

$$\mathbf{4.}\quad \frac{\partial w}{\partial t}=a\frac{\partial}{\partial x}\bigg(w^m\frac{\partial w}{\partial x}\bigg)+bw^{1-m}.$$

Functional separable solution:

$$w(x,t) = \left[\frac{(x+A)^2}{F(t)} + B|F(t)|^{-\frac{m}{m+2}} - \frac{bm^2}{4a(m+1)}F(t)\right]^{1/m}, \quad F(t) = C - \frac{2a(m+2)}{m}t,$$

where A, B, and C are arbitrary constants.

References

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