

7. $Ay(x^a) + By(x^b) + y(x) = 0$.

This functional equation has particular solutions of the form $y(x) = C|\ln x|^p$, where C is an arbitrary constant, and β is a root of the transcendental equation $A|a|^p + B|b|^p + 1 = 0$.

Deference

Polyanin, A. D. and Manzhirov, A. V., *Handbook of Integral Equations: Exact Solutions (Supplement. Some Functional Equations)* [in Russian], Faktorial, Moscow, 1998.

Copyright © 2004 Andrei D. Polyanin

http://eqworld.ipmnet.ru/en/solutions/fe/fe1207.pdf