

$$2. \quad a\frac{\partial^2 w}{\partial x^2} + \frac{\partial}{\partial y} \left(b e^{\mu y} \frac{\partial w}{\partial y} \right) = f(w), \qquad ab > 0.$$

Functional separable solution for $\mu \neq 0$:

$$w = w(\xi),$$
 $\xi = \left[b\mu^2(x + C_1)^2 + 4ae^{-\mu y}\right]^{1/2},$

where C_1 is an arbitrary constant and the function $w(\xi)$ is defined implicitly by

$$\int \left[C_2 + \frac{2}{ab\mu^2} F(w) \right]^{-1/2} dw = C_3 \pm \xi, \qquad F(w) = \int f(w) \, dw,$$

 C_2 and C_3 are arbitrary constants.

References

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