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5. 
$$ax^4 + bx^3 + cx^2 + bx + a = 0$$
  $(a \neq 0)$ .

Reciprocal algebraic equation.

The substitution

$$y = x + \frac{1}{x}$$

leads to a quadratic equation of the form

$$ay^2 + by + c - 2a = 0.$$

## Reference

Encyclopedia of Mathematics, Vol. 1 [in Russian], Sovetskaya Entsiklopediya, Moscow, pp. 740–741, 1977.

Reciprocal Algebraic Equation - 4

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http://eqworld.ipmnet.ru/en/solutions/ae/ae0105.pdf