

11. $y(x)y(a/x) = b^2$.

Solution:

$$y(x) = \pm b \exp[\Phi(x, a/x)],$$

where $\Phi(x,z) = -\Phi(z,x)$ is any antisymmetric function of two arguments. For $\Phi(x,z) = C(\ln x - \ln z)$, there are particular solutions of the form

$$y = \pm ba^{-C}x^{2C},$$

where C is an arbitrary constant.

Reference

Polyanin, A. D. and Manzhirov, A. V., *Handbook of Integral Equations: Exact Solutions (Supplement. Some Functional Equations)* [in Russian], Faktorial, Moscow, 1998.

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