7. $y''_{xx} = x^{-3} f(y x^{-1})$.

The transformation $\xi = 1/x$, $w = y/x$ leads to an autonomous equation of the form 3.1: $w''_{\xi\xi} = f(w)$.

References

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