

First-Order Partial Differential Equations > Nonlinear Equations > Section 3.3

9.
$$w = x \frac{\partial w}{\partial x} + y \frac{\partial w}{\partial y} + F\left(\frac{\partial w}{\partial x}, \frac{\partial w}{\partial y}\right)$$
.

Clairaut's equation.

Complete integral:

$$w = C_1 x + C_2 y + F(C_1, C_2),$$

where C_1 and C_2 are arbitrary constants.

References

Kamke, E., Differentialgleichungen: Lösungsmethoden und Lösungen, II, Partielle Differentialgleichungen Erster Ordnung für eine gesuchte Funktion, Akad. Verlagsgesellschaft Geest & Portig, Leipzig, 1965.

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