

Propagation in Dielectric Medium

Maxwell's equation (3D)

$$\begin{aligned}\frac{\partial \mathbf{E}}{\partial t} &= -\frac{1}{\epsilon_r \epsilon_0} \nabla \times \mathbf{H} \\ \frac{\partial \mathbf{H}}{\partial t} &= -\frac{1}{\mu_0} \nabla \times \mathbf{E}\end{aligned}$$



Different propagation velocity

$$\begin{aligned}E_x^{n+\frac{1}{2}}(k) &= E_x^{n-\frac{1}{2}}(k) - \frac{dt}{\epsilon_r \epsilon_0 \cdot dz} \left[H_y^n \left(k + \frac{1}{2} \right) - H_y^n \left(k - \frac{1}{2} \right) \right] \\ H_y^{n+1} \left(k + \frac{1}{2} \right) &= H_y^n \left(k + \frac{1}{2} \right) - \frac{dt}{\mu_0 \cdot dz} \left[E_x^{n+\frac{1}{2}}(k+1) - E_x^{n-\frac{1}{2}}(k) \right]\end{aligned}$$