

18.
$$y(x^{a_n}) + b_{n-1}y(x^{a_{n-1}}) + \ldots + b_1y(x^{a_1}) + b_0y(x) = 0.$$

There are particular solutions of the form $y(x) = C|\ln x|^p$, where C is an arbitrary constant, and p is a root of the transcendental equation $|a_n|^p + b_{n-1}|a_{n-1}|^p + \cdots + b_1|a_1|^p + b_0 = 0$.

Deference

Polyanin, A. D. and Manzhirov, A. V., *Handbook of Integral Equations: Exact Solutions (Supplement. Some Functional Equations)* [in Russian], Faktorial, Moscow, 1998.

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