

First-Order Partial Differential Equations > Nonlinear Equations > Section 3.3

20. 
$$F\left(w, \frac{\partial w}{\partial x}, \frac{\partial w}{\partial y}\right) = 0.$$

Complete integral:

$$w = w(z), \qquad z = C_1 x + C_2 y,$$

where  $C_1$  and  $C_2$  are arbitrary constants, and w = w(z) is determined by the autonomous ordinary differential equation  $F(w, C_1w_z', C_2w_z') = 0$ .

## References

Kamke, E., Differentialgleichungen: Lösungsmethoden und Lösungen, II, Partielle Differentialgleichungen Erster Ordnung für eine gesuchte Funktion, Akad. Verlagsgesellschaft Geest & Portig, Leipzig, 1965.

Polyanin, A. D., Zaitsev, V. F., and Moussiaux, A., Handbook of First Order Partial Differential Equations, Taylor & Francis, London, 2002.

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