

4.  $f(x+y) + f(x-y) = 2f(x) \cosh y$ .

Solution:

$$f(x) = C_1 e^x + C_2 e^{-x},$$

where  $C_1$  and  $C_2$  are arbitrary constants.

## References

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