

5. 
$$f(x+y) + f(x-y) = 2f(x)\cos y$$
.

Solution:

$$f(x) = C_1 \cos x + C_2 \sin x,$$

where  $C_1$  and  $C_2$  are arbitrary constants.

## Reference

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