

23. y(x) + y(a/x) = f(x).

The right-hand side is assumed to satisfy the condition f(x) = f(a/x). Solution:

$$y(x) = \frac{1}{2}f(x) + \Phi(x, a/x),$$

where $\Phi(x, z) = -\Phi(z, x)$ is any antisymmetric function of two arguments.

Reference

Polyanin, A. D. and Manzhirov, A. V., *Handbook of Integral Equations: Exact Solutions (Supplement. Some Functional Equations)* [in Russian], Faktorial, Moscow, 1998.

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