

20.
$$(ax^2 + b)y_{xx}'' + axy_x' + cy = 0$$
.

The substitution $z = \int \frac{dx}{\sqrt{ax^2 + b}}$ leads to a constant coefficient linear equation: $y''_{zz} + cy = 0$.

Reference

Polyanin, A. D. and Zaitsev, V. F., *Handbook of Exact Solutions for Ordinary Differential Equations, 2nd Edition,* Chapman & Hall/CRC, Boca Raton, 2003.

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http://eqworld.ipmnet.ru/en/solutions/ode/ode0220.pdf