

Exact Solutions > Basic Handbooks > A. D. Polyanin, *Handbook of Linear Partial Differential Equations* for Engineers and Scientists, Chapman & Hall/CRC Press, Boca Raton, 2002

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