

43.
$$y'_x = -\frac{n}{x} + f(x)g(x^n e^y)$$
.

The substitution $z=x^ne^y$ leads to a separable equation: $z_x'=f(x)zg(z)$.

Reference

Polyanin, A. D. and Zaitsev, V. F., *Handbook of Exact Solutions for Ordinary Differential Equations, 2nd Edition,* Chapman & Hall/CRC, Boca Raton, 2003.

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http://eqworld.ipmnet.ru/en/solutions/ode/ode0143.pdf