{i=1}^n E_i \quad (3.3)$$

251 **Cluster Position ($x_{cluster}, y_{cluster}$)**

252 The position of the cluster is defined by its center of energy, and the position is
253 calculated by the equation below.

$$x_{cluster} = \frac{\sum_{i=1}^n E_i x_i}{E_{cluster}} \quad (3.4)$$

$$y_{cluster} = \frac{\sum_{i=1}^n E_i y_i}{E_{cluster}} \quad (3.5)$$

254 **3.2 Reconstruction of π^0**

255 The π^0 is reconstructed by two photon clusters. Figure 3.3 shows the schematic diagram
256 of the $\pi^0 \rightarrow 2\gamma$ decay process. First, the decay vertex needs to be determined, assum-
257 ing the decay vertex is $(0, 0, z_{vtx})$. Therefore, the three momenta of the photon can be
258 calculated by

$$\vec{P}_\gamma = k \cdot (x, y, \Delta z) \quad (3.6)$$

259 where the k is a constant does not determine yet. And the Δz is the difference between
260 the z position of the cluster and the decay vertex.

$$\Delta z = z_{CsI} - z_{vtx} \quad (3.7)$$

261 Based on four-momentum conservation, the opening angle (θ) between two photons is
262 calculated by

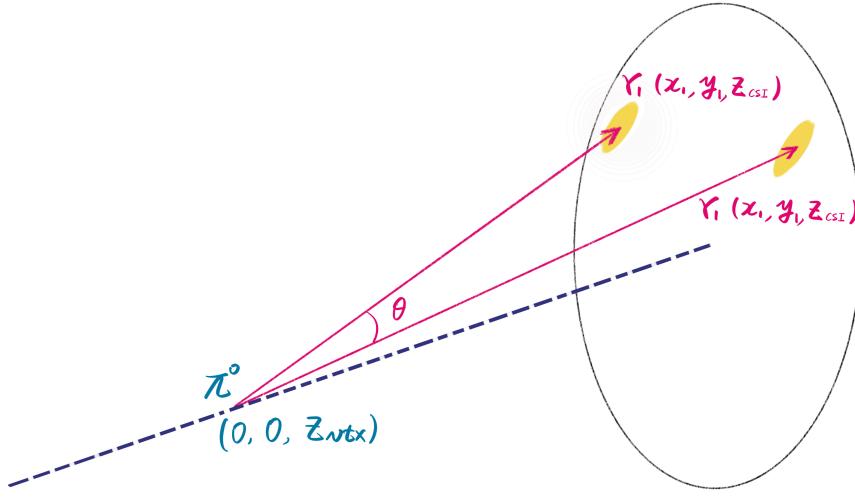


FIGURE 3.3: The schematic diagram of the $\pi^0 \rightarrow 2\gamma$ decay process.

$$\cos(\theta) = 1 - \frac{M_{\pi^0}^2}{2 \cdot E_{\gamma 1} \cdot E_{\gamma 2}} \quad (3.8)$$

and combine with the inner product of two photons' momentum, the following equation can derive the z_{vtx} .

$$1 - \frac{M_{\pi^0}^2}{2 \cdot E_{\gamma 1} \cdot E_{\gamma 2}} = \frac{\vec{P}_{\gamma 1} \cdot \vec{P}_{\gamma 2}}{|\vec{P}_{\gamma 1}| \cdot |\vec{P}_{\gamma 2}|} \quad (3.9)$$

After determining the z_{vtx} , the momentum of the photon can be calculated by

$$|\vec{P}_\gamma| = E_\gamma \quad (3.10)$$

The energy and momentum of the π^0 can be calculated by

$$E_{\pi^0} = E_{\gamma 1} + E_{\gamma 2} \quad (3.11)$$

$$\vec{P}_{\pi^0} = \vec{P}_{\gamma 1} + \vec{P}_{\gamma 2} \quad (3.12)$$

3.3 Reconstruction of Decays

In this section, the reconstruction algorithm for the $K_L^0 \rightarrow 3\pi^0$ and $K_L^0 \rightarrow \gamma\bar{\gamma}$ decay will be introduced. The $K_L^0 \rightarrow 3\pi^0$ decay is used to evaluate the K_L^0 yield, and the $K_L^0 \rightarrow \gamma\bar{\gamma}$ decay is for the physics analysis. In other KOTO experiment studies, the $K_L^0 \rightarrow \pi^0\pi^0$ and $K_L^0 \rightarrow 2\gamma$ decay are also used in the yield estimation and are not covered in this section. Because the $K_L^0 \rightarrow 3\pi^0$ is the only decay channel used for the yield estimation.

All the K_L^0 decay reconstruction is based on the result from the clustering process. A minimal energy selection of 20 MeV is required for the photon cluster. Also, the number of photon cluster requirement need to be equal to the final state of the decay. For the

²⁷⁶ $K_L^0 \rightarrow 3\pi^0$ decay, the event needs to have exactly 6 photon clusters. For the $K_L^0 \rightarrow \gamma\bar{\gamma}$
²⁷⁷ decay, the event should contain only 1 photon cluster.

²⁷⁸ After the K_L^0 decay vertex reconstruction, then calculate the kinematic variables. The
²⁷⁹ kinematic variable will be utilized in the next step analysis.

²⁸⁰ **3.3.1 Reconstruction of $K_L^0 \rightarrow 3\pi^0$**

²⁸¹ $K_L^0 \rightarrow 3\pi^0$ decay has three π^0 in the decay process, the reconstruction of π^0 will use
²⁸² the same algorithm as the previous section. The special situation is there are six photon
²⁸³ clusters on the CsI, and the π^0 can be reconstructed in different combinations. All the
²⁸⁴ combinations will be considered because the true combination is unknown. The most
²⁸⁵ number of combinations for $K_L^0 \rightarrow 3\pi^0$ is

$$\binom{6}{2} \binom{4}{2} \binom{2}{2} / 3! = 15$$

²⁸⁶ Because of the short lift time of the π^0 , the decay vertex of the π^0 's should be very close.
²⁸⁷ Therefore, the χ_z^2 could be used to select the best combination.

$$\chi_z^2 = \sum_i^{N_{\pi^0}} \left(\frac{z_{vtx}^i - \bar{z}_{vtx}}{\sigma_i^2} \right)^2 \quad (3.13)$$

²⁸⁸ where N_{π^0} is the number of π^0 in the decay, z_{vtx}^i is the decay vertex z of the i -th π^0 , \bar{z}_{vtx}
²⁸⁹ is the average decay vertex z of all π^0 , and σ_i is the uncertainty propagated from the
²⁹⁰ calorimeter of the i -th π^0 . The best combination of π^0 should have the smallest χ_z^2 . The
²⁹¹ weighted average decay vertex z is also defined as the decay vertex z of K_L^0 , calculated
²⁹² by

$$\bar{z}_{vtx} = \frac{\sum_i^{N_{\pi^0}} z_{vtx}^i / \sigma_i^2}{\sum_i^{N_{\pi^0}} 1 / \sigma_i^2} \quad (3.14)$$

²⁹³ From the π^0 reconstruction, the π^0 decay vertex was assumed in the center of the CsI.
²⁹⁴ To determine the real decay vertex, a correction process was applied. As shown in Figure
²⁹⁵ 3.4, the K_L^0 travels start from the target and end at the decay vertex, then decay to the π^0 s
²⁹⁶ and γ s hit on the CsI, and K_L^0 project to the center of energy (COE). Therefore, the K_L^0
²⁹⁷ decay vertex can be calculated based on the geometry, by the following equation.

$$x_{vtx} = x_{COE} \cdot \frac{z_{vtx} - z_{target}}{z_{CsI} - z_{target}} \quad (3.15)$$

$$y_{vtx} = y_{COE} \cdot \frac{z_{vtx} - z_{target}}{z_{CsI} - z_{target}} \quad (3.16)$$

²⁹⁸ where z_{target} is the z position of the target. The x_{COE} and y_{COE} can calculate by

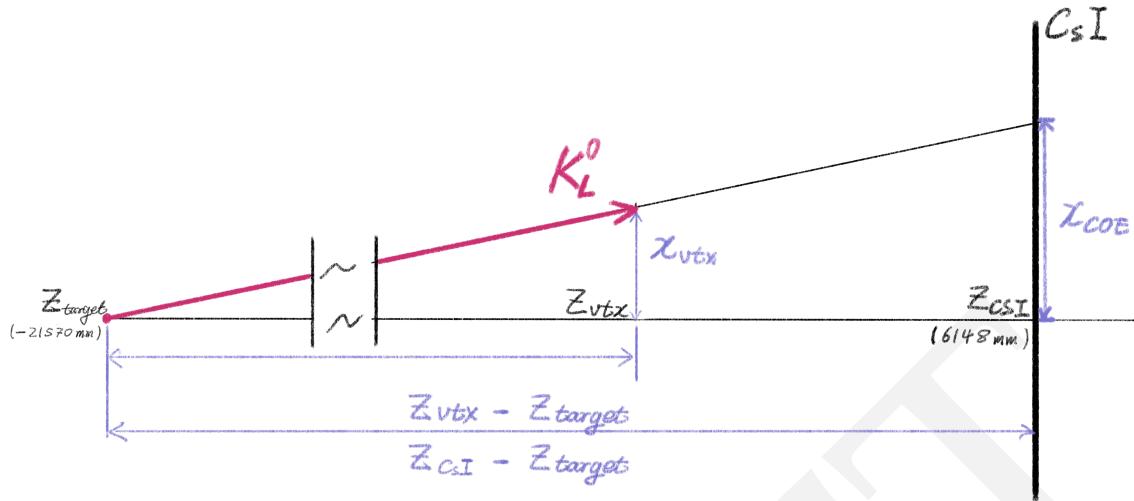


FIGURE 3.4: The schematic diagram of the K_L^0 travel and decay process and geometry relationships

$$x_{\text{COE}} = \frac{\sum_{i=1}^{n_\gamma} E_i x_i}{\sum_{i=1}^{n_\gamma} E_i} \quad (3.17)$$

$$y_{\text{COE}} = \frac{\sum_{i=1}^{n_\gamma} E_i y_i}{\sum_{i=1}^{n_\gamma} E_i} \quad (3.18)$$

After obtaining the corrected decay vertex, the energy and momentum of the K_L^0 can be obtained intuitively from the summation of all the π^0 's energy and momentum, as same as the Equation 3.11.

$$E_{K_L^0} = \sum_{i=1}^{N_{\pi^0}} E_{\pi^0} \quad (3.19)$$

$$\vec{P}_{K_L^0} = \sum_{i=1}^{N_{\pi^0}} \vec{P}_{\pi^0} \quad (3.20)$$

3.3.2 Reconstruction of $K_L^0 \rightarrow \gamma\bar{\gamma}$

$K_L^0 \rightarrow \gamma\bar{\gamma}$ Decay is the primary target of this analysis. The final state of $K_L^0 \rightarrow \gamma\bar{\gamma}$ is similar to $K_L^0 \rightarrow 2\gamma$, but one photon is a dark photon. Due to the missing energy, the signature on CsI of $K_L^0 \rightarrow \gamma\bar{\gamma}$ decay is only one photon cluster hit. Based on Section 3.1, the information that could be obtained from one photon cluster is only its energy, timing, and position on the CsI surface. With this limited information, it is impossible to reconstruct the K_L^0 decay vertex. Therefore, the lack of kinematic information is the biggest challenge of the $K_L^0 \rightarrow \gamma\bar{\gamma}$ decay search study.

3.3.3 Correction for Energy and Position of Photon Clusters

After the reconstruction of the K_L^0 decay, and also obtaining the corrected decay vertex, the energy and position of the photon clusters will be possible to correct. Because this

313 correction process needs the incident angle of the photon, this process has to be done
 314 after the K_L^0 decay reconstruction. After the correction, we will use the new position to
 315 recalculate the decay vertex.

316 **Position Correction**

317 The position of the photon cluster obtained from the clustering process is the position of
 318 the center of energy of the cluster. As shown in the Figure 3.5. The z position for the
 319 center of energy of the cluster is inside the crystal. However, the z position of the CsI
 320 we used in the reconstruction is the position of the crystal surface. This difference will
 321 introduce a bias for the reconstruction of the vertex position. To eliminate this bias, the x
 322 and y positions of the photon cluster need to be corrected to the real incident position.

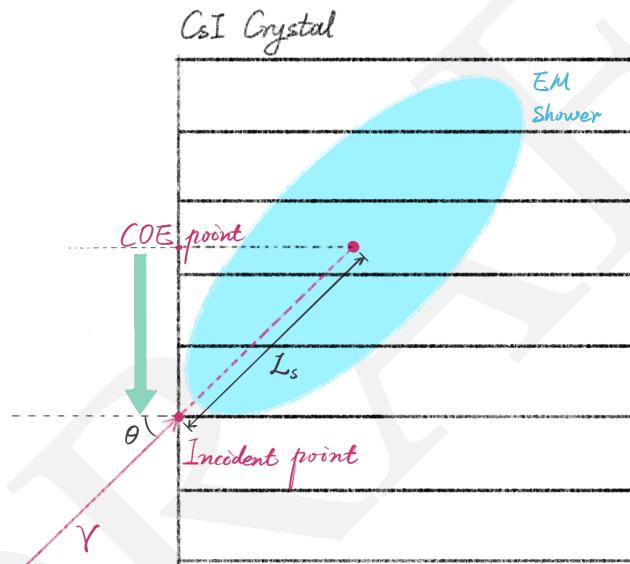


FIGURE 3.5: The schematic diagram of the correction of the photon cluster position.

323 From the decay vertex reconstruction, the incident angle (θ) of the photon was ob-
 324 tained. And the corrected distance (L_c) can be calculated by

$$L_c = L_s \cdot \sin(\theta) \quad (3.21)$$

325 where the L_s is the distance from the incident point to the cluster COE of the EM shower,
 326 and the L_s can be calculated by

$$L_s/X_0 = p_0 + p_1 \ln(E[\text{GeV}]) \quad (3.22)$$

327 where the $X_0 = 18.5$ is the radiation length of the CsI, E is the cluster energy in GeV, and
 328 the $p_0 = 6.490$ and $p_1 = 0.993$ are the parameters obtains from the MC simulation.

329 **Energy Correction**

330 In the clustering process, a 3 MeV energy threshold was applied to the seed crystal. And
 331 EM shower also possibly has leakage energy from the crystals and is not included in the
 332 cluster. These factors will cause the energy lost from the measurement. To correct these
 333 energy losses, a correction function dependence on energy was obtained from the MC
 334 simulation.

$$E_{corr} = E \cdot (1 + w(E)) \quad (3.23)$$

335 where $w(E)$ is the correction function.

336 After the correction of the energy and position of the photon cluster, the decay recon-
 337 struction will be repeated. The final result will be used in the next step of the analysis.

338 **3.4 Veto Hit Reconstruction**

339 The veto counter is used in the background rejection. The rejection is based on the tim-
 340 ing of the veto hit and the deposited energy. And that is the information we need to
 341 reconstruct from the veto hit.

342 The reject criteria require an energy deposit over the energy threshold, which can dis-
 343 tinguish the signal from the background noise, and a hit timing within the timing win-
 344 dow to ensure the hit is from the same K_L^0 decay event, this kind of hit is called an "on-
 345 time" hit. Because the veto information is exclusively utilized for background rejection
 346 criteria in this study, the hit timing was selected as the hit that was closest to the nominal
 347 timing if there was more than one hit on the veto counter.

348 To do the timing criteria, a veto timing(T_{veto}) was defined, which is the difference
 349 between the veto hit timing and the K_L^0 decay timing. The veto timing is defined as

$$\begin{cases} T_{veto} = T_{mod} - T_{vtx} - TOF \\ TOF = D/c, \end{cases} \quad (3.24)$$

350 where the T_{mod} is the veto hit timing, T_{vtx} is the K_L^0 decay timing, TOF is the time-of-
 351 flight of the particle, D is the distance between the decay vertex and the veto hit position.
 352 As shown in the Figure 3.6.

353 However, this equation has to involve the vertex information, which is not available
 354 in the $K_L^0 \rightarrow \gamma\bar{\gamma}$ analysis. Therefore, the T_{veto} needs to be modified to be independent of
 355 the vertex information. The vertex timing T_{vtx} can be approximated by

$$T_{vtx} \approx T_{CsI} - \Delta z/c \quad (3.25)$$

356 where the T_{CsI} is the corrected average timing of the CsI clusters, and the Δz is the
 357 difference between the z position of the CsI surface and the decay vertex. And with the

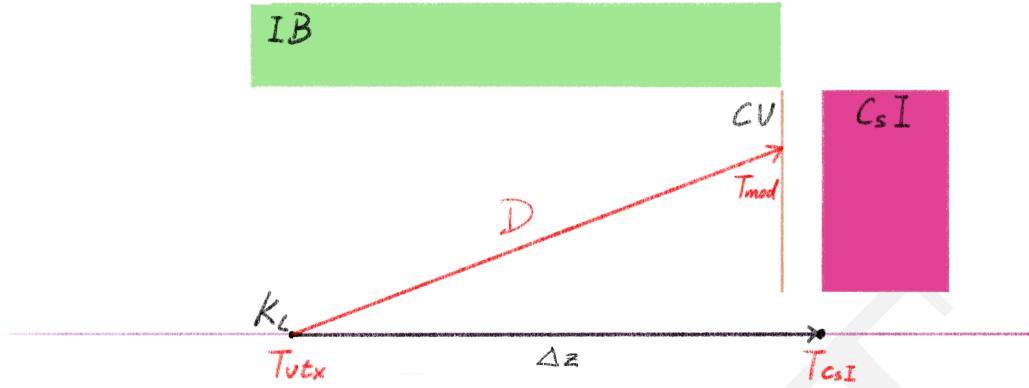


FIGURE 3.6: Schematic view of the timings used in the module-veto-timing calculation.

358 Equation 3.24 the T_{veto} can be derived as

$$T_{veto} \approx T_{mod} - T_{CsI} + (\Delta z - D)/c \quad (3.26)$$

359 The $(\Delta z - D)$ is an uncontrolled variable because D still needs the vertex position information. Thankfully, most veto counters do not have a large scale along the z-axis, thus 360 the variant of the $(\Delta z - D)$ is small. Therefore, $(\Delta z - D)$ can be treated as a constant in 361 most cases, and the T_{veto} can be equivalent to 362

$$T_{veto} \equiv T_{mod} - T_{CsI} \quad (3.27)$$

363 This definition can be used in the all downstream veto count and also the FBAR and the 364 NCC veto counter. However, the Barrel veto counter does not satisfy the condition that 365 has a large scale along the z-axis, and the $(\Delta z - D)$ is not negligible.

366 In the following section, some special treatment of the veto hit will be explained,

367 3.4.1 Barrel Veto Counters

368 The Barrel veto counters contain the Main Barrel(MB) and the Inner Barrel(IB), which 369 have a Both-End Readout system. The mechanism of the both-end readout veto hit is 370 shown in Figure 3.7. And the T_{mod} could be calculated by the upstream and downstream 371 PMT timing.

$$\begin{cases} T_{mod} = T_u - L_u/v, \\ T_{mod} = T_d - L_d/v \end{cases} \quad (3.28)$$

372 where the T_u and T_d are the timing of the upstream and downstream, and $L_u(L_d)$ is the 373 distance between the hit position to the upstream (downstream) PMT, v is the propagated 374 velocity in the module. Therefore, the T_{mod} can be calculated by

$$T_{mod} = \frac{T_u + T_d}{2} - \frac{L}{2v} \quad (3.29)$$

³⁷⁵ The hit position z_{hit} of the veto counter can be derived as

$$z_{hit} = z_{center} + \frac{v \cdot (T_u - T_d)}{2} \quad (3.30)$$

³⁷⁶ where the z_{center} is the z position of the center of the barrel veto counter.

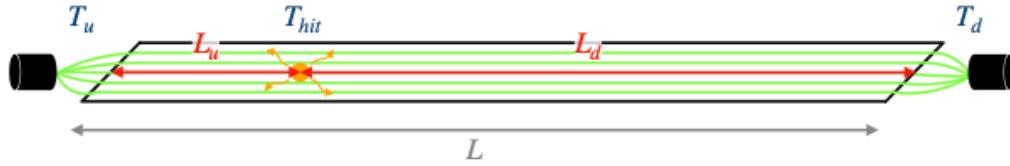


FIGURE 3.7: The Schematic diagram of a photon hit with the generated scintillation lights propagating to both directions and captured by PMTs. Figure courtesy of [15]

³⁷⁷ The geometry relationships of the Barrel veto hit are shown in Figure 3.8. The $(\Delta z - D)$
³⁷⁸ from Equation 3.26 can be approximated by

$$\Delta z - D \approx \Delta S, \quad (3.31)$$

$$\Delta S = \sqrt{R^2 + (z_{hit} - z_{CsI})^2} \quad (3.32)$$

³⁷⁹ where R is the radius of the Barrel veto counter. And the T_{veto} can be derived as

$$T_{veto} = T_{mod} - T_{CsI} + \Delta S/c \quad (3.33)$$

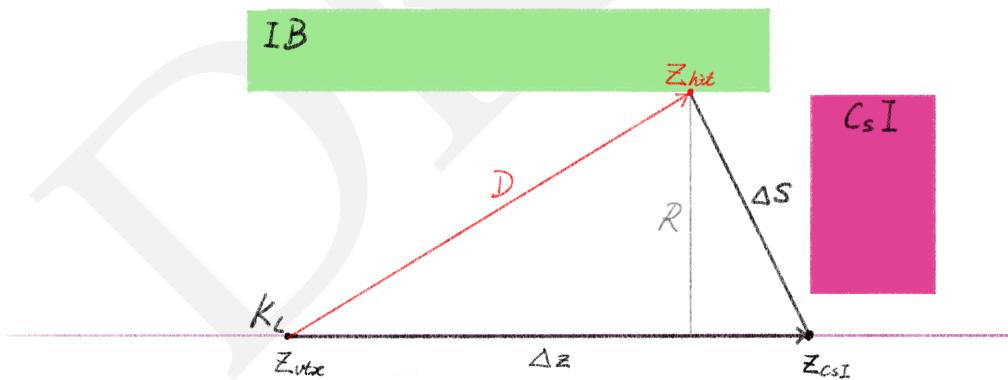


FIGURE 3.8: The Schematic diagram of geometry relationships of the Barrel veto counter.

³⁸⁰ 3.4.2 CsI Calorimeter

³⁸¹ As Section 3.1 mentioned, the CsI calorimeter is used to reconstruct the photon cluster.
³⁸² All the crystal hits on the CsI Calorimeter will be used in the clustering process. How-
³⁸³ ever, some crystal hits cannot be assigned to any cluster, and these hits are defined as
³⁸⁴ "Isolated Crystal Hits". Even though a cluster has been constructed, if it does not satisfy

385 the π^0 reconstruction criteria, it will not be assigned to any K_L^0 or π^0 , and these clusters
 386 are defined as "Extra Clusters". The mechanism of these hits could come from a photo-
 387 nuclear reaction in the shower propagation. These two types of hits will be used in the
 388 veto rejection.

389 Because this detector is also the calorimeter, the veto timing definition needs to be
 390 modified. For the "extra clusters" the timing of the decay vertex (T_{vtx}) is not recalculated
 391 for each cluster,

$$T_{vtx} = T_{cluster} - L/c \quad (3.34)$$

392 where L is the distance between the decay vertex and the cluster.

393 For the "isolated crystal hits", because it possibly split from the other cluster. To avoid
 394 this situation, the selection criteria variables are correlated to the nearest cluster. The
 395 variable that needs to be reconstructed is the distance (D) and the timing difference (T)
 396 between the isolated crystal hit and the nearest cluster.

$$T_{veto} = T_{crystal} - T_{cluster} \quad (3.35)$$

$$D = \sqrt{(x_{crystal} - x_{cluster})^2 + (y_{crystal} - y_{cluster})^2} \quad (3.36)$$

³⁹⁷ **Chapter 4**

³⁹⁸ **Monte Carlo Simulation**

³⁹⁹ In this chapter, the Monte Carlo (MC) simulation of the KOTO experiment is described,
⁴⁰⁰ which is used for the $K_L^0 \rightarrow \gamma\bar{\gamma}$ analysis. In the HEP analysis field, there are so many
⁴⁰¹ physics mechanisms behind the physics data, to verify these mechanisms, the MC simu-
⁴⁰² lation is used to simulate the physics process to help us understand the data behaviors.
⁴⁰³ The simulations were performed to reproduce real physics data and to estimate the K_L^0
⁴⁰⁴ source background events. The MC simulation should reproduce the real data as much
⁴⁰⁵ as possible. Ideally, if all the background sources and mechanisms are well considered,
⁴⁰⁶ the MC simulation should reproduce the real data perfectly.

⁴⁰⁷ The simulation procedure consists of the following steps. First, generate a set of K_L^0
⁴⁰⁸ particles to enter the KOTO detector, simulate the decay of such particles in the detec-
⁴⁰⁹ tor, and simulate the detector response with the interaction of the decay products. The
⁴¹⁰ simulation is performed using the GEANT4 toolkit [18, 19, 20]. Then convert the MC sim-
⁴¹¹ ulation result to the same format as the real data. To reproduce the same conditions of
⁴¹² the K_L^0 as the real data run, a K_L^0 momentum spectrum and beam structure are prepared
⁴¹³ based on the real data. The MC simulation is performed with the same beam structure
⁴¹⁴ and detector conditions as the real data. In addition, some other MC simulation is also
⁴¹⁵ performed in this analysis to estimate the background events, such as the beamline sim-
⁴¹⁶ ulation, upstream π^0 background.

⁴¹⁷ **4.1 GEANT4 toolkit**

⁴¹⁸ GEANT4 (GEometry ANd Tracking) is a comprehensive software toolkit, which is pop-
⁴¹⁹ ular in high energy physics, used for the simulation of the passage of particles through
⁴²⁰ matter. In the GEANT4 simulation, the simulation is performed step by step. In each
⁴²¹ step, the particle interacts with the detector material, and the energy deposits and the
⁴²² direction change of the particle are calculated. The particle quantities are all stored in the
⁴²³ simulation output, thus it is easy to analyze the particle decay because its whole proce-
⁴²⁴ dure is traceable.

425 4.2 Detector Response

426 The GEANT4 simulation toolkit can provide the timing, energy deposit, and position of
 427 the particle interaction, but it is the ideal information, called "true information", which
 428 cannot be directly compared with the real data. The kinematic information is recon-
 429 structed from the data detected by sensors. Therefore, simulations are necessary to repli-
 430 cate the information given by the detector readout.

431 The KOTO detector contains several sub-detectors with different detected principles.
 432 The majority method uses the scintillation process, to detect the propagated light by PMT.
 433 The Čerenkov radiation was used in the BHPV and BHGC, and the gas ionization was
 434 used in the BHCV.

435 4.3 Pulse Simulation

436 The FADC digitized pulses can be described by an asymmetric Gaussian function $f(t)$ as
 437

$$f(t) = A \exp \left(- \left(\frac{t - \mu}{(\sigma_0 + a(t - \mu))} \right)^2 \right) \quad (4.1)$$

438 where t is the time of the pulse, μ is the peak timing, σ_0 and a are the parameters that
 439 determine the shape of the pulse which are given for each detector channel. A is the
 440 normalization factor determined by the integration of $f(t)$ to energy.

441 4.4 K_L^0 Generation

442 In the Monte Carlo simulation, the K_L^0 particles are generated at the K_L^0 beam exit which
 443 is 1507 mm upstream of the detector. Given the momentum and production position of
 444 the K_L^0 particles, the decay process can be simulated. There are two methods that can
 445 obtain the momentum and position distribution, one is called beamline simulation and
 446 the other is called the empirical K_L^0 momentum spectrum.

447 4.4.1 Beamline Simulation

448 The K_L^0 beam in the KOTO experiment is produced from the proton-gold fix target colli-
 449 sions. The simulation that starts from the proton collisions is called the beamline simula-
 450 tion. Because the beamline simulation simulates the whole beamline, the K_L^0 momentum
 451 and position can be obtained directly.

452 In the simulation, a 30 GeV proton beam hit the gold target was simulated. The beam-
 453 line simulation simulates all the structures between the target and the 2nd collimator exit,
 454 such as the photon absorber, sweeping magnet, and two collimators. If any particles re-
 455 main at the 2nd collimator exit, the event will be recorded as an event seed. However,
 456 the beamline simulation is inefficient to generate and cannot reproduce the K_L^0 spectrum

perfectly. In the KOTO experiment, the empirical method is used to obtain the K_L^0 momentum and position distribution.

Although the beamline simulation cannot be used to obtain the K_L^0 spectrum, it is still useful to study the beam contents other than the K_L^0 particles. Figure 4.1 shows the beam content population simulated by the beamline simulation under 10^{12} POT.

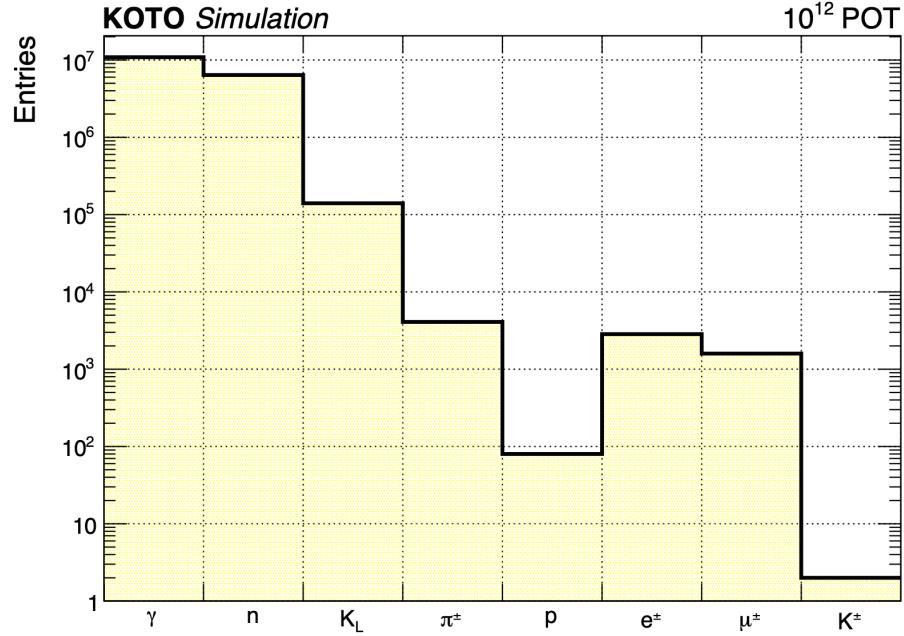


FIGURE 4.1: Beam content at the KOTO detector entrance based on the beamline simulation. Figure courtesy of [15]

In the KOTO experiment, the beamline simulation is used to study some background sources caused by the in-beam particle interaction, such as the NCC background, the halo K_L^0 background, and the Charge Kaon background.

4.4.2 Empirical K_L^0 Spectrum Simulation

The K_L^0 momentum spectrum was obtained from the measurement result of the $K_L^0 \rightarrow \pi^+ \pi^-$ and $K_L^0 \rightarrow \pi^+ \pi^- \pi^0$ decays in 2012 engineering run [21]. Figure 4.2 shows the K_L^0 momentum spectrum which is fitting by the asymmetry Gaussian function as

$$f(p) = \exp\left(-\frac{(p - \mu)^2}{2\sigma_0(1 - (A + Sp)(p - \mu))^2}\right) \quad (4.2)$$

where p is the momentum of the K_L^0 , $\mu = 1.420$ GeV/c is the mean value of the momentum, $\sigma_0 = 0.8102$ GeV/c is the width of the momentum, $A = -0.3014$ and $S = 0.01709$ (GeV/c) $^{-1}$ are the asymmetry parameters to be determined by fitting.

However, compared to the beamline simulation and empirical model, the K_L^0 particles around the beam core (halo K_L^0 particle) are not reproduced by the empirical model, as

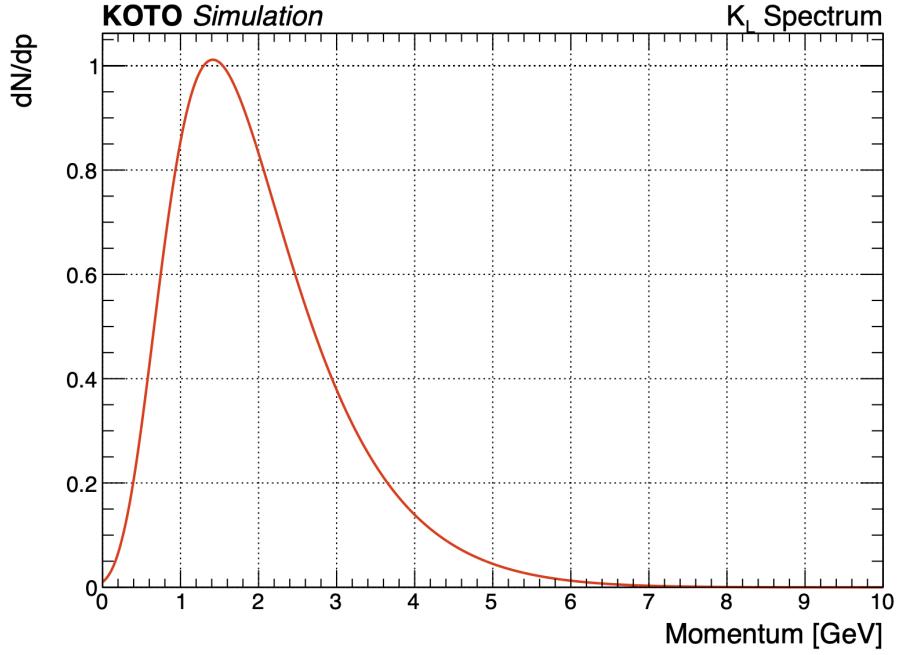


FIGURE 4.2: The K_L^0 momentum spectrum at the exit of the second collimator. Figure courtesy of [15]

474 shown in Figure 4.3. This is because the empirical model does not consider the interactions
 475 in the beamline. Therefore, the halo K_L^0 may contribute to a background source and
 476 need to be emulated by the beamline simulation.

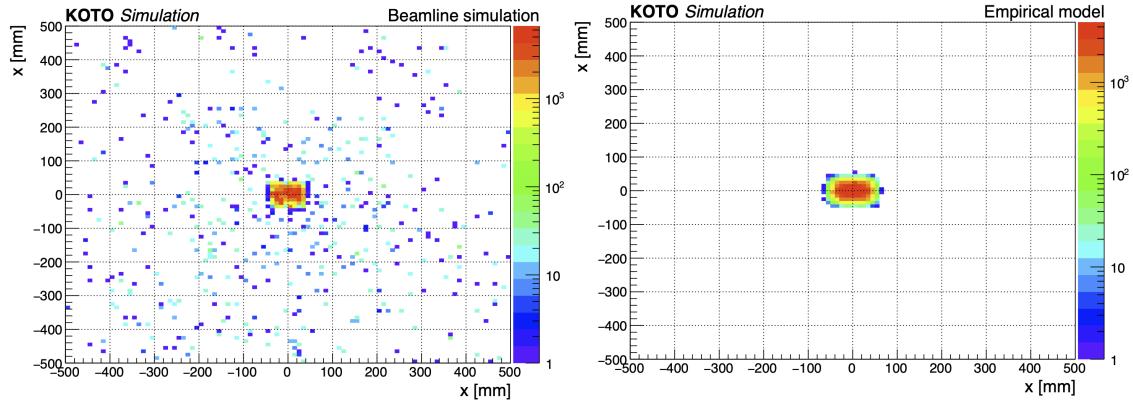


FIGURE 4.3: Comparison of K_L^0 beam profile at the exit of the second collimator between the beamline simulation and the empirical model. Figure courtesy of [15]

4.5 Fast Simulation

478 Because the KOTO experiment has a large amount of data, the Monte Carlo simulation is
 479 time-consuming. Especially for the large branching ratio K_L^0 decay channels, such as the
 480 $K_L^0 \rightarrow \pi^\pm e^\mp \nu_e$ and $K_L^0 \rightarrow 3\pi^0$ decays. It not only takes a long time to simulate the decay
 481 process but also occupies a large amount of disk space.

482 Take this study as an example, there are only 2-hour physics data with the protons
 483 on target (POT) of 5.03×10^{16} . A full MC simulation of a $K_L^0 \rightarrow 3\pi^0$ decay would take
 484 approximately 3 days to generate the same decay statistics as data. In this study, we
 485 ended up generating 12 times as many $K_L^0 \rightarrow 3\pi^0$ decays as the same amount of data.
 486 If we use the full MC simulation method, it would take around 30 days to generate the
 487 same statistics. The time consumption does not consider the priority of the batch job
 488 system, which consumes more time in real time. The branching ratio of $K_L^0 \rightarrow \pi^\pm e^\mp \nu_e$
 489 and $K_L^0 \rightarrow \pi^\pm \mu^\mp \nu_\mu$ are even larger than the $K_L^0 \rightarrow 3\pi^0$ decay. To prevent wasting the
 490 whole life being spent on the MC simulation, a fast simulation method is developed to
 491 speed up the MC simulation.

492 The fast simulation method is the same as the full simulation but breaks the generation
 493 process into three steps. In the first step, the K_L^0 and its daughter particles are generated,
 494 and stop the simulation when they hit any detectors. Record the information that we are
 495 interested in. In the second step, make a simple selection of the events to reject the events
 496 that are not interested in. Take the $K_L^0 \rightarrow 3\pi^0$ decay as an example, only the photon
 497 decay from the π^0 was considered. The photon has to hit the CsI fiducial region and the
 498 decay vertex has to be before the CsI. Retention events pass the above selection, require a
 499 minimal number of photons which depends on the study, and require the total energy of
 500 the photon to be larger than the online trigger threshold. In the third step, based on the
 501 information of the retained events, restarted the simulation and simulated the detector
 502 response.

503 The fast simulation method is much faster than the full simulation. In the $K_L^0 \rightarrow 3\pi^0$
 504 decay case, the total MC simulation is done in 10 days which is 3 times faster than the
 505 full simulation. The enhancement of the speed depends on the selection criteria, if a more
 506 strict selection is applied, the enhancement of the speed will be more significant.

507 4.6 Accidental Overlay

508 Because the MC simulation is generated one by one K_L^0 decays which is the ideal simulation
 509 To reproduce the real data situation, the accidental activities need to be considered.
 510 For example, the triggered K_L^0 decay event with another K_L^0 decay coincidently, or the
 511 particle in the beam has some interaction and produces a cluster. To reproduce the acci-
 512 dental activities, the accidental activities were overlaid on the MC simulated events. The
 513 accidental activities' information was taken from the TMON-triggered data, which could
 514 reflect the accidental rate of the real data beam.

515 When doing the accidental overlay, an accidental event is randomly selected from the
 516 library, and superimposed to each channel of the event data. Figure 4.4 shows an example
 517 of an accidental overlay on a simulated pulse for a channel in the FBAR detector.

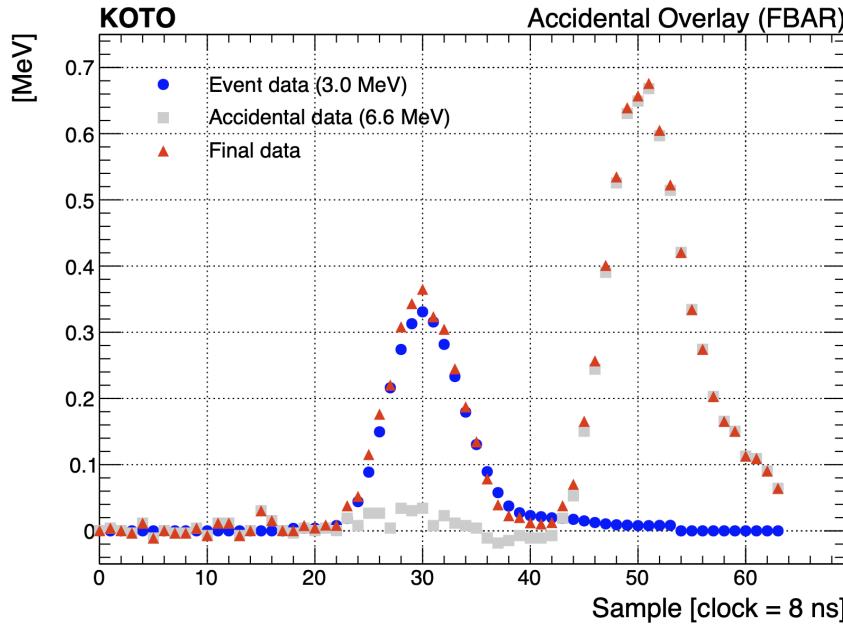


FIGURE 4.4: An example of the accidental overlay on a simulated pulse, subtracting the pedestal.
Figure courtesy of [15]

518 4.7 Neutron background Simulation

519 Neutron background is one of the serious background sources in the KOTO experiment.
 520 As shown in Figure 4.1, there is a large amount of neutron background in the beam.
 521 The mechanism is simply neutron directly interacts with the CsI calorimeter. Because
 522 the GEANT4 toolkit cannot generate a good reliable neutron interaction simulation, a
 523 data-driven method is used to estimate the neutron background. An aluminum plate
 524 target was inserted in front of the KOTO detector entrance perpendicularly to the beam
 525 direction to enhance the neutron in the beam. This target is called the "Z0-Al target" and
 526 the run with the Z0-Al target is called the "Z0-Al run". The Z0-Al run data is used to be
 527 the neutron sample in the background suppression and the estimation study.

⁵²⁸ **Chapter 5**

⁵²⁹ **K_L^0 Yield Estimation**

⁵³⁰ The yield of K_L is an important parameter for most analysis in KOTO. To normalize the
⁵³¹ Monte Carlo Simulation number of events to the real data, the yield of the $K_L z$ was
⁵³² required. The K_L yield is usually estimated by well-known neutral decay channels with
⁵³³ large branching ratios, which are $K_L^0 \rightarrow 3\pi^0$, $K_L^0 \rightarrow \pi^0\pi^0$, and $K_L^0 \rightarrow 2\gamma$. The branching
⁵³⁴ ratio of these three decays is shown in the Table 5.1. The background source of these three
⁵³⁵ channels is also limited.

TABLE 5.1: Branching ratio of K_L decays

Decay mode	Branching ratio
$K_L^0 \rightarrow 3\pi^0$	$(19.52 \pm 0.12)\%$
$K_L^0 \rightarrow \pi^0\pi^0$	$(8.64 \pm 0.06) \times 10^{-4}$
$K_L^0 \rightarrow 2\gamma$	$(5.47 \pm 0.04) \times 10^{-4}$

⁵³⁶ The ideal decay channel for the normalization study is $K_L^0 \rightarrow 2\gamma$ decay because the
⁵³⁷ diphoton final state is relatively similar to the $K_L^0 \rightarrow \gamma\bar{\gamma}$ decay. However, due to insuffi-
⁵³⁸ cient time for collecting special run data, the statistics of $K_L^0 \rightarrow \pi^0\pi^0$ and $K_L^0 \rightarrow 2\gamma$ decay
⁵³⁹ are inadequate to estimate the K_L^0 yield. The $K_L^0 \rightarrow 3\pi^0$ decay is a good place to estimate
⁵⁴⁰ the K_L yield because its branching ratio is far greater than other neutral decay channels,
⁵⁴¹ and a restrictive requirement of the signal signature. Therefore, the $K_L^0 \rightarrow 3\pi^0$ decay was
⁵⁴² accepted to estimate the K_L^0 yield and do the normalization study in this search. If we
⁵⁴³ can get more statistics from the data set, we could do On further study of this search with
⁵⁴⁴ better statistics, the normalization study could be based on $K_L^0 \rightarrow 2\gamma$ decay, and use the
⁵⁴⁵ other two decays to do the cross-check.

⁵⁴⁶ **5.1 Data Set**

⁵⁴⁷ The whole special run physics data with the normalization trigger was treated as the data
⁵⁴⁸ sample. The pre-scaling factor used to scale the number of events collected is set as 13.
⁵⁴⁹ The control sample uses the Monte Carlo simulation of $K_L^0 \rightarrow 3\pi^0$ including the acciden-
⁵⁵⁰ tal overlay. Because of the restrictive signal signature of the $K_L^0 \rightarrow 3\pi^0$, the contribution
⁵⁵¹ of other decay modes can be ignored in the normalization study.

552 In this study, $1 \times 10^9 K_L^0 \rightarrow 3\pi^0$ decays were prepared for the control sample.

553 5.2 Event Selections

554 In the K_L^0 Yield study, the event selection aims to purify the $K_L^0 \rightarrow 3\pi^0$ decay events
 555 and reject corresponding background events. The event selection consists of the veto
 556 cut and kinematic cut. The veto cut is a simple criterion of an in-time hit in the veto
 557 counter. The kinematic cut is based on the photon information and the reconstructed
 558 physics quantities of K_L^0 and π^0 . The kinematic cut could be categorized by Trigger Cut,
 559 Photon Selection, and K_L^0 Selection. A detailed explanation of the cut is shown in the
 560 following section.

561 5.2.1 Trigger Cut

562 Because the Monte Carlo simulation could not reproduce the online DAQ system. Thus,
 563 it doesn't have the same trigger condition as the real data. The trigger cut was introduced
 564 to eliminate the online trigger effect.

565 Trigger Timing Window

566 In one 64-sample window, there may maybe more than one trigger hit. If there are sep-
 567 arate events, it may cause a double counting of overlay events. To eliminate the bias
 568 from this effect, an average photon timing window of ± 15 ns of the nominal timing was
 569 required.

570 Total Energy in CsI

571 The online Total energy in CSI (CSIET) threshold is set as 500 MeV in the special physics
 572 run normalized trigger. To eliminate this online effect, a CSIET threshold offline was
 573 required higher than the online threshold. In this study, an offline $CSIET$ threshold of
 574 650 MeV was required, which is the same as the $K_L^0 \rightarrow \pi^0\nu\bar{\nu}$ study. The offline CSIET
 575 threshold is determined by examining the ET efficiency curve, as explained in Section
 576 6.3.1 of Jay's dissertation[15].

577 5.2.2 Photon Selection

578 Figure 5.1 shows the distribution of the photon selection variables for the $K_L^0 \rightarrow 3\pi^0$
 579 decay. The photon selection cuts include the photon energy, photon hit position, and
 580 minimum cluster distance. These cuts are based on the photon information and are used
 581 to select photons with good reconstruction reproducibility.

582 Photon Energy (E_γ)

583 To improve the reconstruction quality of the photon, the ultra-soft photon with energy
 584 less than 50 MeV was rejected.

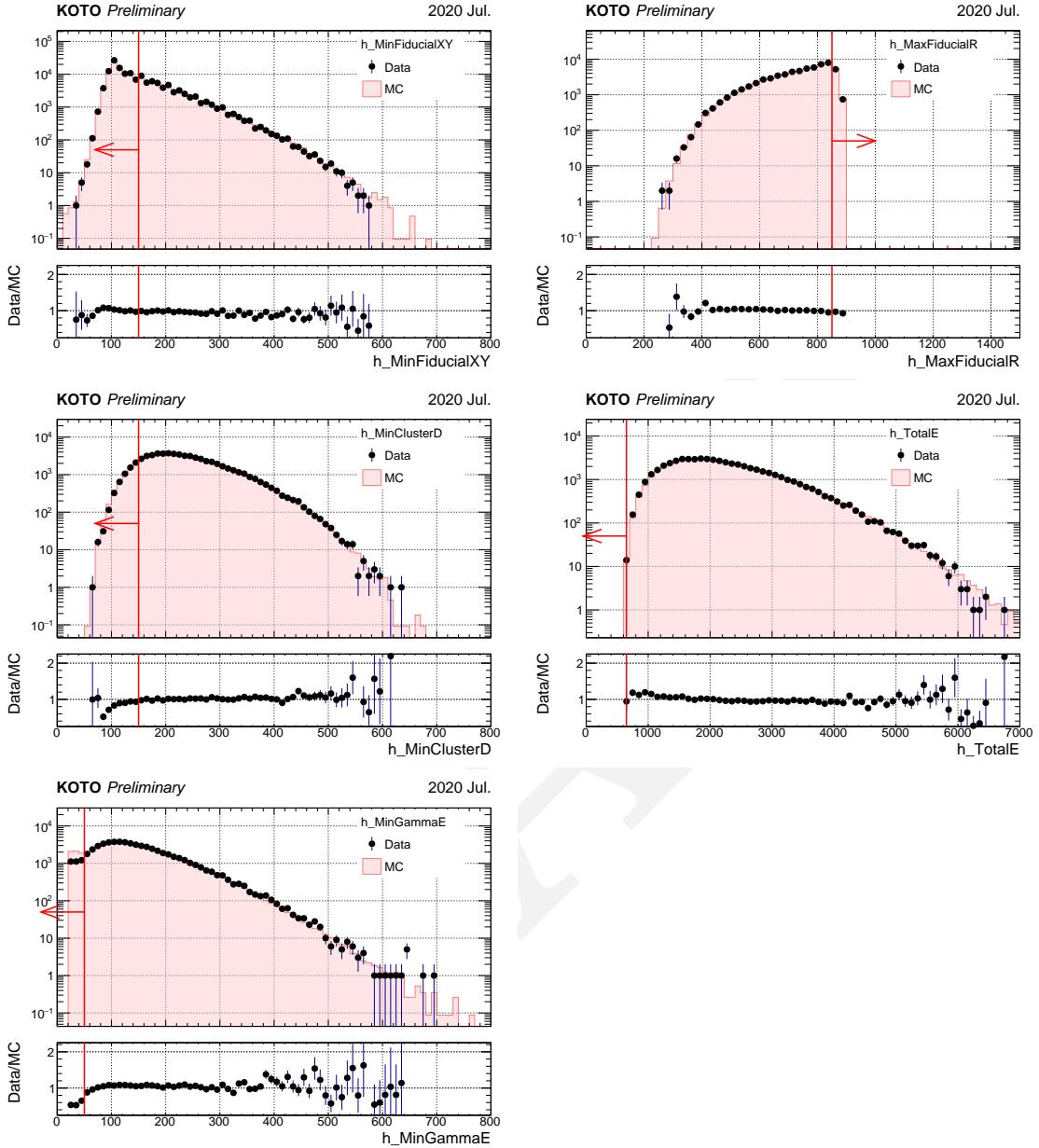


FIGURE 5.1: Distribution of the photon selection variables for the $K_L^0 \rightarrow 3\pi^0$ decay. The photon selection cuts are applied except for the variable shown in the plot. The black point shows the data, and the fill histogram shows the Monte Carlo simulation. The red arrow indicates the cut-off value of the variable.

585 Photon Hit Position (Fiducial Cut)

586 To ensure the EM shower was well contained in the CsI calorimeter, a photon hit position
 587 cut was applied. Any photon in an event that hit the outermost and innermost edge
 588 of the CsI calorimeter was rejected. This cut is also called the Fiducial Cut. The outer
 589 boundary requires the radius of the photon hit position within 850 mm, $R_\gamma < 850$ mm,
 590 while the inner boundary requires the photons 150 mm away from the square beam hold,
 591 $\min\{|x_\gamma|, |y_\gamma|\} > 150$ mm.

592 **Minimum Cluster Distance**

593 If two-photon clusters are too close to each other, the EM shower may overlap, and the
 594 energy reconstruction will be incorrect, or the two photons may be misidentified as one
 595 photon. To avoid this situation, a minimum cluster distance of 150 mm was required.

596 **5.2.3 K_L^0 Selection**

597 Figure 5.2 and 5.3 show the distribution of the K_L^0 selection variables for the $K_L^0 \rightarrow 3\pi^0$
 598 decay. The K_L^0 selection cuts include the χ^2 of the decay Z, ΔT of the vertex, K_L^0 decay
 599 vertex Z, K_L^0 mass, $K_L^0 P_T$, $\Delta\pi^0$ mass, and $K_L^0 \Delta Z_{vtx}$.

600 χ_z^2

601 To make sure the reconstructed π^0 is good quality, the χ_z^2 cut was applied. The χ_z^2 could
 602 indicate the goodness of the photon pair to the π^0 reconstructed, defined in Equation

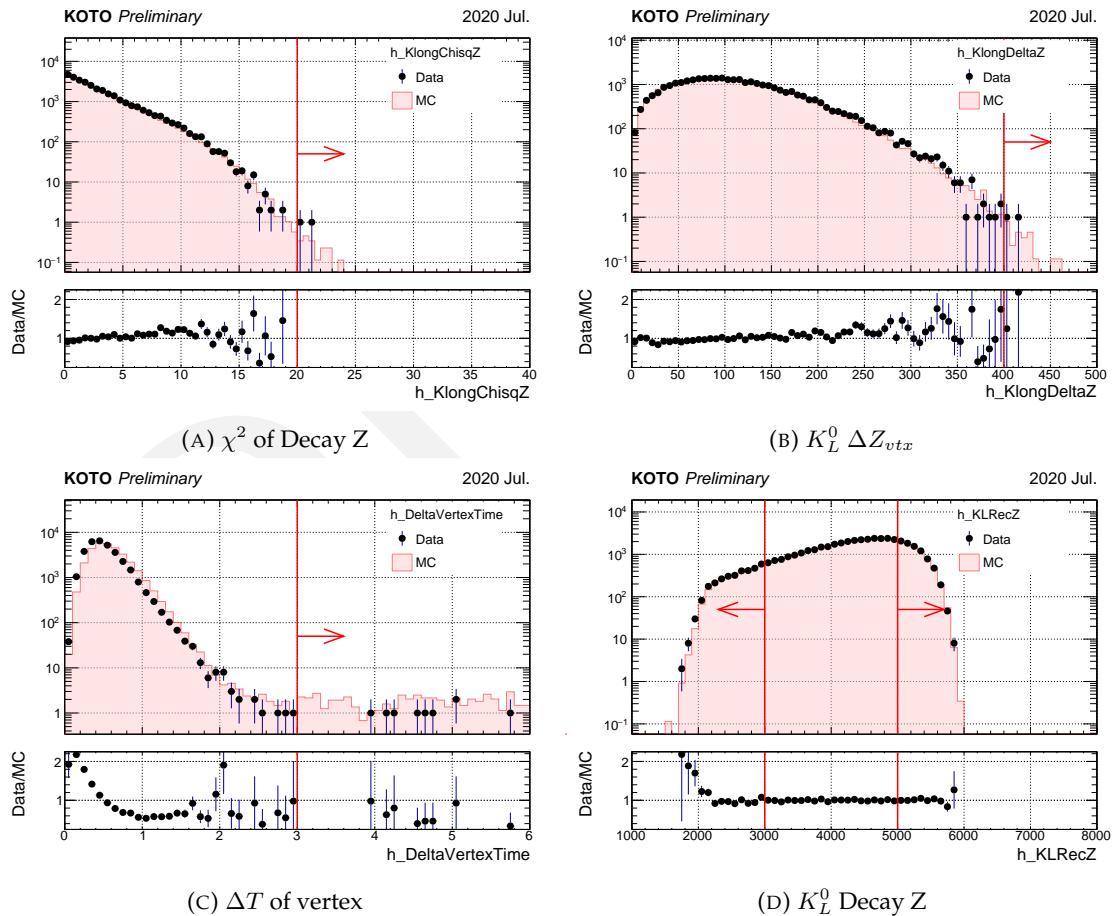


FIGURE 5.2: Distribution of the K_L^0 selection variables for the $K_L^0 \rightarrow 3\pi^0$ decay. The photon and K_L^0 selection cuts are applied except for the variable shown in the plot. The black point shows the data, and the fill histogram shows the Monte Carlo simulation. The red arrow indicates the cut-off value of the variable.

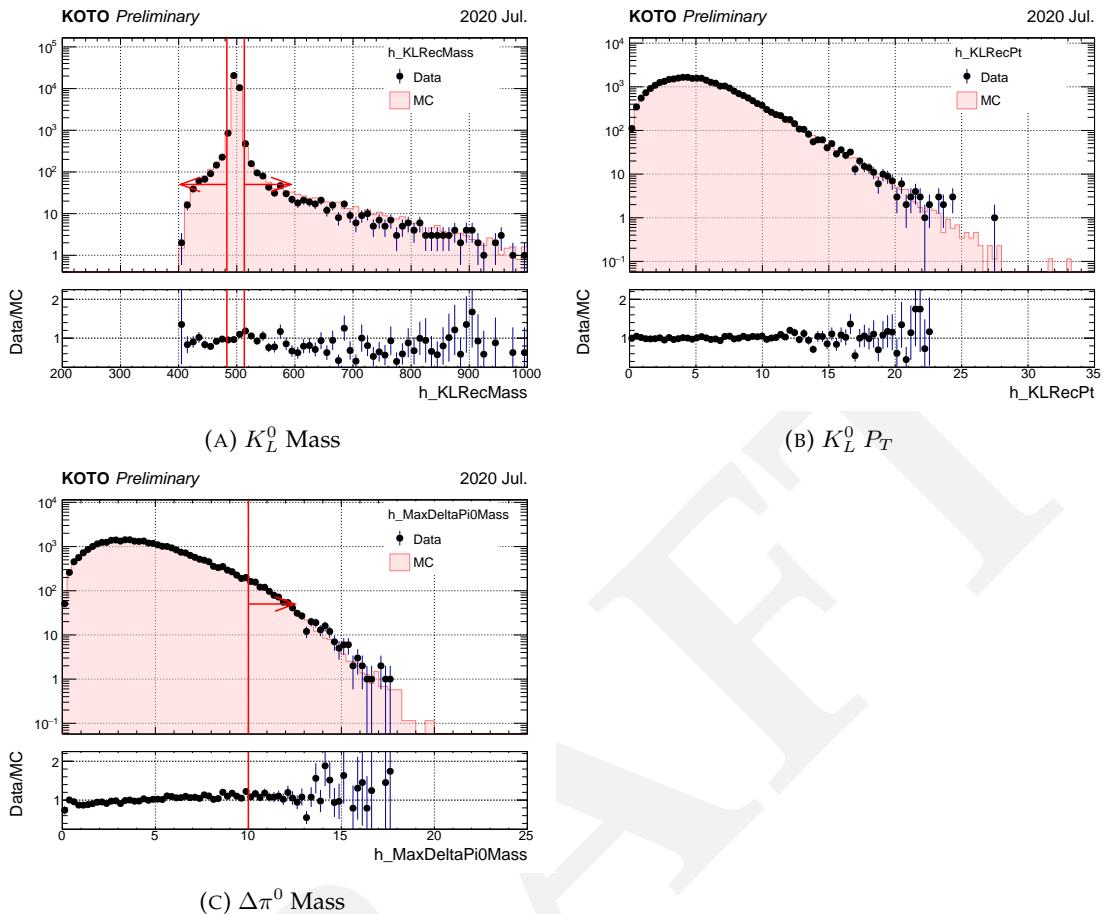


FIGURE 5.3: Distribution of the K_L^0 selection variables for the $K_L^0 \rightarrow 3\pi^0$ decay. The photon and K_L^0 selection cuts are applied except for the variable shown in the plot. The black point shows the data, and the fill histogram shows the Monte Carlo simulation. The red arrow indicates the cut-off value of the variable.

603 3.13. This cut was used to ensure the consistency of the reconstructed π^0 vertex, and the
 604 χ_z^2 was required to be less than 20.

$$605 \quad K_L^0 \Delta Z_{vtx}$$

The ΔZ_{vtx} is defined as the maximum difference between the reconstructed π^0 's, as shown in Equation 5.1. This cut is also used to ensure the consistency of the reconstructed π^0 vertexes. The ΔZ_{vtx} was required to be less than 400 mm.

$$\Delta Z_{vtx} = \max \left(|Z_{vtx}^i - Z_{vtx}^j| \right) \quad (5.1)$$

609 Maximum Difference of Vertex Timing (ΔT_{vtx})

610 The vertex timing of each photon cluster that belongs to the same event should be con-
 611 sistent with each other. The maximum vertex timing difference between reconstruction
 612 K_L^0 and each photon cluster was required to be less than 3 ns.

613 **K_L^0 Decay Vertex Z (Z_{vtx})**

614 The Decay vertex of the K_L^0 was required within the decay volume of the KOTO detector,
 615 $3000 \text{ mm} \leq Z_{vtx} \leq 5000 \text{ mm}$.

616 **K_L^0 Mass**

617 In the reconstruction of K_L , the invariant mass of photons was required to be within
 618 $\pm 15 \text{ MeV}/c^2$ of the nominal K_L mass of $497.614 \text{ MeV}/c^2$ [22]. This criterion significantly
 619 reduces event contamination from mispairing in both the $K_L \rightarrow 3\pi^0$ analyses. It also
 620 minimizes the interference of $K_L \rightarrow 3\pi^0$ decays in the analysis.

621 **$K_L^0 P_T$**

622 In the normalization study, K_L^0 should not have missing particles, so the reconstructed
 623 transverse momentum (P_T) of the K_L^0 is expected to be small. The P_T of the K_L^0 was
 624 required to be less than $50 \text{ MeV}/c$.

625 **$\Delta\pi^0$ Mass**

626 The $\Delta\pi^0$ mass is the difference between the reconstructed π^0 mass and the nominal π^0
 627 mass of $134.9766 \text{ MeV}/c^2$ [22]. The π^0 mass was calculated by the reconstructed K_L^0 de-
 628 cay vertex. A large $\Delta\pi^0$ mass indicates a bad pairing of the photon cluster, which may
 629 come from the accidental hit. The reconstructed $\Delta\pi^0$ mass was required to be within
 630 $\pm 10 \text{ MeV}/c^2$ of the nominal π^0 mass.

631 **5.2.4 Veto Cut**

632 All the veto cuts applied to the yield study are the same as the veto cuts used in the
 633 $K_L^0 \rightarrow \pi^0\nu\bar{\nu}$ analysis[15]. The summary of the veto cut is shown in Table 5.2.

634 In the following section, a detailed explanation of the Veto Cut is shown.

635 **Isolated Crystal Veto**

636 An isolated crystal hit very close in time to the photon clusters are possibly comes from
 637 the same K_L^0 decay. To reject this kind of background, a timing window of $\pm 10 \text{ ns}$ of the
 638 nearest photon cluster timing is required in this veto. A multistep cut based on the hit
 639 Energy(E) and Distance(D) from the closest cluster is applied, as the following equation:

$$\begin{cases} E > 10 \text{ [MeV]} & , \text{if } D < 200 \text{ [mm]} \\ E > 10 - \frac{7 \cdot (D - 200)}{400} \text{ [MeV]} & , \text{if } 200 \leq D \leq 600 \text{ [mm]} \\ E > 3 \text{ [MeV]} & , \text{if } D > 600 \text{ [mm]} \end{cases} \quad (5.2)$$

640 As shown in Figure 5.4, a higher energy threshold is required for the isolated crystal
 641 to hit nearer to the cluster, to bypass the shower propagation effect.

TABLE 5.2: Summary of the veto cut

Veto Counter	Energy Threshold	Timing Window
FB	1 MeV	51ns
NCC and HINEMOS	1 MeV	40ns
MB	1 MeV	20ns
IB	1 MeV	20ns
MBCV	0.5 MeV	60ns
IBCV	0.5 MeV	60ns
CV	0.2 MeV	20ns
LCV	0.6 MeV	30ns
CSI (isolated crystal)	see Sec. 5.2.4	20ns
CSI (extra cluster)	see Sec. 5.2.4	20ns
OEV	1 MeV	20ns
CC03	3 MeV	30ns
CC04, CC05, CC06 (CSI crystal)	3 MeV	30ns
CC04, CC05, CC06 (plastic scintillator)	1 MeV	30ns
BPCV	1 MeV	24ns
BHCV ¹	221 eV	25ns
BHPV ²	2.5 p.e.	15ns
BHGC ³	2.5 p.e.	15ns

¹ BHCV requires hits in more than two modules.

² BHPV requires hits in more than three consecutive modules.

³ BHGC veto accepts the number of equivalent photons instead of energy.

642 Extra Cluster Veto

643 A cluster hit in the CsI calorimeter that is not associated with the $\pi^0 \rightarrow \gamma\gamma$ decay is considered
 644 an extra cluster. If the timing of the extra cluster is within ± 10 ns of the reconstructed π^0
 645 vertex time, it is considered as a background and rejected.

646 5.3 Yield Estimation

647 The Yield of the K_L^0 (Y) in the data set is defined by the following equation:

$$Y = \frac{N_{mode}}{\mathcal{BR}_{mode} \times A_{mode}} \quad (5.3)$$

648 where N_{mode} is the number of events, \mathcal{BR}_{mode} is the branching ratio, and A_{mode} is the
 649 acceptance. The mode could be any decay channel of the K_L^0 . The acceptance(A_{mode}) can
 650 be evaluated by the Monte Carlo simulation, as the following equation:

$$A_{mode} = \frac{N_{remaind}}{N_{gen}} \quad (5.4)$$

651 where $N_{remaind}$ is the number of events that pass the event selection, and N_{gen} is the
 652 number of generated K_L^0 decays. And because the K_L^0 yield is proportional to the number
 653 of protons on target (POT), the K_L^0 flux (F) can be defined as the yield per POT, as shown

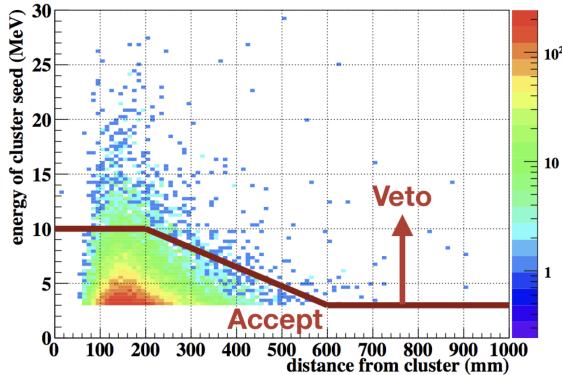


FIGURE 5.4: Distribution of isolated crystal hit energy(E) vs. its distance(D) from the nearest cluster. The red line shows the cut based on Equation 5.2. The sample was obtained from the $K_L^0 \rightarrow \pi^0 \nu \bar{\nu}$ Monte Carlo simulation.[23]

654 in the following equation:

$$F = \frac{Y}{\text{POT}} \quad (5.5)$$

655 As mentioned in Section 5.1, the normalization trigger was used to be the data sample.
 656 Because the normalization trigger was taken simultaneously with the physics trigger, the
 657 K_L^0 yield is the same as the physics trigger. Therefore, the K_L^0 yield evaluated by the
 658 normalization trigger can be used directly in the physics analysis.

659 In this study, the K_L^0 yield was estimated by the $K_L^0 \rightarrow 3\pi^0$ decay. All the kinematic
 660 cuts introduced in Section ?? and the veto cuts summarized in Table 5.2 were imposed.

661 5.3.1 Estimation by $K_L^0 \rightarrow 3\pi^0$ Decays

662 Figure 5.6 and 5.7 show the distribution of the kinematic variables for the $K_L^0 \rightarrow 3\pi^0$
 663 decay after imposed all selection cuts referred in Section 5.2. The purity of the $K_L^0 \rightarrow 3\pi^0$
 664 decay is high because there is no other K_L^0 decay mode that can mimic the six-cluster
 665 signature on CSI. The most discrepancy comes from the statistics of the special physics
 666 data is not enough to match the Monte Carlo simulation.

667 Figure 5.5 shows the beam shape of x and y projection at the exit of the second colli-
 668 mator. The beam core shows a good agreement between the data and the Monte Carlo
 669 simulation.

670 5.4 Summary of K_L^0 Yield Estimation

671 The K_L^0 yield of the special physics run was estimated to be 1.29×10^{10} by the $K_L^0 \rightarrow 3\pi^0$
 672 decay as shown in Figure ???. The systematic uncertainty will be considered in the Single
 673 Event Sensitivity (SES) study in Section 6.5.1.

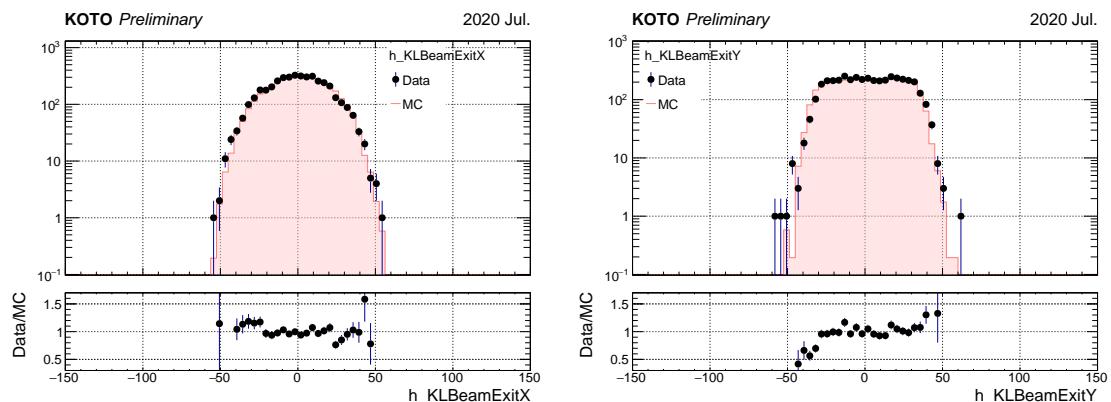


FIGURE 5.5: Beam profile at the exit of the second collimator via the $K_L^0 \rightarrow 3\pi^0$ decay analysis. All the selection cuts are imposed. Filled histograms are predicted by the Monte Carlo simulation.

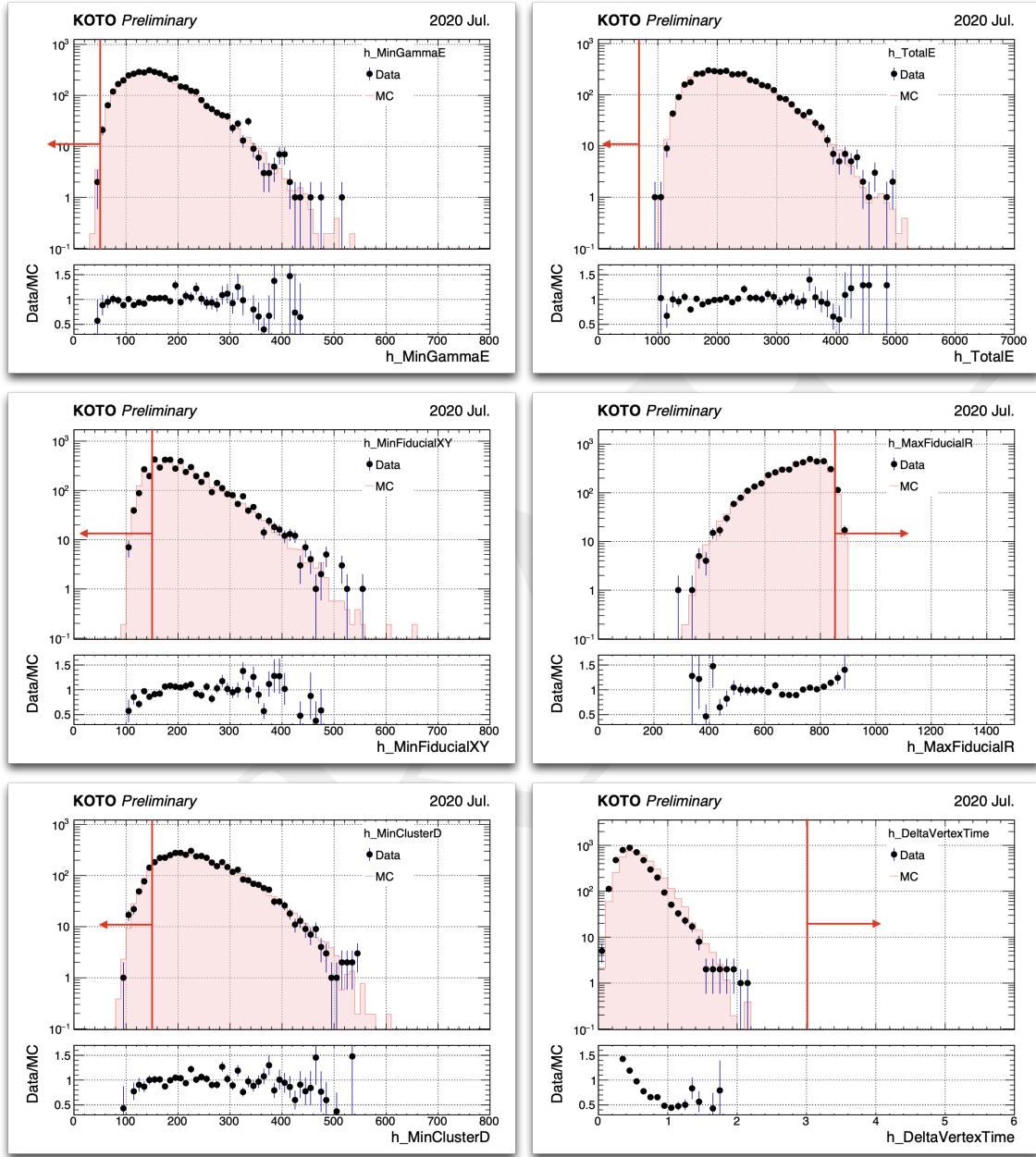


FIGURE 5.6: Distribution of the kinematic variables for the $K_L^0 \rightarrow 3\pi^0$ decay. All the selections are applied except the variable shown in the plot. The black point shows the data, and the fill histogram shows the Monte Carlo simulation. The red arrow indicates the cut-off value of the variable.

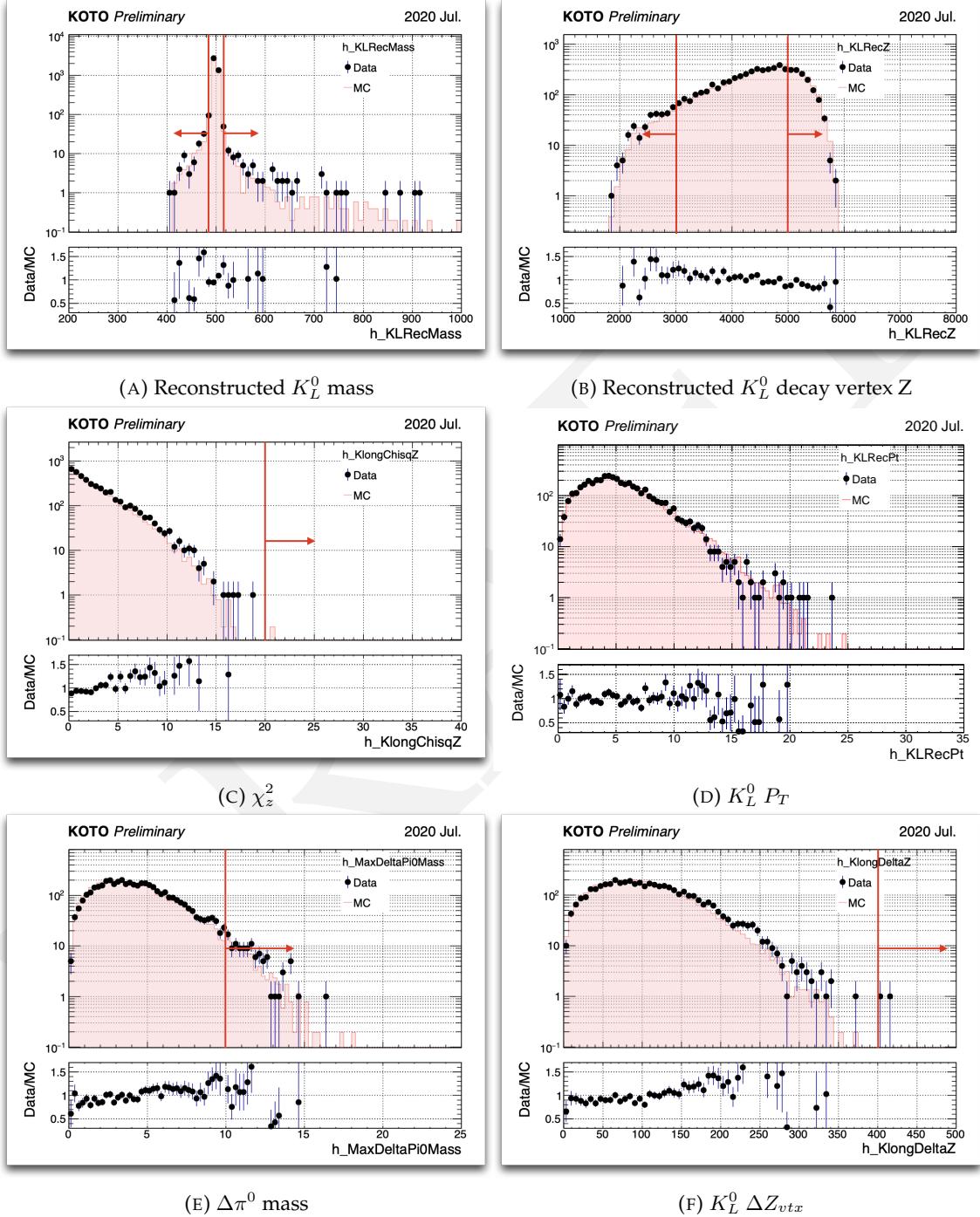


FIGURE 5.7: Distribution of the kinematic variables for the $K_L^0 \rightarrow 3\pi^0$ decay. All the selections are applied except the variable shown in the plot. The black point shows the data, and the fill histogram shows the Monte Carlo simulation. The red arrow indicates the cut-off value of the variable.

⁶⁷⁴ **Chapter 6**

⁶⁷⁵ **Analysis of $K_L \rightarrow \gamma\bar{\gamma}$**

⁶⁷⁶ The goal of the $K_L^0 \rightarrow \gamma\bar{\gamma}$ analysis is to estimate the branching ratio (\mathcal{BR}) of this decay,
⁶⁷⁷ we took a 2-hour special run with a single cluster trigger in 2020. The distinctive signal
⁶⁷⁸ signature of $K_L^0 \rightarrow \gamma\bar{\gamma}$ manifests as a singular photon hit on the CsI calorimeter, devoid
⁶⁷⁹ of any in-time hits on other detectors.

⁶⁸⁰ Employing a blind analysis method, we define a specific region, characterized by en-
⁶⁸¹ ergy deposition $800 \text{ MeV} < E_\gamma < 3000 \text{ MeV}$ and a spatial constraint of $300 \text{ mm} < H_{XY}$
⁶⁸² $< 850 \text{ mm}$, where H_{XY} denotes the maximum distance between the hit location and the
⁶⁸³ center of the CsI crystal along the x and y axes. The signal region has to be within the
⁶⁸⁴ blind region and has been optimized.

⁶⁸⁵ Our principal objective revolves around suppressing background noise and accentu-
⁶⁸⁶ ating signal events through event selection. Subsequently, we estimate the residual back-
⁶⁸⁷ ground events within the signal region post-selection. Under the assumption of negli-
⁶⁸⁸ gible background noise, we calculate the Single Event Sensitivity (SES) to estimate the
⁶⁸⁹ branching ratio upon observing signal events within the defined signal region. The SES,
⁶⁹⁰ representing the reciprocal of the product of the total K_L^0 yield and the acceptance of
⁶⁹¹ signal decays, is expressed mathematically as:

$$\text{SES} = \frac{1}{Y \times A_{sig}} \quad (6.1)$$

⁶⁹² Here, Y represents the K_L^0 yield, and A_{sig} signifies the signal acceptance. The branching
⁶⁹³ ratio (\mathcal{BR}) is then inferred from SES and the observed number of signal events (N_{sig})
⁶⁹⁴ within the signal region, as articulated by:

$$\mathcal{BR} = \text{SES} \times N_{sig} \quad (6.2)$$

⁶⁹⁵ However, when background contributions cannot be negligible, a statistical methodol-
⁶⁹⁶ ogy becomes imperative to ascertain the upper and lower bounds of signal event counts.
⁶⁹⁷ The background level (N_{bg}) is estimated through two approaches in this study. For K_L
⁶⁹⁸ decay backgrounds, Monte Carlo simulations are employed to evaluate N_{bg} , defined by:

$$N_{bg} = Y \times \mathcal{BR}_{bg} \times A_{bg} \quad (6.3)$$

699 Where \mathcal{BR}_{bg} represents the branching ratio of specific background decays (e.g., $K_L \rightarrow$
700 2γ), and A_{bg} denotes the acceptance corresponding to this background decay. For neu-
701 tron backgrounds, a dedicated neutron data run is utilized, employing a data-driven
702 approach for background-level evaluation through normalization against the neutron-
703 dominant region between physics data and neutron data sample. Upon combining all
704 background sources, a prediction of the background level within the signal region is de-
705 termined. After an examination of reliability through the side-band region, uncover the
706 blind region.

707 This chapter unfolds with a presentation of the event selection criteria, followed by
708 a discussion on background suppression methodologies. Subsequently, the reliability
709 of our analysis is assessed through a comparison between physics data and simulation
710 results in the side-band region. The computation of background levels and SES is then
711 detailed. With the final estimation in hand, we will proceed to open the box and the
712 interpretation of the statistical result will be presented at the latest.

713 6.1 Data Set

714 As mention in the above section, for this analysis a special 2-hour run was taken in June
715 2020 (RUN85). In this special run, a single cluster trigger was adopt as the physics data,
716 the energy threshold was set at 300 MeV with online veto and a pre-scale factor in 1. To
717 normalize this run, a normalization trigger also accept, this trigger does not contain the
718 cluster number trigger, and only adopt CV as the online veto, with a pre-scale factor in
719 13. The POT of the 2-hour special is around 5.03×10^{-6} with the total 1.29×10^{10} number
720 of K_L^0 enter KOTO detector, as shown in Chapter 5.

721 For the neutron background study, neutron sample run was taken. As Section 4.7
722 mention, the GEANT4 MC toolkits cannot simulation the neutron interaction correctly,
723 the data driven method was adopted to do the neutron background study. Ideally, for the
724 single cluster study a single cluster trigger neutron should be used in the study. Follow
725 this thought, a special single cluster Z0-Al run was taken in RUN85. However, after
726 the further study we notice that the single cluster Z0-Al run cannot stand the neutron
727 sample. Because we don't have a good method to purify the neutron event from the Z0
728 data. Therefore, as a compromise, we use the 2-cluster trigger Z0 run in RUN85 which
729 is taken for the $K_L^0 \rightarrow \pi^0\nu\bar{\nu}$ decay study. The mechanism of the 2-clster neutron event is
730 that a neutron hits the CsI calorimeter and generates a new hadron through the hadronic
731 interactions. Because there are two clusters on the CsI, the reconstruction was possible.
732 Consequently, use the kinematic variable to select the neutron event, then a pure neutron
733 sample data set was obtain. For the single cluster study, only the cluster with higher
734 energy was selected because the primary neutron usually has a higher energy than the
735 second one.

Because the neutron flux is unable to obtain, the background was normalized by the number of event in the neutron dominated region in the neutron study. In this study, we adopt all Z0 data in RUN85, and the scale factor obtain by the normalization was around 1.6. This means the statistic of neutron sample is far away to compare with physics data, it will behave on the statistic uncertainty.

6.2 Basic Strategy of the Single Cluster Study

6.2.1 Signal Identification

$K_L^0 \rightarrow \gamma\bar{\gamma}$ decay requires only one photon cluster to hit the CsI calorimeter and without any in-time hit in the rest of the detector. A single cluster can only provide the energy and position information. The lack of kinematic constraints will be the challenge of this study. Moreover, single cluster signatures are easily mimicked by some unknown arbitrary background. Requiring a high photon energy may help to suppress this kind of background but also reduce the signal efficiency.

6.2.2 Major Background Sources

The major background sources are K_L^0 decay background and neutron-like background.

K_L^0 decay background

Table 6.1 shows the main K_L^0 decay backgrounds. Other decay channels are unnecessary to be considered because of the low branching ratio. Only $K_L^0 \rightarrow \pi^\pm e^\mp \nu_e$ and $K_L^0 \rightarrow \pi^\pm \mu^\mp \nu_\mu$ are considered for the decay channel of charged particles in the final state, due to the high branching ratio. To suppress the K_L^0 decay background, studying these decay channels and understanding their characteristics are important. All of these decay channels produce more than one photon in the final state. Therefore, it is easy to suppress these decay channels with the KOTO detector. Except for the decay of $K_L^0 \rightarrow 2\gamma$, whose final state is similar to the signal signature and may be a potentially non-eliminable source of background.

TABLE 6.1: Main K_L^0 decay background modes and their branching ratios.

Decay mode	Branching Ratio
$K_L \rightarrow \pi^\pm e^\mp \nu_e$	$(40.55 \pm 0.11)\%$
$K_L \rightarrow \pi^\pm \mu^\mp \nu_\mu$	$(27.04 \pm 0.07)\%$
$K_L \rightarrow 3\pi^0$	$(19.52 \pm 0.12)\%$
$K_L \rightarrow \pi^+ \pi^- \pi^0$	$(12.54 \pm 0.05)\%$
$K_L \rightarrow 2\pi^0$	$(8.64 \pm 0.06) \times 10^{-4}$
$K_L \rightarrow 2\gamma$	$(5.47 \pm 0.04) \times 10^{-4}$

761 **Neutron-like background**

762 The neutron originating from the beamline poses a significant background challenge.
 763 Accurately simulating the in-beam neutron background is nearly impossible, especially
 764 without a defined mechanism to avoid it. The primary method to mitigate this back-
 765 ground involves distinguishing the cluster from the photon event.

766 **6.3 Single Cluster Event Selection**

767 The event selection included trigger cuts, kinematic cuts, and veto cuts. The trigger cuts
 768 were designed to mimic the online trigger effect, while the kinematic cuts and veto cuts
 769 were implemented to suppress background noise. The kinematic cuts were based on the
 770 reconstruction quantities of the photon cluster, while the veto cuts were just the criteria
 771 of hit on the veto counters. In the single cluster study, the signal significance of $K_L \rightarrow \gamma\bar{\gamma}$
 772 is only one photon cluster hit on the CsI calorimeter. And other vetoes keep silent in
 773 time. Which means a very loose condition for hitting events. It is also a challenge for this
 774 study.

775 **6.3.1 Trigger Selection**

776 The online trigger effect is the source of the difference between the collected data and the
 777 Monte Carlo simulation. To mimic the online trigger effect and ensure the consistency of
 778 the data and MC simulation, two trigger selections were implemented: the trigger timing
 779 cut and the total energy cut.

780 • **Timing window**

781 The online trigger will reject all events with any on-time veto hit, thus a trigger
 782 timing window as shown in Figure 6.1 is required to eliminate the online trigger
 783 effect. In the real data taking, due to the 8-ns clock dead time, the real physics data
 784 timing distribution will be wider than the Monte Carlo simulation. A wide enough
 785 timing window is selected to cover the distribution inconsistency between the data
 and the MC simulation.

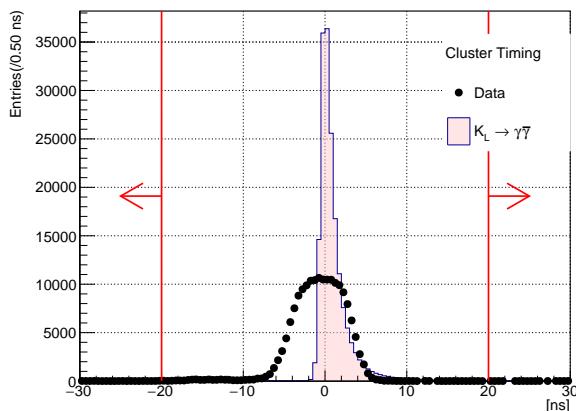


FIGURE 6.1: Distribution of cluster timing after relative timing correction. The dot is from real physics data, and the filled histogram is the MC simulation. The red arrow is the cut-off region.

786 • **Total Energy**

787 The offline energy cut should be larger than the online ET threshold to eliminate the
 788 online ET trigger effect. The online ET threshold of 300 MeV was required in the
 789 special run. Thus, the offline energy cut is set as 500 MeV. As shown in the Figure
 6.2, the signal acceptance is 91.0%

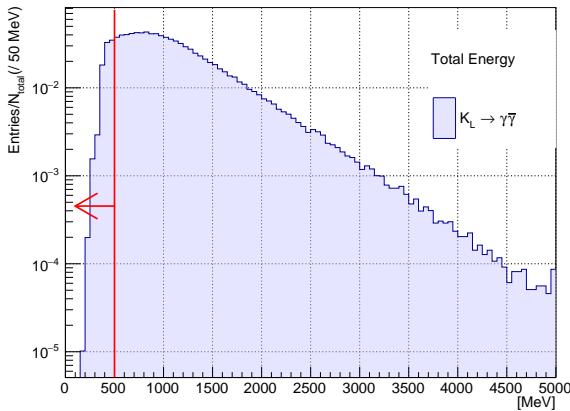


FIGURE 6.2: Distribution of total energy from Monte Carlo simulation. The histogram area is normalized to 1. The red line is the cut-off region.

790

791 **6.3.2 Kinematic Cuts**

792 The $K_L \rightarrow \gamma\bar{\gamma}$ decays require only one photon cluster on the CsI calorimeter. Therefore,
 793 the reconstruction of the mother particle is not possible, and also some variables based
 794 on multiple photon clusters will be absent, such as the vertex position, cluster distance,
 795 and KL kinematic quantities. As kinematic constraints are lacking, kinematic selection is
 796 determined by only two variables: the photon hit position and photon energy.

797 • **Innermost and Outermost Photon Hit Position**

798 To prevent the edge of the calorimeter from affecting cluster reconstruction, any
 799 event that hits the boundary will be removed. Based on the geometry of the calorimeter,
 800 the outer boundary is evaluated using radius of hit position, R_γ , while the inner
 801 boundary is evaluated using the maximum of the absolute values of x and y of the
 802 photon hit position, $\max\{|x_\gamma|, |y_\gamma|\}$. The inner boundary is set as a 300×300 mm²
 803 box, while the outer boundary is a circle with a radius of 850 mm, as shown in
 804 Figure 6.3.

805 • **Photon energy**

806 Because of the 1 cluster study, the photon energy is almost equivalent to the total
 807 energy. Therefore, simply required photon energy to be larger than 500 MeV, which
 808 is the same as the total energy cut.

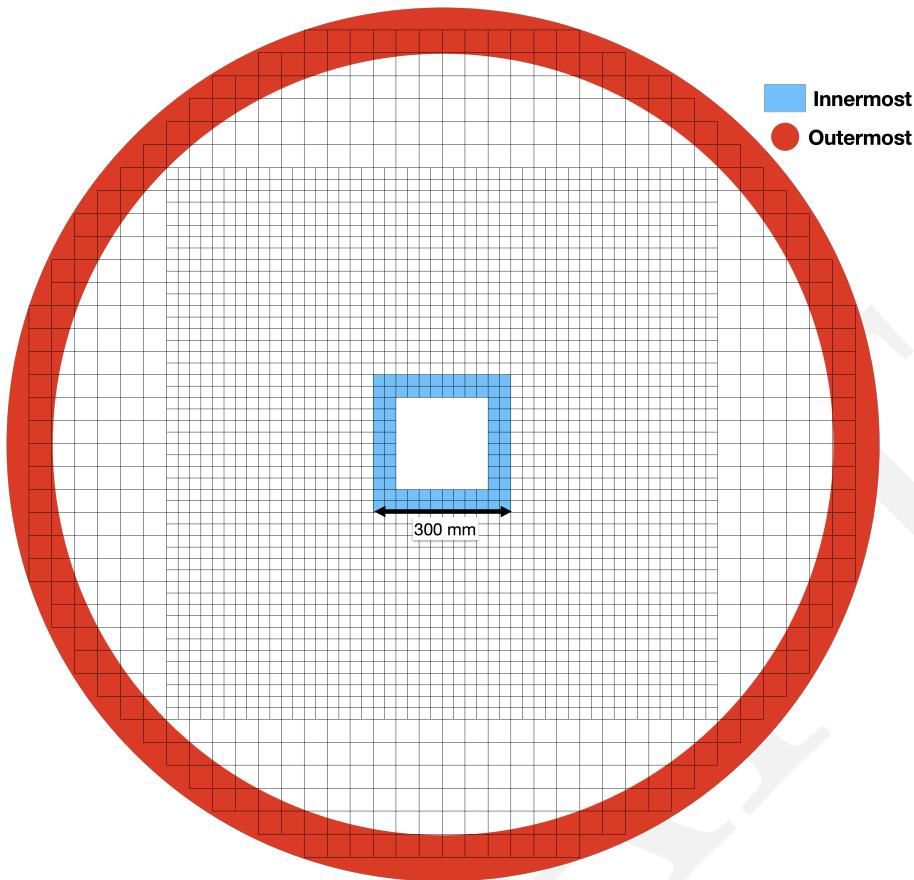


FIGURE 6.3: An upstream view of the CsI calorimeter. The red region is the outermost boundary, while the blue region is the innermost boundary.

6.3.3 Veto Cuts

Veto counters are the primary tool for Kaon decay background suppression in the KOTO experiment. The veto hits within the veto timing window and above the veto energy threshold will be tagged as an in-time veto hit. The event with any in-time veto hits will be treated as a background event and rejected. To determine a veto cut, the veto timing window and the energy threshold was required. The energy threshold was simply selected over than the online veto and within the precision of the veto counter. The veto timing for veto hits is defined as talk in the Section 3.4. To determine the reject window of the veto timing a timing study of each veto counter is required. First, the nominal timing should be determined, the hit close to the nominal timing should be considered as a background hit. Then determined the exact reject window of this veto, because the hit could produce by the accidental hit not from the K_L^0 decay source. The window decision should consider the signal loss from the accidental hits.

In some veto counter, the source of the veto hit is dominated by the K_L^0 decay, thus the timing distribution will behave a symmetry, as shown in the Figure 6.4. For this type of veto counters, the timing window decision is simply select a \pm few ns to the peak position, the window width depends on the shape of the distribution. In the following

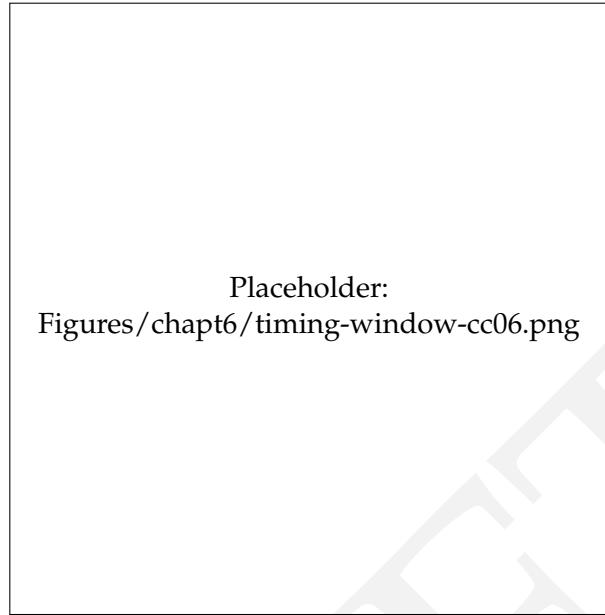


FIGURE 6.4: Distribution of veto timing window of CC06

826 veto cuts study, the determined of the veto timing window will be discussed.

827 However, in some veto counter especially for which surrounding the decay volume,
 828 the accidental hits are mixed with the background hit. In the following subsection, the
 829 veto study for these veto counter will be discussed.

830 **FBAR and NCC**

831 The veto timing is defined by the Equation 3.26 The FBAR and NCC is placed on the
 832 upstream of the decay volume, the distribution of timing shown in Figure 6.5. The mech-
 833 anisms of the hits can be categorized to these three types.

834 • **Upstream decays**

835 If a K_L^0 decay inside the FBAR chamber, the photon product can hit on the FBAR
 836 or NCC, and the timing accumulated is the nominal time. In the Figure 6.5, is the
 837 event in decay vertex Z less than 2719 mm region. For NCC the veto timing in
 838 this region does not have a large variant which is because the K_L^0 decay before the
 839 NCC and the $(\Delta z - D)$ in Equation 3.26 is almost a constant and equivalent to the
 840 distance between NCC and CsI, regardless the decay position. However, because
 841 the K_L^0 decay inside the FBAR, and it has a large volume, the $(\Delta z - D)$ will
 842 variant in a large range depends on the decay position.

843 In the Figure 6.5, the veto timing of FBAR is break into two peak around the nom-
 844 inal time, which is because the NCC cover a part of FBAR detector. In the Figure
 845 6.5a can show the agreement.

846 • **Backward hit**

847 When a K_L^0 decay in the decay volume, the photon could fly backward and hit the

NCC and FBAR. Base on the Equation 3.26, the $(\Delta z - D)/c$ term will be a variant and the veto timing will depend on the decay vertex. However, the variate of this term is controllable,

$$\Delta z - D \approx \Delta z - (L - \Delta z) = 2\Delta z - L \quad (6.4)$$

$$T_{veto}(\Delta z) \approx \frac{2}{c}\Delta z + T_{mod} - T_{CsI} - L/c \quad (6.5)$$

where L represent the distance between veto and CsI. Equation 3.26 could be seen as a function to Δz with a slope $2/c$. Which explained the slope of the backward hit distribution in Figure 6.5a and 6.5b

- **CsI backsplash**

As shown in Figure 6.5a and 6.5b, a set of event with a veto timing independent of the decay vertex z . This phenomenon called "backsplash" which is because the calorimeter did not consume all the EM shower but splash toward upstream. Because the distance of the trajectory is a constant, the veto timing will also be a constant.

Based on these three mechanisms, clearly only the CsI backsplash is the fake signal and other two is the backgrounds. Therefore, the veto timing window for NCC and FBAR is excluded the backsplash peak, as shown in Figure ?? and ??.

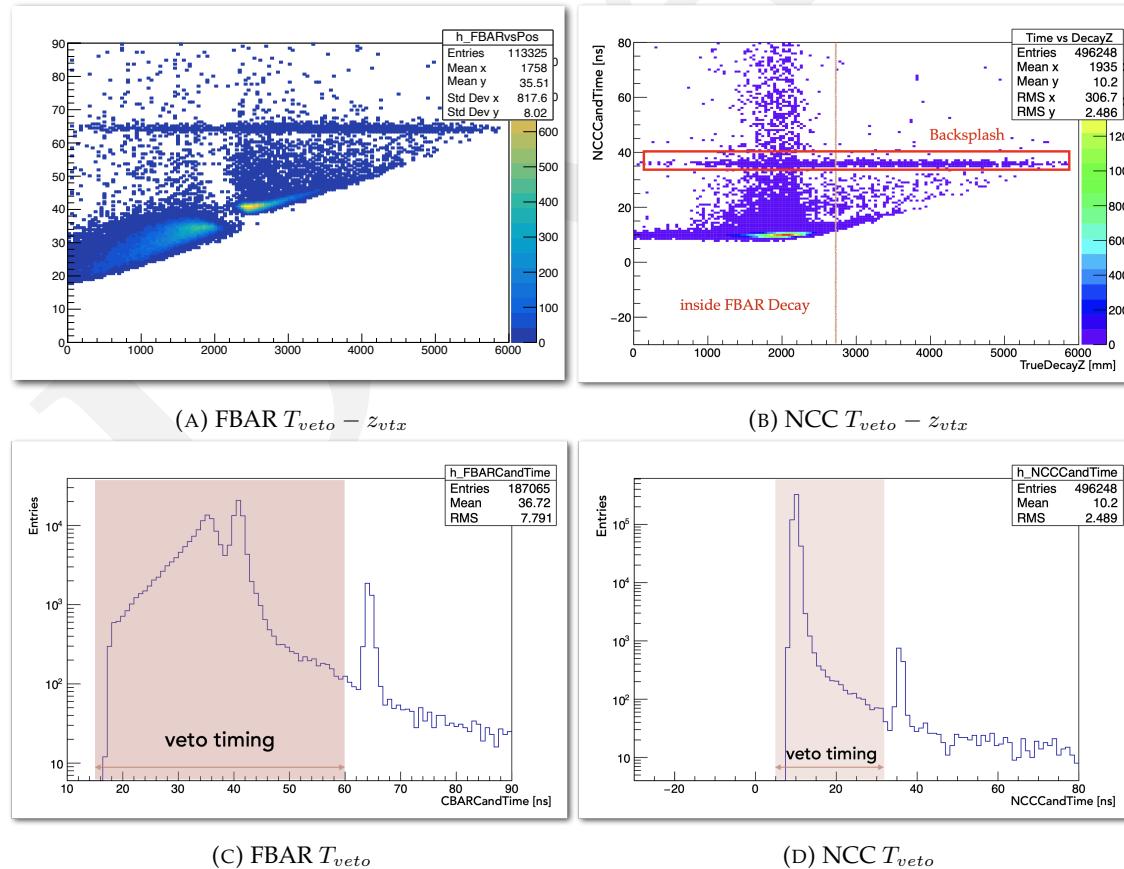


FIGURE 6.5: Temporary plots of FBAR and NCC

6.4 Background Suppression

There are two main category background sources in this analysis: K_L decay events and Hadronic cluster. Besides these two main background sources, we will also discuss the other background sources that we study in this analysis, such as Charge Kaon decays, NCC background, and Halo Kaon backgrounds. In the following section, we will talk about the background suppression strategy for each category.

6.4.1 K_L Decay Background

In this analysis, we have studied the major three K_L^0 neutral decay channels, like $K_L^0 \rightarrow 3\pi^0$, $K_L^0 \rightarrow \pi^0\pi^0$, and $K_L^0 \rightarrow 2\gamma$. And also the K_{e3}^0 , $K_{\mu 3}^0$, and $K_L^0 \rightarrow \pi^+\pi^-\pi^0$, which is the charge decay channel with a large branching ratio.

There are 3 kinds of possible mechanisms from K_L^0 decays were found:

- **Missing photon**

One photon hits the CsI, but other particles hit the dead material of the KOTO detector or missing in the beam hole.

- **Upstream decay**

K_L^0 decay upstream of the FBAR, one photon hits the CsI, and the other photon missing outside the detector.

- **Fusion cluster**

The decay position along the Z-axis (Z_{tx}) is too close to the CsI, all decay products hit the nearby crystal and are noted as a single cluster by the clustering process. As shown in Figure 6.8

In this section, all the studied K_L^0 backgrounds will be discussed. All the Monte Carlo simulations were applied the accidental overlay.

$K_L^0 \rightarrow 2\gamma$ Background

Because of the extreme hermetic of the KOTO detector, the possibility of missing multiple particles is very low. And with our powerful charge veto counter, it is also very difficult to miss a charged particle. Therefore, $K_L^0 \rightarrow 2\gamma$ decay with one missing photon will be the primary K_L^0 decay background in this study.

$K_L^0 \rightarrow 2\gamma$ background consists of two mechanisms, missing photon and upstream decay. $K_L^0 \rightarrow 2\gamma$ has very similar signature with the $K_L^0 \rightarrow \gamma\bar{\gamma}$, the only difference is another photon is visible. This means if the other photon of $K_L^0 \rightarrow 2\gamma$ is missing detecting, this event will be an ineliminable background in this study. The upstream decay mechanism is also having a missing photon. But its decay position is upstream of the FBAR, which highly constrains the hit radius (R_{XY}) of the cluster. Based on the geometry calculation

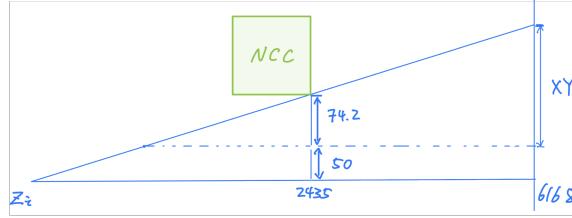


FIGURE 6.6: The schematic geometry diagram of the mechanism of the upstream decay background.

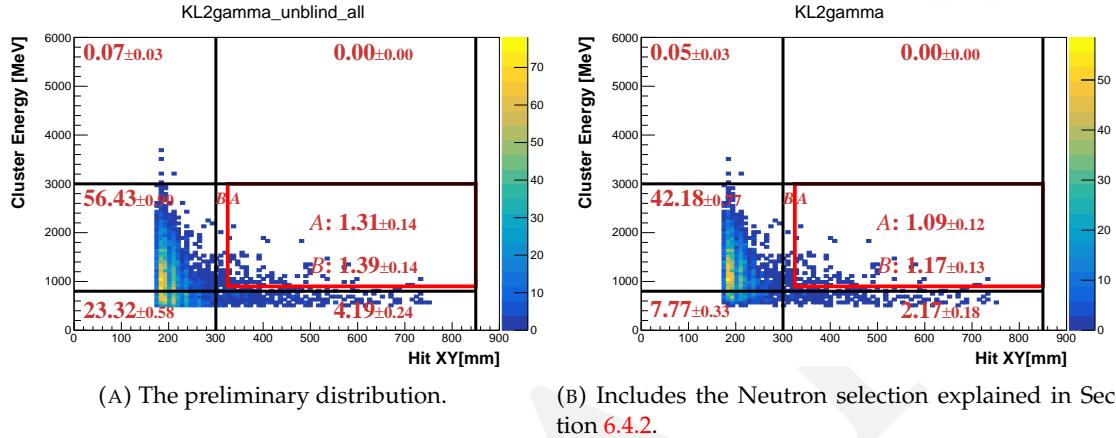


FIGURE 6.7: $E_\gamma - R_{XY}$ distributions of scattered $K_L^0 \rightarrow 2\gamma$ decays with various cut. The red frame indicates the signal region. The red number indicates the background level in each region.

as shown in Figure 6.6, the maximum R_{XY} of the cluster of upstream decay is 265 mm, which is outside the signal region.

Figure 6.7 shows the result of K_L^0 selection. A background level of 1.09 ± 0.12 is estimated in the signal region.

Other K_L^0 decay Backgrounds

Besides the $K_L^0 \rightarrow 2\gamma$ background, the other K_L^0 decay backgrounds are also studied in this analysis. Such as $K_L^0 \rightarrow 3\pi^0$, $K_L^0 \rightarrow \pi^0\pi^0$, K_{e3}^0 , $K_{\mu 3}^0$ and $K_L^0 \rightarrow \pi^+\pi^-\pi^0$. After the event selection explained in Section 6.3 and 6.4.2, the event inside the signal region of all decays except $K_L^0 \rightarrow 2\gamma$ is all rejected. All the three mechanisms mentioned above existed in these decays. The missing photon is also an ineliminable background, but because the decay products are much more than the $K_L^0 \rightarrow 2\gamma$, the missing photon background is negligible. And the upstream decay background has the same geometry constraint as the $K_L^0 \rightarrow 2\gamma$.

The fusion cluster mechanism is the most challenging one because the usual method to reject this kind of background is to restrict the decay vertex Z (Z_{vtx}) position in a reasonable region. However, in this study, the Z_{vtx} is not available due to the lack of kinematic variables. Therefore, we have to distinguish the fusion cluster from the single cluster by the cluster shape.

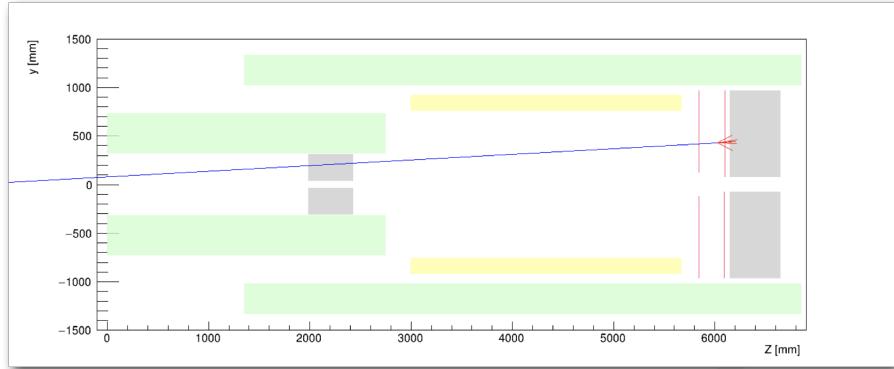


FIGURE 6.8: The schematic geometry diagram of the mechanism of the fusion cluster background.

915 The fusion cluster will have a wider shape than the single cluster because the fusion
 916 cluster is the combination of two clusters. Which is more likely to be a hadronic-like clus-
 917 ter. Thus, cluster shape discrimination with deep learning (CSDDL), which is explained
 918 in Section 6.4.2, is sensitive to distinguish the fusion cluster from the single cluster.

919 If we assume the BR to be $\mathcal{O}(10^{-3})$, the number of signal events inside the signal region
 920 is $\mathcal{O}(10^5)$. That means the Kaon decay background is negligible in this study.

921 Figure 6.9 shows the background level of other K_L^0 decays. The upper limit at 90%
 922 confidence level is estimated in the signal region, as shown in Table 6.3.

923 6.4.2 Neutron Background

924 The in-beam neutron background is the dominant background in this study. The neutron
 925 is generated by the hadronic interaction in the beamline, and it is called the "halo neutron"
 926 also. The mechanism is that a neutron hits the CsI calorimeter with one cluster, and there
 927 is no other in-time hit in the rest of the veto counters. Because the signature is the same as
 928 the signal event, the regular background reject method can not reduce this background,
 929 the neutron background is the most challenging in this study. Therefore, we developed
 930 three techniques based on the $\gamma - n$ discrimination to suppress the neutron background.
 931 The first and most powerful method is to discriminate the neutron cluster by the cluster
 932 shape with deep learning. The second one is discriminating the neutron cluster by the
 933 pulse shape difference with Fourier transformation. The last one is to use the both-end
 934 readout system of CsI crystal to measure the shower depth of the cluster. These three
 935 methods are explained in the following sections.

936 Cluster Shape Discrimination with Deep Learning(CSDDL)

937 The Cluster Shape Discrimination (CSD) method is based on the difference in the cluster
 938 shape between the neutron event and the photon event. Because of the shower depth
 939 difference, the neutron-like event will tend to be wider and shallower, and the photon-
 940 like event will be more narrow and depth, as shown in Figure 6.10. The difference is

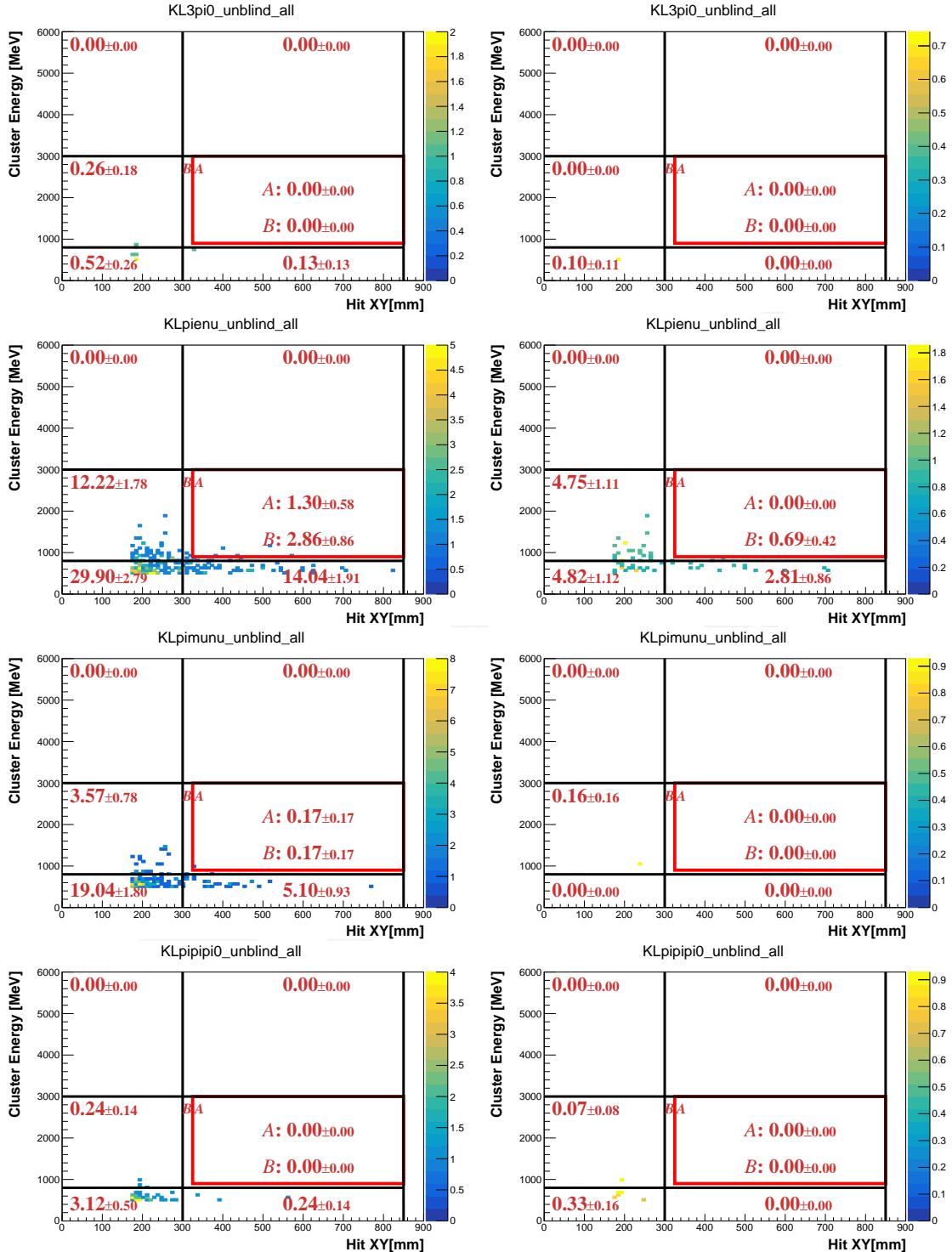


FIGURE 6.9:

Present the upper limit at 90% confidence level.

$E_\gamma - R_{XY}$ distributions of various background sources after applying all selection cuts. Left-hand side plots exclude the neutron cuts and the right-hand side plots include it. The red frame indicates the signal region. The red number indicates the background level in each region. (Region A indicates the Signal Region and Region B indicates the Blind Region exclude signal region.)

941 very easy to distinguish by the human eye, but it is very difficult to be quantified by the
 942 algorithm. Therefore, a neural network model was developed to quantify the difference
 943 of the cluster shape difference.

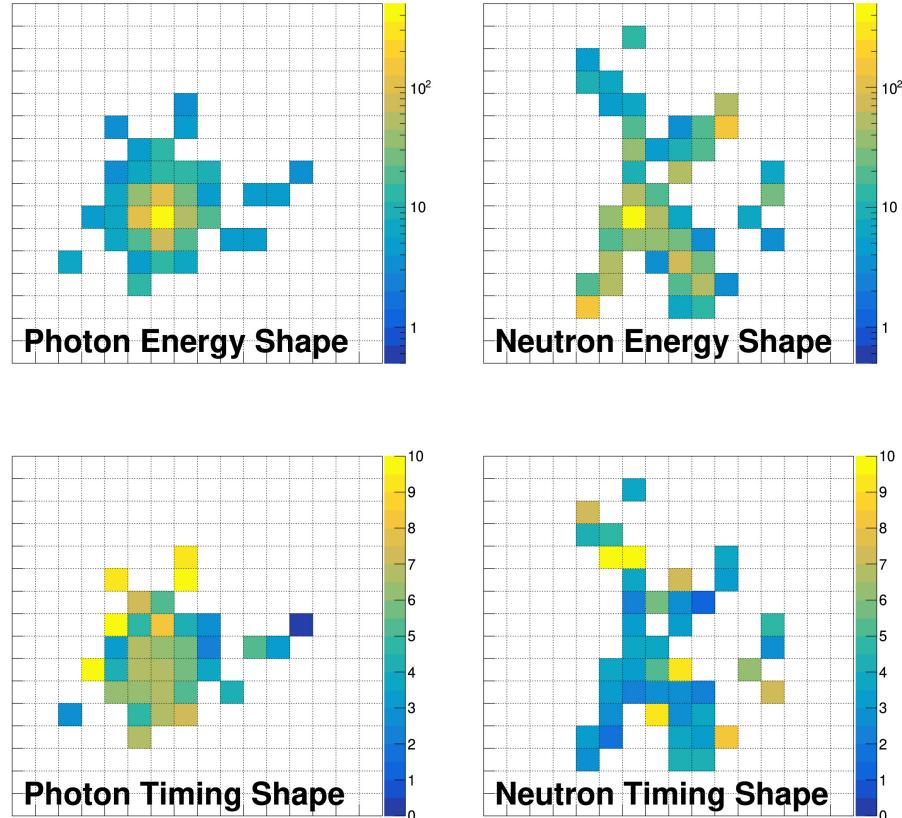


FIGURE 6.10: Example of the energy and timing shapes of photon cluster from the Monte Carlo simulation and neutron cluster from data. The color code represents the deposited energy in MeV and the timing in nanoseconds for each crystal in the cluster. [24]

944 In this study, the Convolutional Neural Network (CNN) architecture via TensorFlow
 945 was employed to classify the neutron and photon clusters by the energy and timing
 946 shapes [24]. We use the energy and timing for each crystal the cluster energy and the
 947 reconstructed angle on CsI (Φ) as the input parameter of the model training. The archi-
 948 tecture of the CNN training process is shown in Figure 6.11.

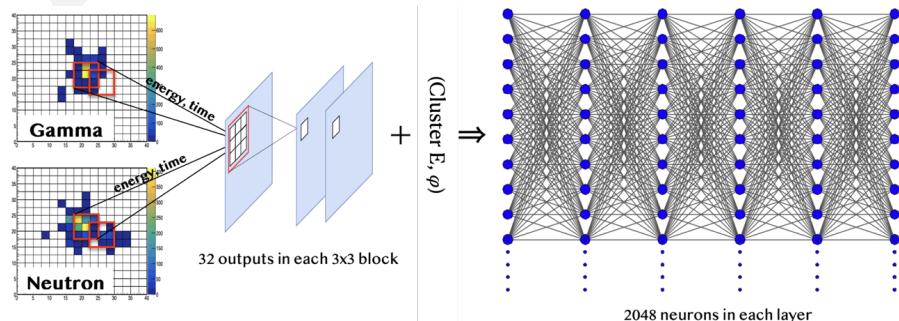


FIGURE 6.11: The architecture of CSD neural network training process.

949 The model training were using photon sample from the Monte Carlo simulation and
 950 the neutron sample from data. The photon sample was obtain from the $K_L^0 \rightarrow \gamma\bar{\gamma}$ decay
 951 MC simulation with accidental overlay. Neutron sample was obtain from the Z0-Al run
 952 as talk in Section 4.7.

953 The performance of the CSD training result is illustrated by the acceptance of photon
 954 clusters in comparison to the rejection of neutron clusters on the CSD score, as shown
 955 in Figure ???. This training result gives a very high neutron rejection with high photon
 956 acceptance. A selection cut point was decided at a CSDDL score larger than 0.984 based
 957 on the 90% signal acceptance. At this point, the inefficiency of the neutron sample is up
 958 to $\mathcal{O}(-\infty)$

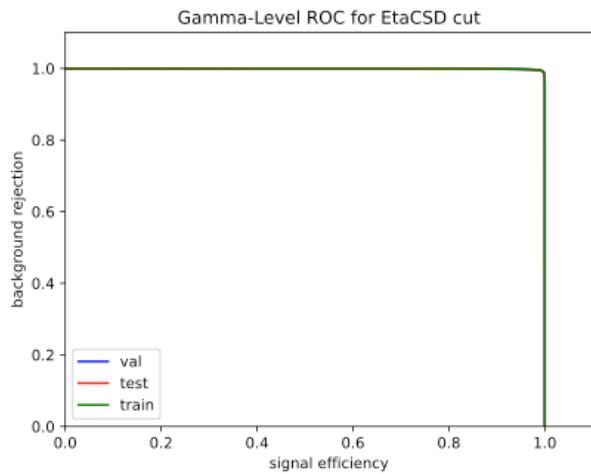


FIGURE 6.12: The ROC curve of the training model. The x-axis is the photon acceptance, and the y-axis is the neutron rejection.

959 Fourier transforms for Pulse shape discrimination (FPSD)

960 The difference in shower development of neutron and photon particle also manifests in
 961 the pulse shape difference in the CsI. The neutron pulses have a longer tail than the pho-
 962 ton sample because the difference between the hadronic interaction and electromagnetic
 963 interactions, as shown in the Figure 6.13

964 The data set to

965 FPSD discriminated the neutron cluster and photon clusters based on the shape of the
 966 ADC waveform. We applied FTT to the ADC raw pulse and then extracted the differ-
 967 ences between the neutron and photon in the frequency domain. Figure 6.14 shows the
 968 likelihood ratio. By requiring the 90% signal acceptance, the neutron cluster background
 969 rejection efficiency is 89.6%.

970 Shower-depth

971 The radiation length for photons is shorter than the interaction length for neutrons, re-
 972 sulting in different shower depths in the calorimeter for photons and neutrons. Multi-
 973 pixel photon counters (MPPC) were installed in front of the CSI calorimeter, to get the

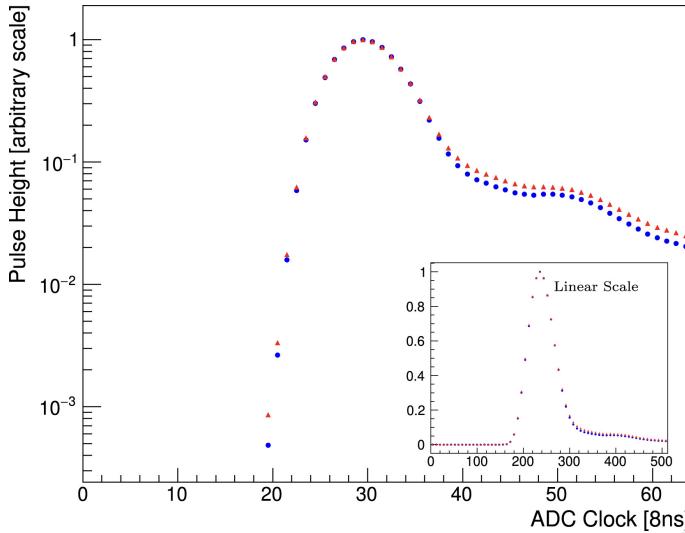


FIGURE 6.13: Average pulse shape of the neutron sample (blue dots) and photon sample (red dots) from one CsI crystal.[24]

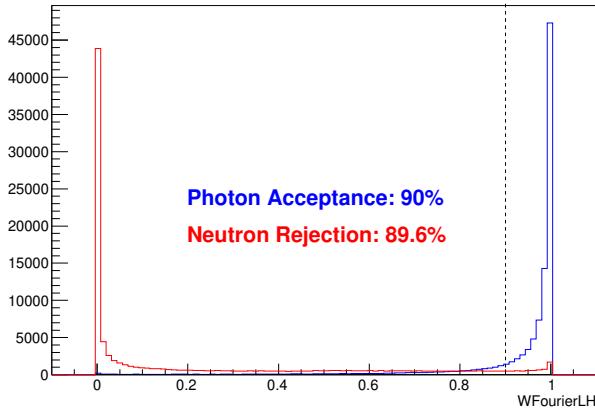


FIGURE 6.14: Distribution of the likelihood ratio for hadronic cluster events (red) and photon cluster events (blue). The photon cluster events are obtained through the $K_L^0 \rightarrow 3\pi^0$ decay analysis of data. The neutron sample is obtained from neutron data.

974 timing difference(ΔT) between PMT and MPPC as shown in figure 6.15. The distribution
 975 of ΔT is shown in figure 6.16. By requiring ΔT to be less than 29.5 ns, the background
 976 rejection efficiency is 84% with a signal loss of 9%.

977 6.5 Single Event Sensitivity

978 After considering the 175 mm cut for the low-radius background and all the selection
 979 cuts, the single event sensitivity (SES) is calculated by the equation 6.1. The SES is calcu-
 980 lated by the K_L^0 yield and the signal acceptance. For this study, The K_L^0 yield is evaluated
 981 by the $K_L^0 \rightarrow 3\pi^0$ decay, because the statistics of the 2-hour special physics data set are
 982 not enough to evaluate the yield by $K_L^0 \rightarrow \pi^0\pi^0$ and $K_L^0 \rightarrow 2\gamma$ decays. After the selection
 983 cuts in Section ??, no event will leave for the $K_L^0 \rightarrow \pi^0\pi^0$ and $K_L^0 \rightarrow 2\gamma$ decays. The
 984 signal acceptance is evaluated by the Monte Carlo simulation with accidental overlay.
 985 After applying all the selection cuts in Section 6.3, the signal acceptance is 2.66×10^{-3} .
 986 And the K_L^0 yield is 1.29×10^{10} . The single event sensitivity (SES) is estimated to be
 987 $(2.91 \pm 0.05_{stat.}) \times 10^{-8}$.

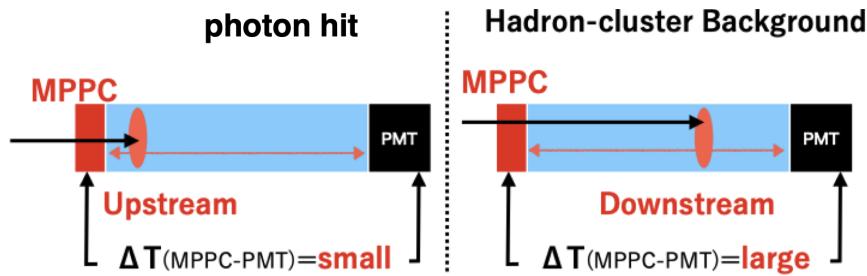


FIGURE 6.15: Illustration of shower depth means. An MPPC is installed on the upstream side. The time difference between the photon arriving upstream and downstream ($\Delta T = T_{MPPC} - T_{PMT}$) is used to measure the depth of the reaction and distinguish between photon events (left) and neutron events (right).

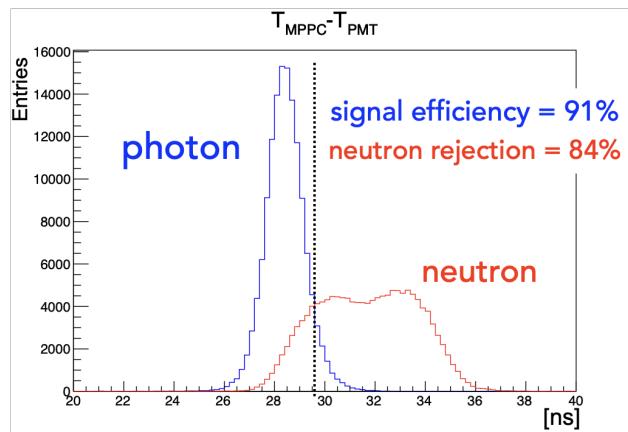


FIGURE 6.16: Distribution of the ΔT for neutron events and photon events. The photon cluster events are obtained through the $K_L^0 \rightarrow 3\pi^0$ decay analysis of data. The neutron sample is obtained by scattering neutrons in the beam with an Al plate.

$$SES = \frac{1}{Y \times A_{sig}} \quad (6.6)$$

$$= \frac{1}{1.29 \times 10^{10} \times 2.66 \times 10^{-3}} \quad (6.7)$$

$$= 2.91 \times 10^{-8} \quad (6.8)$$

988 6.5.1 Systematic Uncertainty of SES

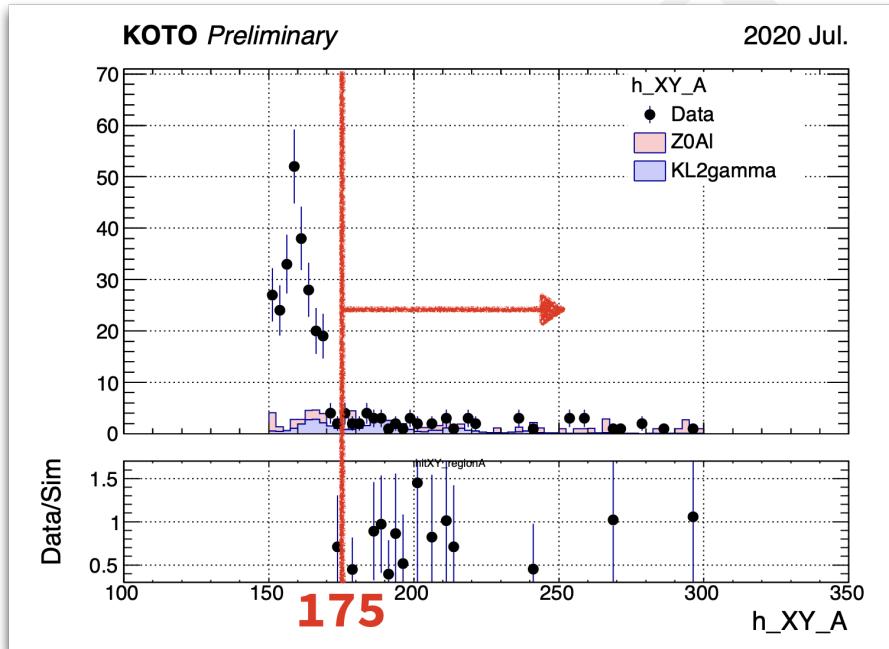
989 Table 6.2 shown the summary of the systematic uncertainty from each sources for the
990 SES.

991 6.6 Additional Background Source Study

992 After the event selection, there is a large discrepancy between the data and the simulation
993 in the low-radius region where $H_{XY} < 175$ mm. As shown in Figure 6.17, the data has
994 a higher level of background in the low-radius region than the simulation. To figure out
995 the contribution of this discrepancy, we studied some extra background source. In the
996 following subsection, the description of these sources was shown.

TABLE 6.2: Summary of Systematic Uncertainty for SES

Sources	Uncertainty
Veto Cuts	6.6%
Kinematic Cuts for $K_L^0 \rightarrow 3\pi^0$	3.3%
Kinematic Cuts for $K_L^0 \rightarrow \gamma\bar{\gamma}$	1.4%
Neutron Cuts for $K_L^0 \rightarrow \gamma\bar{\gamma}$	4.8%
K_L^0 momentum spectrum	0.9%
Trigger Effect	1.6%
Branching ratio of $K_L^0 \rightarrow 3\pi^0$	0.6%

FIGURE 6.17: The R_{XY} distribution of the region 2. The red line and arrow indicated the cutoff region

Upstream Decay from 2nd Collimator

The discrepancy is centered at the region $R_{XY} < 175$ mm and the maximum R_{XY} of the cluster of upstream decay is 265 mm, as Section 6.4.1 discussed. This means the upstream decay is a very possible background source. Therefore, we extend the generated position in the Monte Carlo simulation to the start of the 2nd collimator to study the very upstream decay background. In the usual simulation, the decay position is generated at the end of the 2nd collimator, which is -1507 mm from the upstream of the FBAR. The 2nd collimator is 4 m long, which means the new decay position is -5507 mm from the upstream of the FBAR. The geometry calculation, as Figure 6.6, shows that the maximum R_{XY} of the cluster of the new decay position is 133 mm, which completely covers the discrepancy region.

The $K_L^0 \rightarrow 2\gamma$ decay was studied in this section. The normalization method is the

1009 same as the usual Monte Carlo simulation but uses the upstream $K_L^0 \rightarrow 3\pi^0$ decay (Z=-
 1010 5507 mm) to estimate the K_L^0 yield.

1011 **NCC background**

1012 When a halo neutron hit NCC, a π^0 might produce by the hadronic interaction. The
 1013 π^0 will decay to two photons and if one of them missing due to the inefficiency of the
 1014 detector, it will become a background sources.

1015 **Charge Kaon Decay**

1016 As shown in the Figure 4.1, thought it is not a large mount, the charge Kaon is still re-
 1017 mained in the beamline.

1018 **Halo K_L^0 Background**

1019 Halo K_L^0 is the K_L^0 particles that are in the periphery of the beam core. As mentioned in
 1020 Section 4.4.2, the empirical K_L^0 spectrum does not consider the halo K_L^0 . The beamline
 1021 simulation was required to simulate the halo K_L^0 .

1022 **Summary of the Study**

1023 After above extra background source study, the discrepancy in low radius region is still
 1024 existed. Currently, there are not any further idea for the search stratagem. It is also
 1025 possible just from something upstream accidental hit in the beamline which is almost
 1026 impossible to prob because the sources unknown and unclear. To handle with is problem,
 1027 we simply enlarge the innermost fiducial cut from 150 mm to 175 mm.

1028 **6.7 Background Level Estimation**

1029 Table 6.3 shows the background level of each background source in the signal region. The
 upper limit at 90% confidence level is estimated in the signal region.

TABLE 6.3: Number of events predicted for each source inside the signal region

Source		Number of events
K_L decay	$K_L \rightarrow 2\gamma$	1.09 ± 0.12
	$K_L \rightarrow 3\pi^0$	< 0.18 (90% C.L.)
	$K_L \rightarrow 2\pi^0$	< 0.51 (90% C.L.)
	$K_L \rightarrow \pi^\pm e^\mp \nu_e$	< 0.27 (90% C.L.)
	$K_L \rightarrow \pi^\pm \mu^\mp \nu_\mu$	< 0.25 (90% C.L.)
	$K_L \rightarrow \pi^+ \pi^- \pi^0$	< 0.17 (90% C.L.)
Neutron		11.57 ± 4.42

1031 Figure ?? shows the E_γ - H_{XY} distribution of physics data for each region. In the
 1032 side band region, the expected number shows the agreement with the observations. The
 1033 background level in signal region is 12.66 ± 4.42 .

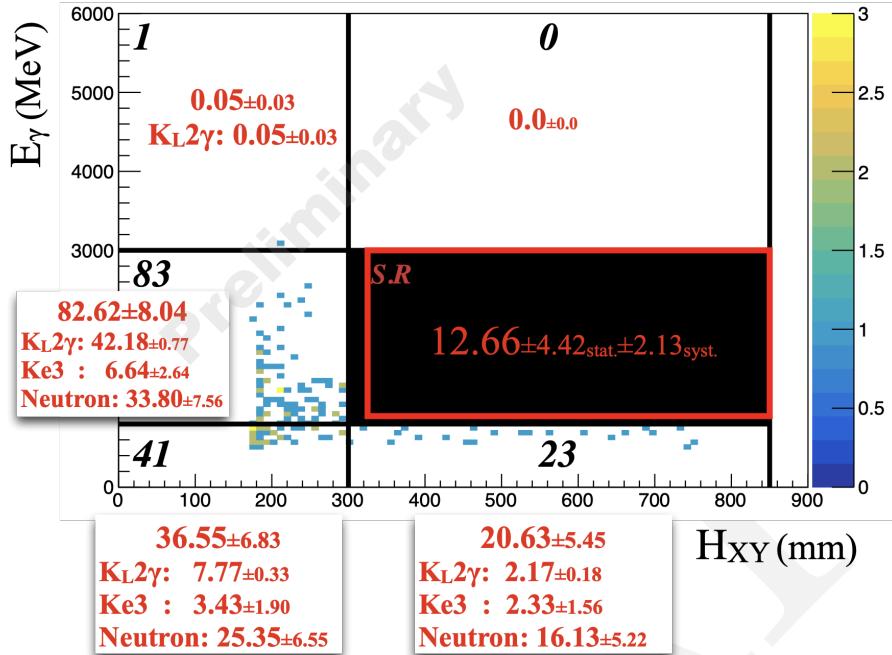


FIGURE 6.18: E_γ - H_{XY} distribution of physics data after apply all the selection cuts. The black box is the blind region the red frame is the signal region. The black (red) number is the observed (expected) number of events.

1034 6.8 Un-blind the Signal Region

1035 After all the study we're done, we decided to open the box. The observed result is 13
 1036 events inside the signal region, as shown in the Figure 6.19, which is agreed with the ex-
 1037 pected number of events. To estimate the Branching ratio of the $K_L^0 \rightarrow \gamma\bar{\gamma}$, the Feldman-
 1038 Cousins method was adopted, because we still have a large number of expected back-
 1039 ground in the signal region. After the calculation, an upper limit of branching ratio was
 1040 obtained at 90% C.L.,

$$\mathcal{BR}(K_L^0 \rightarrow \gamma\bar{\gamma}) < 11.9 \times SES(K_L^0 \rightarrow \gamma\bar{\gamma}) \quad (6.9)$$

$$= 3.47 \times 10^{-7} (90\% \text{ C.L.}) \quad (6.10)$$

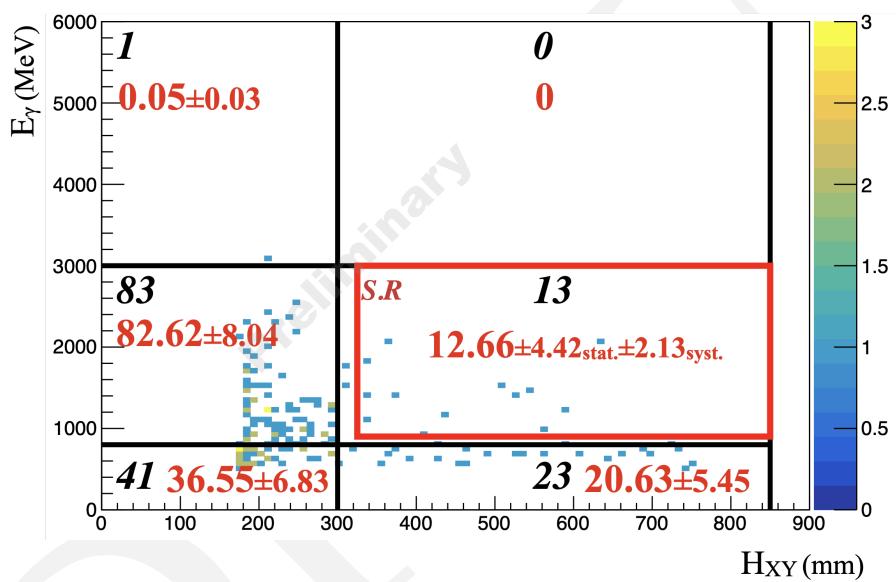


FIGURE 6.19: E_γ - H_{XY} distribution of physics data after open the blind box. The black (red) number is the observed (expected) number of events.

1041 **Chapter 7**

1042 **Conclusion and Discussion**

1043 We present the study of $K_L^0 \rightarrow \gamma\bar{\gamma}$ search in this thesis. The $K_L^0 \rightarrow \gamma\bar{\gamma}$ analysis is based
 1044 on the 2-hour spacial run taken in 2020. The total number of K_L^0 decays is 1.29×10^{10} ,
 1045 which is estimated by the $K_L^0 \rightarrow 3\pi^0$ decay. Two kinds of backgrounds are major in
 1046 this analysis, the K_L^0 decay background and the in-beam neutron background. We use
 1047 different methods to suppress these two backgrounds.

1048 To suppress the K_L^0 decay source background, we use the veto system of the KOTO
 1049 detector. Because the one cluster signal signature is a pretty strict criterion to reject most
 1050 of the K_L^0 decay channel with multiple products in the final state. The only background
 1051 that can pass the veto system is the $K_L^0 \rightarrow 2\gamma$ channel. With one photon missing due to
 1052 detection inefficiency, the $K_L^0 \rightarrow 2\gamma$ background cannot be rejected. Thanks to the her-
 1053 metic veto system of the KOTO Experiment, the $K_L^0 \rightarrow 2\gamma$ background is well suppressed
 1054 by the veto system with only $1.09 \pm 0.12_{stat.} \pm 0.05_{syst.}$ events estimated remaining in the
 1055 signal region.

1056 To suppress the in-beam neutron background, we use three techniques based on the
 1057 $n - \gamma$ discrimination to suppress the neutron background. The first one is cluster shape
 1058 discrimination based on deep learning, which is the most powerful technique to classify
 1059 neutrons and photons. The other two are the pulse shape discrimination based on the
 1060 Fourier Transform and the show-depth measure by the CsI both-end readout system.
 1061 These two techniques also provide a good rejection power on the neutron background.
 1062 Combining these three techniques, rejected the neutron background by $\mathcal{O}(10^{03})$ for the
 1063 single cluster with 83.9% signal acceptance. After all the selections, the total neutron
 1064 background is estimated to be $11.57 \pm 4.42_{stat.} \pm 2.13_{syst.}$ events in the signal region.

1065 Combining all the background sources we have studied, the total background is esti-
 1066 mated to be $12.66 \pm 4.42_{stat.} \pm 2.13_{syst.}$ events in the signal region. After the background
 1067 suppression study, we open the blind region box. The observed events in the signal re-
 1068 gion are 13 events, which is consistent with the background estimation. Because we still
 1069 have a large estimation of the background in the signal region, we decided to use the
 1070 Feldman-Cousins method to evaluate the upper limit on the $K_L^0 \rightarrow \gamma\bar{\gamma}$ branching ratio.
 1071 At 90% C.L., the upper limit on the $K_L^0 \rightarrow \gamma\bar{\gamma}$ branching ratio is 3.47×10^{-7} .

1072 7.1 Massive Dark Photon Search

1073 We finished the massless dark photon study, the massive dark photon should be also an
1074 interesting topic to study. In this study, the search strategy is not strict with the mass of
1075 the dark photon. Therefore, the massive dark photon search will use the same strategy as
1076 the massless dark photon search. The only need to change is the mass of the dark photon
1077 in the MC simulation. Figure 7.1 shows the SES of each mass of the dark photon.

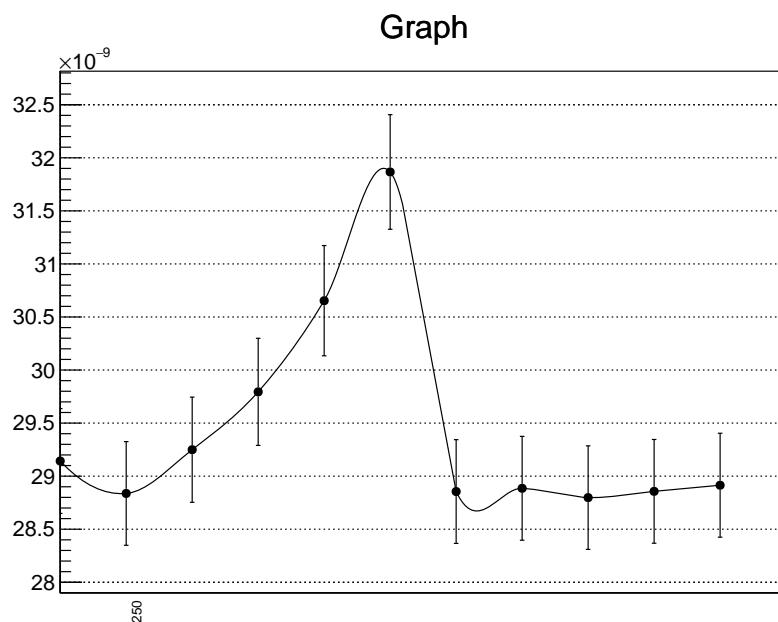


FIGURE 7.1: SES of each mass dark photon from 0 MeV to 250 MeV, step 25 MeV

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