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18.
$$\int_0^{\pi/2} y(\xi) dt = f(x), \qquad \xi = x \sin t.$$

Schlomilch (Schlömilch) equation.

Solution:

$$y(x) = \frac{2}{\pi} \left[f(0) + x \int_0^{\pi/2} f'_{\xi}(\xi) dt \right], \qquad \xi = x \sin t.$$

References

Whittaker, E. T. and Watson, G. N., A Course of Modern Analysis, Cambridge Univ. Press, Cambridge, 1958. Gakhov, F. D., Boundary Value Problems [in Russian], Nauka, Moscow, 1977.

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Schlomilch Equation (Schlömilch Equation)

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