

Comments for Assignment 1 q1 FIT3155

First I pre-process the text and pattern by running the reverse z-algorithm to obtain the z-suffix array. This is to be used later when determining a transposition error. I then run the z-algorithm on the text and pattern to obtain the z-prefix values.

If I encounter a z-value that is equal to the length of the pattern, it indicates that I have found an exact match.

To search for a transposition error, we can view a transposition error as:

$$\text{Error_pat} = \text{prefix} + \text{transposition error} + \text{suffix}$$

Since one transposition error will always have a length of 2 characters, we know that $\text{len}(\text{prefix}) + \text{len}(\text{suffix}) = \text{len}(\text{pat}) - 2$.

To obtain the lengths of the prefix and the suffix, I can make use of the values in the z-array. At step i (where $M < i < N+2$), all the values from $\text{rev_z_array}[i]$ and before are the z-prefix values, whereas all the values after are the z-suffix values. I can obtain the lengths of the prefix and the suffix by accessing $\text{rev_z_array}[i]$ and $\text{rev_z_array}[i+m-1]$ respectively.

Now if there is a possible one transposition error, I simply check the next 2 characters after the matched prefix to see if the flipped characters match the pattern. If it is a match, it means that we have found a transposition error within the text.

The time complexity of the algorithm is $O(n + m)$, where n is the length of the text and m is the length of the pattern. The pre-processing of the z-suffix array takes $O(n + m)$ time. Then by running the algorithm, which is a modified z-algorithm with at most 3 extra steps in every iteration, it is also in $O(n + m)$ time. Therefore the total time complexity is $O(2(n+m)) = O(n + m)$.

The space complexity of the algorithm is $O(n + m)$. I allocated memory for a z-array of length $O(m + n + m)$, where I prepend m extra cells to the z-suffix array. The motivation behind this is because an alternative way of solving this question is to obtain a z-prefix array and a z-suffix array separately, then compare the values as per the formula above. This would result in a space complexity of $O(2(n + m))$ to store 2 z-arrays of space $O(n + m)$. Therefore, by prepending an extra $O(m)$ spaces, $O(n)$ memory is conserved in return.