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1. 数论

1.1 线性筛素数、分解质因数

```
#define N 65536
int sizePrime, prime[N];
bool check[N] = { 0 };
int factSize, factc[128], factv[128];

//线性筛素数
void getPrime(){
    sizePrime = 0;
    for (int i = 2; i < N; i++){
        if (!check[i]) prime[sizePrime++] = i;
        for (int j = 0; j < sizePrime && i*prime[j] < N; j++){
            check[i*prime[j]] = 1;
            if (i%prime[j] == 0) break;
        }
    }
}

//分解质因数
void decompose(int num){
    factSize = 0;
    for (int i = 0; i < sizePrime && prime[i]*prime[i] <= num; i++){
        if (num%prime[i] == 0){
            factv[factSize] = prime[i];
            factc[factSize] = 0;
            while (num%prime[i] == 0){
                factc[factSize]++;
                num /= prime[i];
            }
            factSize++;
        }
    }
    if (num != 1){
        factv[factSize] = num;
        factc[factSize++] = 1;
    }
}
```

1.2 欧几里得算法、求逆元、**stein**算法求最大公约数

```
typedef long long LL;
LL gcd(LL a, LL b){
    if (b == 0) return a;
    return gcd(b, a%b);
}

//扩展欧几里得
LL extend_euclid(LL a, LL b, LL &x, LL &y){
    if (b == 0){
        x = 1; y = 0;
        return a;
    }
    LL d = extend_euclid(b, a%b, y, x);
    y -= x*(a/b);
}
```

```

        return d;
    }

//求逆元 gcd(a, b) = 1
LL getInverse(LL a, LL b){
    LL x, y;
    extend_euclid(a, b, x, y);
    if (x < 0) x = x + ((-x) / b + 1) * b;
    if (x > 0) x = x - x / b * b;
    return x;
}

//最大公约数stein算法
LL stein(LL a, LL b){
    LL t = 0;
    if (a < b){
        a ^= b; b ^= a; a ^= b;
    }
    while (b){
        if ((a&1) && (b&1)){
            b = (a - b)>>1;
            a -= b;
        }
        else if (a&1) b >>= 1;
        else if (b&1){
            a >>= 1;
            if (a < b){
                a ^= b; b ^= a; a ^= b;
            }
        }
        else{
            a >>= 1; b >>= 1; t++;
        }
    }
    return a <= t;
}

```

1.3 中国剩余定理

```

// x = rem[i] mod mm[i]
LL mm[N], rem[N];

LL chineseRemainder(LL M, LL pc){
    LL i, ans = 0, x, y;
    for (i = 0; i < pc; i++){
        extend_euclid(M/mm[i], mm[i], x, y);
        ans = (ans + rem[i] * (M/mm[i]) * x) % M;
    }
    return ans;
}

```

1.4 迭代求模线性方程组

```

typedef long long LL;
int sizeF;
LL modNum[N], remNum[N];

LL calc(){
    LL i, j, k, lcm, d, x, y, z, ans = -1;
    for (i = 0; i < sizeF; i++){

```

```

        if (i+1 == sizeF){
            ans = remNum[i] % modNum[i]; break;
        }
        else{
            d = extend_euclid(modNum[i], modNum[i+1], x, y);
            if (d == 0){
                ans = -1; break;
            }
            j = remNum[i+1]-remNum[i];
            if (j%d != 0){
                ans = -1; break;
            }
            lcm = modNum[i]/d*modNum[i+1];
            z = modNum[i+1]/d;
            k = j/d*x;
            k = (k%z + z) % z;
            k = (remNum[i]%lcm + k*modNum[i]%lcm) % lcm;
            if (k < 0) k = k + ((-k)/lcm+1)*lcm;
            if (k > 0) k = k - k/lcm*lcm;
            remNum[i+1] = k;
            modNum[i+1] = lcm;
        }
    }
    return ans;
}

```

1.5 区间筛素数

```

//返回从l到r之间的素数, 0(sqrt(n))
void intervalPrime(int l, int r){
    for (int i = 0; i < sizePrime; i++){
        int v = l/prime[i]*prime[i];
        while (v < l) v += prime[i];
        for (int j = v; j <= r; j += prime[i]) visit[j-l] = 1;
    }
    for (int i = l; i <= r; i++) if (!visit[i-l]) printf("%d\n", i);
}

```

1.6 线性求欧拉函数

```

LL phi[N], prime[N], sizePrime;
bool check[N] = { 0 };

void calPhi(){
    sizePrime = 0;
    for (int i = 2; i < N; i++){
        if (!check[i]){
            prime[sizePrime++] = i;
            phi[i] = i-1;
        }
        for (int j = 0; j < sizePrime && i*prime[j] < N; j++){
            check[i*prime[j]] = 1;
            if (i%prime[j] == 0){
                phi[i*prime[j]] = phi[i]*prime[j]; break;
            }
            else phi[i*prime[j]] = phi[i]*(prime[j]-1);
        }
    }
}

```

1.7 计算 $a^b \bmod m$

```
//性质: if (b >= phi(m)) b = b % phi(m) + phi(m)
//计算欧拉函数
LL cal_phi(LL x){
    LL ans = x;
    for (int i = 0; i < sizePrime && (LL)prime[i]*prime[i] <= x; i++){
        if (x%prime[i] == 0){
            ans = ans / prime[i] * (prime[i] - 1);
            while (x%prime[i] == 0) x /= prime[i];
        }
    }
    if (x != 1) ans = ans / x * (x - 1);
    return ans;
}
//快速幂取模
LL power(LL x, LL y, LL z){
    if (x == 0 && y == 0) return 1;
    if (x == 0) return 0;
    if (x == 1) return 1;
    LL ans = 1, d = x%z;
    if (x >= z) flag = 1;
    while (y > 0){
        if (y&1) ans = ans*d;
        if (ans >= z){
            flag = 1;
            ans %= z;
        }
        d = d * d;
        if (d >= z){
            flag = 1;
            d %= z;
        }
        y >>= 1;
    }
    return ans;
}

//递归求解
//例子: 求 $a^{(a^{(a^{\dots})})} \bmod M$ 
LL cal_f(int dep, LL mod){
    if (dep == 0){
        flag = 0;
        return 1;
    }
    LL ans, phi, tmp;
    phi = cal_phi(mod);
    tmp = cal_f(dep-1, phi);
    if (flag) tmp += phi;
    flag = 0;
    ans = power(u, tmp, mod);
    return ans;
}
```

1.8 求二次同余方程

```
/*
    求解 $x^2 = a \bmod p$ 
    输入a输出x, 解为x和p-x, 当x==p-x时, 解就一个
    并且返回的是较小的x
*/
```

```

    返回-1表示无解
*/
LL squareRoot(LL a, LL p){
    LL i, j, k, ans;
    if (p == 2) return a%p;
    if (power(a, (p-1)/2, p) == 1){
        if (p%4 == 3) ans = power(a, (p+1)/4, p);
        else {
            for (i = 1; power(i, (p-1)/2, p) == 1; i++);
            j = (p-1)>>1;
            k = 0;
            do {
                j >>= 1;
                k >>= 1;
                if ((power(a, j, p) * power(i, k, p) + 1)%p == 0)
                    k += (p-1)/2;
            } while (j%2 == 0);
            ans = (power(a, (j+1)/2, p) * power(i, k>>1, p)) % p;
        }
        if (ans*2 > p) ans = p-ans;
        return ans;
    }
    return -1;
}

```

1.9 Pell方程求最小正整数解

```

/* 最好用java
* pell:  $x^2 - n * y^2 = 1$ 
* 求最小正整数解, 当n为完全平方数时无解
*  $a_0 = \text{sqrt}(n)$   $a_1 = a_0$ 
*  $p_0 = 0, p_1 = 1, q_0 = 1, q_1 = 0, g_0 = 0, h_0 = 1$ 
*  $g_i = a_i * h_{i-1} - g_{i-1}$ 
*  $h_i = (n - g_i * g_i) / h_{i-1}$ 
*  $a_{i+1} = (g_i + a_0) / h_i$ 
*  $p_i = a_i * p_{i-1} + p_{i-2}$ 
*  $q_i = a_i * q_{i-1} + q_{i-2}$ 
*/
import java.math.*;
import java.util.*;

public class Main {
    public static void main(String[] args){
        Scanner input = new Scanner(System.in);
        long n;
        BigInteger p0, p1, p2;
        BigInteger q0, q1, q2;
        BigInteger a0, a1, a2;
        BigInteger g0, g1, h0, h1;

        while (input.hasNext()){
            n = input.nextLong();
            p0 = BigInteger.ZERO;
            p1 = BigInteger.ONE;
            q0 = BigInteger.ONE;
            q1 = BigInteger.ZERO;
            g0 = BigInteger.ZERO;
            h0 = BigInteger.ONE;

            a0 = BigInteger.valueOf((long)Math.sqrt(n * 1.0));
            a1 = a0;

```

```

        if (a0.multiply(a0).longValue() == n){
            System.out.println("No solution!");
            continue;
        }
        while (true){
            g1 = a1.multiply(h0).subtract(g0);
            g0 = g1;

            h1 = BigInteger.valueOf(n).subtract(g1.multiply(g1));
            h1 = h1.divide(h0);
            h0 = h1;

            a2 = g1.add(a0).divide(h1);

            p2 = a1.multiply(p1).add(p0);
            p0 = p1;
            p1 = p2;

            q2 = a1.multiply(q1).add(q0);
            q0 = q1;
            q1 = q2;

            a1 = a2;

            BigInteger tmp;
            tmp = p2.multiply(p2);
            tmp = tmp.subtract(q2.multiply(q2).multiply
(BigInteger.valueOf(n)));
            if (tmp.equals(BigInteger.ONE)){
                System.out.println(p2 + " " + q2);
                break;
            }
        }
    }
}

```

1.10 不定方程 $a^2 + b^2 = p$

//p为质数

```

int main(){
    LL p, a, b, x, y, u, v, k;
    srand(time(0));
    while (scanf("%lld", &p) != EOF){
        if (p%4 == 3){
            puts("Illegal");
            continue;
        }
        printf("Legal ");
        while (1){
            a = rand() % (p-1) + 1;
            x = power(a, (p-1)/4, p);
            if (x*x%p == p-1) break;
        }
        y = 1;
        while (1){
            if (x > p/2) x = p-x;
            if (y > p/2) y = p-y;
            k = (x*x + y*y)/p;
            if (k == 1) break;
            a = x%k; b = y%k;
        }
    }
}

```



```

        if (a > k/2) a -= k;
        if (b > k/2) b -= k;
        u = (a*x + b*y)/k;
        v = (b*x - a*y)/k;
        if (u < 0) u = -u;
        if (v < 0) v = -v;
        x = u; y = v;
    }
    if (x > y) swap(x, y);
    printf("%lld %lld\n", x, y);
}
}

```

1.11 组合数取模（未预处理版本）

```

#define N 65536
typedef long long LL;
int sizePrime, prime[N];
int facts, factv[128], factc[N];
bool check[N] = { 0 };
LL temp[N];
//快速幂取模
LL power(LL x, LL y, LL m){
    LL ans = 1, d = x%m;
    while (y > 0){
        if (y&1) ans = ans * d % m;
        d = d * d % m;
        y >>= 1;
    }
    return ans;
}

//calculate: n! % p^c
//cnt -- number of p
LL factorialMod(LL l, int pp, int cc, int &cnt){
    int i, j, MOD;
    LL ans;
    for (i = 1, cnt = 0; i > 0; i /= pp) cnt += i/pp;
    for (i = 0, MOD = 1; i < cc; i++) MOD *= pp;
    temp[0] = 1;
    for (i = 1; i < MOD; i++){
        if (i%pp == 0){
            temp[i] = temp[i-1];
            continue;
        }
        temp[i] = temp[i-1] * i % MOD;
    }
    ans = 1;
    for (i = 1; i > 0; i /= pp){
        //if ... MOD > 数组长度
        ans = ans * power(temp[MOD-1], i/MOD, MOD) % MOD;
        ans = ans * temp[i%MOD] % MOD;
    }
    return ans;
}

//calculate: C(n, k) % m --> chinese remainder
LL combinationMod(int nn, int kk, int mm){
    LL rem[128], pi[128], f;
    LL d, x, y, ans = 0;

```

```

int i, j, sum, ts;
decompose(mm, factv, factc, facts);
for (i = 0; i < facts; i++)
    for (pi[i] = j = 1; j <= factc[i]; j++)
        pi[i] *= factv[i];
for (i = 0; i < facts; i++){
    sum = 0;
    f = factorialMod(nn, factv[i], factc[i], ts);
    sum += ts;
    rem[i] = f;

    f = factorialMod(nn-kk, factv[i], factc[i], ts);
    sum -= ts;
    d = extend_euclid(f, pi[i], x, y);
    if (x < 0) x = x + ((-x) / pi[i] + 1) * pi[i];
    rem[i] = (rem[i] * x % pi[i] + pi[i]) % pi[i];

    f = factorialMod(kk, factv[i], factc[i], ts);
    sum -= ts;
    d = extend_euclid(f, pi[i], x, y);
    if (x < 0) x = x + ((-x) / pi[i] + 1) * pi[i];
    rem[i] = (rem[i] * x % pi[i] + pi[i]) % pi[i];

    if (sum >= factc[i]) rem[i] = 0;
    else rem[i] = rem[i] * power(factv[i], sum, pi[i]) % pi[i];
    //for (j = 0; j < sum; j++) rem[i] = rem[i] * factv[i] % pi[i];
}

for (i = 0; i < facts; i++){
    d = extend_euclid(mm/pi[i], pi[i], x, y);
    ans = (ans + mm/pi[i] * x % mm * rem[i] + mm) % mm;
}
return ans;
}

```

1.12 组合数取模（预处理）

```

//checked by spoj5093
typedef long long LL;
#define N 32768
int n, k, m;
int sizePrime, prime[N];
bool check[N] = { 0 };
int facts, sg, factv[64], factc[64], pk[64], cnt1[16][N];
LL group[128], dp[N], res[16][N], inv[16][N];
LL deg[N], rev[128], crt[128], mul[64][64];

void decompose(LL num, int val[], int cnt[], int &ss){
    int i, j;
    ss = 0;
    for (i = 0; i < sizePrime && (LL)prime[i]*prime[i] <= num; i++){
        if (num%prime[i] == 0){
            val[ss] = prime[i];
            cnt[ss] = 0;
            while (num%prime[i] == 0){
                cnt[ss]++;
                num /= prime[i];
            }
            ss++;
        }
    }
}

```

```

        if (num != 1){
            val[ss] = num;
            cnt[ss++] = 1;
        }
    }

void dfs(int dep, LL num){
    if (dep == facts){
        group[sg++] = num;
        return ;
    }
    dfs(dep+1, num);
    for (int i = 0; i < factc[dep]; i++){
        num *= factv[dep];
        dfs(dep+1, num);
    }
}

LL combModular(LL u, LL v){
    int i, sum;
    LL ans = 0, rem;
    for (i = 0; i < facts; i++){
        sum = cnt1[i][u] - cnt1[i][v] - cnt1[i][u-v];
        rem = res[i][u] * inv[i][v] % pk[i] * inv[i][u-v] % pk[i];

        if (sum >= factc[i]) rem = 0;
        else rem = rem * mul[i][sum] % pk[i];
        ans = (ans + rev[i] * rem) % m;
    }
    return ans;
}

void init(){
    int i, j;
    LL d, x, y;
    decompose(k, factv, factc, facts);
    sg = 0;
    dfs(0, 1);
    sort(group, group+sg);
    decompose(m, factv, factc, facts);
    for (i = 0; i < facts; i++){
        pk[i] = mul[i][0] = 1;
        for (j = 1; j <= factc[i]; j++){
            pk[i] *= factv[i];
            mul[i][j] = pk[i];
        }
        d = extend_euclid(m/pk[i], pk[i], x, y);
        if (x < 0) x = x + ((-x)/pk[i]+1)*pk[i];
        if (x > 0) x %= pk[i];
        crt[i] = x;
        rev[i] = m / pk[i] * crt[i];

        res[i][0] = inv[i][0] = 1;
        cnt1[i][0] = 0;
        for (j = 1; j < N && j <= n; j++){
            x = j;
            y = 0;
            while (x%factv[i] == 0){
                y++;
                x /= factv[i];
            }
        }
    }
}

```

```

        }
        cnt1[i][j] = cnt1[i][j-1] + y;
        res[i][j] = res[i][j-1] * x % pk[i];

        d = extend_euclid(res[i][j], pk[i], x, y);
        if (x < 0) x = x + ((-x)/pk[i]+1)*pk[i];
        if (x > 0) x %= pk[i];
        inv[i][j] = x;
    }
}
for (deg[1] = 1, i = 2; i < N; i++) deg[i] = deg[i-1] * (i-1) % m;
}

void DP(){
    int i, j;
    LL ret;
    dp[0] = 1;
    for (i = 1; i <= n; i++){
        dp[i] = 0;
        for (j = 0; j < sg && i-group[j] >= 0; j++){
            ret = combModular(i-1, group[j]-1);
            ret = ret * dp[i-group[j]] % m * deg[group[j]] % m;
            dp[i] = (dp[i] + ret) % m;
        }
    }
    printf("%lld\n", dp[n]);
}

int main(){
    getPrime();
    while (scanf("%d%d%d", &n, &k, &m) != EOF){
        init();
        DP();
    }
}

```

1.13 Miller-Rabin测试、 Pollard-Rho分解

```

//checked by pku1811
#include <stdio.h>
#include <stdlib.h>
#include <math.h>
using namespace std;
typedef long long LL;
LL p; //the smallest prime

LL gcd(LL x, LL y){
    if (y == 0) return x;
    return gcd(y, x%y);
}

//I got wrong here, exceed long long
LL mul(LL x, LL y, LL m){
    LL t, T, a, b, c, d, e, f, g, h, v, ans;
    T = (LL)( sqrt(double(m)+0.5) );
    t=T*T-m;
    a=x/T; b=x%T; c=y/T; d=y%T;
    e=a*c/T; f=a*c%T;
    v=((a*d+b*c)%m+e*t)%m;
    g=v/T; h=v%T;
    ans=(((f+g)*t%m+b*d)%m+h*T)%m;
}

```

```

        while (ans<0) ans+=m;
        return ans;
}

LL power(LL a, LL u, LL m){
    LL ans = 1, d = a%m;
    while (u > 0){
        if (u&1) ans = mul(ans, d, m);
        d = mul(d, d, m);
        u >>= 1;
    }
    return ans;
}

LL get_random(LL n){
    LL a = rand();
    rand();
    a *= rand()%(n-1);
    a *= rand()%(n-1);
    a = a%(n-1)+1;
    return a;
}

//check pseudo-prime based on a
bool witness(LL a, LL n){
    LL x0, x1, x2, i, u, t;
    u = n-1, t = 0;
    while (u%2 == 0){
        t++;
        u /= 2;
    }
    x1 = x0 = power(a, u, n);
    if ( x1 == 1 ) return true;
    for ( i = 1; i <= t; i++ ){
        x2 = mul( x1, x1, n );
        if ( x2 == 1 && x1 != 1 && x1 != n-1 && x1 != -1 ) return false;
        x1 = x2;
    }
    if ( x1 != 1 ) return false;
    return true;
}

bool miller_rabin( LL n ){
    if ( n == 2 || n == 3 ) return true;
    LL i, a;
    for ( i = 0; i < 10; i++ ){
        a = get_random( n );
        if ( !witness( a, n ) ) break;
    }
    return i == 10;
}

LL f( LL x, LL n ){
    return (mul(x,x,n)+1)%n;
}

LL pollard_rho( LL n ){
    if ( n < 2 ) return 0;
    if ( n%2 == 0 ) return 2;
    LL x, y, i, d;

```

```

    for ( i = 1; i <= 10; i++ ){
        rand( );
        x = rand( )%n;
        y = f( x, n );
        d = gcd( (y-x+n)%n, n );
        while ( d == 1 ){
            x = f( x,n );
            y = f( f(y,n), n );
            d = gcd( (y-x+n)%n, n )%n;
        }
        if ( d ) return d;
    }
    return 0;
}

void smallest_prime( LL n ){
    if ( miller_rabin( n ) ){
        if ( p > n ) p = n;
        return ;
    }
    else {
        LL t = pollard_rho( n );
        if ( t == 0 ) return ;
        smallest_prime( t );
        smallest_prime( n/t );
    }
}

int main( ){
    LL ca, n;
    scanf( "%lld", &ca );
    while ( ca-- ){
        scanf( "%lld", &n );
        if ( miller_rabin( n ) )
            printf( "Prime\n" );
        else {
            p = n;
            smallest_prime( n );
            printf( "%lld\n", p );
        }
    }
}

```

1.14 Mobius反演

```

//checked by zju3435
#include <numeric>
#include <algorithm>
using namespace std;
typedef long long LL;
#define N 1000008
int size = 0, prime[N], mark[N] = { 0 };
int mobius[N], mertens[N];

void getPrime(){
    mobius[0] = 0;
    mobius[1] = 1;
    for (int i = 2; i < N; i++){
        if (!mark[i]){
            prime[size++] = i;
            mobius[i] = -1;

```

```

    }
    for (int j = 0; j < size && prime[j]*i < N; j++){
        mark[i*prime[j]] = 1;
        if (i%prime[j] == 0){
            mobius[i*prime[j]] = 0;
            break;
        }
        else mobius[i*prime[j]] = mobius[i] * mobius[prime[j]];
    }
}
partial_sum(mobius, mobius+N, mertens);
}

//return num of coprime pairs in L, W, O(sqrt(N))
LL coprime(LL x, LL y){
    if (x > y) swap(x, y);
    LL ans = 0, u, v;
    for (LL i = x, j; i > 0; i = j){
        u = x/i, v = y/i;
        j = max(x/(u+1), y/(v+1));
        ans += u * v * (mertens[i] - mertens[j]);
    }
    return ans;
}

//return num of coprime triples in L, W, H
LL coprime(LL x, LL y, LL z){
    if (x > y) return coprime(y, x, z);
    if (x > z) return coprime(z, y, x);
    LL ans = 0, u, v, w;
    for (LL i = x, j; i > 0; i = j){
        u = x/i, v = y/i, w = z/i;
        j = max(max(x/(u+1), y/(v+1)), z/(w+1));
        ans += u * v * w * (mertens[i] - mertens[j]);
    }
    return ans;
}

int main(){
    LL x, y, z, ans;
    getPrime();
    while (scanf("%lld%lld%lld", &x, &y, &z) != EOF){
        x--; y--; z--;
        ans = 3;
        ans += coprime(x, y) + coprime(y, z) + coprime(z, x);
        ans += coprime(x, y, z);
        printf("%lld\n", ans);
    }
}

```

2. 博弈

2.1 nim游戏

2.2 multi-sg游戏

Multi-SG 游戏规定,在符合拓扑原则的前提下,一个单一游戏的后继可以为多个单一游戏。

2.3 anti-sg游戏

桌子上有 N 堆石子,游戏者轮流取石子,每次只能从一堆中取出任意数目的石子,但不能不取。取走最后一个为败。

SJ 定理先手必胜:

(1)游戏的 SG 函数不为 0 且游戏中某个单一游戏的 SG 函数大于 1

(2)游戏的 SG 函数为 0 且游戏中没有单一游戏的 SG 函数大于 1

//checked by pku3480

```
#include <cstdio>
#include <cstring>
int main(){
    int ca, n, i, v, sg, mark;
    scanf("%d", &ca);
    while (ca--){
        scanf("%d", &n);
        sg = mark = 0;
        for (i = 0; i < n; i++){
            scanf("%d", &v);
            if (v > 1) mark = 1;
            sg ^= v;
        }
        if ((sg != 0 && mark) || (sg == 0 && !mark)) puts("John");
        else puts("Brother");
    }
}
```

2.4 every-sg游戏

对于没有结束的单一游戏,必须进行一步决策

定义step

$$\text{step}(u) = \begin{cases} 0 & \text{p状态} \\ \max\{\text{step}(v) + 1\} & \text{sg}(u) > 0 \\ \min\{\text{step}(v) + 1\} & \text{sg}(u) = 0 \end{cases}$$

先手必胜当且仅当单一游戏中最大step为奇数

2.5 nim积

//checked by pku3533

```
#include <cstdio>
```

```
#include <cstring>
```

```
using namespace std;
```

```
int tab[20][20];
```

//初始化

```
void init(){
    int i, j, x, y;
    bool visit[64];
    for (i = 0; i < 16; i++) tab[i][0] = tab[0][i] = 0;
    for (i = 1; i < 16; i++){
        for (j = 1; j < 16; j++){
```



```

        memset(visit, 0, sizeof(visit));
        for (x = 0; x < i; x++)
            for (y = 0; y < j; y++)
                visit[tab[x][y]^tab[x][j]^tab[i][y]] = 1;
        for (x = 0; visit[x]; x++);
        tab[i][j] = x;
    }
}

int nim_multi_power(int x, int y){
    int M, p, s, t, d1, d2, i;
    if (x < 16) return tab[x][y];
    for (i = 0; ; i++){
        if ((1<<(1<<i)) <= x && x < (1<<(1<<(i+1)))) break;
    }
    M = 1<<(1<<i);
    p = x/M;
    s = y/M; t = y%M;
    d1 = nim_multi_power(p, s);
    d2 = nim_multi_power(p, t);
    return M * (d1 ^ d2) ^ nim_multi_power(M>>1, d1);
}

int nim_multi(int x, int y){
    int c1, c2, c3, M, p, q, s, t, i;
    if (x < y) return nim_multi(y, x);
    if (x < 16) return tab[x][y];
    for (i = 0; ; i++){
        if ((1<<(1<<i)) <= x && x < (1<<(1<<(i+1)))) break;
    }
    M = 1<<(1<<i);
    p = x/M; q = x%M;
    s = y/M; t = y%M;
    c1 = nim_multi(p, s);
    c2 = nim_multi(p, t) ^ nim_multi(q, s);
    c3 = nim_multi(q, t);
    return (c1 ^ c2) * M ^ c3 ^ nim_multi_power(M>>1, c1);
}

int main(){
    init();
    int n, x, y, z, ans, tmp;
    while (scanf("%d", &n) != EOF){
        ans = 0;
        while (n--){
            scanf("%d%d%d", &x, &y, &z);
            tmp = nim_multi(x, y);
            ans ^= nim_multi(tmp, z);
        }
        if (ans) puts("No");
        else puts("Yes");
    }
}

```

3. 字符串

3.1 ac自动机多串匹配

```
//root = 0
struct Node{
    int end, fail, next[KIND];
    void init(){
        end = fail = 0;
        memset(next, 0, sizeof(next));
    }
}node[200000];
int size, mark[1008], pnt[1008];
int que[1000000];
char str[100008];

inline int hash(char ch){
    if (ch < 'a') return ch-'A';
    else return ch-'a'+26;
}

void init(){
    node[0].init();
    size = 1;
    memset(pnt, 0, sizeof(pnt));
}

//插入字典树
void insert(char *s, int id){
    int p = 0, q, i;
    for (i = 0; s[i]; i++){
        q = hash(s[i]);
        if (node[p].next[q] == 0){
            node[p].next[q] = size++;
            p = node[p].next[q];
            node[p].init();
        }
        else p = node[p].next[q];
    }
    if (node[p].end == 0) node[p].end = id;
    else pnt[id] = node[p].end;
}

//建立自动机
void build_ac_automation(){
    int i, p, q, r, head = 0, tail = 1;
    node[0].fail = 0;
    que[head] = 0;
    while (head < tail){
        p = que[head++];
        for (i = 0; i < 52; i++){
            if (node[p].next[i] != 0){
                q = node[p].next[i];
                if (p == 0) node[q].fail = 0;
                else{
                    r = node[p].fail;
                    while (r != 0){
                        if (node[r].next[i] != 0){
                            node[q].fail = node[r].next[i];

```

```

        break;
    }
    r = node[r].fail;
}
if (node[r].next[i] != 0)
    node[q].fail = node[r].next[i];
else node[q].fail = 0;
}
que[tail++] = q;
}
}
}

//查询s中匹配了多少个串, mark记录是否匹配
void query(char *s){
    int i, p = 0, q, r;
    memset(mark, 0, sizeof(mark));
    for (i = 0; s[i]; i++){
        q = hash(s[i]);
        while (node[p].next[q] == 0 && p != 0) p = node[p].fail;
        p = node[p].next[q];
        p = (p == 0 ? 0 : p);
        r = p;
        while (r != 0 && node[r].end > 0){
            mark[node[r].end] = 1;
            node[r].end = 0;
            r = node[r].fail;
        }
    }
}

int main(){
    int i, n;
    char patt[2048];
    while (scanf("%s", str) != EOF){
        init();
        scanf("%d", &n);
        for (i = 1; i <= n; i++){
            scanf("%s", patt);
            insert(patt, i);
        }
        build_ac_automation();
        query(str);
        for (i = 1; i <= n; i++){
            if (mark[i] || (pnt[i] != 0 && mark[pnt[i]])) puts("Y");
            else puts("N");
        }
    }
}

```

3.2 字符串最小循环表示

```

//返回最小循环表示的位置
//注意tar数组是原来字符串的2倍
int minimum_expression( ){
    int i = 0, j = 1, k = 0;
    while ( i < size && j < size && k < size ){
        if ( tar[i+k] == tar[j+k] ) k++;
        else {

```

```

        if ( tar[i+k] > tar[j+k] ){
            i = i+k+1;
            if ( i == j ) j++;
        }
        else {
            j = j+k+1;
            if ( i == j ) j++;
        }
        k = 0;
    }
}
i = MIN( i, j );
return i;
}

```

3.3 KMP算法

```

//计算fail数组
void make_fail(char *str, int *fail){
    int i = 1, j = 0;
    for ( ; i <= len; i++, j++){
        fail[i] = j;
        while (j > 0 && str[i] != str[j]) j = fail[j];
    }
}

//匹配
void kmp(char *pattern, char *text, int *fail, bool *mark){
    int i, j;
    for (i = 1, j = 1; i <= len; i++){
        while (j > 0 && pattern[j] != text[i]) j = fail[j];
        if (i == len){
            j = fail[j];
        }
        j++;
    }
}

```

3.4 Suffix Array 倍增算法

```

int len, ll, sa1[N], sa2[N], rank1[N], rank2[N], height[N], h[N][20];

//比较函数
inline int cmp( int x, int y ){
    return str[x] < str[y];
}

//求suffix array
void create_suffix_array( ){
    int i, k, *s1 = sa1, *s2 = sa2, *r1 = rank1, *r2 = rank2;
    for ( i = 0; i < len; i++ ) s1[i] = i;
    sort( s1, s1+len, cmp );
    for ( r1[s1[0]] = 0, i = 1; i < len; i++ ){
        if ( str[s1[i]] == str[s1[i-1]] ) r1[s1[i]] = r1[s1[i-1]];
        else r1[s1[i]] = r1[s1[i-1]]+1;
    }
    for ( k = 1; k < len && r1[s1[len-1]] < len-1; k <= 1 ){
        for ( i = 0; i < len; i++ ) r2[r1[s1[i]]] = i;
        for ( i = len-1; i >= 0; i-- )
            if ( k <= s1[i] )
                s2[r2[r1[s1[i]]-k]]-- = s1[i]-k;
    }
}

```

```

        for ( i = len-k; i < len-(k>>1); i++ ) s2[r2[r1[i]]] = i;
        swap( s1, s2 );
        for ( r2[s1[0]] = 0, i = 1; i < len; i++ ){
            if ( r1[s1[i]] != r1[s1[i-1]]
                || r1[s1[i]+k] != r1[s1[i-1]+k] )
                r2[s1[i]] = r2[s1[i-1]]+1;
            else r2[s1[i]] = r2[s1[i-1]];
        }
        swap( r1, r2 );
    }
    if ( s1 != sa1 ) for ( i = 0; i < len; i++ ) sa1[i] = s1[i];
    if ( r1 != rank1 ) for ( i = 0; i < len; i++ ) rank1[i] = r1[i];
}

//计算高度数组
void cal_height( ){
    int i, j, k;
    for ( i = k = 0; i < len; i++ ){
        if ( rank1[i] == 0 ) rank2[i] = 0;
        else{
            for ( j = sa1[rank1[i]-1]; str[i+k] == str[j+k]; k++ );
            rank2[i] = k;
            if ( k > 0 ) k--;
        }
    }
    for ( i = 0; i < len; i++ ) height[i] = rank2[sa1[i]];
}

//rmq初始
void rmq_init( ){
    int i, j, l;
    for ( i = 0; i < len; i++ ) h[i][0] = height[i];
    for ( j = l = 1; l*2 <= len; j++, l <= 1 )
        for ( i = 0; i <= len-l*2; i++ )
            h[i][j] = MIN( h[i][j-1], h[i+l][j-1] );
}

//rmq查询 s+1, t
inline int rmq_query( int left, int right ){
    int j = 0, l = 1;
    while ( l*2 <= right-left+1 ){
        l <= 1;
        j++;
    }
    return MIN( h[left][j], h[right-l+1][j] );
}

```

3.5 Suffix Array DC3算法

```

const int maxn=210000;
char s[maxn];
int len,k;
int sa[maxn],rank[maxn],h[maxn],height[maxn];
int num[maxn];

inline bool leq(int a1, int a2, int b1, int b2){
    return (a1 < b1 || a1 == b1 && a2 <= b2);
}

inline bool leq(int a1, int a2, int a3, int b1, int b2, int b3){

```

```

        return(a1 < b1 || a1 == b1 && leq(a2, a3, b2, b3));
    }

static void radixPass(int* a, int* b, int* r, int n, int K){
    int* c = new int[K + 1];
    for(int i = 0; i <= K; i++) c[i] = 0;
    for(int i = 0; i < n; i++) c[r[a[i]]]++;
    for(int i = 0, sum = 0; i <= K; i++){
        int t = c[i]; c[i] = sum; sum += t;
    }
    for(int i = 0; i < n; i++) b[c[r[a[i]]]] = a[i];
    delete [] c;
}

void suffixArray(int* T, int* SA, int n, int K){
    int n0 = (n + 2) / 3, n1 = (n + 1) / 3, n2 = n / 3, n02 = n0 + n2;
    int* R = new int[n02 + 3]; R[n02] = R[n02+1] = R[n02 + 2] = 0;
    int* SA12 = new int[n02+3]; SA12[n02] = SA12[n02+1] = SA12[n02+2] = 0;
    int* R0 = new int[n0];
    int* SA0 = new int[n0];
    for(int i = 0, j = 0; i < n + (n0 - n1); i++) if(i % 3 != 0) R[j++] = i;
    radixPass(R, SA12, T + 2, n02, K);
    radixPass(SA12, R, T + 1, n02, K);
    radixPass(R, SA12, T, n02, K);
    int name = 0, c0 = -1, c1 = -1, c2 = -1;
    for(int i = 0; i < n02; i++){
        if(T[SA12[i]] != c0 || T[SA12[i]+1] != c1 || T[SA12[i]+2] != c2){
            name++; c0 = T[SA12[i]]; c1 = T[SA12[i]+1]; c2 = T[SA12[i]+2];
        }
        if(SA12[i] % 3 == 1) { R[SA12[i] / 3] = name; }
        else{ R[SA12[i] / 3 + n0] = name; }
    }
    if(name < n02){
        suffixArray(R, SA12, n02, name);
        for(int i = 0; i < n02; i++) R[SA12[i]] = i + 1;
    }
    else for(int i = 0; i < n02; i++) SA12[R[i] - 1] = i;
    for(int i = 0, j = 0; i < n02; i++) if(SA12[i] < n0) R0[j++] = 3 * SA12[i];
    radixPass(R0, SA0, T, n0, K);
    for(int p = 0, t = n0 - n1, k = 0; k < n; k++){
#define GetI() (SA12[t] < n0 ? SA12[t] * 3 + 1 : (SA12[t] - n0) * 3 + 2)
        int i = GetI();
        int j = SA0[p];
        if(SA12[t] < n0 ?
            leq(T[i], R[SA12[t] + n0], T[j], R[j / 3]) :
            leq(T[i], T[i+1], R[SA12[t]-n0+1], T[j], T[j+1], R[j/3+n0]))
        {
            SA[k] = i; t++;
            if(t == n02)
                for(k++; p < n0; p++, k++) SA[k] = SA0[p];
        }
        else{
            SA[k] = j;
            if(++p == n0)for(k++; t < n02; t++, k++) SA[k] = GetI();
        }
    }
    delete [] R; delete [] SA12; delete [] SA0; delete [] R0;
}

```

4. 经典动态规划

4.1 字符串编辑距离

```
//增删改使得a串和b串相等
//checked by spoj6219
#define MIN(a, b) ((a) < (b) ? (a) : (b))
#define N 2048
int m, n, dp[2][N];
char str1[N], str2[N];

void DP(){
    int i, j, pre, cur, u, v;
    pre = 0, cur = 1;
    m = strlen(str1+1);
    n = strlen(str2+1);
    for (i = 0; i <= n; i++) dp[0][i] = i;
    for (i = 1; i <= m; i++){
        dp[cur][0] = i;
        for (j = 1; j <= n; j++){
            u = dp[pre][j]+1;
            v = dp[cur][j-1]+1;
            if (str1[i] == str2[j])
                dp[cur][j] = MIN(dp[pre][j-1], MIN(u, v));
            else
                dp[cur][j] = MIN(dp[pre][j-1]+1, MIN(u, v));
        }
        pre ^= 1; cur ^= 1;
    }
    printf("%d\n", dp[pre][n]);
}

int main(){
    int ca;
    scanf("%d", &ca);
    while (ca--){
        scanf("%s%s", str1+1, str2+1);
        DP();
    }
}
```

4.2 背包问题

```
#define N 256
#define M 100000
int n, vi[N], wi[N], ci[N];
int s, dp[M];

// 0/1背包
void knapsack01(){
    memset(dp, -1, sizeof(dp));
    dp[0] = 0;
    for (int i = 0; i < n; i++){
        for (int j = s; j-wi[i] >= 0; j--){
            if (dp[j-wi[i]] == -1) continue;
            if (dp[j] == -1 || dp[j] < dp[j-wi[i]] + vi[i])
                dp[j] = dp[j-wi[i]] + vi[i];
        }
    }
}
```

```
// 完全背包
void knapsackComplete(){
    int i, j;
    memset(dp, -1, sizeof(dp));
    dp[0] = 0;
    for (i = 0; i < n; i++){
        for (j = 0; j+wi[i] <= s; j++){
            if (dp[j] == -1) continue;
            if (dp[j+wi[i]] == -1 || dp[j+wi[i]] < dp[j] + vi[i])
                dp[j+wi[i]] = dp[j] + vi[i];
        }
    }
}
```

```
// 多重背包 mnlog(n)
void knapsackMulti(){
    int i, j, k, x, y, z;
    memset(dp, -1, sizeof(dp));
    dp[0] = 0;
    for (i = 0; i < n; i++){
        if (ci[i] == 0) continue;
        for (j = 0; ci[i]-(1<<j)+1 > 0; j++){
            j--;
            for (k = 0; k <= j; k++){
                if (k != j) x = 1<<k;
                else x = ci[i]-(1<<k)+1;
                for (y = s; y-x*wi[i] >= 0; y--){
                    z = y-x*wi[i];
                    if (dp[z] == -1) continue;
                    if (dp[y] == -1 || dp[y] < dp[z] + x*vi[i])
                        dp[y] = dp[z] + x*vi[i];
                }
            }
        }
    }
}
```

//二维费用背包
 //二维费用的背包问题是指对于每件物品，具有两种不同的费用；选择这件物品必须同时付出这两种代价；
 //对于每种代价都有一个可付出的最大值（背包容量）。问怎样选择物品可以得到最大的价值。
 //f[i][v][u]=max{f[i-1][v][u], f[i-1][v-a[i]][u-b[i]]+w[i]}

//分组背包
 //有N件物品和一个容量为V的背包。第i件物品的费用是c[i]，价值是w[i]。这些物品被划分为若干组，每
 //组中的物品互相冲突，最多选一件。求解将哪些物品装入背包可使这些物品的费用总和不超过背包容量，
 //且价值总和最大。
 //f[k][v]表示前k组物品花费费用v能取得的最大权值，则有
 //f[k][v]=max{f[k-1][v], f[k-1][v-c[i]]+w[i] | 物品i属于组k}

//差值背包DP

4.3 最长上升公共子序列 n^2

```
int n, m;
int seq1[N], seq2[N];
int dp[N], pre[N];

//longest common increasing subsequence of sequence 1 and 2
void lcis(){
    int i, j, tmp;
    memset(dp, 0, sizeof(dp));
```



```

memset(pre, 0, sizeof(pre));
for (i = 1; i <= n; i++){
    for (j = i-1; j > 0; j--){
        if (seq1[i] == seq1[j]) {
            pre[i] = j;
            break;
        }
    }
}
for (i = 1; i <= m; i++){
    tmp = 0;
    for (j = 1; j <= n; j++){
        if (seq1[j] < seq2[i] && tmp < dp[j]) tmp = dp[j];
        if (seq1[j] == seq2[i]){
            if (pre[j] != 0 && tmp < dp[pre[j]]) dp[j] = dp[pre[j]];
            else dp[j] = tmp+1;
        }
    }
}
for (tmp = 0, i = 1; i <= n; i++) tmp = max(tmp, dp[i]);
printf("%d\n", tmp);
}

```

4.4 最大M子段和 $O(n*m)$

```

//dp[i,j] = MAX(dp[i-1,j], f[j-1]) + val[i];
//f 数组记录分成i段的最优值
#define N 1000008
#define INF 0x3fffffff
int n, m, seq[N];
int dp[N], f[N];

void DP(){
    int i, j, k;
    for (i = 1; i <= n; i++){
        k = min(i, m);
        for (j = 1; j <= k; j++){
            dp[j] = max(dp[j], f[j-1]) + seq[i];
            f[j-1] = max(f[j-1], dp[j-1]);
        }
        f[j-1] = max(f[j-1], dp[j-1]);
    }
    printf("%d\n", f[m]);
}

int main(){
    int i;
    while (scanf("%d%d", &m, &n) != EOF){
        for (i = 1; i <= n; i++){
            dp[i] = f[i] = -INF;
            scanf("%d", seq+i);
        }
        DP();
    }
}

```

4.5 连通性状态压缩DP

```

//check by fzu1977
//ternary to encode state
//state is a rotation
//0:no brace 1: left brace 2:right brace

```

```

typedef long long LL;
#define N 16
int d[] = { 1, 3, 9, 27, 81, 243, 729, 2187, 6561, 19683, 59049, 177147, 531441,
1594323 };
int digit[16], temp[16], stk[16];
short visit[2][1594323] = { {0}, {0} };
short itr = 1;
LL dp[2][1594323];
int que[2][40000];
int rn, cn, cur, nxt, sq[2];
char mp[N][N];

void ternary(int val, int seq[]){
    for (int i = 0; i <= cn; ++i){
        seq[i] = val%3;
        val /= 3;
    }
}

//return the position matches left brace
int matchLeft(int seq[], int pos){
    int i, j = 0;
    for (i = 0; i <= cn; ++i){
        if (seq[i] == 1) stk[j++] = i;
        else if (seq[i] == 2){
            if (stk[j-1] == pos) return i;
            j--;
        }
    }
    return -1;
}

//return the position matches right brace
int matchRight(int seq[], int pos){
    int i, j = 0;
    for (i = cn; i > 0; --i){
        if (seq[i] == 2) ++j;
        else if (seq[i] == 1) j--;
        if (j < 0) return i;
    }
    return -1;
}

//change the value
inline void set(int s, LL delta){
    if (visit[nxt][s] < itr){
        visit[nxt][s] = itr;
        dp[nxt][s] = 0;
        que[nxt][sq[nxt]++] = s;
    }
    dp[nxt][s] += delta;
}

//9 transmissions
LL DP(){
    int i, j, k, ex, ey, pos, u, v;
    LL ans = 0, delta;
    for (i = 0; i < rn; ++i){
        for (j = 0; j < cn; ++j)
            if (mp[i][j] == '0'){

```

```

        ex = i; ey = j;
    }
}
dp[0][0] = 1;
cur = 0, nxt = 1;
que[cur][0] = 0;
sq[cur] = 1;
for (i = 0; i < rn; ++i){
    for (j = 0; j < cn; ++j, ++itr){
        sq[nxt] = 0;
        for (k = 0; k < sq[cur]; k++){
            u = que[cur][k];
            delta = dp[cur][u];
            if (j == 0 && u%3 != 0) continue;
            digit[0] = u%3;
            digit[1] = u/3%3;
            if (mp[i][j] == 'X'){
                if (digit[0] == 0 && digit[1] == 0){
                    v = u/3;
                    set(v, delta);
                }
            }
            else {
                if (mp[i][j] == '*'){
                    if (digit[0] == 0 && digit[1] == 0){
                        v = u/3;
                        set(v, delta);
                    }
                }
                if (digit[0] == 0 && digit[1] == 0){
                    v = u/3 + 2 + d[cn];
                    set(v, delta);
                }
                else if (digit[0] == 1 && digit[1] == 1){
                    ternary(u, digit);
                    pos = matchLeft(digit, 1);
                    v = (u - 2*d[pos])/3 + d[pos-1];
                    v = v - v%3;
                    set(v, delta);
                }
                else if (digit[0] == 2 && digit[1] == 2){
                    ternary(u, digit);
                    pos = matchRight(digit, 1);
                    v = (u - d[pos])/3 + 2*d[pos-1];
                    v = v - v%3;
                    set(v, delta);
                }
                else if (digit[0] == 2 && digit[1] == 1){
                    v = u/3 - 1;
                    set(v, delta);
                }
                else if (digit[0] == 1 && digit[1] == 2){
                    if (u == 7){
                        if ((i >= ex && j >= ey) || (i > ex)){
                            ans += delta;
                        }
                    }
                }
            }
            else if (digit[0] > 0 && digit[1] == 0){
                v = u/3 + d[cn]*digit[0];

```

```

        set(v, delta);
        v = u/3 + digit[0];
        set(v, delta);
    }
    else if (digit[0] == 0 && digit[1] > 0){
        v = u/3 - (u/3%3) + d[cn]*digit[1];
        set(v, delta);
        v = u/3;
        set(v, delta);
    }
}
}
cur ^= 1; nxt ^= 1;
}
return ans;
}
}

int main(){
    int ca, t, i;
    scanf("%d", &ca);
    for (t = 1; t <= ca; ++t){
        scanf("%d%d", &rn, &cn);
        for (i = 0; i < rn; i++) scanf("%s", mp[i]);
        printf("Case %d: %lld\n", t, DP());
    }
}

```

4.6 最大公共矩形，直方图最大矩形

```

//checked by zju3367 O(n^3)
#include <cstdio>
#include <cstring>
struct anonymous {
    int x, y, l, r, t, b, s;
} tmp, ans;
char a[150][150], b[50][50];
int c[50], l[50], r[50];

int main(){
    bool flag;
    int m1, n1, m2, n2;
    while (scanf("%d%d", &m1, &n1) != EOF){
        memset(a, '#', sizeof(a));
        for (int i = 0; i < m1; ++i){ scanf("%s", a[50 + i] + 50); }
        scanf("%d%d", &m2, &n2);
        for (int i = 0; i < m2; ++i){ scanf("%s", b[i]); }
        flag = false;
        ans.s = 0;
        for (tmp.x = -m2 + 1; tmp.x < m1; ++tmp.x){
            for (tmp.y = -n2 + 1; tmp.y < n1; ++tmp.y){
                memset(c, 0, sizeof(c));
                for (int i = 0; i < m2; ++i){
                    for (int j = 0; j < n2; ++j) {
                        if (a[50+i+tmp.x][50+j+tmp.y] != b[i][j]){
                            c[j] = 0;
                        }
                        else {
                            ++c[j];
                        }
                    }
                }
            }
        }
    }
}

```

```

    }

    for (int j = 0; j < n2; ++j) {
        int k = j - 1;
        while (k >= 0 && c[k] >= c[j]){
            k = l[k];
        }
        l[j] = k;
    }
    for (int j = n2 - 1; j >= 0; --j){
        int k = j + 1;
        while (k < n2 && c[k] >= c[j]){
            k = r[k];
        }
        r[j] = k;
    }
    for (int j = 0; j < n2; ++j){
        tmp.l = l[j] + 1;
        tmp.r = r[j];
        tmp.t = i - c[j] + 1;
        tmp.b = i + 1;
        tmp.s = (tmp.r - tmp.l) * (tmp.b - tmp.t);
        if (tmp.s > ans.s){ ans = tmp; }
        else if (tmp.s == ans.s){ flag = true; }
    }
}

}

}
if (ans.s == 0) { puts("0 0"); }
else { printf("%d %d\n%d %d\n%d %d\n", ans.b - ans.t, ans.r - ans.l, ans.x +
ans.t + 1, ans.y + ans.l + 1, ans.t + 1, ans.l + 1); }
}
return 0;
}

```

4.7 四边形DP

```

//checked by hdu3369 dp[n] = min{ dp[i] + w[i+1, n] }
#define MAX(a, b) ((a) > (b) ? (a) : (b))
#define MIN(a, b) ((a) < (b) ? (a) : (b))
typedef long long LL;
const LL INF = 1000000000000000001ll;
const int N = 65536;
struct Node {
    int x, y;
    Node(){}
    Node(int _x, int _y): x(_x), y(_y){}
    bool operator<(const Node &v) const {
        if (x != v.x) return x < v.x;
        return y < v.y;
    }
}node[N];
int n, m, top, stk[N], pos[2][N];
LL dp[2][N], yy[N];

void DP(){
    int i, j, k, cur = 0, nxt = 1;
    LL ans, tmp;
    memset(dp, 0, sizeof(dp));
    for (i = 1; i <= n; i++){

```

```

        dp[0][i] = yy[1]*node[i].x;
        pos[0][i] = 0;
    }
    ans = dp[0][n];
    for (i = 2; i <= m; i++){
        for (j = i; j <= n; j++) dp[nxt][j] = INF;
        //I was wrong here
        for (j = MAX(pos[cur][n], i-1); j < n; j++){
            tmp = dp[cur][j] + yy[j+1]*node[n].x;
            if (dp[nxt][n] > tmp){
                dp[nxt][n] = tmp; pos[nxt][n] = j;
            }
        }
        for (j = n-1; j >= i; j--){
            //I was wrong here
            for (k = MAX(pos[cur][j], i-1); k <= pos[nxt][j+1] && k < j; k++){
                tmp = dp[cur][k] + yy[k+1] * node[j].x;
                if (dp[nxt][j] > tmp){
                    dp[nxt][j] = tmp; pos[nxt][j] = k;
                }
            }
        }
        ans = MIN(ans, dp[nxt][n]);
        cur ^= 1; nxt ^= 1;
    }
    cout << ans << endl;
}

void init(){
    int i, j;
    top = 0;
    for (i = 1; i <= n; i++){
        while (top > 0){
            if (node[stk[top]].y <= node[i].y)
                top--;
            else break;
        }
        stk[++top] = i;
    }
    for (i = 1, j = 1; i <= top; i++){
        while (j <= stk[i]){
            yy[j] = node[stk[i]].y;
            j++;
        }
    }
}

int main(){
    int i, u, v;
    while (scanf("%d%d", &n, &m) != EOF){
        for (i = 1; i <= n; i++){
            scanf("%d%d", &u, &v);
            node[i] = Node(u, v);
        }
        sort(node+1, node+1+n);
        init();
        DP();
    }
}

```

5. 数据结构

5.1 用树状数组解决区间查询问题

```
#include <cstdio>
#define LOWBIT(x) ((x)&(-(x)))
const int MAXN = 1024;
int B[MAXN], C[MAXN];

void bit_update(int *a, int p, int d) {
    for ( ; p && p < MAXN ; p += LOWBIT(p)) a[p] += d;
}

int bit_query(int *a, int p) {
    int s = 0;
    for ( ; p ; p -= LOWBIT(p)) s += a[p];
    return s;
}

void bit_update2(int *a, int p, int d) {
    for ( ; p ; p -= LOWBIT(p)) a[p] += d;
}

int bit_query2(int *a, int p) {
    int s = 0;
    for ( ; p && p < MAXN ; p += LOWBIT(p)) s += a[p];
    return s;
}

inline void _insert(int p, int d) {
    bit_update(B, p, p*d);
    bit_update2(C, p-1, d);
}

inline int _query(int p) {
    return bit_query(B, p) + bit_query2(C, p) * p;
}

inline void insert_seg(int a, int b, int d) {
    _insert(a-1, -d);
    _insert(b, d);
}

inline int query_seg(int a, int b) {
    return _query(b) - _query(a-1);
}

int main() {
    int com, a, b, c;
```

```

while (scanf("%d%d%d",&com,&a,&b) != EOF) {
    a += 2; b += 2;           //防止出现负数
    if (com == 0) {           //更新
        scanf("%d",&c);
        insert_seg(a, b, c);
    } else {                   //查询
        printf("%d\n",query_seg(a,b));
    }
}
return 0;
}

```

5.2 Range minimum query

```

#define N 1<<18
#define MIN(a, b) ((a) < (b) ? (a) : (b))
int size, h[N][18], val[N];

void rmq_init(){
    int i, j, l;
    for (i = 0; i < size; i++) h[i][0] = val[i];
    for (j = l = 1; l*2 <= size; j++, l <= 1){
        for (i = 0; i <= size-l*2; i++)
            h[i][j] = MIN(h[i][j-1], h[i+l][j-1]);
    }
}

inline int rmq_query(int start, int end){
    int j = 0, l = 1;
    while (2*l <= end-start+1){
        j++;
        l <= 1;
    }
    return MIN(h[start][j], h[end-l+1][j]);
}

```

5.3 划分树

```

#define N 100008
int n, m;
int seq[N], ind[N], next[N], pos[N];
int cntL[20][N];

//比较函数
inline int cmp(int x, int y){ return seq[x] < seq[y]; }

//建树, cntL记录该区间有多少个数走到左子树
void build(int l, int r, int head, int dep){
    if (l == r){
        cntL[dep][l] = cntL[dep][l-1];
        return ;
    }
    int mid = (l+r)>>1;
    int hl = 0, hr = 0, tl = 0, tr = 0;
    for (int i = head, j = l; i != -1; i = next[i], j++){
        cntL[dep][j] = cntL[dep][j-1];
        if (pos[i] <= mid){

```



```

        next[tl] = i;
        tl = i;
        if (hl == 0) hl = i;
        cntL[dep][j]++;
    }
    else{
        next[tr] = i;
        tr = i;
        if (hr == 0) hr = i;
    }
}
next[tl] = next[tr] = -1;
build(l, mid, hl, dep+1);
build(mid+1, r, hr, dep+1);
}

//返回下标
//查询区间[ql, qr]第kth大元素, 递归到dep, 树的区间为[left, right]
int query(int left, int right, int ql, int qr, int kth, int dep){
    if (left == right) return ind[left];
    int mid = (left+right) >> 1;
    if (cntL[dep][qr] - cntL[dep][ql-1] >= kth){
        return query(left, mid, \
            left+cntL[dep][ql-1]-cntL[dep][left-1], \
            left+cntL[dep][qr]-cntL[dep][left-1]-1, \
            kth, dep+1);
    }
    else{
        return query(mid+1, right,
            mid+1+ql-left-(cntL[dep][ql-1]-cntL[dep][left-1]), \
            mid+qr+1-left-(cntL[dep][qr]-cntL[dep][left-1]), \
            kth-(cntL[dep][qr]-cntL[dep][ql-1]), dep+1);
    }
}

int main(){
    int i, u, v, w;
    while (scanf("%d%d", &n, &m) != EOF){
        for (i = 1; i <= n; i++){
            scanf("%d", seq+i);
            ind[i] = i;
        }
        //初始化
        sort(ind+1, ind+1+n, cmp);
        for (i = 1; i <= n; i++){
            pos[ind[i]] = i;
            next[i] = i+1;
        }
        next[n] = -1;
        build(1, n, 1, 0);
        while (m--){
            scanf("%d%d%d", &u, &v, &w);
            i = query(1, n, u, v, w, 0);
            printf("%d\n", seq[i]);
        }
    }
}

```

5.4 树链剖分模板

```
//主要是建树 checked by toj3701
//基本树链剖分: dfs+线段树 complexity:  $(\log(n))^2$ 
#define N 30008
#define INF 1000000000
#define MAX(a, b) ((a) > (b) ? (a) : (b))
#define LC(x) (x<<1)
#define RC(x) (x<<1|1)
//vn:点的个数
//size:图的边数
//mp:head of link list
//son:子树节点个数
//seq:节点的dfs顺序
//_seq:节点在dfs序中的位置
//level:树链的大小
//_level:节点位于树链的第几层
//start:树链的开始位置
int vn, size, mp[N], visit[N], wei[N];
int pnt[N], son[N];
int sizeS, seq[N], _seq[N];
int sizeL, level[N], _level[N], start[N], sl[N];

//node for the segment tree
struct Node{
    int l, r;
    int sum, val;
}tree[N*32];
//edges of tree
struct Edge{
    int v, next;
    Edge(){}
    Edge(int _v, int _next): v(_v), next(_next){}
}edge[N<<1];

inline void add_edge(int u, int v){
    edge[size] = Edge(v, mp[u]); mp[u] = size++;
    edge[size] = Edge(u, mp[v]); mp[v] = size++;
}

//dfs1: 找出子树大小
void dfs1(int u){
    int i, v;
    visit[u] = son[u] = 1;
    for (i = mp[u]; i != -1; i = edge[i].next){
        v = edge[i].v;
        if (visit[v]) continue;
        pnt[v] = u; dfs1(v); son[u] += son[v];
    }
}

//dfs2: 找出重边
void dfs2(int u, int l){
    int i, v, x = -1, y;
    visit[u] = 1;
    _seq[u] = sizeS; seq[sizeS++] = u;
    level[l]++; _level[u] = l;
    for (i = mp[u]; i != -1; i = edge[i].next){
        if (visit[edge[i].v]) continue;
        if (x < son[edge[i].v]){
            x = son[edge[i].v];
            y = edge[i].v;
        }
    }
}
```

```

        x = son[edge[i].v]; y = edge[i].v;
    }
}
if (x == -1) return ;
dfs2(y, l);
for (i = mp[u]; i != -1; i = edge[i].next){
    if (visit[edge[i].v]) continue;
    sizeL++;
    dfs2(edge[i].v, sizeL);
}
}

//build segtree
//org: the start position of the segtree
void build(int org, int id, int l, int r){
    tree[org+id].l = l; tree[org+id].r = r;
    if (l == r){
        tree[org+id].val = tree[org+id].sum = wei[seq[l]];
        return ;
    }
    int mid = (l+r)>>1;
    build(org, LC(id), l, mid);
    build(org, RC(id), mid+1, r);
    tree[org+id].sum = tree[org+LC(id)].sum + tree[org+RC(id)].sum;
    tree[org+id].val = MAX(tree[org+LC(id)].val, tree[org+RC(id)].val);
}

void change(int org, int id, int p, int v){
    if (p <= tree[org+id].l && tree[org+id].r <= p){
        tree[org+id].val = tree[org+id].sum = v;
        return ;
    }
    int mid = (tree[org+id].l + tree[org+id].r)>>1;
    if (p <= mid) change(org, LC(id), p, v);
    if (p > mid) change(org, RC(id), p, v);
    tree[org+id].sum = tree[org+LC(id)].sum + tree[org+RC(id)].sum;
    tree[org+id].val = MAX(tree[org+LC(id)].val, tree[org+RC(id)].val);
}

int queryMax(int org, int id, int l, int r){
    if (l <= tree[org+id].l && tree[org+id].r <= r) return tree[org+id].val;
    int mid = (tree[org+id].l + tree[org+id].r)>>1;
    int a = -INF, b = -INF;
    if (l <= mid) a = queryMax(org, LC(id), l, r);
    if (r > mid) b = queryMax(org, RC(id), l, r);
    return MAX(a, b);
}

int querySum(int org, int id, int l, int r){
    if (l <= tree[org+id].l && tree[org+id].r <= r)
        return tree[org+id].sum;
    int mid = (tree[org+id].l + tree[org+id].r)>>1, ret = 0;
    if (l <= mid) ret += querySum(org, LC(id), l, r);
    if (r > mid) ret += querySum(org, RC(id), l, r);
    return ret;
}

void init(){
    int i, j;
    memset(visit, 0, sizeof(visit));
}

```

```

memset(level, 0, sizeof(level));
pnt[1] = 0;
dfs1(1);
memset(visit, 0, sizeof(visit));
sizeL = sizeS = 1;
dfs2(1, sizeL);
for (sl[0] = 0, i = 1, j = 0; i <= sizeL; i++){
    start[i] = j*4;
    sl[i] = level[i] + sl[i-1];
    build(start[i], 1, j+1, j+level[i]);
    j += level[i];
}

int main(){
    char cmd[16];
    int i, q, u, v, ans, tmp, x, y, a, b;
    while (scanf("%d", &vn) != EOF){
        size = 0;
        memset(mp, -1, sizeof(mp));
        for (i = 1; i < vn; i++){
            scanf("%d%d", &u, &v);
            add_edge(u, v);
        }
        for (i = 1; i <= vn; i++) scanf("%d", wei+i);
        init();
        scanf("%d", &q);
        while (q--){
            scanf("%s%d%d", cmd, &u, &v);
            if (cmd[1] == 'M'){
                ans = -INF;
                while (_level[u] != _level[v]){
                    if (_level[u] < _level[v]) swap(u, v);
                    x = sl[_level[u]] - level[_level[u]] + 1;
                    y = _seq[u];
                    tmp = queryMax(start[_level[u]], 1, x, y);
                    ans = MAX(ans, tmp);
                    u = pnt[seq[x]];
                }
                if (_seq[u] > _seq[v]) swap(u, v);
                tmp = queryMax(start[_level[u]], 1, _seq[u], _seq[v]);
                ans = MAX(ans, tmp);
                printf("%d\n", ans);
            }
            if (cmd[1] == 'S'){
                ans = 0;
                while (_level[u] != _level[v]){
                    if (_level[u] < _level[v]) swap(u, v);
                    x = sl[_level[u]] - level[_level[u]] + 1;
                    y = _seq[u];
                    tmp = querySum(start[_level[u]], 1, x, y);
                    ans += tmp;
                    u = pnt[seq[x]];
                }
                if (_seq[u] > _seq[v]) swap(u, v);
                tmp = querySum(start[_level[u]], 1, _seq[u], _seq[v]);
                ans += tmp;
                printf("%d\n", ans);
            }
            if (cmd[1] == 'H') change(start[_level[u]], 1, _seq[u], v);
        }
    }
}

```

```

    }
}

```

5.5 n维矩形切割

```

#define DIM 16
#define MOD 14121413LL
typedef long long LL;
//bot 记录下端点 top 记录上端点
struct Cube{
    int bot[DIM], top[DIM];
    Cube(){ }
};
int n, dim, s1, s2;
Cube seq[1<<7], cube[1<<15], temp[1<<15];

//判断相交
bool isIntersect(Cube &p, Cube &q){
    int i;
    for (i = 0; i < dim; i++){
        if (p.bot[i] >= q.top[i] || p.top[i] <= q.bot[i])
            return 0;
    }
    return 1;
}

//add into temp
void insD(Cube t){
    for (int i = 0; i < dim; i++) if (t.bot[i] >= t.top[i]) return ;
    temp[s2++] = t;
}

//partition
void divide(Cube p, Cube q){
    Cube t1 = p, t2;
    for (int i = 0; i < dim; i++){
        if (t1.bot[i] <= q.bot[i] && q.bot[i] <= t1.top[i]){
            t2 = t1;
            t2.top[i] = q.bot[i];
            insD(t2);
            t1.bot[i] = q.bot[i];
        }
        if (t1.bot[i] <= q.top[i] && t1.top[i] >= q.top[i]){
            t2 = t1;
            t2.bot[i] = q.top[i];
            insD(t2);
            t1.top[i] = q.top[i];
        }
    }
}

//add a new cube
void add(Cube cb){
    int i;
    s2 = 0;
    for (i = 0; i < s1; i++){
        if (isIntersect(cube[i], cb)) divide(cube[i], cb);
        else temp[s2++] = cube[i];
    }
    for (i = s1 = 0; i < s2; i++) cube[s1++] = temp[i];
    cube[s1++] = cb;
}

```

```

}

void solve(){
    int i, j;
    LL ans = 0, vol;
    s1 = s2 = 0;
    for (i = 0; i < n; i++){
        for (j = 0; j < dim; j++) scanf("%d", &(seq[i].bot[j]));
        for (j = 0; j < dim; j++) scanf("%d", &(seq[i].top[j]));
        add(seq[i]);
    }
    for (i = 0; i < s1; i++){
        vol = 1;
        for (j = 0; j < dim; j++)
            vol = vol * ((LL)cube[i].top[j] - (LL)cube[i].bot[j]) % MOD;
        ans = (ans + vol) % MOD;
    }
    printf("%lld\n", ans);
}

```

5.6 左偏树

```

//checked by 3406
#define N 1000008
int r, n, m, size;
int cnt[100], seq[N/100];
struct LeftTree{
    int key, dist, cnt;
    LeftTree *lc, *rc;
    inline void init(int _key){
        key = _key;
        dist = 0;
        cnt = 1;
        lc = rc = NULL;
    }
    inline void up(){
        cnt = 1;
        if (lc) cnt += lc->cnt;
        if (rc) cnt += rc->cnt;
    }
}node[N], *tree[200], *que[N/10], *play[2];

inline LeftTree *merge(LeftTree *a, LeftTree *b){
    if (a == NULL) return b;
    if (b == NULL) return a;
    if (a->key < b->key) swap(a, b);
    a->rc = merge(a->rc, b);
    a->rc->up();
    if (a->lc == NULL) swap(a->lc, a->rc);
    if (a->rc == NULL){
        a->dist = 0;
        a->up();
        return a;
    }
    if (a->lc->dist < a->rc->dist) swap(a->lc, a->rc);
    a->dist = a->rc->dist+1;
    a->up();
    return a;
}

```

```

LeftTree *build(int s){
    LeftTree *ptr;
    int i, j;
    int head = 0, tail = 0;
    for (i = 0; i < s; i++){
        node[size].init(seq[i]);
        que[tail++] = &node[size];
        size++;
    }
    while (tail-head != 1){
        ptr = merge(que[head], que[head+1]);
        head += 2;
        que[tail++] = ptr;
    }
    return que[head];
}
//删除最小节点
inline void remove(LeftTree *&root){
    if (root == NULL) return ;
    LeftTree *ptr1 = root, *ptr2 = merge(root->lc, root->rc);
    ptr1->lc = ptr1->rc = NULL;
    root = ptr2;
}

inline void exchange(LeftTree *&root, int p){
    if (root == NULL) return ;
    LeftTree *ptr1 = root, *ptr2 = merge(root->lc, root->rc);
    ptr1->lc = ptr1->rc = NULL;
    ptr1->key = p;
    root = merge(ptr2, ptr1);
}

int main(){
    char cmd[10];
    int i, j, u, v, pre, cur;
    int p1 = 0, p2 = 0;
    while (scanf("%d", &r) != EOF){
        while (r--){
            scanf("%d%d", &n, &m);
            for (i = 0; i < m; i++) scanf("%d", cnt+i);
            size = 0;
            for (i = 0; i < m; i++){
                for (j = 0; j < cnt[i]; j++) scanf("%d", seq+j);
                tree[i] = build(cnt[i]);
            }
            play[0] = play[1] = NULL;
            cur = 0, pre = 1;
            for (i = 0; i < n; i++){
                scanf("%s", cmd);
                if (cmd[0] == 'T'){
                    scanf("%d", &u);
                    u--;
                    play[cur] = merge(play[cur], tree[u]);
                }
                else if (cmd[0] == 'C'){
                    if (play[cur]->key > play[pre]->key){
                        play[cur] = merge(play[cur], play[pre]);
                        play[pre] = NULL;
                    }
                    else if (play[cur]->key < play[pre]->key){

```

```

        play[pre] = merge(play[pre], play[cur]);
        play[cur] = NULL;
    }
}
else if (cmd[0] == 'L'){
    remove(play[cur]);
}
else if (cmd[0] == 'A'){
    scanf("%d", &u);
    play[cur]->key += u;
}
else if (cmd[0] == 'E'){
    scanf("%d", &u);
    exchange(play[cur], u);
}
cur ^= 1; pre ^= 1;
}
u = 0;
if (play[0] != NULL) u = play[0]->cnt;
v = 0;
if (play[1] != NULL) v = play[1]->cnt;
printf("%d:%d\n", u, v);
if (u >= v) p1++;
else p2++;
}
if (p1 > p2) printf("Hahaha...I win!!\n");
else printf("I will be back!!\n");
}
}

```

5.7 Splay Tree

```

//checked by 3578
#define N 100008
int n, m, SS, seq[N*3];

struct SplayTree{
    struct Node{
        int key, cnt, rev;
        Node *lc, *rc, *pnt;
    }node[N*3], *root, *size;

    void init(int s){
        Node *p = NULL, *q = NULL;
        root = NULL;
        size = node;
        for (int i = 0; i <= s+1; i++){
            p = newNode(i);
            if (q == NULL) q = p;
            else {
                p->lc = q; q->pnt = p; up(p);
                q = p;
            }
        }
        root = q;
        for (int i = 1; i <= s+1; i += 2) splay(&node[i], root);
    }

    inline Node *newNode( int _key ){
        size->key = _key; size->cnt = 1;
        size->rev = 0;
    }
}

```



```

        size->lc = size->rc = size->pnt = NULL;
        return size++;
    }
    inline void down( Node *p ){
        if ( p->rev ){
            if ( p->lc ) p->lc->rev ^= 1;
            if ( p->rc ) p->rc->rev ^= 1;
            swap(p->lc, p->rc);
            p->rev = 0;
        }
    }
    inline void up( Node *p ){
        p->cnt = 1;
        if ( p->lc ) p->cnt += p->lc->cnt;
        if ( p->rc ) p->cnt += p->rc->cnt;
    }
    inline void zig( Node *p, Node *&rt ){
        int mark = 0;
        Node *q = p->pnt;
        if ( q == rt ) mark = 1;
        q->lc = p->rc;
        if ( p->rc ) p->rc->pnt = q;
        p->rc = q;
        p->pnt = q->pnt;
        q->pnt = p;
        if ( p->pnt ){
            if ( p->pnt->lc == q ) p->pnt->lc = p;
            else p->pnt->rc = p;
        }
        if ( mark ) rt = p;
        up( q ); up( p );
    }
    inline void zag( Node *p, Node *&rt ){
        int mark = 0;
        Node *q = p->pnt;
        if ( q == rt ) mark = 1;
        q->rc = p->lc;
        if ( p->lc ) p->lc->pnt = q;
        p->lc = q;
        p->pnt = q->pnt;
        q->pnt = p;
        if ( p->pnt ){
            if ( p->pnt->lc == q ) p->pnt->lc = p;
            else p->pnt->rc = p;
        }
        if ( mark ) rt = p;
        up( q ); up( p );
    }
    inline void splay( Node *p, Node *&rt ){
        Node *q;
        down( p );
        while ( p != rt ){
            if ( p->pnt == rt ){
                if ( p->pnt->lc == p ) zig( p, rt );
                else zag( p, rt );
                break;
            }
            else {
                q = p->pnt->pnt;
                if ( q->lc == p->pnt ){

```

```

        if ( p->pnt->lc == p ){
            zig( p->pnt, rt ); zig( p, rt );
        }
        else {
            zag( p, rt ); zig( p, rt );
        }
    }
    else {
        if ( p->pnt->lc == p ){
            zig( p, rt ); zag( p, rt );
        }
        else {
            zag( p->pnt, rt ); zag( p, rt );
        }
    }
}
up( rt );
}
inline Node *selectKth( int x ){
    if ( root == NULL ) return NULL;
    Node *p = root;
    int y, z = x;
    while ( 1 ){
        down( p );
        if ( p->lc == NULL ) y = 0;
        else y = p->lc->cnt;
        if ( y+1 == x ) break;
        if ( x > y ) p = p->rc;
        else p = p->lc;
        if ( x > y ) x -= (y+1);
    }
    return p;
}
inline Node *get_max(Node *rt){
    Node *p = rt;
    down(p);
    while (p->rc){
        p = p->rc; down(p);
    }
    return p;
}
inline Node *get_min(Node *rt){
    Node *p = rt;
    down(p);
    while (p->lc){
        p = p->lc; down(p);
    }
    return p;
}
inline void flip(int l, int r){
    splay(selectKth(r+1), root);
    splay(selectKth(l-1), root->lc);
    if (root->lc && root->lc->rc) root->lc->rc->rev ^= 1;
}
inline void cut(int l, int r, int c){
    Node *p, *q;
    splay(selectKth(r+1), root);
    splay(selectKth(l-1), root->lc);
    p = root->lc->rc;

```

```

    root->lc->rc = NULL;
    p->pnt = NULL;
    up(root->lc);
    up(root);
    splay(selectKth(c), root);
    q = root->rc;
    root->rc = p;
    p->pnt = root;
    up(root);
    splay(get_max(root), root);
    root->rc = q;
    if (q != NULL) q->pnt = root;
    up(root);
}
inline void insert( int _key ){
    Node *p = root, *q = root;
    if ( root == NULL ){
        root = newNode( _key );
        return ;
    }
    while ( 1 ){
        q = p;
        if ( p->key < _key ){
            if ( p->rc == NULL ){
                p->rc = newNode( _key );
                p = p->rc;
                break;
            }
            else p = p->rc;
        }
        else {
            if ( p->lc == NULL ){
                p->lc = newNode( _key );
                p = p->lc;
                break;
            }
            else p = p->lc;
        }
    }
    p->pnt = q;
    splay( p, root );
    root->pnt = NULL;
}
inline void remove( int _key ){
    Node *p, *q;
    if ( root == NULL ) return ;
    splay( find( _key ), root );
    root->pnt = NULL;
    if ( root->lc ){
        q = root->rc;
        splay( get_max( root->lc ), root->lc );
        p = root->lc, q = root->rc;
        p->rc = q;
        if ( q ) q->pnt = p;
        root = p;
    }
    else root = root->rc;
    if ( root != NULL ){
        root->pnt = NULL;
        up( root );
    }
}

```

```

    }
}
}tree;

int main(){
    char str[16];
    int l, r, c, ca = 0;
    while (scanf("%d%d", &n, &m) != EOF){
        if (n <= 0 && m <= 0) break;
        tree.init(n);
        int i = 0;
        while ( m-- ){
            i++;
            scanf( "%s", str );
            if ( str[0] == 'F' ){
                scanf("%d%d", &l, &r);
                l++, r++;
                tree.flip(l, r);
            }
            else if ( str[0] == 'C' ){
                scanf("%d%d%d", &l, &r, &c);
                if (c > n-(r-l+1) ) while ( 1 );
                l++, r++, c++;
                tree.cut(l, r, c);
            }
        }
        SS = 0;
        tree.print(tree.root);
        for (l = 1; l < n; l++) printf("%d ", seq[l]);
        printf("%d\n", seq[n]);
    }
}

```

5.8 Dynamic Tree: cut-link tree

```

//checked by hdu3216 spoj4155
#define MAXN 10008
#define isRoot(t) (lc[fa[t]] != t && rc[fa[t]] != t) //t是否为splay根
int n, m, stk[MAXN], size;
int black[MAXN], white[MAXN], val[MAXN];
int sub[MAXN], lc[MAXN], rc[MAXN], fa[MAXN], mark[MAXN];

inline void down(int x){
    if (mark[x]){
        swap(lc[x], rc[x]);
        if (lc[x]) mark[lc[x]] ^= 1;
        if (rc[x]) mark[rc[x]] ^= 1;
        mark[x] = 0;
    }
}

inline void update(int x){
    black[x] = white[x] = 0;
    if (lc[x]){
        black[x] += black[lc[x]]; white[x] += white[lc[x]];
    }
    if (rc[x]){
        black[x] += black[rc[x]]; white[x] += white[rc[x]];
    }
    if (val[x]) black[x]++;
    else white[x]++;
}

```

```

}

//zag: left rotation
void left(int x, int y){
    rc[y] = lc[x];
    fa[rc[x]] = lc[x] = y;
    if (y == lc[fa[y]]) lc[fa[y]] = x;
    else if (rc[fa[y]] == y) rc[fa[y]] = x;
    fa[x] = fa[y];
    fa[y] = x;
    update(y); update(x);
}

//zig: right rotation
void right(int x, int y){
    lc[y] = rc[x];
    fa[lc[x]] = rc[x] = y;
    if (y == lc[fa[y]]) lc[fa[y]] = x;
    else if (rc[fa[y]] == y) rc[fa[y]] = x;
    fa[x] = fa[y];
    fa[y] = x;
    update(y); update(x);
}

void splay(int x){
    int f, ff;
    size = 0;
    stk[size++] = x;
    for (int u = x; !isRoot(u); u = fa[u]) stk[size++] = fa[u];
    for ( ; size > 0; size--) down(stk[size-1]);
    while (!isRoot(x)){
        f = fa[x];
        ff = fa[f];
        if (isRoot(f)){
            if (x == lc[f]) right(x, f);
            else left(x, f);
        }
        else {
            if (f == lc[ff]){
                if (x == lc[f]){
                    right(f, ff); right(x, f);
                }
                else {
                    left(x, f); right(x, ff);
                }
            }
            else {
                if (x == lc[f]){
                    right(x, f); left(x, ff);
                }
                else {
                    left(f, ff); left(x, f);
                }
            }
        }
    }
    update(x);
}

int expose(int u){

```

```

    int v = 0;
    while (u){
        splay(u);
        rc[u] = v;
        update(v = u);
        u = fa[u];
    }
    for ( ; lc[v]; v = lc[v]);
    return v;
}

void modify(int u, int vv){
    splay(u);
    val[u] = vv;
    update(u);
}

bool join(int u, int v){
    int x = expose(u), y = expose(v);
    if (x == y) return false;
    splay(v);
    rc[v] = 0; mark[v] = 1; fa[v] = u;
    return true;
}

bool remove(int u, int v){
    int x = expose(u); splay(u);
    int y = expose(v); splay(v);
    if (x != y) return false;
    fa[u] = 0;
    if (lc[v] == u) lc[v] = 0;
    if (rc[v] == u) rc[v] = 0;
    return true;
}

void query(int u, int v){
    int x = expose(u), y = expose(v);
    if (x != y){
        puts("-1");
        return ;
    }
    for (x = u, y = 0; x > 0; x = fa[x]){
        if (splay(x), !fa[x]){
            int b = black[rc[x]] + black[y];
            int w = white[rc[x]] + white[y];
            if (val[x]) b++;
            else w++;
            printf("%d %d\n", b, w);
            return ;
        }
        rc[x] = y;
        update(y = x);
    }
}

void init(int s){
    memset(lc, 0, sizeof(int)*s); memset(rc, 0, sizeof(int)*s);
    memset(fa, 0, sizeof(int)*s); memset(mark, 0, sizeof(int)*s);
}

int main(){

```

```

int i, u, v;
char str[16];
while (scanf("%d%d", &n, &m) != EOF){
    if (n == 0 && m == 0) break;
    init(n+1);
    for (i = 1; i <= n; i++){
        scanf("%s", str);
        if (str[0] == 'B') val[i] = 1;
        else val[i] = 0;
    }
    while (m--){
        scanf("%s", str);
        if (str[0] == 'a'){
            scanf("%d%d", &u, &v);
            join(u, v);
        }
        else if (str[0] == 'd'){
            scanf("%d%d", &u, &v);
            remove(u, v);
        }
        else if (str[0] == 's'){
            scanf("%d%s", &u, str);
            modify(u, (str[0] == 'B' ? 1 : 0));
        }
        else if (str[0] == 'q'){
            scanf("%d%d", &u, &v);
            query(u, v);
        }
    }
}
}
}

```

5.9 Dancing link for exact cover

```

//checked by pku3740
#include <stdio>
#include <cstring>
using namespace std;
#define N 1000

struct Node {
    int rn, cn;
    Node *l, *r, *u, *d;
}head, row[N], col[N], node[N*N];

int n, size_n, count[N];

void dance_init(){
    size_n = 0;
    memset(count, 0, sizeof(count));
    head.rn = head.cn = 0;
    head.l = head.r = head.u = head.d = &head;
    for (int i = 0; i < n; i++){
        col[i].cn = i;
        col[i].l = head.l;
        head.l = &col[i];
        col[i].r = &head;
        col[i].l->r = &col[i];
        col[i].r->l = &col[i];
        col[i].u = col[i].d = &col[i];
    }
}

```

```

        for (int i = 0; i < n; i++){
            row[i].rn = i;
            row[i].u = head.u;
            head.u = &row[i];
            row[i].d = &head;
            row[i].u->d = &row[i];
            row[i].d->u = &row[i];
            row[i].l = row[i].r = &row[i];
        }
    }

void removerowhead(){
    for ( int i = 0; i < n; i++ ){
        row[i].l->r = row[i].r;
        row[i].r->l = row[i].l;
    }
}

void link(int x, int y){
    count[y]++;
    Node *tmp = &node[size_n++];
    tmp->rn = x;
    tmp->cn = y;
    tmp->u = &col[y];
    tmp->d = col[y].d;
    col[y].d->u = tmp;
    col[y].d = tmp;
    tmp->l = &row[x];
    tmp->r = row[x].r;
    row[x].r->l = tmp;
    row[x].r = tmp;
}

void remove(int coln){
    col[coln].l->r = col[coln].r;
    col[coln].r->l = col[coln].l;
    for (Node *cur = col[coln].d; cur != &col[coln]; cur = cur->d){
        for (Node *tmp = cur->r; tmp != cur; tmp = tmp->r){
            count[tmp->cn]--;
            tmp->u->d = tmp->d;
            tmp->d->u = tmp->u;
        }
    }
}

void resume(int coln){
    for (Node *cur = col[coln].d; cur != &col[coln]; cur = cur->d){
        for (Node *tmp = cur->l; tmp != cur; tmp = tmp->l){
            tmp->u->d = tmp;
            tmp->d->u = tmp;
            count[tmp->cn]++;
        }
    }
    col[coln].l->r = &col[coln];
    col[coln].r->l = &col[coln];
}

bool solve(int k){
    if (head.r == &head)
        return true;
}

```



```

int id, low = N;
for ( Node *cur = head.r; cur != &head; cur = cur->r ){
    if ( low > count[cur->cn] ){
        low = count[cur->cn];
        id = cur->cn;
    }
}
if ( low == 0 ) return false;
remove( id );
for (Node *cur = col[id].d; cur != &col[id]; cur = cur->d){
    for (Node *tmp = cur->r; tmp != cur; tmp = tmp->r)
        remove(tmp->cn);
    if (solve(k+1)) return true;
    for (Node *tmp = cur->l; tmp != cur; tmp = tmp->l)
        resume(tmp->cn);
}
resume(id);
return false;
}

```

5.10 Dancing link for multi cover

```

#define N 300
#define EPS 5e-8
int n, m, limit, size_n, cnt[N];

struct Node {
    int rn, cn;
    Node *l, *r, *u, *d;
}head, row[N], col[N], node[N*N];

void dance_init(){
    size_n = 0;
    memset(cnt, 0, sizeof(cnt));
    head.rn = head.cn = 0;
    head.l = head.r = head.u = head.d = &head;
    for (int i = 0; i < n; i++){
        col[i].cn = i;
        col[i].l = head.l;
        head.l = &col[i];
        col[i].r = &head;
        col[i].l->r = &col[i];
        col[i].l->r = &col[i];
        col[i].u = col[i].d = &col[i];
    }
    for ( int i = 0; i < m; i++ ){
        row[i].rn = i;
        row[i].u = head.u;
        head.u = &row[i];
        row[i].d = &head;
        row[i].u->d = &row[i];
        row[i].d->u = &row[i];
        row[i].l = row[i].r = &row[i];
    }
}

void removerowhead(){
    for (int i = 0; i < m; i++){
        row[i].l->r = row[i].r;
        row[i].r->l = row[i].l;
    }
}

```

```

}

void remove(Node *p){
    for (Node *i = p->d; i != p; i = i->d){
        i->r->l = i->l;
        i->l->r = i->r;
    }
}

void resume(Node *p){
    for (Node *i = p->u; i != p; i = i->u){
        i->r->l = i;
        i->l->r = i;
    }
}

void link( int x, int y ){
    cnt[y]++;
    Node *tmp = &node[size_n++];
    tmp->rn = x;
    tmp->cn = y;
    tmp->u = &col[y];
    tmp->d = col[y].d;
    col[y].d->u = tmp;
    col[y].d = tmp;
    tmp->l = &row[x];
    tmp->r = row[x].r;
    row[x].r->l = tmp;
    row[x].r = tmp;
}

int h(){
    int ret = 0;
    Node *i, *j, *k;
    bool visit[N] = { 0 };
    for (i = head.r; i != &head; i = i->r){
        if (visit[i->cn]) continue;
        visit[i->cn] = 1;
        ret++;
        for ( j = i->d; j != i; j = j->d )
            for ( k = j->r; k != j; k = k->r )
                visit[k->cn] = 1;
    }
    return ret;
}

int dfs(int dep){
    if (dep >= limit || dep+h() >= limit) return 0;
    if (head.r == &head) return 1;
    int low = 1<<10, id;
    Node *i, *j;
    for ( i = head.r; i != &head; i = i->r ){
        if ( cnt[i->cn] < low ){
            low = cnt[i->cn];
            id = i->cn;
        }
    }
    if ( cnt[id] == 0 ) return 0;
    for ( i = col[id].d; i != &col[id]; i = i->d ){
        remove( i );
    }
}

```

```

        for ( j = i->r; j != i; j = j->r ) remove( j );
        if ( dfs( dep+1 ) ) return 1;
        for ( j = i->l; j != i; j = j->l ) resume( j );
        resume( i );
    }
    return 0;
}

```

5.11 LCA+RMQ

```

//checked by zju3195
#define N 50000
#define INF 1000000000
#define MIN(x,y) ((x)<(y)?(x):(y))
int n, q, mark = 0;
int mp[N], size;
int visit[N], dis[N];
int query[N<<1][3];
int cnt, pos[N], level[N], _level[N];
int seq[N<<1], sq;
int h[N<<1][18];
struct Edge{
    int v, w, next;
}edge[N<<1];

void init(){
    memset(mp, -1, sizeof(mp));
    memset(visit, 0, sizeof(visit));
    size = sq = cnt = 0;
}

inline void add_edge(int u, int v, int w){
    edge[size].v = v; edge[size].w = w;
    edge[size].next = mp[u];
    mp[u] = size;
    size++;
}

void dfs(int u, int d){
    int i, v;
    visit[u] = 1;
    _level[cnt] = u;
    level[u] = cnt++;
    dis[u] = d;
    pos[u] = sq;
    seq[sq++] = level[u];
    for (i = mp[u]; i != -1; i = edge[i].next){
        v = edge[i].v;
        if (visit[v]) continue;
        dfs(v, d+edge[i].w);
        seq[sq++] = level[u];
    }
}

void rmq_init(){
    int i, j, l;
    for (i = 0; i < sq; i++) h[i][0] = seq[i];
    for (j = l = 1; l*2 <= sq; j++, l <= 1){
        for (i = 0; i <= sq+1-l*2; i++)
            h[i][j] = MIN(h[i][j-1], h[i+l][j-1]);
    }
}

```

```

}

inline int rmq_query(int start, int end){
    int j = 0, l = 1;
    while (2*l <= end-start+1){
        j++;
        l <= 1;
    }
    return MIN(h[start][j], h[end-l+1][j]);
}

inline int calc(int x, int y){
    int ans, p, q, u, v;
    u = pos[x]; v = pos[y];
    if (u > v) swap(u, v);
    p = _level[rmq_query(u, v)];
    ans = dis[x]+dis[y]-2*dis[p];
    return ans;
}

void solve(){
    int i, j, ans, x, y, z;
    dfs(0, 0);
    rmq_init();
    if (mark) puts("");
    mark = 1;
    for (i = 0; i < q; i++){
        x = query[i][0];
        y = query[i][1];
        z = query[i][2];
        ans = calc(x, y) + calc(y, z) + calc(z, x);
        printf("%d\n", ans/2);
    }
}

bool input(){
    if (scanf("%d", &n) == EOF) return false;
    int i, j, u, v, w;
    init();
    for (i = 0; i < n-1; i++){
        scanf("%d%d%d", &u, &v, &w);
        add_edge(u, v, w); add_edge(v, u, w);
    }
    scanf("%d", &q);
    for (i = 0; i < q; i++)
        for (j = 0; j < 3; j++)
            scanf("%d", &query[i][j]);
    return true;
}

```

5.12 树套树

不用模板了，其实就是线段树+set在节点上

5.13 线段树内存模拟

```

//checked by 3358, 懒操作, 离散化
#define N 65536
int n, m;
struct Node{

```

```

    int l, r, flag;
    int lc, rc, cnt;
    inline void set(int _flag){
        flag = _flag;
        if (_flag == 0) lc = rc = cnt = r-l+1;
        else if (_flag ==1) lc = rc = cnt = 0;
    }
}tree[N*4];
struct Block{
    int l, r;
    Block(){ }
    Block(int _l, int _r): l(_l), r(_r) { }
    bool operator<(const Block &b) const{ return l < b.l; }
    bool operator==(const Block &b) const{ return l == b.l && r == b.r; }
};
vector<Block> mem;
vector<Block>::iterator itr;

void build(int id, int l, int r){
    tree[id].l = l; tree[id].r = r;
    tree[id].set(0);
    if (l == r) return ;
    int mid = (l+r)>>1;
    build(id<<1, l, mid);
    build((id<<1)+1, mid+1, r);
}

inline void down(int id){
    if (tree[id].flag == -1) return;
    if (tree[id].flag == 0){
        tree[id<<1].set(0);
        tree[(id<<1)+1].set(0);
    }
    if (tree[id].flag == 1){
        tree[id<<1].set(1);
        tree[(id<<1)+1].set(1);
    }
}

inline void up(int id){
    if (tree[id<<1].flag == 0 && tree[(id<<1)+1].flag == 0){
        tree[id].set(0);
        return;
    }
    if (tree[id<<1].flag == 1 && tree[(id<<1)+1].flag == 1){
        tree[id].set(1);
        return;
    }
    tree[id].flag = -1;
    tree[id].lc = tree[id<<1].lc;
    if (tree[id<<1].flag == 0) tree[id].lc += tree[(id<<1)+1].lc;
    tree[id].rc = tree[(id<<1)+1].rc;
    if (tree[(id<<1)+1].flag == 0) tree[id].rc += tree[id<<1].rc;
    tree[id].cnt = max(max(tree[id].lc, tree[id].rc), \
        max(tree[id<<1].cnt, tree[(id<<1)+1].cnt));
    tree[id].cnt = max(tree[id].cnt, tree[id<<1].rc+tree[(id<<1)+1].lc);
}

int find(int id, int d){
    if (d > tree[id].cnt) return 0;

```

```

    if (tree[id].flag == 0 && d <= tree[id].cnt) return tree[id].l;
    down(id);
    if (tree[id<<1].cnt >= d) return find(id<<1, d);
    if (tree[id<<1].rc+tree[(id<<1)+1].lc >= d)
        return tree[id<<1].r-tree[id<<1].rc+1;
    if (tree[(id<<1)+1].cnt >= d) return find((id<<1)+1, d);
    return 0;
}

void insert(int id, int ll, int rr){
    if (ll <= tree[id].l && tree[id].r <= rr){
        tree[id].set(1);
        return ;
    }
    int mid = (tree[id].l+tree[id].r)>>1;
    down(id);
    if (ll <= mid) insert(id<<1, ll, rr);
    if (rr > mid) insert((id<<1)+1, ll, rr);
    up(id);
}

void remove(int id, int ll, int rr){
    if (ll <= tree[id].l && tree[id].r <= rr){
        tree[id].set(0);
        return ;
    }
    int mid = (tree[id].l+tree[id].r)>>1;
    down(id);
    if (ll <= mid) remove(id<<1, ll, rr);
    if (rr > mid) remove((id<<1)+1, ll, rr);
    up(id);
}

inline int bsearch(int pos){
    if (mem.size() == 0) return -1;
    int low = 0, up = mem.size()-1, mid;
    while (low < up){
        mid = (low+up)>>1;
        if (mem[mid].l <= pos && pos <= mem[mid].r) return mid;
        if (pos < mem[mid].l) up = mid-1;
        else if (pos > mem[mid].r) low = mid+1;
    }
    if (mem[up].l <= pos && pos <= mem[up].r) return up;
    return -1;
}

int main(){
    Block temp;
    int d, pos;
    char str[16];
    while (scanf("%d%d", &n, &m) != EOF){
        build(1, 1, n);
        mem.clear();
        while (m--){
            scanf("%s", str);
            if (str[0] == 'N'){
                scanf("%d", &d);
                pos = find(1, d);
                if (pos == 0) puts("Reject New");
                else {

```

```

        temp = Block(pos, pos+d-1);
        insert(1, pos, pos+d-1);
        printf("New at %d\n", pos);
        if (mem.size() == 0)
            mem.push_back(temp);
        else {
            itr = lower_bound(mem.begin(), mem.end(), temp);
            if (itr == mem.end())
                mem.push_back(temp);
            else
                mem.insert(itr, temp);
        }
    }
}
else if (str[0] == 'F'){
    scanf("%d", &d);
    pos = bsearch(d);
    if (pos == -1)
        puts("Reject Free");
    else {
        printf("Free from %d to %d\n", mem[pos].l, mem[pos].r);
        remove(1, mem[pos].l, mem[pos].r);
        mem.erase(mem.begin()+pos);
    }
}
else if (str[0] == 'G'){
    scanf("%d", &d);
    if (d > mem.size())
        puts("Reject Get");
    else
        printf("Get at %d\n", mem[d-1].l);
}
else if (str[0] == 'R'){
    tree[1].set(0);
    mem.clear();
    puts("Reset Now");
}
}
puts("");
}
}

```

6. 图论问题

6.1 找两棵不相交的生成树

```
//checked by hdu3267
#define N 32
struct Edge{
    int u, v, id;
    Edge(){ }
    Edge(int _u, int _v, int _id): u(_u), v(_v), id(_id) {}
    bool operator==(const Edge &e) const{ return id == e.id; }
    bool operator!=(const Edge &e) const{ return !(*this == e); }
}tree[N], edge[N];
int n, m, size, comp;
int set1[N], set2[N], visit[N], mark[N];
vector<int> mp[N];

//先dfs一棵树出来，size记录边数
void dfs(int u){
    int i, v;
    visit[u] = 1;
    for (i = 0; i < mp[u].size(); i+=2){
        v = mp[u][i];
        if (visit[v]) continue;
        tree[size++] = Edge(u, v, mp[u][i+1]);
        dfs(v);
    }
}

//并查集
inline int find_set(int u, int set[]){
    if (set[u] == u) return u;
    return (set[u] = find_set(set[u], set));
}

inline void join_set(int u, int v, int set[]){
    int x = find_set(u, set), y = find_set(v, set);
    if (x != y) set[y] = x;
}

//判断e是否连通
inline int connect1(Edge e[], int set[], int vn, int en){
    int i, j;
    for (i = 0; i < vn; i++) set[i] = i;
    for (i = 0; i < en; i++) join_set(e[i].u, e[i].v, set);
    for (i = 1; i < vn; i++)
        if (set[i] != set[0])
            return 0;
    return 1;
}

//判断剩余边集是否连通
inline int connect2(Edge e[], int set[], int vn, int en){
    int i, j = 1;
    for (i = 0; i < vn; i++) set[i] = i;
    for (i = 0; i < en; i++){
        if (mark[i] == 0) continue;
        join_set(e[i].u, e[i].v, set);
    }
    for (i = 1; i < vn; i++)
```



```

        if (find_set(i, set) == find_set(0, set))
            j++;
    return j;
}

bool search(int dep){
    int i, j, k, c, cc;
    Edge e1, e2;
    //记录与0点连通个数
    c = connect2(edge, set2, n, m);
    if (c == n) return true;
    for (i = 0; i < size; i++){
        for (j = 0; j < m; j++){
            if (!mark[j]) continue;
            e1 = tree[i]; e2 = edge[j];
            for (k = 0; k < m && edge[k] != e1; k++);
            tree[i] = e2;
            mark[j] = 0; mark[k] = 1;
            if (connect1(tree, set1, n, size)){
                cc = connect2(edge, set2, n, m);
                if (cc > c){
                    if (search(dep+1)) return true;
                }
            }
            tree[i] = e1;
            mark[j] = 1; mark[k] = 0;
        }
    }
    return false;
}

int main(){
    int i, j, u, v;
    while (scanf("%d%d", &n, &m) != EOF){
        if (n == -1 && m == -1) break;
        for (i = 0; i < n; i++) mp[i].clear();
        //加边
        for (i = 0; i < m; i++){
            scanf("%d%d", &u, &v);
            mp[u].push_back(v); mp[u].push_back(i);
            mp[v].push_back(u); mp[v].push_back(i);
            edge[i] = Edge(u, v, i);
        }
        memset(visit, 0, sizeof(visit));
        size = 0;
        dfs(0);
        if (size < n-1){
            puts("NO");
            continue;
        }
        for (i = 0; i < m; i++) mark[i] = 1;
        //边分成两个集合
        for (i = 0; i < size; i++)
            for (j = 0; j < m; j++)
                if (tree[i] == edge[j])
                    mark[j] = 0;
        if (search(0)) puts("YES");
        else puts("NO");
    }
}

```

6.2 一般图匹配

```
/*
带花树开花算法
1、贪心初始化
2、找可增广路。交错树。两个外点有边，形成花。
3、缩圈，边两端点在圈B上的，收缩掉。仅一个端点属于B的变成以VB 为一端的边。
*/
#include <stdio.h>
#include <string.h>

#define MAXV 1008
#define MAXE 200008
#define SBN (sizeof(bool) * (n + 1))
#define SIN (sizeof(int) * (n + 1))

struct Edge {
    int v, next;
    Edge(){}
    Edge(int _v, int _next):
        v(_v), next(_next){}
};

struct Graph {
    int n, match[MAXV], que[MAXV], pre[MAXV], base[MAXV];
    bool flag[MAXV], inBlossom[MAXV], inPath[MAXV];
    Edge edge[MAXE];
    int head[MAXV], size;
    inline void initg(int _n) {
        size = 0;
        n = _n;
        memset(head, -1, SIN);
    }
    inline void addEdge(int u, int v) {
        if (u == v) return;
        edge[size] = Edge(v, head[u]);
        head[u] = size++;
        edge[size] = Edge(u, head[v]);
        head[v] = size++;
    }
    int MaxMatch() {
        memset(match, -1, SIN);
        int i, j, ans = 0;
        for (i = 1; i <= n; ++i) {
            if (match[i] != -1) continue;
            for (j = head[i]; j != -1 && match[i] == -1; j = edge[j].next)
                if (match[edge[j].v] == -1) {
                    match[edge[j].v] = i;
                    match[i] = edge[j].v;
                    ans++;
                }
        }
        for (i = 1; i <= n; ++i)
            if (match[i] == -1)
                ans += bfs(i);
        return ans;
    }
    int bfs(int p) { //寻找可增广路
        int i, j, u, v, b, front, rear;
        memset(pre, -1, SIN);
```

```

memset(flag, 0, SBN);
for (i = 1; i <= n; ++i)
    base[i] = i;
front = rear = 0;
que[rear++] = p;
flag[p] = 1;
while (front != rear) {
    u = que[front++];
    for (i = head[u]; i != -1; i = edge[i].next) {
        v = edge[i].v;
        if (base[u] != base[v] && v != match[u]) {
            if (v == p || (match[v] != -1 && pre[match[v]] != -1)) {
                b = contract(u, v);
                for (j = 1; j <= n; ++j) {
                    if (inBlossom[base[j]]) {
                        base[j] = b;
                        if (flag[j] == 0) {
                            flag[j] = 1;
                            que[rear++] = j;
                        }
                    }
                }
            }
            else if (pre[v] == -1) {
                pre[v] = u;
                if (match[v] == -1) {
                    argument(v);
                    return 1;
                }
                else {
                    que[rear++] = match[v];
                    flag[match[v]] = 1;
                }
            }
        }
    }
}
return 0;
}

void argument(int u) { //增广
    int v, k;
    while (u != -1) {
        v = pre[u];
        k = match[v];
        match[u] = v;
        match[v] = u;
        u = k;
    }
}

void changeBlossom(int b, int u) { //哪些点属于当前圈
    int v;
    while (base[u] != b) {
        v = match[u];
        inBlossom[base[v]] = inBlossom[base[u]] = true;
        u = pre[v];
        if (base[u] != b)
            pre[u] = v;
    }
}

int contract(int u, int v) { //缩圈

```

```

        memset(inBlossom, 0, SBN);
        int b = findBase(base[u], base[v]);
        changeBlossom(b, u);
        changeBlossom(b, v);
        if (base[u] != b)
            pre[u] = v;
        if (base[v] != b)
            pre[v] = u;
        return b;
    }
    int findBase(int u, int v) { //属于哪个圈
        memset(inPath, 0, SBN);
        while (true) {
            inPath[u] = true;
            if (match[u] == -1)
                break;
            u = base[pre[match[u]]];
        }
        while (!inPath[v])
            v = base[pre[match[v]]];
        return v;
    }
}GP;

```

6.3 弦图判定

//checked by 1972

#define N 1024

int n, m;

int mp[N], size;

int mark[N], deg[N], g[N][N], seq[N];

```

int isChordal(){
    int i, j, p, q;
    memset(mark, 0, sizeof(mark));
    memset(deg, 0, sizeof(deg));
    for (i = 1; i <= n; i++){
        p = q = -1;
        for (j = 1; j <= n; j++)
            if (!mark[j] && (p == -1 || deg[j] > deg[p]))
                p = j;
        mark[p] = 1;
        seq[i] = p;
        for (j = i-1; j > 0; j--){
            if (g[p][seq[j]]){
                if (q < 0) q = seq[j];
                else if (!g[q][seq[j]]) return 0;
            }
        }
        for (j = 1; j <= n; j++)
            if (!mark[j] && g[p][j])
                deg[j]++;
    }
    return 1;
}

```

```

int main(){
    int u, v;
    while (scanf("%d%d", &n, &m) != EOF){
        if (n == 0 && m == 0) break;
        size = 0;
        memset(mp, -1, sizeof(mp));
    }
}

```

```

        memset(g, 0, sizeof(g));
        while (m--){
            scanf("%d%d", &u, &v);
            g[u][v] = g[v][u] = 1;
        }
        if (isChordal()) puts("Perfect\n");
        else puts("Imperfect\n");
    }
}

```

6.4 无根树的同构

```

//checked by utsc1117
//首先topsort, 然后dfs做hash; 如果是有根树直接dfs
typedef long long LL;
#define N 1024
const LL MOD = 30007;
const LL MUL = 1911111110;
int vn;
int deg[N], seq[N], visit[N], leave[N], que[N];
LL hash[N], h1[2], h2[2];
vector<int> tree[N];

//比较两个节点的hash值
inline int cmp(int a, int b){ return hash[a] < hash[b]; }

//递归做hash
void dfs(int u, int pnt){
    int i, v, c = 0;
    visit[u] = 1;
    for (i = 0; i < tree[u].size(); i++){
        v = tree[u][i];
        if (v == pnt || visit[v]) continue;
        dfs(v, u);
        c++;
    }
    sort(tree[u].begin(), tree[u].end(), cmp);
    if (c == 0){
        hash[u] = 1; return ;
    }
    else{
        LL h = 1908;
        for (i = 0; i < tree[u].size(); i++){
            v = tree[u][i];
            if (v == pnt) continue;
            h = ((h * MUL) ^ hash[v]) % MOD;
        }
        hash[u] = h;
    }
}

//seq数组记录出队列顺序, leave数组记录时间
void topsort(){
    int i, u, v, s = 0, head = 0, tail = 0;
    if (vn == 1){
        seq[1] = 1;
        return ;
    }
    memset(visit, 0, sizeof(visit));
    for (i = 1; i <= vn; i++) deg[i] = tree[i].size();
    for (i = 1; i <= vn; i++){

```

```

        if (deg[i] == 1){
            visit[i] = 1;
            leave[i] = 0;
            que[tail++] = i;
        }
    }
    while (head < tail){
        u = que[head++];
        seq[++s] = u;
        for (i = tree[u].size()-1; i >= 0; i--){
            v = tree[u][i];
            if (visit[v]) continue;
            deg[v]--;
            if (deg[v] == 1){
                que[tail++] = v;
                visit[v] = 1;
                leave[v] = leave[u]+1;
            }
        }
    }
}
//判断是否同构
bool check(){
    int i, j;
    for (i = 0; i < 2; i++){
        if (h1[i] == -1) continue;
        for (j = 0; j < 2; j++){
            if (h2[j] == -1) continue;
            if (h1[i] == h2[j]) return true;
        }
    }
    return false;
}

int main(){
    int ca, i, u, v;
    scanf("%d", &ca);
    while (ca--){
        scanf("%d", &vn);
        for (i = 1; i <= vn; i++) tree[i].clear();
        for (i = 1; i < vn; i++){
            scanf("%d%d", &u, &v);
            tree[u].push_back(v); tree[v].push_back(u);
        }
        topsort();
        memset(visit, 0, sizeof(visit));
        dfs(seq[vn], -1);
        h1[0] = hash[seq[vn]];
        h1[1] = -1;
        if (vn > 1 && leave[seq[vn]] == leave[seq[vn-1]]){
            memset(visit, 0, sizeof(visit));
            dfs(seq[vn-1], -1);
            h1[1] = hash[seq[vn-1]];
        }
        for (i = 1; i <= vn; i++) tree[i].clear();
        for (i = 1; i < vn; i++){
            scanf("%d%d", &u, &v);
            tree[u].push_back(v); tree[v].push_back(u);
        }
        topsort();
    }
}

```

```

        memset(visit, 0, sizeof(visit));
        dfs(seq[vn], -1);
        h2[0] = hash[seq[vn]];
        h2[1] = -1;
        if (vn > 1 && leave[seq[vn]] == leave[seq[vn-1]]){
            memset(visit, 0, sizeof(visit));
            dfs(seq[vn-1], -1);
            h2[1] = hash[seq[vn-1]];
        }
        if (check()) puts("same");
        else puts("different");
    }
}

```

6.5 曼哈顿距离最小生成树

```

/*
    曼哈顿距离最小生成树
    题意：给出 $n \leq 100000$ 个点坐标，求MST。边权为点之间的曼哈顿距离
    题目给出重要提示：对于一个点0，在45度角度的范围内，最多只有一条连出去的边。
    拓展这个提示，对于一个点0，45°的范围内最多只有1条边，8个方向只有8条
    8n条边用kruskal可以解决
    由于是无向图，只需要找到4个方向即可。通过旋转90°，关于 $y=x$ 翻转做到这四个方向区域
    关于原点对称的区域没有访问过。
    那怎么快速找到45°范围内距离 $(x_i, y_i)$ 最小的点呢？
    由于是45°范围的点，有 $x_j > x_i, y_j > y_i$ ，距离为 $x_j + y_j - x_i - y_i$  所以用线段树找 $x+y$ 最小的点
    而且需要是在45°范围内，还有 $y > y_i$ 
    先按照 $w = y - x$ 从小到大排序， $w$ 相同的 $y$ 大的优先
    检查每个点，在线段树中找到距离最小的点（没有时为INF） 线段树中找  $y$  比他大的
    然后再插入
*/
// CII 3662 Another Minimum Spanning Tree

#include <cstdio>
#include <cstring>
#include <cmath>
#include <algorithm>
using namespace std;
#define N 100005
#define BIG 1000000000
const int INF = 1 << 30;
struct POINT {
    int x, y;
    void get() {
        scanf("%d%d", &x, &y);
    }
    void print() {
        printf("%d %d\n", x, y);
    }
    POINT() {}
    POINT(int x, int y) :
        x(x), y(y) {}
};

POINT P[N];
int n, m;
int dis(int a, int b) {
    return abs(P[a].x - P[b].x) + abs(P[a].y - P[b].y);
}

```

```

// MST Kruskal
struct EDGE {
    int x, y, w;
    EDGE() {}
    EDGE(int x, int y, int w) :
        x(x), y(y), w(w) {}
    bool operator <(const EDGE &e) const {
        return w < e.w;
    }
};
EDGE E[N * 10];
int fa[N];
int find(int x) {
    if (fa[x] != x) fa[x] = find(fa[x]);
    return fa[x];
}
long long kruskal() {
    int i, link = 1;
    long long ans = 0;
    sort(E, E + m);
    for (i = 0; i <= n; i++)
        fa[i] = i;
    for (i = 0; i < m && link < n; i++) {
        int x = E[i].x, y = E[i].y;
        x = find(x), y = find(y);
        if (x == y) continue;
        fa[x] = y;
        link++;
        ans += E[i].w;
    }
    return ans;
}
// End of Kruskal
// Sort and query, get all the edges in 45 degree
struct NODE {
    int v, p, l, r;
};
NODE T[N * 5];
int idx[N], yy[N], ny[N];
inline bool cmp(int i, int j) {    //按 w=y-x从小到大排, 然后按y从大到小排
    int v1 = P[i].y - P[i].x;
    int v2 = P[j].y - P[j].x;
    if (v1 == v2) return ny[i] > ny[j];
    return v1 < v2;
}
void build(int p, int l, int r) {
    T[p].l = l, T[p].r = r, T[p].v = INF, T[p].p = -1;
    if (l == r) return;
    int mid = (l + r) >> 1;
    build(p << 1, l, mid);
    build((p << 1) | 1, mid + 1, r);
}
void insert(int p, int i) {
    if (ny[i] < T[p].l || ny[i] > T[p].r) return;
    if (P[i].x + P[i].y < T[p].v) {
        T[p].v = P[i].x + P[i].y;
        T[p].p = i;
    }
}

```



```

        if (T[p].l == T[p].r) return;
        insert(p << 1, i);
        insert((p << 1) | 1, i);
    }
    struct ANS {
        int v, p;
        ANS() {}
        ANS(int v, int p) :
            v(v), p(p) {}
        bool operator <(const ANS &a) const {
            return v < a.v;
        }
    };
    ANS query(int p, int i) {
        if (T[p].r < ny[i]) return ANS(INF, -1);
        if (ny[i] <= T[p].l) return ANS(T[p].v, T[p].p);
        return min(query(p << 1, i), query((p << 1) | 1, i));
    }

    void make() {
        int i, tot;
        for (i = 0; i < n; i++)
            idx[i] = i, yy[i] = P[i].y;
        sort(yy, yy + n);
        tot = unique(yy, yy + n) - yy;
        for (i = 0; i < n; i++)
            ny[i] = lower_bound(yy, yy + tot, P[i].y) - yy;
        sort(idx, idx + n, cmp);
        build(1, 0, tot + 1);
        for (i = 0; i < n; i++) {
            ANS a = query(1, idx[i]);
            if (a.p != -1) E[m++] = EDGE(idx[i], a.p, dis(idx[i], a.p));
            insert(1, idx[i]);
        }
    }

    void solve() {
        int i, j;
        for (i = 0; i < n; i++)
            P[i].get();
        m = 0;
        for (i = 0; i < 4; i++) { //旋转
            if (i > 0) {
                for (j = 0; j < n; j++) {
                    int x = -P[j].y, y = P[j].x;
                    if (i == 2) swap(x, y);
                    P[j] = POINT(x, y);
                }
            }
            make();
        }
    }

    int main() {
        int T = 1;
        while (scanf("%d", &n) && n) {
            solve();
            printf("Case %d: Total Weight = %lld\n", T++, kruskal());
        }
    }

```

6.6 网络流无向图的连通度

```
//拆点, 固定源点枚举汇点, checked by 1692
#include <cstdio>
#include <cstring>
#define N 200
#define MIN(x,y) ((x)<(y)?(x):(y))
#define INF 1000000
int n, m;
struct Edge{
    int v, cap, flow, next;
    inline void set(int _v, int _cap, int _flow, int _next){
        v = _v; cap = _cap; flow = _flow; next = _next;
    }
}edge[N*N];
int vn, size, src, dst, mp[N], dist[N], que[N*N];

void init(){
    size = 0;
    memset( mp, -1, sizeof(mp) );
}

inline void add_edge(int u, int v, int c1, int c2){
    edge[size].set(v, c1, 0, mp[u]); mp[u] = size++;
    edge[size].set(u, c2, 0, mp[v]); mp[v] = size++;
}

bool dinic_bfs(){
    int head = 0, tail = 1, u, v;
    memset(dist, -1, sizeof(dist));
    dist[src] = 0;
    que[head] = src;
    while (head < tail){
        u = que[head++];
        for (v = mp[u]; v != -1; v = edge[v].next){
            if (edge[v].cap > edge[v].flow && dist[edge[v].v] < 0){
                dist[edge[v].v] = dist[u]+1;
                que[tail++] = edge[v].v;
            }
        }
    }
    return dist[dst] > 0;
}

int dinic_dfs(int u, int f){
    if (u == dst) return f;
    int i, v, ret = 0, tmp;
    for (i = mp[u]; i != -1; i = edge[i].next){
        v = edge[i].v;
        if (edge[i].cap > edge[i].flow && dist[v] == dist[u]+1){
            tmp = dinic_dfs(v, MIN(f, edge[i].cap-edge[i].flow));
            ret += tmp;
            f -= tmp;
            edge[i].flow += tmp;
            edge[i^1].flow -= tmp;
        }
        if (f == 0) break;
    }
    return ret;
}
```

```

}

int dinic(){
    int ans = 0, tmp;
    while (dinic_bfs()){
        tmp = dinic_dfs(src, INF);
        if (tmp == 0) break;
        ans += tmp;
    }
    return ans;
}

int main(){
    int i, j, u, v;
    while (scanf("%d%d", &n, &m) != EOF){
        if (n == 0 || n == 1){
            printf("%d\n", n);
            continue;
        }
        init();
        for (i = 1; i <= n; i++) add_edge(i, i+n, 1, 0);
        while (m--){
            while (getchar() != '(');
            scanf("%d", &u); getchar();
            scanf("%d", &v); getchar();
            if (u == v) continue;
            u++, v++;
            add_edge(u+n, v, INF, 0);
            add_edge(v+n, u, INF, 0);
        }
        int ans = 2*INF, tmp;
        for (i = 1; i <= n; i++){
            if (i == 1) continue;
            src = 1+n;
            dst = i;
            for (u = 1; u <= 2*n; u++){
                for (v = mp[u]; v != -1; v = edge[v].next)
                    edge[v].flow = 0;
            }
            tmp = dinic();
            if (ans > tmp) ans = tmp;
        }
        if (ans >= n) printf("%d\n", n);
        else printf("%d\n", ans);
    }
}

```

6.7 树的分治

```

//checked by pku1741 pku1987
const int MAX_N = 10000;
bool flag[MAX_N];
int k, n, ret, v[MAX_N];
queue<pair<int, int> > q;

struct edge{int v, w; edge *next; } *e[MAX_N], data[MAX_N*2-2], *it;
void insert(int u, int v, int w){
    *it = (edge){v, w, e[u]}; e[u] = it++;
    *it = (edge){u, w, e[v]}; e[v] = it++;
}

```

```

int count(int *first, int *last){
    int ret = 0;
    sort(first, last--);
    while (first < last)
        if (*first+*last <= k) ret += last-first++;
        else --last;
    return ret;
}

int best_size, center;
int centerOfGravity(int root, int pred){
    int max_sub = 0, size = 1;
    for (edge *it = e[root]; it; it = it->next)
        if (it->v != pred && flag[it->v]){
            int t = centerOfGravity(it->v, root);
            size += t;
            if (t > max_sub) max_sub = t;
        }
    if (q.front().second-q.front().first-max_sub > max_sub)
        max_sub = q.front().second-q.front().first-max_sub;
    if (max_sub < best_size)
        best_size = max_sub, center = root;
    return size;
}

int dists[MAX_N], len;
void find(int root, int pred, int dist){
    v[len] = root;
    dists[len++] = dist;
    int last = len;
    for (edge *it = e[root]; it; it = it->next)
        if (it->v != pred && flag[it->v]){
            find(it->v, root, dist+it->w);
            if (pred == -1){
                q.push(make_pair(last, len));
                ret -= count(dists+last, dists+len);
                last = len;
            }
        }
}

int main(){
    int x;
    char dir[4];
    while (scanf("%d%d", &n, &k) != EOF){
        if (n == 0 && k == 0) break;
        it = data;
        memset(e, 0, sizeof(e[0])*n);
        for (int i = 1; i < n; i++){
            int u, v, w;
            scanf("%d%d%d", &u, &v, &w);
            --u; --v;
            insert(u, v, w);
        }
        ret = 0;
        for (int i = 0; i < n; ++i) v[i] = i;
        for (q.push(make_pair(0, n)); !q.empty(); q.pop()){
            if (q.front().first == q.front().second-1) continue;
            for (int i = q.front().first; i < q.front().second; ++i)
                flag[v[i]] = true;
        }
    }
}

```

```

        best_size = numeric_limits<int>::max();
        centerOfGravity(v[q.front().first], -1);
        len = q.front().first;
        find(center, -1, 0);
        ret += count(dists+q.front().first, dists+q.front().second);
        for (int i = q.front().first; i < q.front().second; ++i)
            flag[v[i]] = false;
    }
    printf("%d\n", ret);
}
}

```

6.8 割点割边

//checked by zju2588 有重边的情况

```

#define N 10008
struct Edge{
    int v, id, next;
    Edge(){}
    Edge(int _v, int _id, int _next): v(_v), id(_id), next(_next){}
}edge[200008];
int n, m, b, size, mp[N];
int dep[N], low[N], visit[N], mark[100008], bridge[100008];

inline void add_edge(int u, int v, int id){
    edge[size] = Edge(v, id, mp[u]);
    mp[u] = size++;
}

void dfs(int u, int d, int p){
    int i, v, son = 0;
    visit[u] = 1;
    dep[u] = low[u] = d;
    for (i = mp[u]; i != -1; i = edge[i].next){
        if (mark[edge[i].id]) continue;
        mark[edge[i].id] = 1;
        v = edge[i].v;
        if (visit[v]){
            low[u] = min(low[u], dep[v]);
            continue;
        }
        dfs(v, d+1, u);
        low[u] = min(low[u], low[v]);
        son++;
        //cut-vertex -> if ((u == rt && son > 1) || (u != rt && low[v] >= dep[u]))
        //bridge
        if (low[v] > dep[u]){
            b++;
            bridge[edge[i].id] = 1;
        }
    }
}

int main(){
    int t, ca, i, u, v;
    scanf("%d", &t);
    for (ca = 0; ca < t; ++ca){
        scanf("%d%d", &n, &m);
        size = 0;
        memset(mp, -1, sizeof(mp));
    }
}

```

```

        for (i = 1; i <= m; ++i){
            scanf("%d%d", &u, &v);
            add_edge(u, v, i);
            add_edge(v, u, i);
        }
        memset(dep, 0, sizeof(dep));
        memset(low, 0, sizeof(low));
        memset(visit, 0, sizeof(visit));
        memset(mark, 0, sizeof(int)*(m+1));
        memset(bridge, 0, sizeof(int)*(m+1));
        b = 0;
        dfs(1, 1, 0);
        if (ca) puts("");
        printf("%d\n", b);
        for (u = 1, v = 0; u <= m; ++u){
            if (bridge[u]){
                if (v) putchar(' ');
                v = 1;
                printf("%d", u);
            }
        }
        if (b != 0) puts("");
    }
}

```

6.9 2-SAT建图

经典2-sat验证题。

假设 a 为1, 则 $\neg a$ 为0。建图转换:

a and $b = 1$ 转换为: $(\neg a \rightarrow a), (\neg b \rightarrow b)$, 因为 a, b 必选, $\neg a \rightarrow a$ 这样会导致 a 一定被选, 为什么? 想想构造一组解的时候, 经过求强连通分量和缩点后, 对新图进行拓扑排序, 然后按拓扑倒序对点进行染色。现在明白了吧! 因为存在 $\neg a \rightarrow a$, 所以呢染色的顺序一定是 $a, \neg a$, 这时如果 a 没被染色, 那么 a 就一定被染红色, 则 $\neg a$ 一定被染蓝色。如果 a 与 $\neg a$ 之间不存在边的关系, 则表示 $a, \neg a$ 任选一个, 因为其中一个被染红色, 则另外一个一定被染蓝色, 具体你的程序选择哪个, 就看你的拓扑部分是怎么写的 (点的访问顺序)。

a and $b = 0$ 转换为: $(a \rightarrow \neg b), (b \rightarrow \neg a)$

a or $b = 1$ 转换为: $(\neg a \rightarrow b), (\neg b \rightarrow a)$

a or $b = 0$ 转换为: $(a \rightarrow \neg a), (b \rightarrow \neg b)$

a xor $b = 1$ 转换为: $(a \rightarrow \neg b), (\neg b \rightarrow a), (b \rightarrow \neg a), (\neg a \rightarrow b)$

a xor $b = 0$ 转换为: $(a \rightarrow b), (b \rightarrow a), (\neg a \rightarrow \neg b), (\neg b \rightarrow \neg a)$

建完图后, 剩下的就是套模板了。

6.10 最小直径生成树

//checked by spoj735, Dynamic programming

#define MAXN 1024

int n, m, ans;

vector<int> g[MAXN];

int dist[MAXN][MAXN], flg[MAXN];

int qu[MAXN], qs, qe;

void bfs(int s){

int i, j, x, y, cnt;

memset(flg, 0, sizeof(flg));

flg[s] = 1;

qs = qe = 0;

qu[qe++] = s;

cnt = 0;

dist[s][s] = 0;

while (qs < qe){

```

        x = qu[qs++];
        for (i = 0; i < g[x].size(); i++){
            y = g[x][i];
            if (flg[y] == 0){
                flg[y] = 1;
                qu[qe++] = y;
                dist[s][y] = dist[s][x] + 1;
            }
        }
    }
}

int main(){
    int i, j, x, y, k;
    int csnum, id;
    scanf ("%d", &csnum);
    while (csnum--){
        scanf ("%d", &n);
        for (i = 1; i <= n; i++) g[i].clear();
        for (i = 1; i <= n; i++){
            scanf ("%d %d", &id, &k);
            for (j = 0; j < k; j++){
                scanf ("%d", &x);
                g[id].push_back(x);
            }
        }
        for (i = 1; i <= n; i++) bfs(i);
        int mx;
        ans = n;
        for (i = 1; i <= n; i++){
            mx = 0;
            for (j = 1; j <= n; j++) if (dist[i][j] > mx) mx = dist[i][j];
            if (2 * mx < ans) ans = 2 * mx;
        }
        int l;
        for (i = 1; i <= n; i++){
            for (k = 0; k < g[i].size(); k++){
                j = g[i][k];
                mx = 0;
                for (l = 1; l <= n; l++){
                    mx = max(mx, min(dist[i][l], dist[j][l]));
                }
                ans = min(ans, 2*mx+1);
            }
        }
        printf ("%d\n", ans);
    }
}

```

7. 组合数学、数值计算

7.1 常用公式

多重组合: n 个球放入 k 个盒子

$$C(n+k-1, n), C(n+k-1, k-1)$$

集合划分: 将大小为 n 的集合划分为 k 个子集, 第二类斯特林数

$$S(n, k) = S(n-1, k-1) + k * S(n-1, k)$$

$$S(n, k) = \sigma_{0 \dots k} \{ (-1)^j * C(k, j) * (k-j)^n \} / k!$$

bell数: 将大小为 n 的集合划分为若干个子集

$$B(n) = \sigma_{1 \dots n} S(n, k)$$

$$B(n+1) = \sigma_{0 \dots n} B(k) * C(n, k)$$

整数拆分: 将 n 拆成 k 个正整数, $\sigma(A_k) = n, a_1 \geq a_2 \geq \dots \geq a_k$

$$// dp[i][j] = dp[i-1][j-1] + dp[i-j][j];$$

$$LL dp[N][N] = \{ 0 \};$$

```
int main(){
    int i, j, t;
    LL ans;
    for (i = 1; i < N; i++){
        dp[i][1] = dp[i][i] = 1;
        for (j = 2; j < i; j++){
            dp[i][j] = dp[i-1][j-1] + dp[i-j][j];
        }
        while (scanf("%d", &t) != EOF){
            for (ans = 0, i = 1; i <= t; i++) ans += dp[t][i];
            printf("%lld\n", ans);
        }
    }
}
```

第一类斯特林数: n 排列有 k 个cycle

$$c(n, k) = c(n-1, k-1) + (n-1) * c(n-1, k)$$

$$n! = \sigma(c(n, k))$$

$$\sigma(c(n, k) * x^k) = (x+n-1) * (x+n-2) * \dots * (x+1) * x$$

permutation of a given type

$p: (a_1, a_2, \dots, a_n)$ a_i cycles for length i

$$n! / (1^{a_1} * 2^{a_2} * \dots * n^{a_n} * a_1! * a_2! * \dots * a_n!)$$

欧拉数: n 的排列含有 k 个升程

$$A(n, k) = k * A(n-1, k) + (n-k+1) * A(n-1, k-1)$$

$$A(n, k) = \sum (-1)^j * (k-j)^n * C(n+1, j), j=0 \dots k$$

$$A(n, k) = A(n, n-1-k)$$

second-order eulerian number:

$$\langle\langle n, k \rangle\rangle = (k+1) * \langle\langle n-1, k \rangle\rangle + (2*n-1-k) * \langle\langle n-1, k-1 \rangle\rangle$$

逆序数: n 的排列逆序数为 k

$$b(n, k) = b(n-1, k) + b(n-1, k-1) + \dots + b(n-1, m)$$

$$m = \max(0, k-n+1)$$

cayley公式: 有标号的无根树个数 n^{n-2}

Prufer编码

Given positive integers d_1, \dots, d_n summing to $2n-2$.

$$(n-2)! / \pi(d_i-1)!$$

矩阵树定理:

无圈图G, $a[i, j]$ 为 v_i, v_j 边的条数,

Q 为矩阵, $i=j$ 时, $Q[i, j] = d[i]$, $i \neq j$, $Q[i, j] = -a[i, j]$

生成树个数为 Q 的任意一个 $n-1$ 阶代数余子式

the number of unlabeled rooted trees with n nodes

$$a(n+1) = (1/n) * \sum_{k=1..n} (\sum_{d|k} d * a(d)) * a(n-k+1)$$

the number of unlabeled unrooted trees with n nodes

Generating Function:

$$A(x) = 1 + T(x) - T^2(x)/2 + T(x^2)/2$$

$T(x)$ 为上面数列的母函数

catalan数:

$$c[n] = C(2n, n)/(n+1)$$

$$c[n] = (4n-2)/(n+1) * c[n-1];$$

$$c[n] = \sum c[i] * c[n-i] \quad i \geq 1$$

相关问题 :

不穿过对角线的路径数、完全加括号方案数、满二叉树数目、多边形三角剖分方案数

合法括号序列方案数、排队找零钱问题、出栈顺序问题

7.2 求连通图个数

/*pku 1737

1. 随便从 n 个点里面拿出来 2 个点, 放到 2 边, 当成是 2 个子连通图

2. 然后从剩下的 $n-2$ 个点选 $k-1$ 个, $ans = c(n-2, k-1)$, 放到左边, 那么它和我们刚才取出来的某个点组合成了一个大小为 k 的连通图它的种类数是 $dp[k]$, 表示大小为 k 的时候的连通种类数

显然右边有 $(n-k)$ 个, 所以 $ans = dp[k] * dp[n-k]$;

3. 由于你必须保证 2 个子图最少有一条边连起来, 所以 $ans = 2^k - 1$, 既对于左边的 k 个点, 要么和右边的有连边, 要么没边, 所以一共是 2^k , 必须减掉都不连边的情况.

*/

import java.util.*;

import java.math.*;

public class Main {

public static BigInteger []g = new BigInteger[60];

public static BigInteger []f = new BigInteger[60];

public static BigInteger [][]co = new BigInteger[60][60];

static void init(){

int i, j;

co[0][0] = BigInteger.ONE;

for (i = 1; i <= 50; i++){

co[i][0] = co[i][i] = BigInteger.ONE;

for (j = 1; j < i; j++){

co[i][j] = co[i-1][j].add(co[i-1][j-1]);

}

}

public static void main(String args[]){

init();

int i, j;

Scanner cin = new Scanner(System.in);

g[1] = f[1] = BigInteger.ONE;

for (i = 2; i <= 50; i++){

g[i] = BigInteger.valueOf(2).pow(co[i][2].intValue());

for (i = 2; i <= 50; i++){

f[i] = g[i];

for (j = 1; j < i; j++){

f[i] = f[i].subtract(f[j].multiply(g[i-j]).multiply(co[i-1][j-1]));

```

        }
    }
    while (cin.hasNext()){
        i = cin.nextInt();
        if (i == 0) break;
        System.out.println(f[i]);
    }
}
}

```

7.3 置换

正方形棋盘的置换：

1. 旋转0, 90, 180, 270三种
 0度, 置换为 $n \times n$
 90度, $n \times n / 4$ (n 为偶), $(n \times n - 1) / 4 + 1$ (n 为奇)
 180度, $n \times n / 2$ (n 为偶), $(n \times n - 1) / 2 + 1$ (n 为奇)
 270度, $n \times n / 4$ (n 为偶), $(n \times n - 1) / 4 + 1$ (n 为奇)
2. 沿对角线反射, 沿边中线反射
 n 为偶时:
 沿边中线反射 $n \times n / 2$
 沿对角线反射 $(n \times n - n) / 2 + n$
 n 为奇时:
 沿边中线反射 $(n \times n - n) / 2 + n$
 沿对角线反射 $(n \times n - n) / 2 + n$

```

//checked by 3532
#include <stdio.h>
#include <string.h>
#include <math.h>
#include <map>
#include <algorithm>
using namespace std;
#define N 65536
typedef long long LL;
const LL MOD = 1000000007;
int A, C;
int size, prime[N], check[N] = {0};
int seq[32], cnt[32], fcnt[32], sq, sp;
LL val[N], phi[N], col_sqr, ring, len, total;
map<LL, LL> phi_set;

void get_prime(){
    int i, j;
    size = 0;
    for (i = 2; i < N; i++){
        if (!check[i]) prime[size++] = i;
        for (j = 0; j < size && i*prime[j] < N; j++){
            check[i*prime[j]] = 1;
            if (i%prime[j]==0) break;
        }
    }
}

void decompose(LL u, LL v, int seq[], int cnt[], int &sq){
    int i;
    sq = 0;
    for (i = 0; i < size && ((LL)prime[i]*prime[i] <= v || (LL)prime[i]*prime[i] <= u); i++){
        if (v%prime[i] == 0 || u%prime[i] == 0){

```

```

        seq[sq] = prime[i];
        cnt[sq] = 0;
        while (v%prime[i] == 0){
            cnt[sq]++;
            v /= prime[i];
        }
        while (u%prime[i] == 0){
            cnt[sq]++;
            u /= prime[i];
        }
        sq++;
    }
}
if (v != 1){
    seq[sq] = v;
    cnt[sq++] = 1;
}
if (u != 1){
    seq[sq] = u;
    cnt[sq++] = 1;
}
}

LL power(LL x, LL y){
    LL ans = 1, d = x%MOD;
    while (y > 0){
        if (y&1) ans = ans*d%MOD;
        d = d*d%MOD;
        y >>= 1;
    }
    return ans;
}

LL extend_euclid(LL a, LL b, LL &x, LL &y){
    if (b == 0){
        x = 1; y = 0;
        return a;
    }
    LL d = extend_euclid(b, a%b, y, x);
    y -= x*(a/b);
    return d;
}

LL calSquare(LL b){
    LL ans = 0, x, y;
    if (b == 1) return C;
    if (b%2){
        ans = (ans + power((LL)C, b * b)) % MOD;
        ans = (ans + 2 * power((LL)C, (b * b - 1) / 4 + 1) % MOD) % MOD;
        ans = (ans + power((LL)C, (b * b - 1) / 2 + 1)) % MOD;
    }
    else{
        ans = (ans + power((LL)C, b * b)) % MOD;
        ans = (ans + 2 * power((LL)C, b * b / 4) % MOD) % MOD;
        ans = (ans + power((LL)C, b * b / 2)) % MOD;
    }
    ans = ans * (LL)250000002 % MOD;
    return ans;
}

```

```

void calPhi(){
    int i, j, k, t;
    map<LL, LL>::iterator itr1, itr2;
    sp = 1, val[0] = 1;
    phi_set.clear();
    phi_set.insert(pair<LL, LL>(1ll, 1ll));
    for (i = 0; i < sq; i++){
        for (j = 0; j < cnt[i]; j++){
            t = sp;
            for (k = 0; k < t; k++){
                LL x = val[k]*seq[i];
                itr1 = phi_set.find(val[k]);
                itr2 = phi_set.find(x);
                if (itr2 == phi_set.end()){
                    val[sp++] = x;
                    if (itr1->first % seq[i] == 0)
                        phi_set.insert(pair<LL, LL>(x, (itr1->second)*seq[i]));
                    else
                        phi_set.insert(pair<LL, LL>(x, (itr1->second)*(seq[i]-1)));
                }
            }
        }
    }
    for (i = 0, itr1 = phi_set.begin(); itr1 != phi_set.end(); i++, itr1++){
        val[i] = itr1->first;
        phi[i] = itr1->second;
    }
    sp = i;
}

void dfs(int dep, LL fact){
    if (dep == sq){
        LL sub = (LL)(A-1)*(A+1)/(LL)fact;
        LL b = (LL)sqrt(sub*1.0);
        if (b*b == sub){
            col_sqr = calSquare(b);
            len = fact;
            ring = 0;
            LL x, y;
            for (int i = 0; i < sp && val[i] <= fact; i++){
                if (fact%val[i] == 0){
                    ring += (power(col_sqr, fact/val[i]) * (phi[i] % MOD))%MOD;
                    ring %= MOD;
                }
            }
            extend_euclid(len, MOD, x, y);
            if (x < 0) x = x + ((-x) / MOD + 1) * MOD;
            if (x > 0) x = x - x/MOD*MOD;
            ring = ring * x % MOD;
            total = (total + ring*C%MOD) % MOD;
        }
        return ;
    }
    dfs(dep+1, fact);
    for (int i = 1; i <= cnt[dep]; i++){
        fact *= seq[dep];
        dfs(dep+1, fact);
    }
}

```

```

int main(){
    int ca, t = 0;
    get_prime();
    scanf("%d", &ca);
    while (ca--){
        t++;
        scanf("%d%d", &A, &C);
        if (A == 1){
            printf("Case %d: %d\n", t, C);
            continue;
        }
        decompose(A-1, A+1, seq, cnt, sq);
        total = 0;
        calPhi();
        dfs(0, 1);
        printf("Case %d: %lld\n", t, total);
    }
}

```

7.4 行列式取模

```

//checked by spoj2832 uestc1217
#include <cstdio>
#include <cstring>
#include <algorithm>
using namespace std;
#define N 208
typedef long long LL;
LL n, p, a[N][N];

void det(){
    int i, j, k;
    LL ans = 1, t;
    for (i = 0; i < n; i++)
        for (j = 0; j < n; j++)
            a[i][j] = (a[i][j]%p + p) % p;
    for (i = 0; i < n; i++){
        for (j = i+1; j < n; j++){
            while (a[j][i] != 0){
                t = a[i][i] / a[j][i];
                for (k = i; k < n; k++){
                    a[i][k] = (a[i][k] - a[j][k] * t) % p;
                    a[i][k] = (a[i][k] + p) % p;
                }
                for (k = 0; k < n; k++) swap(a[i][k], a[j][k]);
                ans = -ans;
            }
        }
        if (a[i][i] == 0){
            ans = 0;
            break;
        }
        ans = ans * a[i][i] % p;
        ans = (ans + p) % p;
    }
    printf("%lld\n", ans);
}

int main(){
    int i, j;

```

```

        while (scanf("%lld%lld", &n, &p) != EOF){
            for (i = 0; i < n; i++)
                for (j = 0; j < n; j++)
                    scanf("%lld", &a[i][j]);

            det();
        }
    }
}

```

7.5 高斯消元法xor equation

```

int n, a[N][N], b[N], val[N];
void gauss( ){
    int i, j, k, row, ans = 0;
    for ( i=row=0; i<n; i++ ){
        for ( j=row; j<n&&!a[j][i]; j++ );
        if ( j>=20 ) continue;
        if ( j>row ){
            for ( k = 0; k <= 20; k++ )
                swap( a[row][k], a[j][k] );
        }
        for ( j = row+1; j < 20; j++ ){
            if ( a[j][i] == 0 ) continue;
            for ( k = 0; k <= 20; k++ ) a[j][k] ^= a[row][k];
        }
        row++;
    }
}

void check(){
    int i, j, k;
    for (i=n-1; i>=0; i--){
        k = a[i][n];
        for (j = i+1; j < n; j++) k ^= a[i][j]*val[j];
        val[i] = k;
    }
}

```

7.6 线性规划单纯形(我的模板)

```

//checked by uva10498, 缺少线性规划的初始化步骤
#include <cstdio>
#include <cstring>
#include <algorithm>
#include <cmath>
using namespace std;
#define N 128
#define INF 1000000000
const double EPS = 1e-6;
int n, m;
int mark_n[N], mark_b[N];
double a[N][N], b[N], c[N]; //a*x <= b
double _a[N][N], _b[N], _c[N]; //中间变量
double V, var[N];
//for debugging
void output(){
    int i, j;
    puts("-----");
    for (i = 0; i < n+m; i++) printf("%.2lf ", c[i]); puts("");
    for (i = 0; i < n+m; i++){
        for (j = 0; j < n+m; j++) printf("%.2lf ", a[i][j]);
    }
}

```

```

        printf(": %.2lf\n", b[i]);
    }
    printf("AA %d %d\n", n, m);
    puts("Non-basic");
    for (i = 0; i < n+m; i++) printf("%d ", mark_n[i]); puts("");
    puts("Basic");
    for (i = 0; i < n+m; i++) printf("%d ", mark_b[i]); puts("");
    puts("-----");
}

bool input(){
    if (scanf("%d%d", &n, &m) == EOF) return false;
    int i, j;
    memset(a, 0, sizeof(a));
    memset(b, 0, sizeof(b));
    memset(c, 0, sizeof(c));
    for (i = 0; i < n; i++){
        scanf("%lf", c+i);
        c[i] *= m;
    }
    for (i = 0; i < m; i++){
        for (j = 0; j < n; j++) scanf("%lf", a[i+n]+j);
        scanf("%lf", &b[i+n]);
    }
    memset(mark_n, 0, sizeof(mark_n));
    memset(mark_b, 0, sizeof(mark_b));
    for (i = 0; i < n; i++) mark_n[i] = 1;
    for (i = n; i < n+m; i++) mark_b[i] = 1;
    return true;
}

void init_simplex(){
    int i, j;
    for (i = 0; i < n; i++) var[i] = 0;
    for (i = n; i < n+m; i++) var[i] = b[i];
    V = 0;
}
//算法导论上的伪代码
void pivot(int leave, int enter){
    int i, j;
    memset(_a, 0, sizeof(_a));
    memset(_b, 0, sizeof(_b));
    memset(_c, 0, sizeof(_c));
    //part 1
    _b[enter] = b[leave]/a[leave][enter];
    for (i = 0; i < n+m; i++){
        if (mark_n[i] == 1 && i != enter)
            _a[enter][i] = a[leave][i]/a[leave][enter];
    }
    _a[enter][leave] = 1/a[leave][enter];
    for (i = 0; i < n+m; i++){
        if (mark_b[i] == 0 || i == leave) continue;
        _b[i] = b[i] - a[i][enter]*_b[enter];
        for (j = 0; j < n+m; j++)
            if (mark_n[j] == 1 && j != enter)
                _a[i][j] = a[i][j] - a[i][enter]*_a[enter][j];
        _a[i][leave] = -a[i][enter]*_a[enter][leave];
    }
    V = V+c[enter]*_b[enter];
    for (i = 0; i < n+m; i++){

```

```

        if (!mark_n[i] || i == enter) continue;
        _c[i] = c[i] - c[enter]*_a[enter][i];
    }
    _c[leave] = -c[enter]*_a[enter][leave];
    mark_n[enter] = 0; mark_b[leave] = 0;
    mark_b[enter] = 1; mark_n[leave] = 1;
    memcpy(a, _a, sizeof(_a));
    memcpy(b, _b, sizeof(_b));
    memcpy(c, _c, sizeof(_c));
}

void simplex(){
    int i, j, k;
    int enter, leave;
    double delta;
    while (1){
        for (i = 0; i < n+m; i++){
            if (mark_n[i] == 0) continue;
            if (c[i] > EPS) break;
        }
        if (i == n+m) break;
        enter = i;
        delta = INF;
        for (j = 0; j < n+m; j++){
            if (mark_b[j] == 0) continue;
            if (a[j][enter] > 0){
                if (delta > b[j]/a[j][enter]){
                    delta = b[j]/a[j][enter];
                    leave = j;
                }
            }
        }
        if (delta == INF){
            puts("Wrong Answer");
            break;
        }
        pivot(leave, enter);
    }
    for (i = 0; i < n+m; i++){
        if (mark_b[i]) var[i] = b[i];
        else var[i] = 0;
    }
    printf("Nasa can spend %d taka.\n", (int)(ceil(V)));
}

int main(){
    while (input()){
        init_simplex();
        simplex();
    }
}

```

7.7 Romberg积分

```

//checked by hdu3310
#include<iostream>
#include<stdio.h>
#include<string.h>
#include<cmath>
#define eps 1e-5

```



```

using namespace std;
#define MAX_N 1000
double r1,r2;
double f(double x){
    return sqrt(r1*r1-x*x)*sqrt(r2*r2-x*x);
}

double Romberg (double a, double b, double (*f)(double x)){
    int i, j, temp2, mini;
    double h, R[2][MAX_N], temp4;
    for (i=0; i<MAX_N; i++) {
        R[0][i] = 0.0;
        R[1][i] = 0.0;
    }
    h = b-a;
    mini = (int)(log(h*10.0)/log(2.0));
    R[0][0] = ((*f)(a)+(*f)(b))*h*0.50;
    i = 1;
    temp2 = 1;
    while (i<MAX_N){
        i++;
        R[1][0] = 0.0;
        for (j=1; j<=temp2; j++)
            R[1][0] += (*f)(a+h*((double)j-0.50));
        R[1][0] = (R[0][0] + h*R[1][0])*0.50;
        temp4 = 4.0;
        for (j=1; j<i; j++) {
            R[1][j] = R[1][j-1] + (R[1][j-1]-R[0][j-1])/(temp4-1.0);
            temp4 *= 4.0;
        }
        if ((fabs(R[1][i-1]-R[0][i-2])<eps)&&(i>mini))
            return R[1][i-1];
        h *= 0.50;
        temp2 *= 2;
        for (j=0; j<i; j++) R[0][j] = R[1][j];
    }
    return R[1][MAX_N-1];
}

int main(){
    int t;
    for(scanf("%d",&t);t;t--){
        scanf("%lf%lf",&r1,&r2);
        if(r1>r2)swap(r1,r2);
        printf("%.2lf\n",8*Romberg(0,r1,f));
    }
    return 0;
}

```

8. 附录：vim配置

```
set encoding=utf8
set modelines=0
syntax enable
set showcmd
filetype indent on
set autoindent
set cindent
set showmatch
set matchtime=5
set ruler
set number
set backspace=2
set tabstop=4
set shiftwidth=4
set ai!

map <F5> :call CompileRunGcc(<CR>
func! CompileRunGcc()
    exec "w"
    exec "!gcc -Wall %"
    exec "! ./a.out"
endfunc

map <F6> :call CompileRunGpp(<CR>
func! CompileRunGpp()
    exec "w"
    exec "!g++ -Wall %"
    exec "! ./a.out"
endfunc
```