Bayesian Calibration of Numerical Model Output by an R package: ${\rm spCalibration}$

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1 Data structure

1.1 Data layout

```
base dataset from pollution
   Model_Base_Tab[, c(1, 3:8, 12, 15, 17:19, 24)]
                    CITY STATION NAME CMAQ ID
                                                 LON
                                                        LAT DATE_TIME YEAR_MONTH
   ##
          1: Shijiazhuang Shijigongyuan
                                         5724 114.542 38.031 2015-06-01
                                                                          201506
   ##
          2: Shijiazhuang Shijigongyuan
                                         5724 114.542 38.031 2015-06-02
                                                                          201506
          3: Shijiazhuang Shijigongyuan
                                         5724 114.542 38.031 2015-06-03
   ##
                                                                          201506
   ##
          4: Shijiazhuang Shijigongyuan
                                         5724 114.542 38.031 2015-06-04
                                                                          201506
          5: Shijiazhuang Shijigongyuan
                                         5724 114.542 38.031 2015-06-05
                                                                          201506
   ## 12508:
                                         7932 116.650 40.410 2016-01-27
                                                                          201601
                 Beijing
                               Shunyi
   ## 12509:
                 Beijing
                               Shunyi
                                         7932 116.650 40.410 2016-01-28
                                                                          201601
   ## 12510:
                 Beijing
                               Shunyi
                                         7932 116.650 40.410 2016-01-29
                                                                          201601
10
   ## 12511:
                 Beijing
                               Shunyi
                                         7932 116.650 40.410 2016-01-30
                                                                          201601
11
   ## 12512:
                 Beijing
                               Shunyi
                                         7932 116.650 40.410 2016-01-31
                                                                          201601
12
             REAL_PM25 SITEID
   ##
                                 LON_X
                                         LAT_Y CMAQ_PM25 NA.Kalman
13
          1: 87.20833
                           1 -242926.92 4243177 53.104367
                                                              NΑ
   ##
   ##
          2:
             44.04167
                           1 -242926.92 4243177 47.539544
                                                              NA
15
             59.45833
                           1 -242926.92 4243177 53.139121
                                                              NA
16
                           1 -242926.92 4243177 39.686555
             75.04167
                                                              NA
17
   ##
          5: 100.25000
                           1 -242926.92 4243177 37.311844
                                                              NΑ
18
19
   ## 12508: 110.20833
                             -38955.09 4492669 42.721178
                                                              NA
   ## 12509: 119.37500
                             -38955.09 4492669 12.222126
                                                              NA
21
   ## 12510: 86.25000
                             -38955.09 4492669 37.876560
                                                              NΑ
22
   ## 12511: 64.91667
                            -38955.09 4492669 15.412478
                                                              NA
```

```
## 12512: 15.62500 76 -38955.09 4492669 4.373301
                                                      NA
   the coordinates of monitoring station
   head(Site)
        SITEID
                    CITY STATION_NAME
                                      LON
   ##
                                            LAT
                                                   LON_X
            1 Shijiazhuang Shijigongyuan 114.542 38.031 -242926.9 4243177
   ##
     2:
            2 Shijiazhuang Xinangaojiao 114.467 38.012 -249721.6 4241671
            4 Shijiazhuang Zhigongyiyuan 114.455 38.051 -250376.2 4246107
   ## 3:
   ## 4:
            5 Shijiazhuang Renminhuitang 114.521 38.052 -244560.1 4245683
            6 Shijiazhuang Xibeishuiyuan 114.502 38.140 -245328.9 4255626
   ## 5:
           7 Shijiazhuang
                            Gaoxingu 114.605 38.040 -237292.7 4243672
   dataset of CMAQ
2
   CMAQ_PM25
   ##
            CMAQ_ID DATE_TIME CMAQ_PM25
                                       LON
                                              LAT
                                                     LON_X LAT_Y
   ##
              4619 2015-06-01 9.824296 113.5025 36.71028 -349353.9 4105037
         1:
2
         2.
              4619 2015-06-02 10.246346 113.5025 36.71028 -349353.9 4105037
              4619 2015-06-03 17.661194 113.5025 36.71028 -349353.9 4105037
   ##
         3:
              4619 2015-06-04 4.019376 113.5025 36.71028 -349353.9 4105037
              4619 2015-06-05 3.203634 113.5025 36.71028 -349353.9 4105037
         5:
   ##
   ## 459812:
             11438 2016-01-27 86.914974 119.7762 39.98793 224742.0 4431396
             11438 2016-01-28 20.297575 119.7762 39.98793 224742.0 4431396
   ## 459813:
     459814:
             11438 2016-01-29 20.376099 119.7762 39.98793 224742.0 4431396
10
   ## 459815:
             11438 2016-01-30 34.814252 119.7762 39.98793 224742.0 4431396
11
     459816:
             11438 2016-01-31 41.928738 119.7762 39.98793 224742.0 4431396
   ##
12
   ##
            YEAR_MONTH
13
   ##
         1:
               201506
14
   ##
         2:
               201506
15
               201506
16
   ##
         4:
               201506
17
               201506
   ##
         5:
18
19
               201601
   ## 459812:
20
   ## 459813:
               201601
21
   ## 459814:
               201601
22
               201601
23
   ## 459815:
               201601
   ## 459816:
24
   #
                    the coordinates of CMAQ lattice
2
   cmaq_site
   ##
          CMAQ_ID
                    LON
                            T.A.T
                                  LON_X LAT_Y
                                                    CTTY
                                                          TD
            4619 113.5025 36.71028 -349353.9 4105037
                                                   Handan
```

```
2:
##
            4638 113.5744 38.30076 -325010.6 4281459 Shijiazhuang
##
            4639 113.5783 38.38442 -323712.1 4290736 Shijiazhuang
                                                                      3
      3:
      4:
            4640 113.5822 38.46806 -322412.8 4300010 Shijiazhuang
                                                                      4
      5:
            4641 113.5860 38.55172 -321112.5 4309285 Shijiazhuang
##
           11199 119.5909 40.25370 210047.3 4461493
## 2495:
                                                      Qinhuangdao 2495
## 2496:
           11317 119.6677 39.99614 215508.6 4432649
                                                       Qinhuangdao 2496
## 2497:
           11318 119.6783 40.07928 216765.3 4441846
                                                       Qinhuangdao 2497
## 2498:
           11319 119.6890 40.16242 218020.3 4451043
                                                       Qinhuangdao 2498
## 2499:
           11438 119.7762 39.98793 224742.0 4431396
                                                       Qinhuangdao 2499
```

1.2 Create grids by CMAQ or INLA

```
A. Create directly grids by CMAQ lattices
   # temp <- cmaq_site</pre>
   # coordinates(temp) = ~ LON_X + LAT_Y
   # coords <- temp@coords</pre>
   # Neighbor_order <- dnearneigh(coords, 0, 1e4)
   # # View(Neighbor_order)
   # adjacent.matrix <- matrix(0, nrow(coords), nrow(coords))</pre>
   # for(i in 1:nrow(coords))
   # {
11
      for( j in 1: length(Neighbor_order[[i]]))
12
13
       Ad.num <- Neighbor_order[[i]][j]
14
       adjacent.matrix[i, Ad.num] = -1
     }
   #
16
   # }
17
   # grid <- list(grid.coords = cmaq_site,
18
               adjacent.matrix = adjacent.matrix)
19
   B. Create grids by INLA
21
   22
23
                          # Monitoring stations data
   grid <- ProduceGrid(Site,
24
                  max.edge = c(0.3, 0.7), # max.edge, offset and cutoff: see INLA
25
                  offset = c(0.4, 0.6),
26
                  cutoff = 0.1,
27
                  col = "black",
28
                  size = 1)
29
30
   grid$plot.grid
```

1.3 Mapping matrix: H

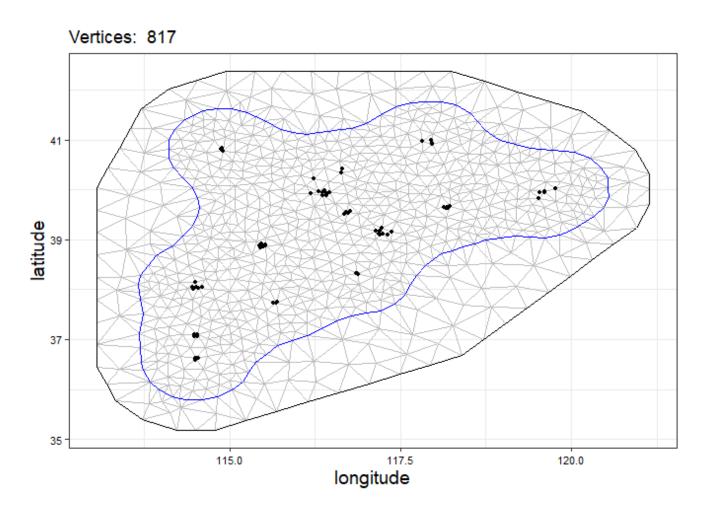


Figure 1.1: The irregular division of spatial domain by INLA $\,$

1.4 Initialize parameter

1.4.1 Prior

```
initialize parameters
{
# true.para <- list(beta = rep(NA, 2), nugget.tau2 = NA,
         theta = c(NA, NA), kO = NA, k = NA)
prior distribution
prior <- list(</pre>
      beta = list(mu = c(0, 1), Sigma2 = 1e5*diag(2))
      , nugget.tau2 = list(a = 2, b = 1)
      , theta1 = list(mu = 0.005, Sigma2 = 1e5)
     )
}
```

1.4.2 Importance sampling

1.4.3 Initialization

```
initial.para <- list(
    beta = list(E_beta = c(2, 0.5), Sigma2 = diag(2))
    , theta1 = list(E_theta1 = 0.005, Sigma2 = 2)
    , k = list(E_k = 5, a = 2, b = 1)
    , k0 = list(E_k0 = 5, a = 2, b = 1)</pre>
```

2. DATA TRUNCATION CONTENTS

```
, theta2 = list(mu = c(1))
, tau2 = list(E_tau2 = 1, a = 2, b = 1)
)
```

2 Data truncation

3 Model cross validation

```
leave one city out
city_num = 1
GSD = Test_Train_Fun(Site, Data_Str, Yts_Xts, city_num)
##
##
## Test city: Baoding ...
Train = GSD$Train
Test = GSD$Test
Train$Y_ts = sqrt(Train$Y_ts)
Train$X_ts = sqrt(Train$X_ts)
Test$X_ts = sqrt(Test$X_ts)
fit model
# CV <- spVBEnKs(data = Train,
#
          prior = prior,
#
          IS = IS,
          para = initial.para,
#
          true.para = NULL,
          parallel = TRUE,
          verbose = TRUE,
          verbose. VB = TRUE,
#
          Ensemble.size = 50,
#
          cs = 0.4,
          ct = 1,
#
          Remove. CPU. Count = 2,
          N.Chunk = 1,
#
          itMax = 1e2,
          tol.vb = 1e-3,
```

```
tol.real = 1e-3)
load( "./data/Generate_Data/Test/CV.Rdata")
#
print(CV)
##
## Call: spVBEnKs(data = Train, prior = prior, IS = IS, para = initial.para,
     true.para = NULL, parallel = TRUE, verbose = TRUE, verbose.VB = TRUE,
##
     Ensemble.size = 50, cs = 0.4, ct = 1, Remove.CPU.Count = 2,
     N.Chunk = 1, itMax = 100, tol.vb = 0.001, tol.real = 0.001)
##
##
## Iterations: 12
## Log-likelihood: 171854.001
##
## Parameter estimation:
##
      beta0 beta1 tau_2 theta1 theta2
                                       k0 iter
## True:
       NA
             NΑ
                  NA
                                  NA
                                       NA
## Init: 2.000 0.500 1.000 0.005 1.000 5.000 5.000
## Esti: 1.281 0.672 0.995 0.008 0.601 9.639 4.357
##
## (...output suppressed due to large dimension!)
    Prediction
3.1
prediction
P <- predict(CV, test = Test, site = Site, method = c("ensemble"),
          transf = "square", ncol.layout = 2)
P$error
## $Diff.Station.RMSE
      34
            35
                  36
                        37
                               38
  72.143 63.381 105.185 66.283 60.597 57.315
##
## $Total.Error
   Pearson.before Pearson.after RMSE
                                   MB
                                         NMB
                                              NME
          0.628
                    0.815 72.613 -26.288 -16.514 32.422
P$ensemble.plot
```

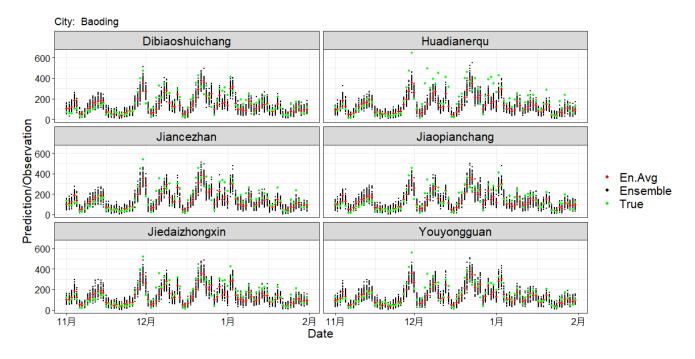


Figure 3.1: Prediction by ensemble

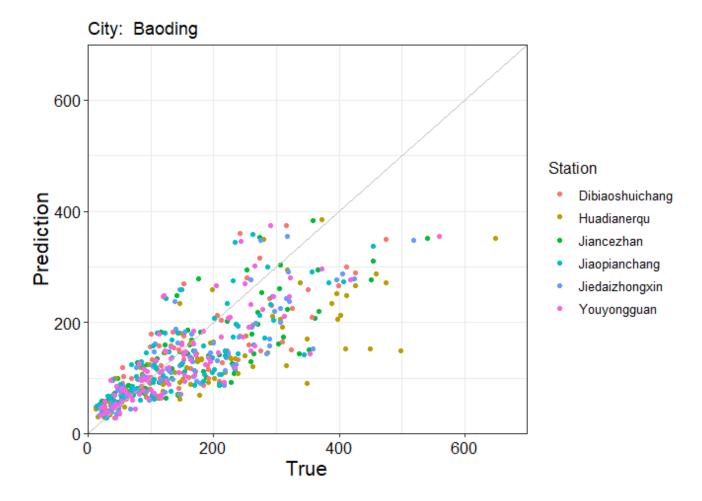


Figure 3.2: Prediction by ensemble mean

4. COMPLETE DATASET CONTENTS

```
P$mean.plot
```

3.2 The distributions of parameters

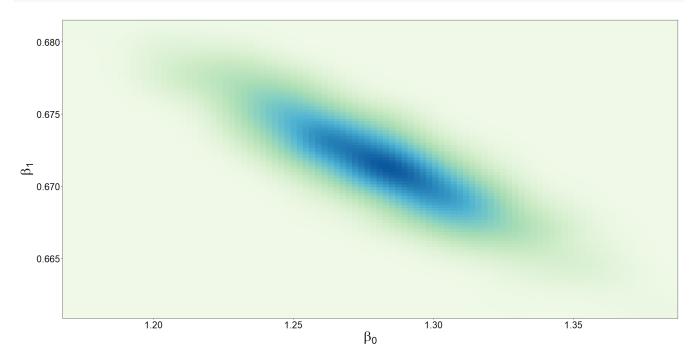


Figure 3.3: The distribution of Beta parameter

P\$Close.Dist

P\$NoClose.Dist

4 Complete dataset

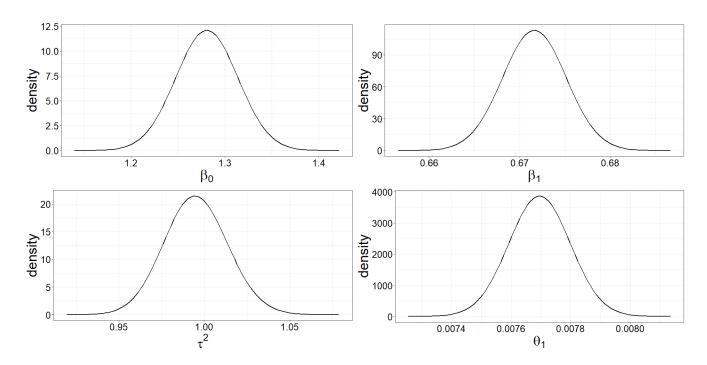


Figure 3.4: The distributions of parameters of close form

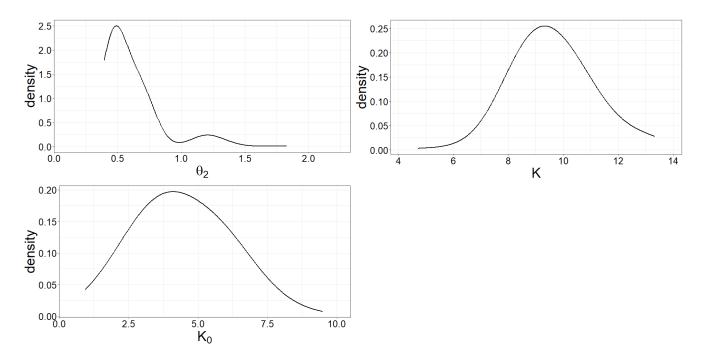


Figure 3.5: The distributions of parameters of no close form

4. COMPLETE DATASET CONTENTS

```
, Hs = Data_Str$Hs
Total_Data$Y_ts = sqrt(Total_Data$Y_ts)
Total_Data$X_ts = sqrt(Total_Data$X_ts)
fit model and prediction
# Total <- spVBEnKs(data = Total_Data,</pre>
                  prior = prior,
#
                  IS = IS,
#
                  para = initial.para,
                  true.para = NULL,
#
#
                  parallel = TRUE,
                  verbose = TRUE,
                  verbose. VB = TRUE,
#
                  Ensemble.size = 50,
#
                  cs = 0.4,
#
                  ct = 1,
                  Remove. CPU. Count = 2,
                  N. Chunk = 1,
#
                  itMax = 1e2,
                  tol.vb = 1e-3,
#
                  tol.real = 1e-3)
load("./data/Generate_Data/Total.Rdata")
print(Total)
##
## Call: spVBEnKs(data = Total_Data, prior = prior, IS = IS, para = initial.para,
      true.para = NULL, parallel = TRUE, verbose = TRUE, verbose.VB = TRUE,
##
##
      Ensemble.size = 50, cs = 0.4, ct = 1, Remove.CPU.Count = 2,
##
      N.Chunk = 1, itMax = 100, tol.vb = 0.001, tol.real = 0.001)
##
## Iterations: 12
##
## Log-likelihood: 170404.298
## Parameter estimation:
       beta0 beta1 tau_2 theta1 theta2
                                        k k0 iter
## True:
          NA
                NA
                     NA
                            NA
                                  NA
                                       NA
                                            NA
## Init: 2.00 0.500 1.000 0.005 1.000 5.000 5.00
                                                 0
## Esti: 1.22 0.667 1.018 0.008 0.604 9.475 4.33
##
## (...output suppressed due to large dimension!)
```

4.1 The distributions of parameters

4. COMPLETE DATASET CONTENTS

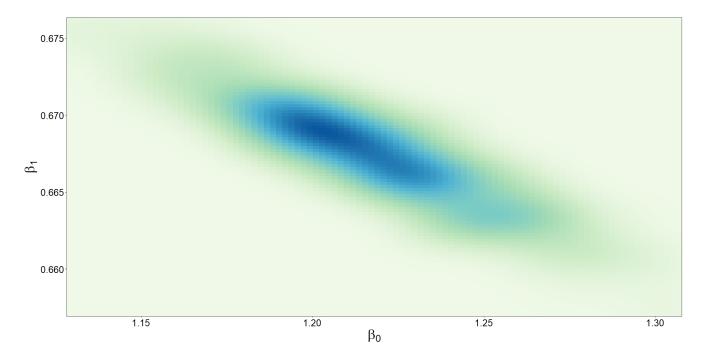


Figure 4.1: The distribution of Beta parameter

P\$Close.Dist

P\$NoClose.Dist

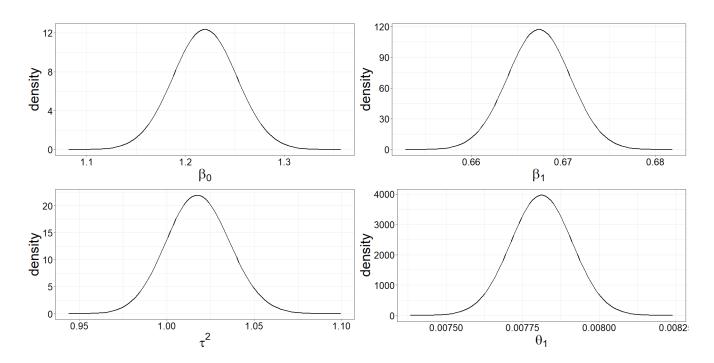


Figure 4.2: The distributions of parameters of close form

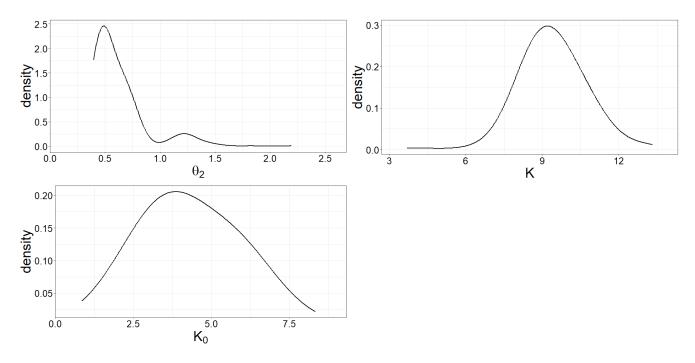


Figure 4.3: The distributions of parameters of no close form