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21.　$F\left(ax + by + cw,\ \dfrac{\partial w}{\partial x},\ \dfrac{\partial w}{\partial y}\right) = 0.$

For $c = 0$, see equation 3.3.19. If $c \neq 0$, then the substitution $cu = ax + by + cw$ leads to an equation of the form 3.3.20: $F\left(cu,\ \dfrac{\partial u}{\partial x} - \dfrac{a}{c},\ \dfrac{\partial u}{\partial y} - \dfrac{b}{c}\right) = 0.$

Reference

Polyanin, A. D., Zaitsev, V. F., and Moussiaux, A., *Handbook of First Order Partial Differential Equations*, Taylor & Francis, London, 2002.