

14.
$$y(x) - \int_{a}^{x} g(x)h(t)y(t) dt = f(x)$$
.

Solution:

$$y(x) = f(x) + \int_{a}^{x} R(x,t)f(t) dt, \quad \text{where} \quad R(x,t) = g(x)h(t) \exp\left[\int_{t}^{x} g(s)h(s) ds\right].$$

Reference

Polyanin, A. D. and Manzhirov, A. V., Handbook of Integral Equations, CRC Press, Boca Raton, 1998.

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