Exact Solutions > Ordinary Differential Equations > Higher-Order Linear Ordinary Differential Equations

4. Higher-Order Linear Ordinary Differential Equations

$$1. \quad y_{xxx}^{\prime\prime\prime} + \lambda y = 0.$$

$$2. \quad y_{xxx}^{\prime\prime\prime} = ax^{\beta}y.$$

3.
$$(x-a)^3(x-b)^3y'''_{xxx}-cy=0$$
, $a \neq b$.

4.
$$(ax^2 + bx + c)^3 y'''_{xxx} = ky$$
.

5.
$$y_{xxxx}^{''''} + ay = 0$$
.

6.
$$y_{xxxx}^{""} + ax^n y_{xx}^{"} + b(ax^n - b)y = 0$$
.

7.
$$x^2 y_{xxxx}^{""} + 6x y_{xxx}^{""} + 6y_{xx}^{"} - a^2 y = 0$$
. Equation of transverse vibrations of a pointed bar.

8.
$$(ax^2 + bx + c)^4 y_{max}^{""} = ky$$
.

9.
$$y_x^{(6)} + ay = 0$$
.

10.
$$y_x^{(2n)} = a^{2n}y$$
.

11.
$$y_x^{(n)} = axy + b$$
, $a > 0$.

12.
$$y_x^{(n)} = ax^{\beta}y$$
.

13.
$$(ax+b)^n(cx+d)^ny_x^{(n)}=ky$$
.

14.
$$(ax^2 + bx + c)^n y_x^{(n)} = ky$$
.

15.
$$a_n y_x^{(n)} + a_{n-1} y_x^{(n-1)} + \dots + a_1 y_x' + a_0 y = 0$$
. Constant coefficient linear equation.

16.
$$a_n x^n y_x^{(n)} + a_{n-1} x^{n-1} y_x^{(n-1)} + \dots + a_1 x y_x' + a_0 y = 0$$
. Euler equation.

The EqWorld website presents extensive information on solutions to various classes of ordinary differential equations, partial differential equations, integral equations, functional equations, and other mathematical equations.

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http://eqworld.ipmnet.ru/en/solutions/ode/ode-toc4.pdf