13.　$(ax + b)^n (cx + d)^n y_x^{(n)} = ky.$

The transformation

$$\xi = \ln \frac{ax + b}{cx + d}, \quad w = \frac{y}{(cx + d)^{n-1}}$$

leads to a constant coefficient linear equation.

References

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