

Exact Solutions > Ordinary Differential Equations > First-Order Ordinary Differential Equations > Riccati Equation, Special Case 2

8.
$$y'_x = f(x)y^2 + ay - ab - b^2 f(x)$$
.

Riccati equation, special case 2.

Particular solution: $y_0 = b$.

The general solution can be written as:

$$y = b + \Phi(x) \left[C - \int f(x) \Phi(x) \, dx \right]^{-1}, \quad \text{where} \quad \Phi(x) = \exp \left\{ ax + 2b \int f(x) \, dx \right\}$$

 ${\cal C}$ is an arbitrary constant.

Reference

Polyanin, A. D. and Zaitsev, V. F., *Handbook of Exact Solutions for Ordinary Differential Equations, 2nd Edition*, Chapman & Hall/CRC, Boca Raton, 2003.

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