

1. 
$$\int_a^b |x-t| \, y(t) \, dt = f(x), \qquad 0 \le a < b < \infty.$$

Solution:

$$y(x) = \frac{1}{2} f_{xx}^{"}(x).$$

The right-hand side f(x) of the integral equation must satisfy certain relations. The general form of f(x) is as follows:

$$f(x) = F(x) + Ax + B,$$

$$A = -\frac{1}{2} \left[ F'_x(a) + F'_x(b) \right], \quad B = \frac{1}{2} \left[ aF'_x(a) + bF'_x(b) - F(a) - F(b) \right],$$

where F(x) is an arbitrary bounded twice differentiable function (with bounded first derivative).

## Reference

Polyanin, A. D. and Manzhirov, A. V., Handbook of Integral Equations, CRC Press, Boca Raton, 1998.

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