

37.
$$y_{xx}'' + xfy_x' - fy = 0$$
, $f = f(x)$.

Particular solution: $y_0 = x$.

Solution:

$$y = y_0 \left(C_1 + C_2 \int \frac{e^{-F}}{y_0^2} dx \right)$$
, where $F = \int x f dx$,

 C_1 and C_2 are arbitrary constants.

Reference

Polyanin, A. D. and Zaitsev, V. F., *Handbook of Exact Solutions for Ordinary Differential Equations, 2nd Edition,* Chapman & Hall/CRC, Boca Raton, 2003.

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