18. $y(x) + g(x)y(a - x) = f(x)$.

Solution:

$$y(x) = \frac{f(x) - g(x)f(a - x)}{1 - g(x)g(a - x)}.$$

References

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